Homework 1

Sung Chang {style='background-color: yellow;'}

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l Due: Sun, Jan 29, 2023 @ 11:59pm

Please read the instructions carefully before submitting your assignment.

- 1. This assignment requires you to:
 - Upload your Quarto markdown files to a git repository
 - Upload a PDF file on Canvas
- 2. Don't collapse any code cells before submitting.
- 3. Remember to make sure all your code output is rendered properly before uploading your submission.

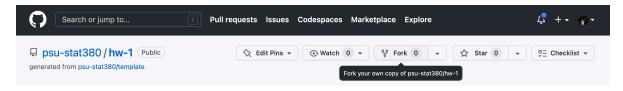
Please add your name to the the author information in the frontmatter before submitting your assignment.

Question 1



In this question, we will walk through the process of *forking* a git repository and submitting a *pull request*.

1. Navigate to the Github repository here and fork it by clicking on the icon in the top right



Provide a sensible name for your forked repository when prompted.

2. Clone your Github repository on your local machine

```
$ git clone <<insert your repository url here>>
$ cd hw-1
```

Alternatively, you can use Github codespaces to get started from your repository directly.

3. In order to activate the R environment for the homework, make sure you have renv installed beforehand. To activate the renv environment for this assignment, open an instance of the R console from within the directory and type

```
::: {.cell}
renv::activate()
```

::: Follow the instrutions in order to make sure that renv is configured correctly.

- 4. Work on the *remaining part* of this assignment as a .qmd file.
 - Create a PDF and HTML file for your output by modifying the YAML frontmatter for the Quarto .qmd document
- 5. When you're done working on your assignment, push the changes to your github repository.

6. Navigate to the original Github repository here and submit a pull request linking to your repository.

Remember to **include your name** in the pull request information!

If you're stuck at any step along the way, you can refer to the official Github docs here

Question 2



30 points

Consider the following vector

```
my_vec <- c(
    "+0.07",
    "-0.07",
    "+0.25",
    "-0.84",
    "+0.32",
    "-0.24",
    "-0.97",
    "-0.36",
    "+1.76",
    "-0.36")
```

For the following questions, provide your answers in a code cell.

1. What data type does the vector contain?

```
typeof(my_vec)
```

[1] "character"

2. Create two new vectors called my_vec_double and my_vec_int which converts my_vec to Double & Integer types, respectively.

```
my_vec_double <- as.double(my_vec)</pre>
  my_vec_double
 [1] 0.07 -0.07 0.25 -0.84 0.32 -0.24 -0.97 -0.36 1.76 -0.36
  my_vec_int <- as.integer(my_vec)</pre>
  my_vec_int
 [1] 0 0 0 0 0 0 0 0 1 0
  3. Create a new vector my_vec_bool which comprises of:
       • TRUEif an element in my_vec_double is \leq 0
       • FALSE if an element in my\_vec\_double is \geq 0
    How many elements of my_vec_double are greater than zero?
  my_vec_bool <- c()</pre>
  for (i in 1:length(my_vec_double)) {
    if(my_vec_double[i] < 0){</pre>
      my_vec_bool[i] <- 'TRUE'</pre>
    }
    else{
      my_vec_bool[i] <- 'FALSE'</pre>
    }
  my_vec_bool
 [1] "FALSE" "TRUE" "FALSE" "TRUE" "FALSE" "TRUE" "TRUE" "FALSE"
[10] "TRUE"
  sum(my_vec_bool=='TRUE')
[1] 6
  4. Sort the values of my_vec_double in ascending order.
  sort(my_vec_double, decreasing = FALSE)
 [1] -0.97 -0.84 -0.36 -0.36 -0.24 -0.07 0.07 0.25 0.32 1.76
```

Question 3



In this question we will get a better understanding of how R handles large data structures in memory.

1. Provide R code to construct the following matrices:

```
\begin{bmatrix} 1 & 2 & 3 & 4 & 5 & \dots & 100 \\ 1 & 4 & 9 & 16 & 25 & \dots & 10000 \end{bmatrix}
                                 \begin{bmatrix} 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix}
                                                    and
        ::: {.cell}
    matrix(1:9, nrow = 3, ncol = 3, byrow=TRUE)
        [,1] [,2] [,3]
[1,]
             1
                     2
                              3
[2,]
             4
                     5
                              6
[3,]
             7
                     8
                              9
::: ::: {.cell}
    vec1 <- c(1:100)
    vec2 \leftarrow vec1^2
    vec3 <- c(vec1,vec2)</pre>
    matrix(
       vec3,
       nrow = 2,
       ncol = 100,
       byrow = TRUE
```

```
[,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
[1,]
        1
              2
                   3
                         4
                              5
                                    6
                                         7
                                               8
                                                    9
                                                          10
                                                                 11
                                                                       12
                                                                              13
                                                                                     14
[2,]
        1
              4
                   9
                        16
                             25
                                        49
                                                         100
                                                                121
                                                                             169
                                                                                    196
                                   36
                                              64
                                                   81
                                                                      144
     [,15] [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] [,24] [,25] [,26]
[1,]
        15
               16
                      17
                            18
                                   19
                                         20
                                                21
                                                       22
                                                             23
                                                                    24
                                                                           25
                                                                                 26
[2,]
                                                                          625
       225
              256
                    289
                           324
                                  361
                                        400
                                               441
                                                      484
                                                            529
                                                                   576
                                                                                676
```

```
[,27] [,28] [,29] [,30] [,31] [,32] [,33] [,34] [,35] [,36] [,37] [,38]
[1,]
               28
                      29
                             30
                                    31
                                           32
                                                  33
                                                        34
                                                               35
                                                                      36
         27
                                                                             37
                                                                                    38
[2,]
       729
              784
                     841
                            900
                                   961
                                        1024
                                               1089
                                                      1156
                                                             1225
                                                                    1296
                                                                           1369
                                                                                  1444
     [,39]
           [,40] [,41]
                          [,42] [,43] [,44] [,45]
                                                     [,46]
                                                            [,47]
                                                                   [,48]
                                                                         [,49] [,50]
[1,]
        39
               40
                      41
                             42
                                    43
                                           44
                                                  45
                                                        46
                                                               47
                                                                      48
                                                                             49
                                                                                    50
[2,]
      1521
             1600
                    1681
                           1764
                                        1936
                                               2025
                                                      2116
                                                             2209
                                                                           2401
                                  1849
                                                                    2304
                                                                                  2500
                                                     [,58]
     [,51]
            [,52]
                   [,53]
                          [,54]
                                [,55]
                                       [,56]
                                              [,57]
                                                            [,59]
                                                                   [,60]
                                                                          [,61]
                                                                                [,62]
[1,]
        51
               52
                      53
                             54
                                    55
                                           56
                                                  57
                                                        58
                                                               59
                                                                      60
                                                                             61
                                                                                    62
[2,]
      2601
             2704
                    2809
                           2916
                                 3025
                                        3136
                                               3249
                                                      3364
                                                             3481
                                                                    3600
                                                                           3721
                                                                                  3844
     [,63]
            [,64]
                   [,65]
                         [,66] [,67]
                                       [,68] [,69]
                                                     [,70]
                                                            [,71]
                                                                   [,72]
                                                                          [,73]
                                                                                [,74]
[1,]
        63
               64
                      65
                             66
                                    67
                                           68
                                                  69
                                                        70
                                                               71
                                                                      72
                                                                             73
                                                                                    74
             4096
                    4225
[2,]
      3969
                           4356
                                  4489
                                        4624
                                               4761
                                                      4900
                                                             5041
                                                                    5184
                                                                           5329
                                                                                 5476
     [,75]
            [,76]
                   [,77]
                          [,78]
                                 [,79]
                                       [,80]
                                              [,81]
                                                     [,82]
                                                            [,83]
                                                                   [,84]
                                                                          [,85]
                                                                                 [,86]
        75
               76
                      77
                             78
                                    79
                                           80
                                                  81
                                                        82
                                                               83
                                                                      84
                                                                             85
[1,]
                                                                                    86
      5625
             5776
                    5929
                           6084
                                                                           7225
[2,]
                                 6241
                                        6400
                                               6561
                                                      6724
                                                             6889
                                                                    7056
                                                                                 7396
     [,87]
            [88,]
                   [,89]
                          [,90]
                                 [,91]
                                       [,92]
                                              [,93]
                                                     [,94]
                                                            [,95]
                                                                   [,96]
                                                                          [,97]
                                                                                 [,98]
[1,]
        87
               88
                      89
                             90
                                    91
                                           92
                                                  93
                                                        94
                                                               95
                                                                      96
                                                                             97
                                                                                    98
             7744
[2,]
      7569
                    7921
                          8100
                                 8281
                                        8464
                                               8649
                                                      8836
                                                             9025
                                                                    9216
                                                                          9409
                                                                                 9604
     [,99]
            [,100]
[1,]
        99
               100
[2,]
      9801
             10000
```

:::



Recall the discussion in class on how R fills in matrices

In the next part, we will discover how knowledge of the way in which a matrix is stored in memory can inform better code choices. To this end, the following function takes an input n and creates an $n \times n$ matrix with random entries.

```
generate_matrix <- function(n){
    return(
          matrix(
          rnorm(n^2),
          nrow=n
        )
    )
}</pre>
```

For example:

```
generate_matrix(4)
```

```
[,1] [,2] [,3] [,4]
[1,] -0.9440637 0.2834577 0.52954119 1.0623674
[2,] -0.2662691 0.1334337 -0.98357101 2.6584331
[3,] -1.0945384 1.4056832 -0.07112489 1.4536182
[4,] 0.7110382 0.6207309 1.13202080 -0.5753715
```

Let M be a fixed 50×50 matrix

```
M <- generate_matrix(50)
mean(M)</pre>
```

[1] -0.04947487

2. Write a function row_wise_scan which scans the entries of M one row after another and outputs the number of elements whose value is ≥ 0 . You can use the following starter code

```
row_wise_scan <- function(x){
    n <- nrow(x)
    m <- ncol(x)

# Insert your code here
    count <- 0
    for(row in 1:n){
        if(x[row,col] > 0){
            count <- count + 1
        }
    }
}
return(count)
}</pre>
```

3. Similarly, write a function col_wise_scan which does exactly the same thing but scans the entries of M one column after another

```
col_wise_scan <- function(x){
    count <- 0
    n <- nrow(x)
    m <- ncol(x)

    for(col in 1:n){
        if(x[row,col] > 0){
            count <- count + 1
        }
    }
}

return(count)
}</pre>
```

You can check if your code is doing what it's supposed to using the function here¹

4. Between col_wise_scan and row_wise_scan, which function do you expect to take shorter to run? Why?

#I expect the row_wise_scan to run faster than the column counterpart because typically ac

5. Write a function time_scan which takes in a method f and a matrix M and outputs the amount of time taken to run f(M)

```
time_scan <- function(f, M){
   initial_time <- Sys.time() # Write your code here
   f(M)
   final_time <- Sys.time() # Write your code here

   total_time_taken <- final_time - initial_time
   return(total_time_taken)
}</pre>
```

Provide your output to

```
list(
    row_wise_time = time_scan(row_wise_scan, M),
    col_wise_time = time_scan(row_wise_scan, M)
)
```

 $^{^1\}mathrm{If}$ your code is right, the following code should evaluate to be \mathtt{TRUE}

```
$row_wise_time
Time difference of 0.006244421 secs
$col_wise_time
Time difference of 0.0001690388 secs
Which took longer to run? ::: {.cell}
  #The row function took longer to run.
:::
  6. Repeat this experiment now when:
       • M is a 100 \times 100 matrix
       • M is a 1000 \times 1000 matrix
       • M is a 5000 \times 5000 matrix
  M <- generate_matrix(100)</pre>
  list(
       row_wise_time = time_scan(row_wise_scan, M),
       col_wise_time = time_scan(row_wise_scan, M)
   )
$row_wise_time
Time difference of 0.0007793903 secs
$col_wise_time
Time difference of 0.0006275177 secs
  M <- generate_matrix(1000)</pre>
  list(
       row_wise_time = time_scan(row_wise_scan, M),
       col_wise_time = time_scan(row_wise_scan, M)
   )
$row_wise_time
Time difference of 0.06817174 secs
$col_wise_time
Time difference of 0.06753349 secs
```

```
M <- generate_matrix(5000)
list(
    row_wise_time = time_scan(row_wise_scan, M),
    col_wise_time = time_scan(row_wise_scan, M)
)

$row_wise_time
Time difference of 2.71675 secs

$col_wise_time
Time difference of 2.703362 secs

What can you conclude? ::: {.cell}

#It seems like the row function still takes longer in all the experiments.
:::</pre>
```

Appendix

Print your R session information using the following command

```
sessionInfo()
R version 4.2.2 Patched (2022-11-10 r83330)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Ubuntu 20.04.5 LTS
Matrix products: default
        /usr/lib/x86_64-linux-gnu/blas/libblas.so.3.9.0
LAPACK: /usr/lib/x86_64-linux-gnu/lapack/liblapack.so.3.9.0
locale:
 [1] LC_CTYPE=en_US.UTF-8
                                LC_NUMERIC=C
 [3] LC_TIME=en_US.UTF-8
                                LC_COLLATE=en_US.UTF-8
 [5] LC_MONETARY=en_US.UTF-8
                                LC_MESSAGES=en_US.UTF-8
 [7] LC_PAPER=en_US.UTF-8
                                LC_NAME=C
```

```
[9] LC_ADDRESS=C LC_TELEPHONE=C
```

[11] LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C

attached base packages:

[1] stats graphics grDevices datasets utils methods base

loaded via a namespace (and not attached):

```
[1] compiler_4.2.2 fastmap_1.1.0 cli_3.6.0 htmltools_0.5.4
```

[5] tools_4.2.2 yaml_2.3.7 rmarkdown_2.20 knitr_1.42

[9] xfun_0.36 digest_0.6.31 jsonlite_1.8.4 rlang_1.0.6

[13] renv_0.16.0-53 evaluate_0.20

This resulted in TRUE but I could not compile pdf and html due to an error with %>%.

 $\#\{R\}$ # sapply(1:100, function(i) { # x <- generate_matrix(100) #

row_wise_scan(x) == col_wise_scan(x) # }) %>% sum == 100 #