Homework 1

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Link to the Github repository

Due: Sun, Jan 29, 2023 @ 11:59pm

Please read the instructions carefully before submitting your assignment.

- 1. This assignment requires you to:
 - Upload your Quarto markdown files to a git repository
 - Upload a PDF file on Canvas
- 2. Don't collapse any code cells before submitting.
- 3. Remember to make sure all your code output is rendered properly before uploading your submission.

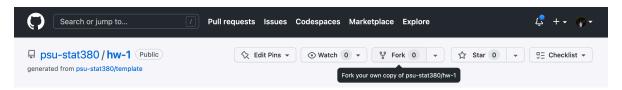
Please add your name to the the author information in the frontmatter before submitting your assignment.

Question 1



In this question, we will walk through the process of *forking* a git repository and submitting a *pull request*.

1. Navigate to the Github repository here and fork it by clicking on the icon in the top right



Provide a sensible name for your forked repository when prompted.

2. Clone your Github repository on your local machine

```
$ git clone <<insert your repository url here>>
$ cd hw-1
```

Alternatively, you can use Github codespaces to get started from your repository directly.

3. In order to activate the R environment for the homework, make sure you have renv installed beforehand. To activate the renv environment for this assignment, open an instance of the R console from within the directory and type

```
renv::activate()
```

Follow the instrutions in order to make sure that renv is configured correctly.

- 4. Work on the *remaining part* of this assignment as a .qmd file.
 - Create a PDF and HTML file for your output by modifying the YAML frontmatter for the Quarto .qmd document
- 5. When you're done working on your assignment, push the changes to your github repository.

6. Navigate to the original Github repository here and submit a pull request linking to your repository.

Remember to **include your name** in the pull request information!

If you're stuck at any step along the way, you can refer to the official Github docs here

Question 2



Consider the following vector

```
my_vec <- c(
    "+0.07",
    "-0.07",
    "+0.25",
    "-0.84",
    "+0.32",
    "-0.24",
    "-0.97",
    "-0.36",
    "+1.76",
    "-0.36")
```

For the following questions, provide your answers in a code cell.

1. What data type does the vector contain?

```
typeof(my_vec)
```

[1] "character"

2. Create two new vectors called my_vec_double and my_vec_int which converts my_vec to Double & Integer types, respectively,

```
my_vec_double <- as.numeric(my_vec)
my_vec_double</pre>
```

```
[1] 0.07 -0.07 0.25 -0.84 0.32 -0.24 -0.97 -0.36 1.76 -0.36
  typeof(my_vec_double)
[1] "double"
  my_vec_int <- as.integer(my_vec)</pre>
  my_vec_int
 [1] 0 0 0 0 0 0 0 0 1 0
  typeof(my_vec_int)
[1] "integer"
  3. Create a new vector my_vec_bool which comprises of:
       • TRUE an element in my_vec_double is \leq 0
       • FALSE if an element in my_vec_double is \geq 0
    How many elements of my_vec_double are greater than zero?
  my_vec_bool <- c()</pre>
  count = 0
  for (i in my_vec_double) {
    if (i > 0) {
      my_vec_bool <- append(my_vec_bool, "TRUE", after = length(my_vec_bool))</pre>
      count <- count + 1
    }
    else{
           my_vec_bool <- append(my_vec_bool, "FALSE", after = length(my_vec_bool))</pre>
    }
  my_vec_bool
 [1] "TRUE" "FALSE" "TRUE" "FALSE" "FALSE" "FALSE" "FALSE" "TRUE"
```

[10] "FALSE"

```
print(paste("There are", count, "elements in 'my_vec_double' greater than zero"))
```

- [1] "There are 4 elements in 'my_vec_double' greater than zero"
 - 4. Sort the values of my_vec_double in ascending order.

```
sort(my_vec_double)
```

[1] -0.97 -0.84 -0.36 -0.36 -0.24 -0.07 0.07 0.25 0.32 1.76

Question 3



9 50 points

In this question we will get a better understanding of how R handles large data structures in memory.

1. Provide R code to construct the following matrices:

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \quad \text{and} \quad \begin{bmatrix} 1 & 2 & 3 & 4 & 5 & \dots & 100 \\ 1 & 4 & 9 & 16 & 25 & \dots & 10000 \end{bmatrix}$$



Recall the discussion in class on how R fills in matrices

```
matrix(
  c(1,2,3,4,5,6,7,8,9),
  nrow = 3,
  byrow = TRUE
)
```

```
nrow = 2,
     byrow = TRUE
  )
     [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11] [,12] [,13] [,14]
[1,]
                    3
                          4
                                5
                                      6
                                           7
                                                 8
                                                       9
                                                             10
                                                                           12
         1
              2
                                                                    11
                                                                                  13
                                                                                        14
[2,]
         1
               4
                    9
                         16
                               25
                                    36
                                          49
                                                64
                                                      81
                                                            100
                                                                   121
                                                                         144
                                                                                169
                                                                                       196
           [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] [,24] [,25] [,26]
[1,]
         15
                16
                       17
                             18
                                    19
                                           20
                                                  21
                                                         22
                                                                23
                                                                       24
                                                                              25
                                                                                     26
[2,]
        225
              256
                     289
                            324
                                   361
                                                 441
                                                               529
                                                                             625
                                          400
                                                        484
                                                                      576
                                                                                    676
                                                                    [,36] [,37] [,38]
            [,28] [,29]
                          [,30] [,31] [,32] [,33] [,34]
                                                             [,35]
     [,27]
[1,]
         27
                28
                       29
                             30
                                    31
                                           32
                                                  33
                                                         34
                                                                35
                                                                       36
                                                                              37
                                                                                     38
[2,]
        729
              784
                     841
                            900
                                   961
                                         1024
                                                1089
                                                       1156
                                                              1225
                                                                     1296
                                                                            1369
                                                                                   1444
     [,39]
            [,40]
                                 [,43]
                                        [,44]
                                               [,45]
                                                      [,46]
                                                             [,47]
                   [,41]
                          [,42]
                                                                    [,48]
                                                                          [,49] [,50]
[1,]
         39
                40
                       41
                             42
                                    43
                                           44
                                                  45
                                                         46
                                                                47
                                                                       48
                                                                              49
                                                                                     50
[2,]
                                  1849
                                         1936
                                                2025
                                                              2209
      1521
             1600
                    1681
                           1764
                                                       2116
                                                                     2304
                                                                            2401
                                                                                   2500
      [,51]
            [,52]
                   [,53]
                          [,54]
                                 [,55]
                                        [,56]
                                               [,57]
                                                      [,58]
                                                             [,59]
                                                                    [,60]
                                                                           [,61]
                                                                                 [,62]
[1,]
         51
                52
                       53
                             54
                                    55
                                           56
                                                  57
                                                         58
                                                                59
                                                                       60
                                                                              61
             2704
                    2809
                                                                           3721
[2,]
                           2916
                                  3025
                                         3136
                                                3249
                                                       3364
                                                              3481
      2601
                                                                     3600
                                                                                  3844
     [,63]
            [,64]
                   [,65]
                          [,66]
                                 [,67]
                                        [,68]
                                               [,69]
                                                      [,70]
                                                             [,71]
                                                                    [,72]
                                                                          [,73]
                                                                                  [,74]
                64
                      65
                             66
                                    67
                                           68
                                                  69
                                                         70
                                                                71
                                                                       72
                                                                              73
[1,]
         63
                                                                                     74
[2,]
      3969
             4096
                    4225
                           4356
                                  4489
                                         4624
                                                4761
                                                       4900
                                                              5041
                                                                     5184
                                                                            5329
                                                                                   5476
            [,76]
                          [,78]
                                 [,79]
                                        [,80]
                                               [,81]
                                                      [,82]
                                                             [,83]
                                                                    [,84] [,85]
                                                                                  [,86]
     [,75]
                   [,77]
[1,]
         75
                      77
                             78
                                    79
                                           80
                                                  81
                                                         82
                                                                83
                                                                              85
                76
                                                                       84
                                                                                     86
[2,]
      5625
             5776
                    5929
                           6084
                                  6241
                                         6400
                                                6561
                                                       6724
                                                              6889
                                                                     7056
                                                                            7225
                                                                                   7396
            [,88]
                   [,89]
                          [,90]
                                 [,91]
                                        [,92]
                                               [,93]
                                                      [,94]
                                                             [,95]
                                                                    [,96]
                                                                           [,97]
                                                                                  [,98]
      [,87]
```

In the next part, we will discover how knowledge of the way in which a matrix is stored in memory can inform better code choices. To this end, the following function takes an input n and creates an $n \times n$ matrix with random entries.

```
generate_matrix <- function(n){
    return(
        matrix(</pre>
```

matrix(

[1,]

[2,]

[1,]

[2,]

[,99]

[,100]

c((1:100),(1:100)²),

```
rnorm(n^2),
nrow = n
)
)
}
```

For example:

```
[,1] [,2] [,3] [,4]
[1,] -0.2191921 2.09241648 -0.7228653 -1.5910125
[2,] 1.7090320 -1.16638111 0.3353510 0.1824847
[3,] -1.2521427 0.37207166 -0.6304050 -0.1166592
[4,] -0.5812670 0.02301751 -0.1948661 1.2094028
```

Let M be a fixed 50×50 matrix

```
M <- generate_matrix(50)
mean(M)</pre>
```

[1] 0.01418053

2. Write a function row_wise_scan which scans the entries of M one row after another and outputs the number of elements whose value is ≥ 0 . You can use the following starter code

```
row_wise_scan <- function(x){
    n <- nrow(x)
    m <- ncol(x)

# Insert your code here
    count <- 0
    for(row in 1:n){
        if(x[row,col] >= 0){
            count <- count + 1
        }
    }
}</pre>
```

```
return(count)
}
```

3. Similarly, write a function col_wise_scan which does exactly the same thing but scans the entries of M one column after another

```
col_wise_scan <- function(x){
    count <- 0
    # Insert your code
    n <- nrow(x)
    m <- ncol(x)
    for(col in 1:m){
        if(x[row,col] >= 0){
            count <- count + 1
        }
    }
}
return(count)
}</pre>
```

You can check if your code is doing what it's supposed to using the function here¹

4. Between col_wise_scan and row_wise_scan, which function do you expect to take

```
library(tidyverse)
```

[1] TRUE

¹If your code is right, the following code should evaluate to be TRUE

shorter to run? Why?

I would think that the 'col_wise_scan' would take shorter to run. I think this because matrices in R naturally fill column by column, so I feel as if code that scans in the same way as how the matrix is filled, will result in a quicker scan of the matrix.

5. Write a function time_scan which takes in a method f and a matrix M and outputs the amount of time taken to run f(M)

```
time_scan <- function(f, M){
   initial_time <- Sys.time()
   f(M)
   final_time <- Sys.time()

  total_time_taken <- final_time - initial_time
   return(total_time_taken)
}</pre>
```

Provide your output to

```
list(
    row_wise_time = time_scan(row_wise_scan, M),
    col_wise_time = time_scan(col_wise_scan, M)
)
```

\$row_wise_time
Time difference of 0.0001559258 secs

\$col_wise_time
Time difference of 0.0001490116 secs

Which took longer to run?

The row_wise_scan function took longer to run than the col_wise_scan function.

- 6. Repeat this experiment now when:
 - M is a 100×100 matrix

```
M <- generate_matrix(100)
list(
    row_wise_time = time_scan(row_wise_scan, M),
    col_wise_time = time_scan(col_wise_scan, M)
)</pre>
```

```
$row_wise_time
Time difference of 0.0005640984 secs
$col_wise_time
Time difference of 0.0005571842 secs
    `M` is a $1000 \times 1000$ matrix
  M <- generate_matrix(1000)</pre>
  list(
      row_wise_time = time_scan(row_wise_scan, M),
      col_wise_time = time_scan(col_wise_scan, M)
$row_wise_time
Time difference of 0.06217003 secs
$col_wise_time
Time difference of 0.06008792 secs
    `M` is a $5000 \times 5000$ matrix
  M <- generate_matrix(5000)</pre>
  list(
      row_wise_time = time_scan(row_wise_scan, M),
      col_wise_time = time_scan(col_wise_scan, M)
  )
$row_wise_time
Time difference of 1.922903 secs
$col_wise_time
Time difference of 1.4631 secs
```

What can you conclude?

After running the time scans for both matrix scanning methods on various size matrices, I conclude that the col_wise_scan is faster than the row_wise_scan. The time difference starts out pretty small but as you increase the size of the matrix, the col_wise_scan begins to get noticeably quicker than the row_wise_scan

Appendix

Print your R session information using the following command

```
sessionInfo()
```

```
R version 4.2.2 (2022-10-31 ucrt)
```

Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 22000)

Matrix products: default

locale:

- [1] LC_COLLATE=English_United States.utf8
- [2] LC_CTYPE=English_United States.utf8
- [3] LC_MONETARY=English_United States.utf8
- [4] LC_NUMERIC=C
- [5] LC_TIME=English_United States.utf8

attached base packages:

[1] stats graphics grDevices datasets utils methods base

other attached packages:

- [1] forcats_0.5.2 stringr_1.5.0 dplyr_1.0.10 purrr_1.0.1 [5] readr_2.1.3 tidyr_1.2.1 tibble_3.1.8 ggplot2_3.4.0
- [9] tidyverse_1.3.2

loaded via a namespace (and not attached):

| [1] | tidyselect_1.2.0 | xfun_0.36 | haven_2.5.1 |
|------|---------------------------|------------------|---------------------|
| [4] | gargle_1.2.1 | colorspace_2.0-3 | vctrs_0.5.1 |
| [7] | <pre>generics_0.1.3</pre> | htmltools_0.5.4 | yaml_2.3.6 |
| [10] | utf8_1.2.2 | rlang_1.0.6 | pillar_1.8.1 |
| [13] | withr_2.5.0 | glue_1.6.2 | DBI_1.1.3 |
| [16] | dbplyr_2.2.1 | readxl_1.4.1 | modelr_0.1.10 |
| [19] | lifecycle_1.0.3 | munsell_0.5.0 | gtable_0.3.1 |
| [22] | cellranger_1.1.0 | rvest_1.0.3 | evaluate_0.20 |
| [25] | knitr_1.41 | tzdb_0.3.0 | fastmap_1.1.0 |
| [28] | fansi_1.0.3 | broom_1.0.2 | renv_0.16.0-53 |
| [31] | backports_1.4.1 | scales_1.2.1 | googlesheets4_1.0.1 |
| [34] | jsonlite_1.8.4 | fs_1.5.2 | hms_1.1.2 |
| [37] | digest_0.6.31 | stringi_1.7.12 | grid_4.2.2 |
| [40] | cli_3.6.0 | tools_4.2.2 | magrittr_2.0.3 |

| [43] | crayon_1.5.2 | pkgconfig_2.0.3 | ellipsis_0.3.2 |
|------|----------------------------|------------------|------------------------------|
| [46] | xml2_1.3.3 | reprex_2.0.2 | <pre>googledrive_2.0.0</pre> |
| [49] | <pre>lubridate_1.9.0</pre> | timechange_0.2.0 | assertthat_0.2.1 |
| [52] | rmarkdown_2.20 | httr_1.4.4 | rstudioapi_0.14 |
| [55] | R6_2.5.1 | compiler_4.2.2 | |