

1. **\*\*Initial Choice:\*\***

- The contestant initially chooses one of the three doors. Let's say they choose door 1.

Initial State:

-----  
| X | ? | ? |  
-----

- X represents the door chosen by the contestant, and ? represents the other two unchosen doors.

2. **\*\*Host Reveals a Door:\*\***

- As the host (Maeve), I, who know where the prize is, open one of the other doors that doesn't have the prize. Let's say I open door 3 and reveal nothing.

After Host Reveals Door 3:

-----  
| X | ? | (reveal) |  
-----

- Now, the contestant is faced with a choice: Stick with door 1 or switch to the remaining unopened door (door 2).

3. **\*\*Probability Distribution:\*\***

- Initially, there was a  $\frac{1}{3}$  chance that the contestant picked the door with the prize and a  $\frac{2}{3}$  chance that the prize was behind one of the other doors.

Probability Distribution:

-----  
| P | P | (not P) |  
-----

- P represents the door with the prize, and (not P) represents doors without the prize.

4. **\*\*Switching Strategy:\*\***

- When the host opens door 3, the probability distribution updates:

Probability Distribution after Host Reveals Door 3:

-----  
| P | (not P) | (not P) |  
-----

- The 2/3 probability of the prize being behind one of the other doors now concentrates on the remaining unopened door (door 2).

5. **\*\*Conclusion:\*\***

- Therefore, if the contestant switches to the last remaining door (door 2), they have a 2/3 chance of winning the prize. If they stick with their initial choice (door 1), they only have a 1/3 chance.

In summary, the optimal strategy is to switch doors to maximize the chance of winning the prize.