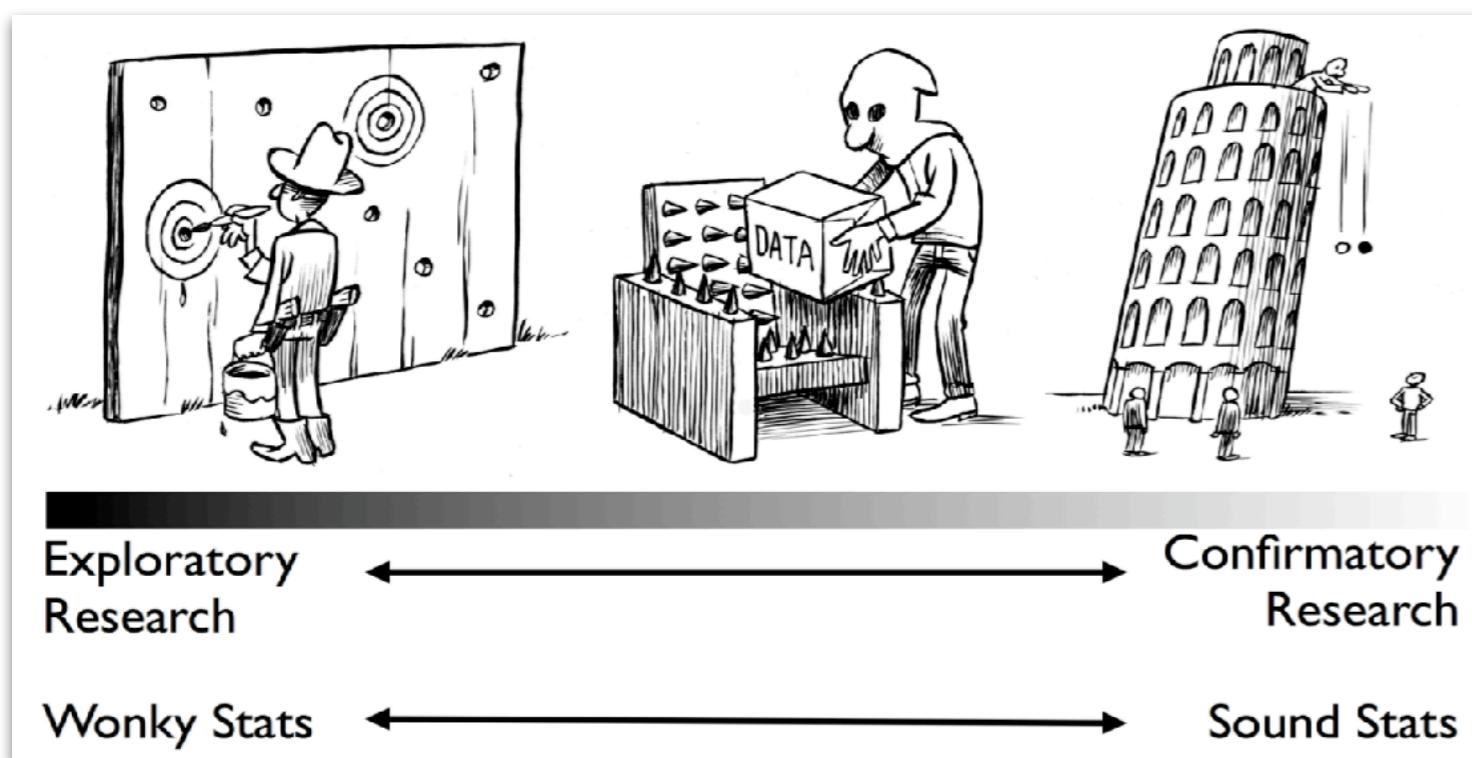


Power analysis



Chat

What is the strangest gift you have ever received?

To: Everyone ▾

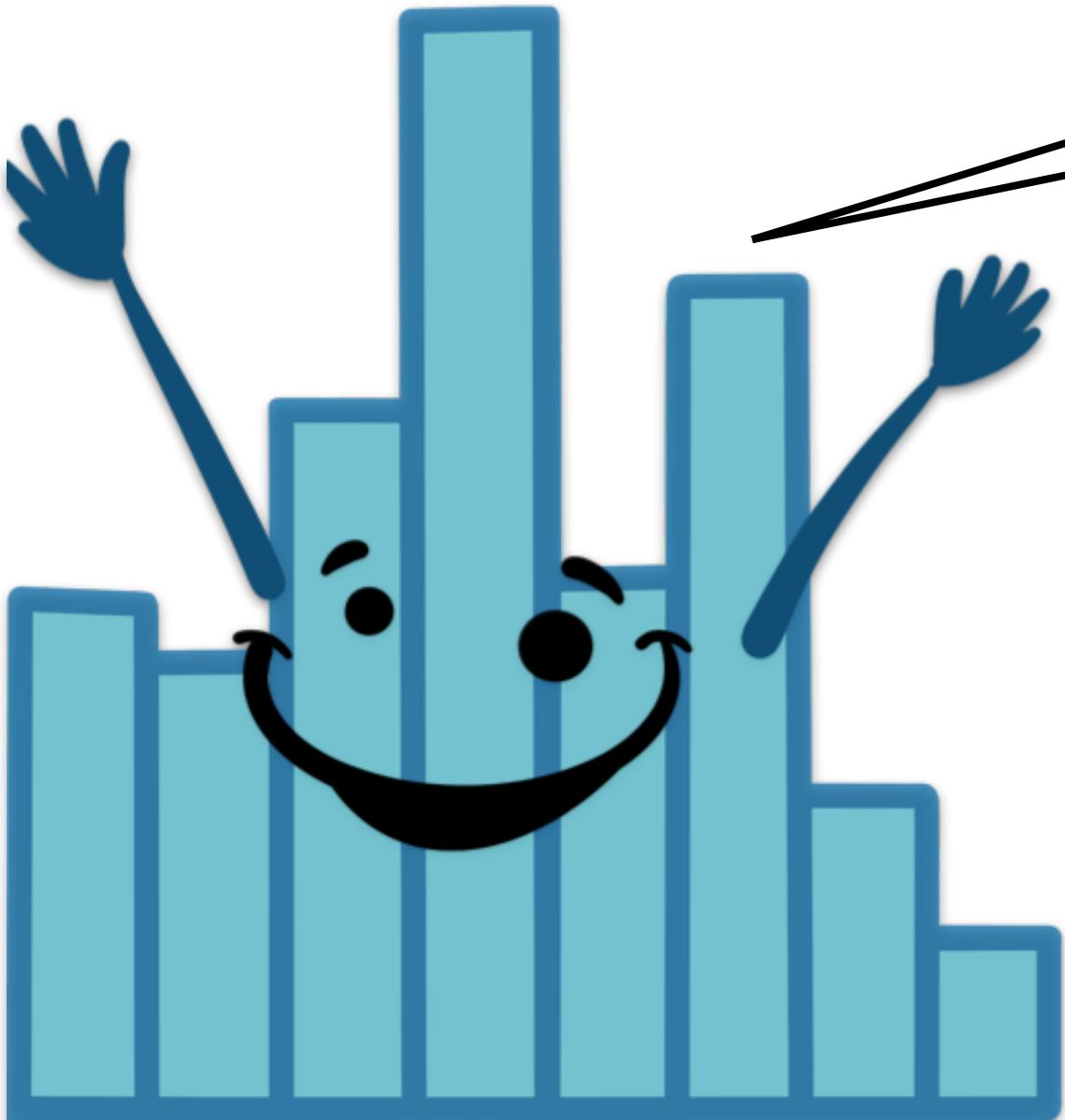
Type message here...

More ▾

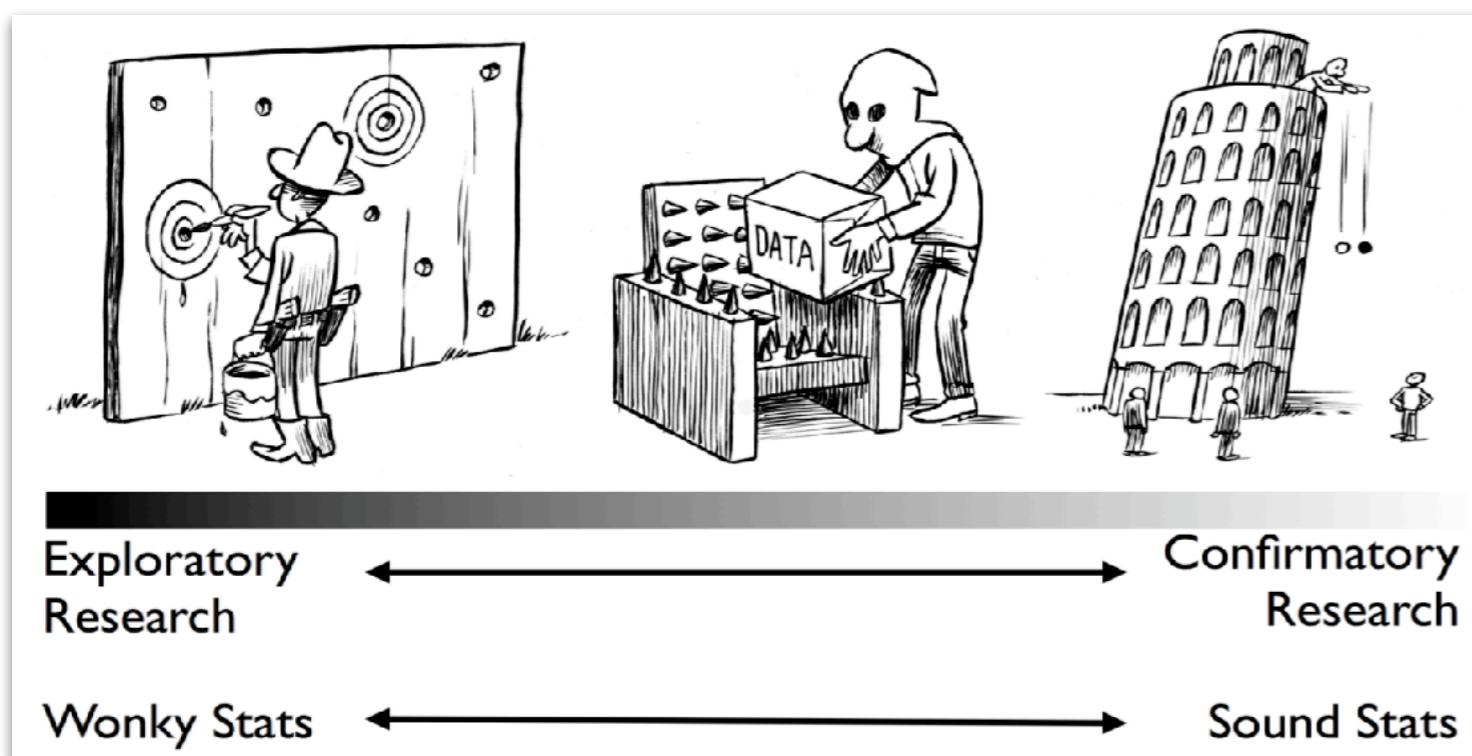


02/12/2021

Remember to
record the
lecture!



Power analysis



Chat

What is the strangest gift you have ever received?

To: Everyone ▾

Type message here...

More ▾



02/12/2021

Things that came up

Go! Go! Linear model



Indrajeet Patil
@patilindrajeets

...

Your periodic reminder that the most common statistical tests are nothing but special cases of linear models 🕵️

[lindeloev.github.io/tests-as-linear...](https://lindeloev.github.io/tests-as-linear/)

I wish someone had pointed out this beautiful simplicity and parsimony when I was learning statistics 🧑

#rstats

Common statistical tests are linear models
Last updated: 28 June, 2019. Also check out the [Python version](#).

Common name	Built-in function in R	Equivalent linear model in R	Exact?	The linear model in words	Icon
y ~ independent of x P: One-sample t-test N: Wilcoxon signed-rank	t.test(y) wilcox.test(y)	lm(y ~ 1) lm(signed_rank(y) ~ 1)	✓ for N > 14	One number (intercept, i.e., the mean) predicts y. -(Same, but it predicts the signed rank of y.)	
P: Paired-sample t-test N: Wilcoxon matched pairs	t.test(y1, y2, paired=TRUE) wilcox.test(y1, y2, paired=TRUE)	lm(y2 - y1 ~ 1) lm(signed_rank(y2 - y1) ~ 1)	✓ for N > 14	One intercept predicts the pairwise y1-y2 differences. -(Same, but it predicts the signed rank of y2-y1.)	
y ~ continuous x P: Pearson correlation N: Spearman correlation	cor.test(x, y, method='Pearson') cor.test(x, y, method='Spearman')	cor.test(x, y, method='Pearson') cor.test(x, y, method='Spearman')		lm(y ~ 1 + x) lm(rank(y) ~ 1 + rank(x))	
y ~ discrete x P: Two-sample t-test P: Welch's t-test N: Mann-Whitney U	t.test(y1, y2, var.equal=TRUE) t.test(y1, y2, var.equal=FALSE) wilcox.test(y1, y2)	t.test(y1, y2, var.equal=TRUE) t.test(y1, y2, var.equal=FALSE) wilcox.test(y1, y2)	✓ ✓ for N > 11	lm(y ~ 1 + G ₂) ^a gls(y ~ 1 + G ₂ , weights=...) ^b lm(signed_rank(y) ~ 1 + G ₂) ^a	
Simple regression: lm(y ~ 1 + x)					
Multiple regression: lm(y ~ 1 + x₁ + x₂ + ...)					
P: One-way ANOVA N: Kruskal-Wallis	aov(y ~ group)	lm(y ~ 1 + G ₂ + G ₃ + ... + G _N) ^a lm(rank(y) ~ 1 + G ₂ + G ₃ + ... + G _N) ^a	✓ ✓ for N > 11	An intercept for group 1 (plus a slope on x). -(Same, but it predicts the rank of y.)	
P: One-way ANCOVA	aov(y ~ group + x)	lm(y ~ 1 + G ₂ + G ₃ + ... + G _N + x) ^a	✓	- (Same, but plus a slope on x). Note: this is discrete AND continuous.	
P: Two-way ANOVA	aov(y ~ group * sex)	lm(y ~ 1 + G ₂ + G ₃ + ... + G _N + S ₂ + S ₃ + ... + S _K + G ₂ *S ₂ + G ₃ *S ₃ + ... + G _N *S _K) ^a	✓	Interaction term: changing sex . Note: G ₂ to N is an Indicator (0 or 1) . Similarly for S ₂ to K for sex. The first level of S ₂ for sex and the third is the group .	
Counts ~ discrete x N: Chi-square test	chisq.test(groupXsex_table)	Equivalent log-linear model glm(y ~ 1 + G ₂ + G ₃ + ... + G _N + S ₂ + S ₃ + ... + S _K + G ₂ *S ₂ + G ₃ *S ₃ + ... + G _N *S _K , family=...) ^a	✓	Interaction term: (Same as Two-way ANOVA). Note: Run glm using the following arguments: glm(y ~ 1 + G ₂ + G ₃ + ... + G _N + S ₂ + S ₃ + ... + S _K + G ₂ *S ₂ + G ₃ *S ₃ + ... + G _N *S _K , family=...). As linear-model, the Chi-square test is <code>glm(y ~ 1 + G₂ + G₃ + ... + G_N + S₂ + S₃ + ... + S_K + G₂*S₂ + G₃*S₃ + ... + G_N*S_K, family=...)</code> where α and β are proportions. See more info in the assumptions note .	
N: Goodness of fit	chisq.test(y)	glm(y ~ 1 + G ₂ + G ₃ + ... + G _N , family=...) ^a	✓	(Same as One-way ANOVA and Chi-square test).	

See worked examples and more details at the accompanying notebook: <https://lindeloev.github.io/tests-as-linear/>

^a See the note to the two-way ANOVA for explanation of the notation.
^b Same model, but with one variance per group: `gls(value ~ 1 + G2, weights = varIdent(form = ~1|group), method="ML")`.

Jonas K. Lindeløv

12:04 AM · Feb 12, 2021 · Twitter Web App

102 Retweets 6 Quote Tweets 373 Likes

Common statistical tests are linear models

Last updated: 28 June, 2019. Also check out the [Python version](#)!

See worked examples and notebook: <https://lindeloev.github.io/tests-as-linear/>

Common name	Built-in function in R	Equivalent linear model in R	Exact?	The linear model in words
y is independent of x P: One-sample t-test N: Wilcoxon signed-rank	t.test(y) wilcox.test(y)	lm(y ~ 1) lm(signed_rank(y) ~ 1)	✓ for N > 14	One number (intercept, i.e., the mean) predicts y. -(Same, but it predicts the signed rank of y.)
P: Paired-sample t-test N: Wilcoxon matched pairs	t.test(y ₁ , y ₂ , paired=TRUE) wilcox.test(y ₁ , y ₂ , paired=TRUE)	lm(y ₂ - y ₁ ~ 1) lm(signed_rank(y ₂ - y ₁) ~ 1)	✓ for N > 14	One intercept predicts the pairwise y ₁ -y ₂ differences. -(Same, but it predicts the signed rank of y ₂ -y ₁ .)
y ~ continuous x P: Pearson correlation N: Spearman correlation	cor.test(x, y, method='Pearson') cor.test(x, y, method='Spearman')	cor.test(x, y, method='Pearson') cor.test(x, y, method='Spearman')		lm(y ~ 1 + x) lm(rank(y) ~ 1 + rank(x))
y ~ discrete x P: Two-sample t-test P: Welch's t-test N: Mann-Whitney U	t.test(y ₁ , y ₂ , var.equal=TRUE) t.test(y ₁ , y ₂ , var.equal=FALSE) wilcox.test(y ₁ , y ₂)	t.test(y ₁ , y ₂ , var.equal=TRUE) t.test(y ₁ , y ₂ , var.equal=FALSE) wilcox.test(y ₁ , y ₂)	✓ ✓ for N > 11	lm(y ~ 1 + G ₂) ^a gls(y ~ 1 + G ₂ , weights=...) ^b lm(signed_rank(y) ~ 1 + G ₂) ^a
Simple regression: lm(y ~ 1 + x)				
Multiple regression: lm(y ~ 1 + x₁ + x₂ + ...)				
P: One-way ANOVA N: Kruskal-Wallis	aov(y ~ group)	lm(y ~ 1 + G ₂ + G ₃ + ... + G _N) ^a lm(rank(y) ~ 1 + G ₂ + G ₃ + ... + G _N) ^a	✓ ✓ for N > 11	An intercept for group 1 (plus a slope on x). -(Same, but it predicts the rank of y.)
P: One-way ANCOVA	aov(y ~ group + x)	lm(y ~ 1 + G ₂ + G ₃ + ... + G _N + x) ^a	✓	- (Same, but plus a slope on x). Note: this is discrete AND continuous.
P: Two-way ANOVA	aov(y ~ group * sex)	lm(y ~ 1 + G ₂ + G ₃ + ... + G _N + S ₂ + S ₃ + ... + S _K + G ₂ *S ₂ + G ₃ *S ₃ + ... + G _N *S _K) ^a	✓	Interaction term: changing sex . Note: G ₂ to N is an Indicator (0 or 1) . Similarly for S ₂ to K for sex. The first level of S ₂ for sex and the third is the group .
Counts ~ discrete x N: Chi-square test	chisq.test(groupXsex_table)	Equivalent log-linear model glm(y ~ 1 + G ₂ + G ₃ + ... + G _N + S ₂ + S ₃ + ... + S _K + G ₂ *S ₂ + G ₃ *S ₃ + ... + G _N *S _K , family=...) ^a	✓	Interaction term: (Same as Two-way ANOVA). Note: Run glm using the following arguments: glm(y ~ 1 + G ₂ + G ₃ + ... + G _N + S ₂ + S ₃ + ... + S _K + G ₂ *S ₂ + G ₃ *S ₃ + ... + G _N *S _K , family=...). As linear-model, the Chi-square test is <code>glm(y ~ 1 + G₂ + G₃ + ... + G_N + S₂ + S₃ + ... + S_K + G₂*S₂ + G₃*S₃ + ... + G_N*S_K, family=...)</code> where α and β are proportions. See more info in the assumptions note .
N: Goodness of fit	chisq.test(y)	glm(y ~ 1 + G ₂ + G ₃ + ... + G _N , family=...) ^a	✓	(Same as One-way ANOVA and Chi-square test).

List of common parametric (P) non-parametric (N) tests and equivalent linear models. The notation $y \sim 1 + x$ is R shorthand for $y = 1 \cdot b + a \cdot x$ which most of us learned in school. Models in similar colors are highly similar, but really, notice how similar they *all* are across colors! For non-parametric models, the linear models are reasonable approximations for non-small sample sizes (see "Exact" column and click links to see simulations). Other less accurate approximations exist, e.g., Wilcoxon for the sign test and Goodness-of-fit for the binomial test. The signed rank function is `signed_rank = function(x) sign(x) * rank(x)`. The variables G and S are "dummy-coded" indicator variables (either 0 or 1) exploiting the fact that when $\Delta x = 1$ between categories the difference equals the slope. Subscripts (e.g., G₂ or y₂) indicate different columns in data. lm requires long-format data for all non-continuous models. All of this is exposed in greater detail and worked examples at <https://lindeloev.github.io/tests-as-linear/>.

^a See the note to the two-way ANOVA for explanation of the notation.

^b Same model, but with one variance per group: `gls(value ~ 1 + G2, weights = varIdent(form = ~1|group), method="ML")`.

<https://lindeloev.github.io/tests-as-linear/>

Excellent online book!

Preface
I Preliminaries
1 General Introduction
2 Basics of R
II Data
3 Data, variables & experimental desi...
4 Data Wrangling
5 Summary statistics
6 Data Visualization
III Bayesian Data Analysis
7 Basics of Probability Theory
8 Statistical models
9 Bayesian parameter estimation
10 Model Comparison
11 Bayesian hypothesis testing
IV Applied (generalized) linear mod...
12 Linear regression
13 Bayesian regression in practice
14 Categorical predictors
15 Generalized linear model
V Frequentist statistics
16 Null Hypothesis Significance Testing
17 Comparing frequentist and Bayesi...

☰ ⌂ A ⬇ ⌂

An Introduction to Data Analysis

Michael Franke

last rendered at: 2021-01-26 08:56:45

Preface

This book provides basic reading material for an introduction to data analysis. It uses R to handle, plot and analyze data. After covering the use of R for data wrangling and plotting, the book introduces key concepts of data analysis from a Bayesian and a frequentist tradition. This text is intended for use as a first introduction to statistics for an audience with some affinity towards programming, but no prior exposition to R.

Many people have supported this project actively by providing text, examples, code or technical support. Many thanks for their support to (in alphabetic order): Tobias Anton, Florence Bockting, Noa Kallioinen, Minseok Kang, Marcel Klehr, Özge Özenoglu, Maria Pershina, Timo Roettger, Polina Tsvilodub and Inga Wohlert.

An Introduction to Data Analysis



Logistics

Midterm

will be available shortly after class today

Psych 252 Midterm

My name goes here

2021-02-12 12:04:21

Introduction

This is a take-home exam. The exam is open notes and open book (in short, you can use any source of information you like as long as you work on the exam by yourself). The maximum score is 120 points. Please adhere to the honor code. Submit the midterm as a PDF on the canvas 'midterm' assignment by **Thursday, February 18th, 8pm**.

The late policy submission policy is:

- We will subtract 2% from your points for each hour that the midterm is submitted late but before midnight. For example, 2% will be subtracted if you submit between 8pm and 9pm, or 8% if you submit between 11pm and midnight.
- 20% will be subtracted if you submit after midnight on Thursday but before 8pm on Friday, February 19th.
- No points will be granted if you submit later than 8pm on Friday, February 19th.

For questions that require written responses, please make sure to show any relevant tables, summaries (e.g. from `lm()` or `anova()`), or visualizations. Some of the code chunks have existing code that you can use to build your code around.

When asked to report results, please do so like you would in a scientific article (see examples from class).

- Please leave the `\clearpage` commands where they are. This makes sure that each question is printed on a separate page in the pdf.
- Some code chunks are set to `eval=F`, make sure to set these to `eval=T` before knitting the final version.
- We note for each question how many points you can get. You can get up to 120 points in total.
- Good coding style matters! We will add or subtract up to 5 points depending on style.

If you have any questions about the midterm, please post them on Piazza addressed to the instructors only. We will answer your question and may choose to share both your question and our answer with the rest of the group.

Best of luck with the midterm!

Honor Code

The Honor Code is the University's statement on academic integrity written by students in 1921. It articulates University expectations of students and faculty in establishing and maintaining the highest standards in academic work:

1. The Honor Code is an undertaking of the students, individually and collectively:
 - a. that they will not give or receive aid in examinations; that they will not give or receive unpermitted aid in class work, in the preparation of reports, or in any other work that is to be used by the instructor as the basis of grading;
 - b. that they will do their share and take an active part in seeing to it that others as well as themselves uphold the spirit and letter of the Honor Code.

Part 1: Wash your hands!

A student investigated how effective different methods are for eliminating bacteria. She tested four different methods: (1) washing her hands with water only, (2) with regular soap, (3) with antibacterial soap (ABS), or (4) using an antibacterial spray (AS). She suspected that the number of bacteria on her hands might vary considerably from day to day. To account for this, she generated random numbers to determine on what day she would use which treatment. After each treatment, she placed her right hand on a sterile media plate to measure bacteria growth. She incubated each plate for 2 days after which she counted the bacteria colonies. She replicated this procedure 9 times for each of the four treatments.

Note: For statistical analysis purposes, we make the assumption that the individual measurements are independent from each other.

Part 2: Life satisfaction

In this exercise, we are interested in seeing what affects life satisfaction. We have a (fake) data set with the following variables:

Table 1: Variables in the satisfaction data set.

variable	description
id	participant id
age	age in years
kids	number of kids
jobsatis	job satisfaction (1 = not at all, 7 = very much)
marsatis	marital satisfaction (1 = not at all, 7 = very much)
lifsatis	life satisfaction (1 = not at all, 7 = very much)

Part 3: You've got the power!

In this exercise, we'll take a look at determining what group sample size we would need in order to achieve adequate statistical power to test our research hypothesis of interest. We will be using the data from "data/power.csv" and you can see its visualization in "figure/df_power.png".

Tip: We will provide saved checkpoints for each problem. Feel free to look ahead to compare your results with ours.

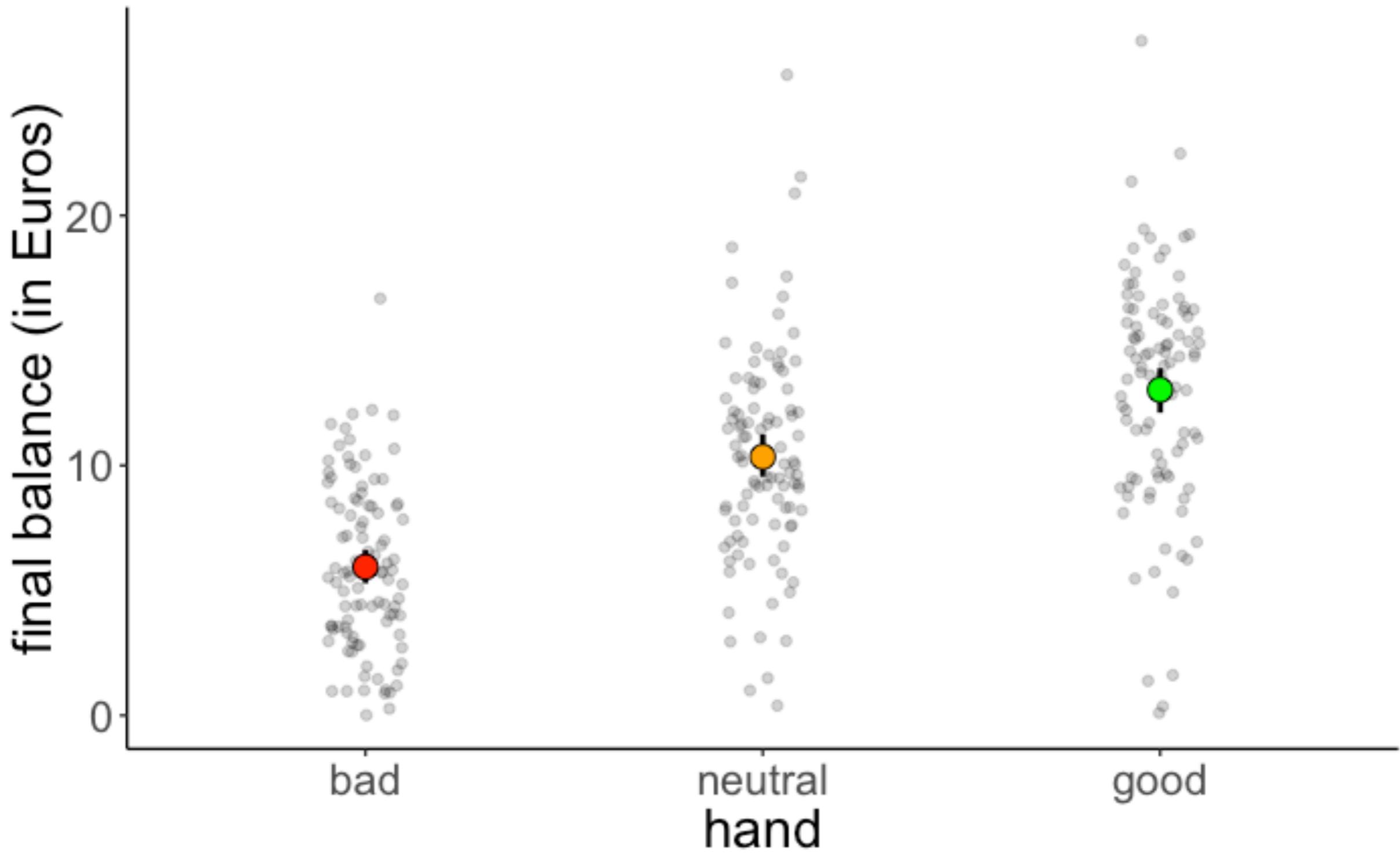
Plan for today

- Linear contrasts
 - Testing specific hypotheses with linear contrasts
 - emmeans for handling linear contrasts in R
- Power analysis
 - Making decisions
 - Calculating power
 - Effect sizes
 - Determining sample size
- Learn about more advanced simulation techniques in R
 - `map()`
 - list columns: `nest()`, `unnest()`

Linear contrasts

Testing (more) specific hypotheses with linear contrasts

Do better hands win more money?



Do better hands win more money?



ANOVA

Does card quality affect the final balance?



post-hoc tests

bad vs. neutral

neutral vs. good

Is there are more direct way of asking this question with a statistical model?

Contrasts

```
1 df.poker = df.poker %>%
2   mutate(hand_contrast = factor(hand,
3                                 levels = c("bad", "neutral", "good"),
4                                 labels = c(-1, 0, 1)),
5   hand_contrast = hand_contrast %>% as.character() %>% as.numeric())
```

participant	hand	balance	hand_contrast
1	bad	4.00	-1
2	bad	5.55	-1
3	bad	9.45	-1
51	neutral	11.74	0
52	neutral	10.04	0
53	neutral	9.49	0
101	good	10.86	1
102	good	8.68	1
103	good	14.36	1

Contrasts

```
1 df.poker = df.poker %>%
2   mutate(hand_contrast = factor(hand,
3                                 levels = c("bad", "neutral", "good"),
4                                 labels = c(-1, 0, 1)),
5   hand_contrast = hand_contrast %>% as.character() %>% as.numeric())
6
7 fit = lm(formula = balance ~ hand_contrast,
8         data = df.poker)
```

```
Call:
lm(formula = balance ~ hand_contrast, data = df.fit)

Residuals:
    Min      1Q  Median      3Q     Max
-13.214 -2.684 -0.019  2.444 15.858

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) 9.7715    0.2381   41.03 <2e-16 ***
hand_contrast 3.5424    0.2917   12.14 <2e-16 ***
---
Signif. codes:  0 '****' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.125 on 298 degrees of freedom
Multiple R-squared:  0.3311, Adjusted R-squared:  0.3289
F-statistic: 147.5 on 1 and 298 DF,  p-value: < 2.2e-16
```

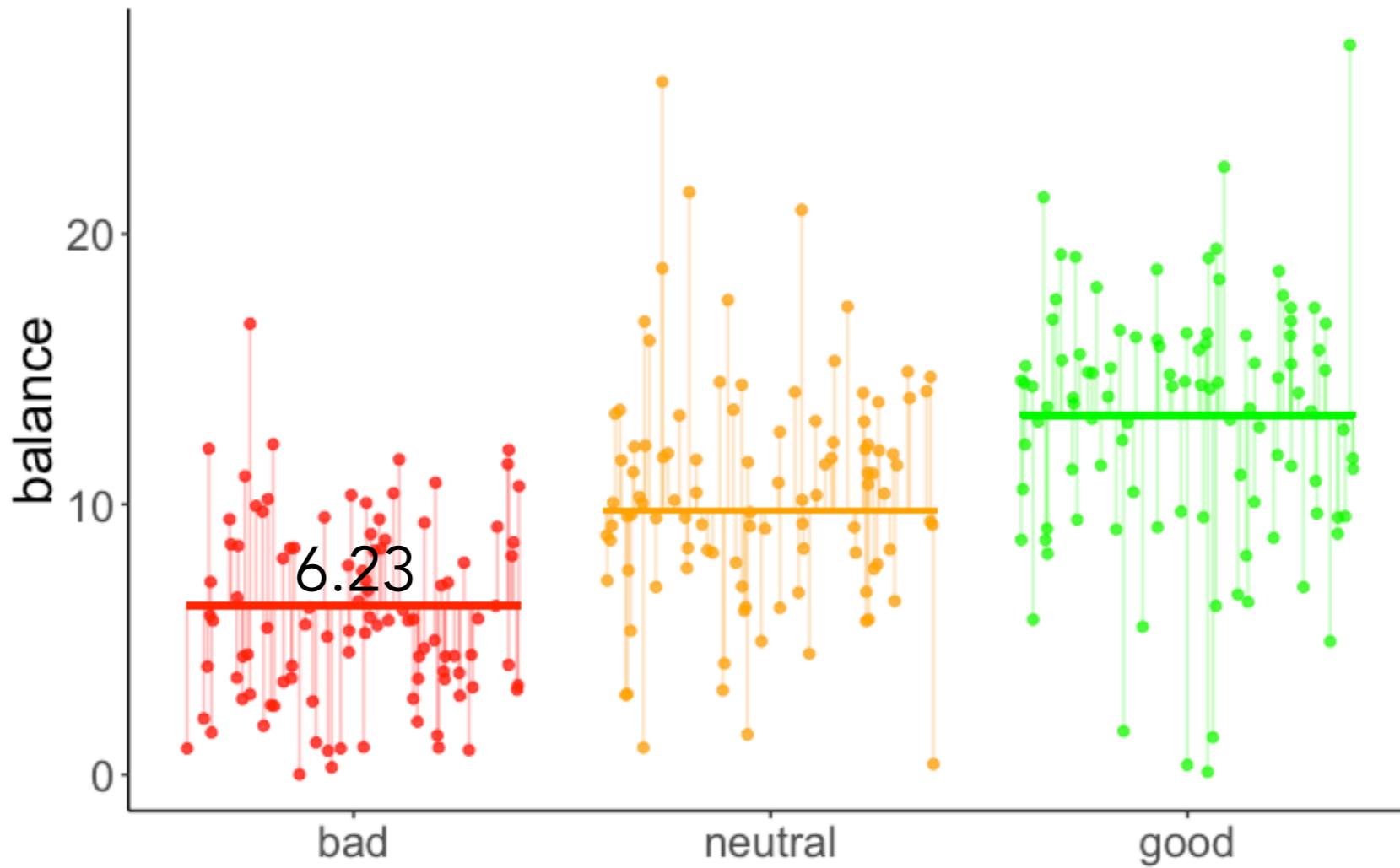
mean in neutral condition

significant contrast

Contrasts

name	estimate	std.error	statistic	p.value
intercept	9.77	0.24	41.03	0
contrast	3.54	0.29	12.15	0

$$\widehat{\text{balance}}_i = b_0 + b_1 \cdot \text{hand_contrast}$$



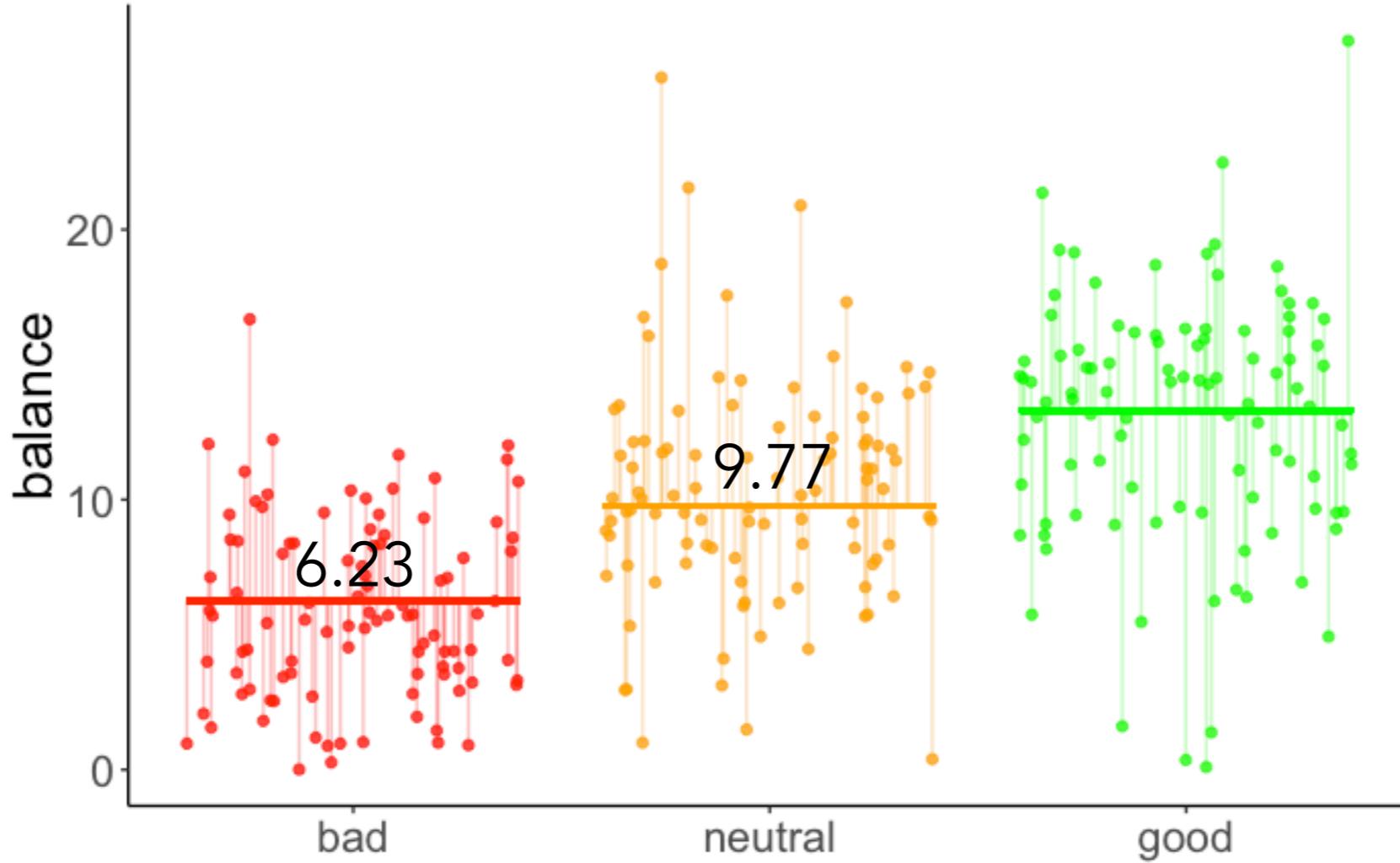
if contrast == -1

$$\begin{aligned}\widehat{\text{balance}}_i &= b_0 + b_1 \cdot \text{hand_contrast}_i \\ &= 9.77 + (-1) \cdot 3.54 = 6.23\end{aligned}$$

Contrasts

name	estimate	std.error	statistic	p.value
intercept	9.77	0.24	41.03	0
contrast	3.54	0.29	12.15	0

$$\widehat{\text{balance}}_i = b_0 + b_1 \cdot \text{hand_contrast}$$



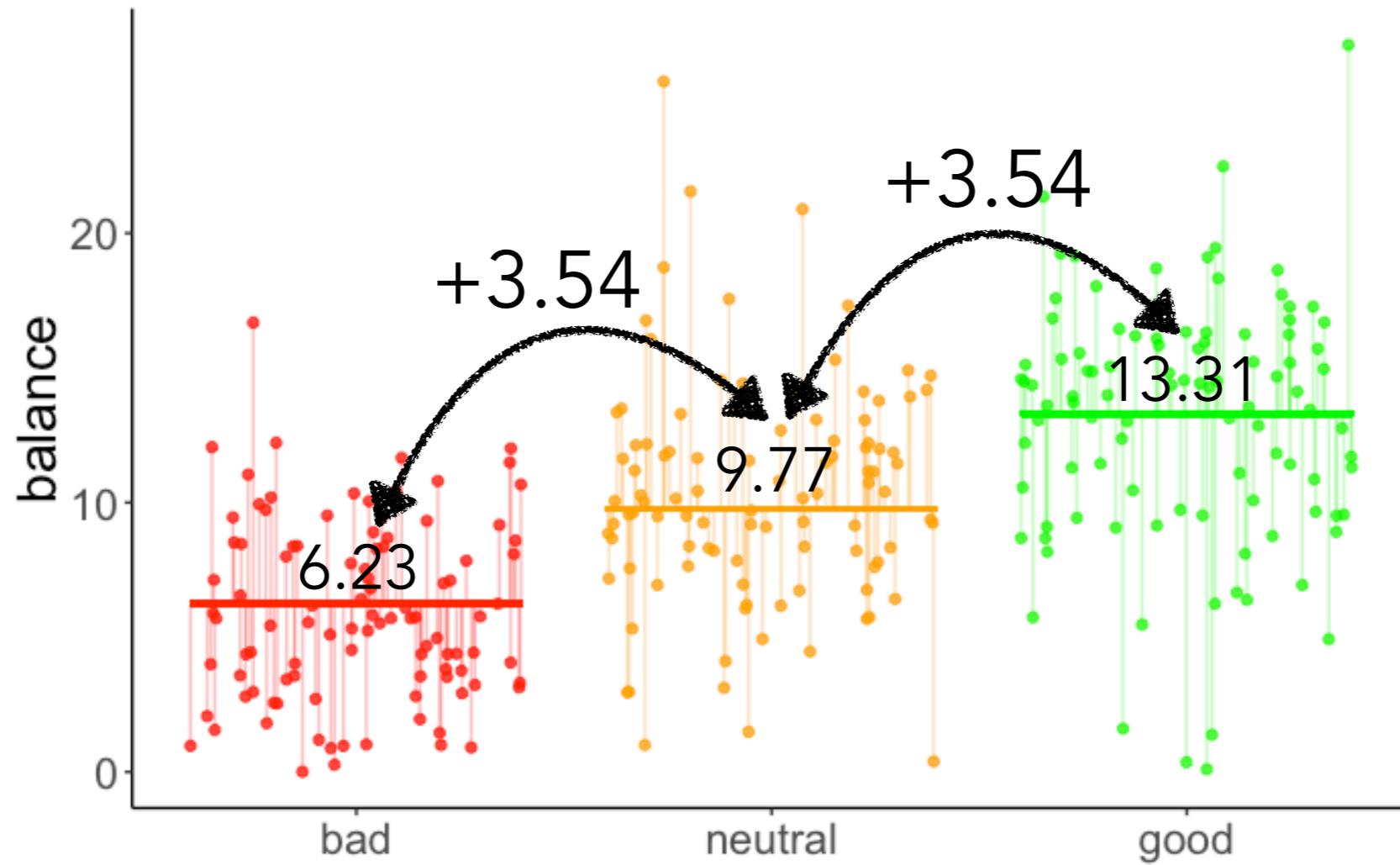
if $\text{contrast} == 0$

$$\begin{aligned}\widehat{\text{balance}}_i &= b_0 + b_1 \cdot \text{hand_contrast}_i \\ &= 9.77 + 0 \cdot 3.54 = 9.77\end{aligned}$$

Contrasts

name	estimate	std.error	statistic	p.value
intercept	9.77	0.24	41.03	0
contrast	3.54	0.29	12.15	0

$$\widehat{\text{balance}}_i = b_0 + b_1 \cdot \text{hand_contrast}$$

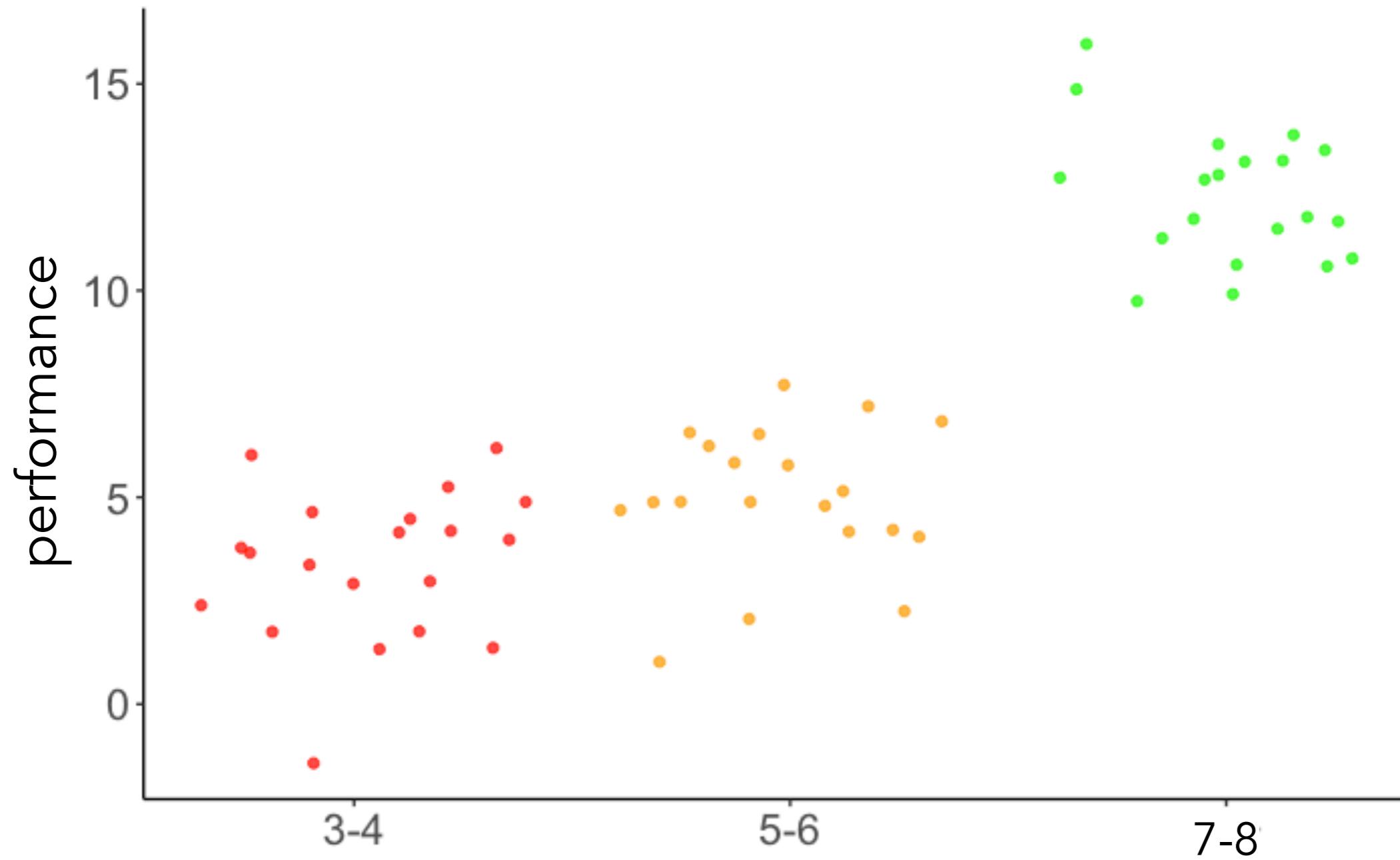


if contrast == 1

$$\begin{aligned}\widehat{\text{balance}}_i &= b_0 + b_1 \cdot \text{hand_contrast}_i \\ &= 9.77 + 1 \cdot 3.54 = 13.31\end{aligned}$$

Contrasts

Does performance increase with age?



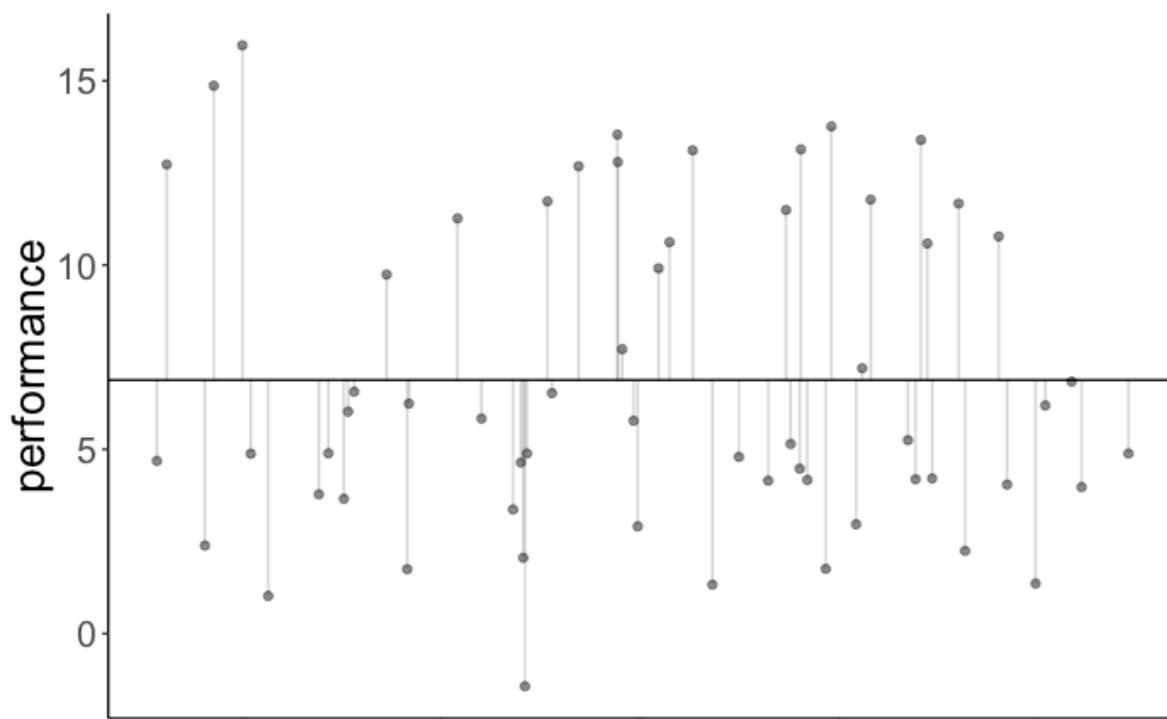
Data from a hypothetical developmental study

Contrasts

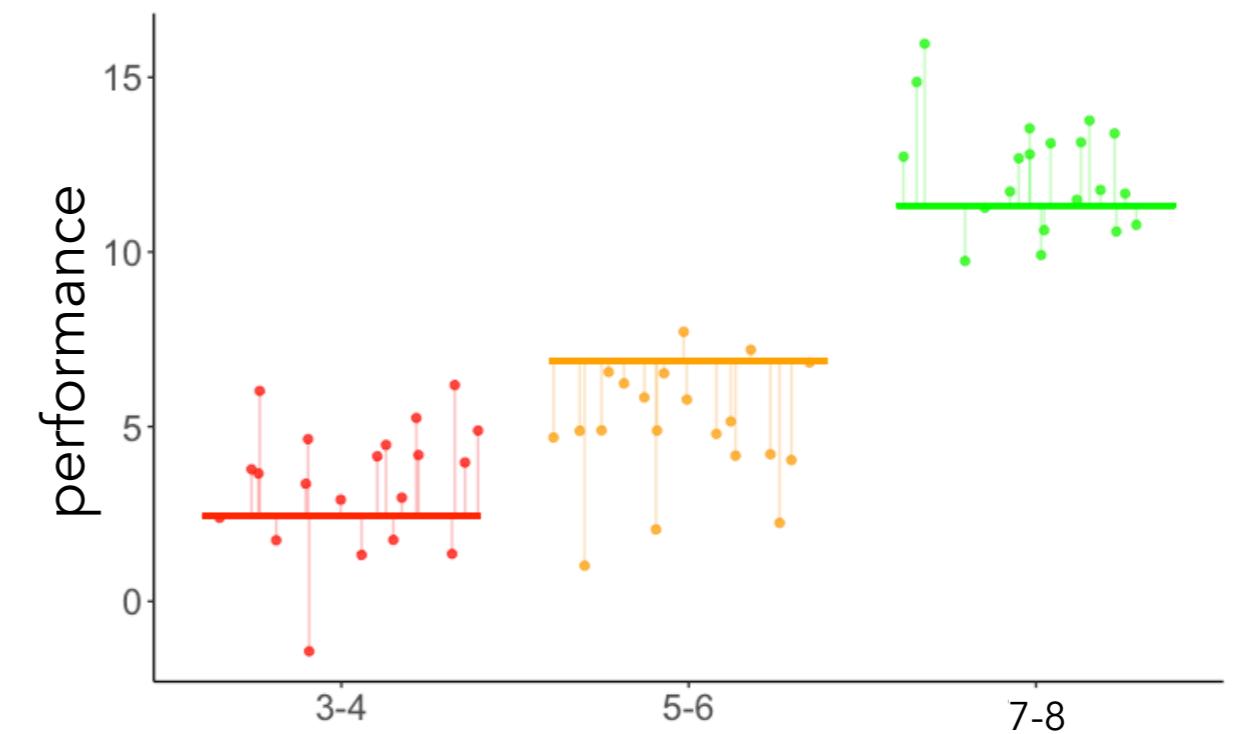
Does performance increase with age?

contrasts = c(-1, 0, 1)

Compact model



Augmented model

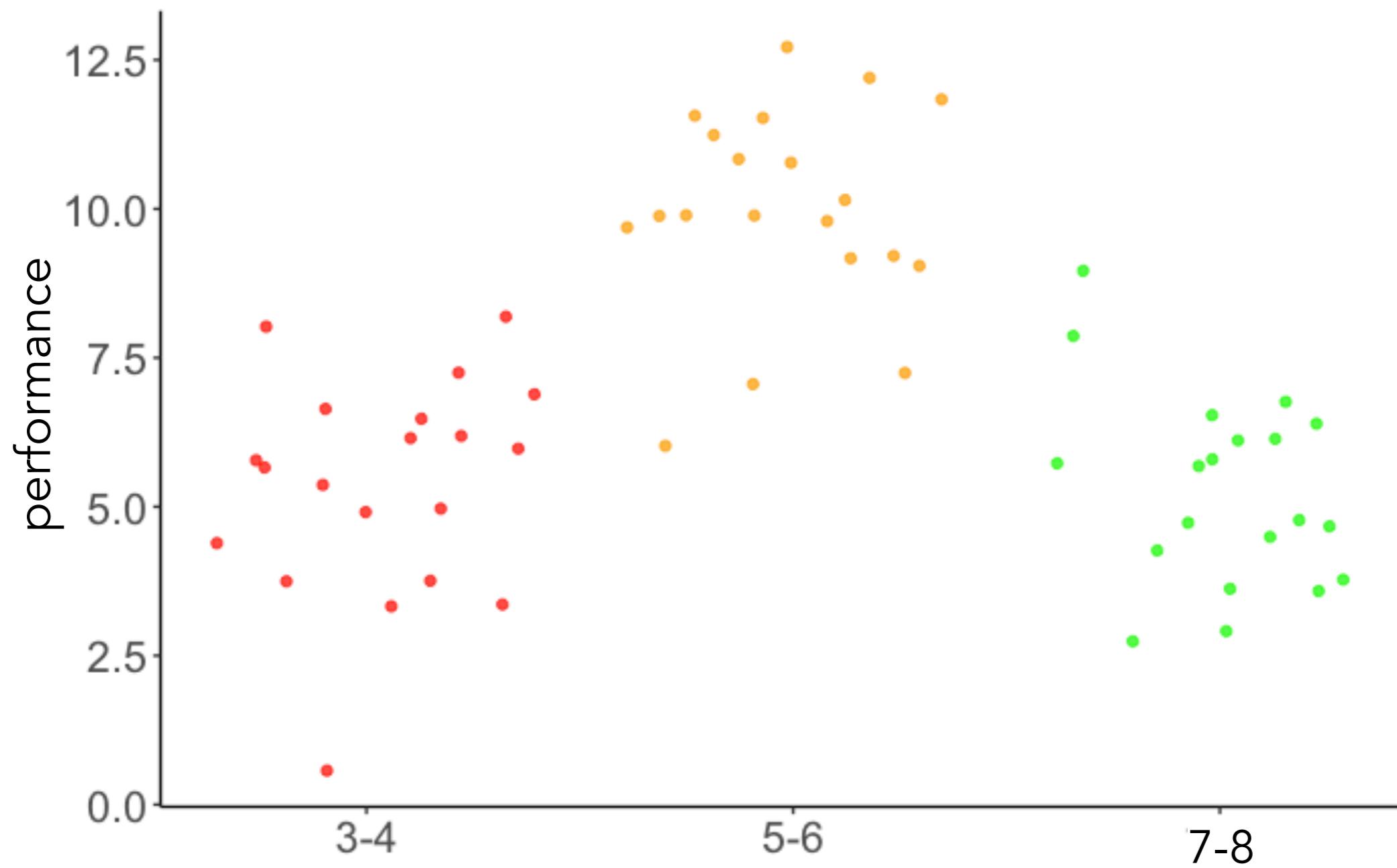


Model comparison

$p < .001$

Contrasts

Does performance increase with age?



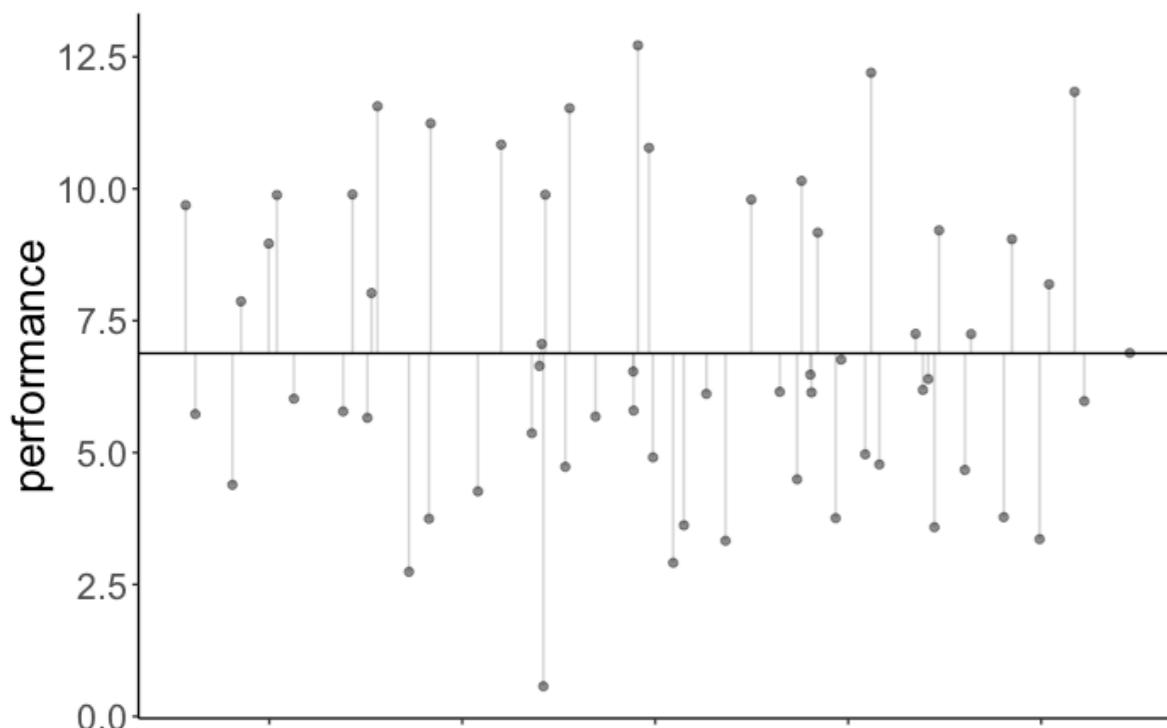
Data from another hypothetical developmental study

Contrasts

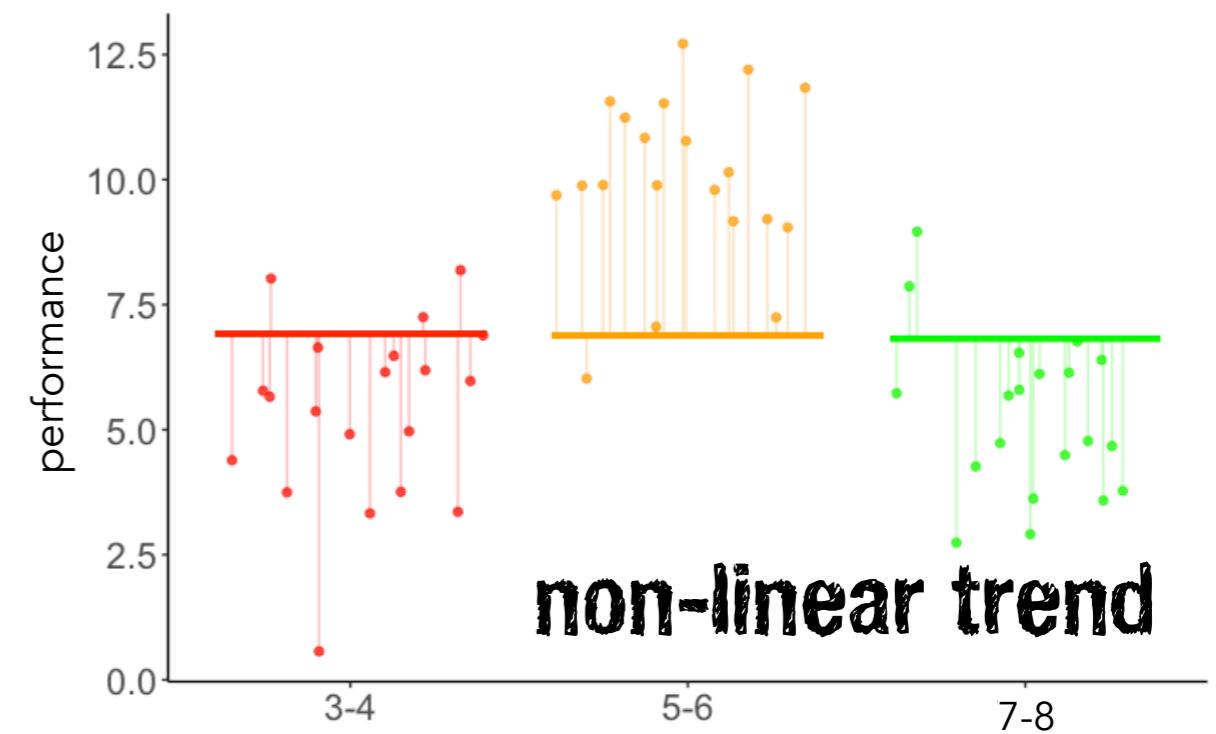
Does performance increase with age?

contrasts = c(-1, 0, 1)

Compact model



Augmented model



Model comparison

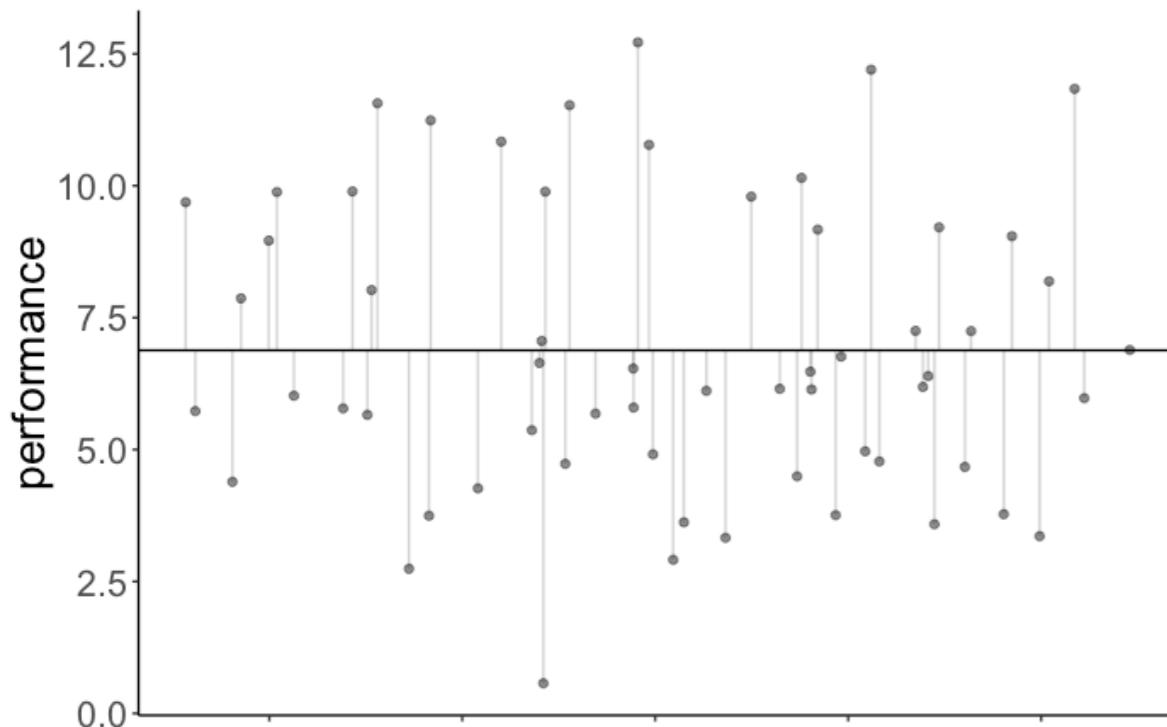
p = .8508

Contrasts

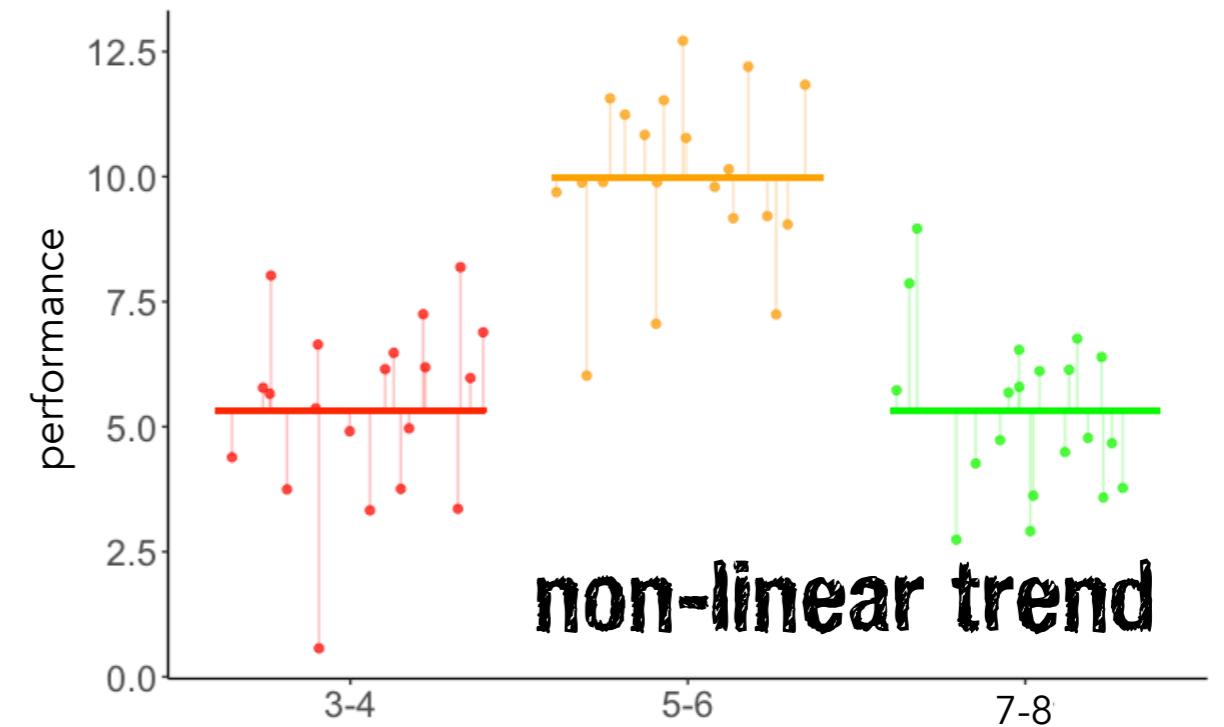
Does performance increase with age?

contrasts = c(-1, 2, -1)

Compact model



Augmented model



Model comparison

$p < .001$

emmeans for handling linear contrasts in R

Linear contrasts

~~How to use contrasts in R~~

In short: don't bother.¹

Like many before me, one of my stats classes technically “taught” me contrasts. But I didn’t get the point and using them was cumbersome, so I promptly ignored them for years.

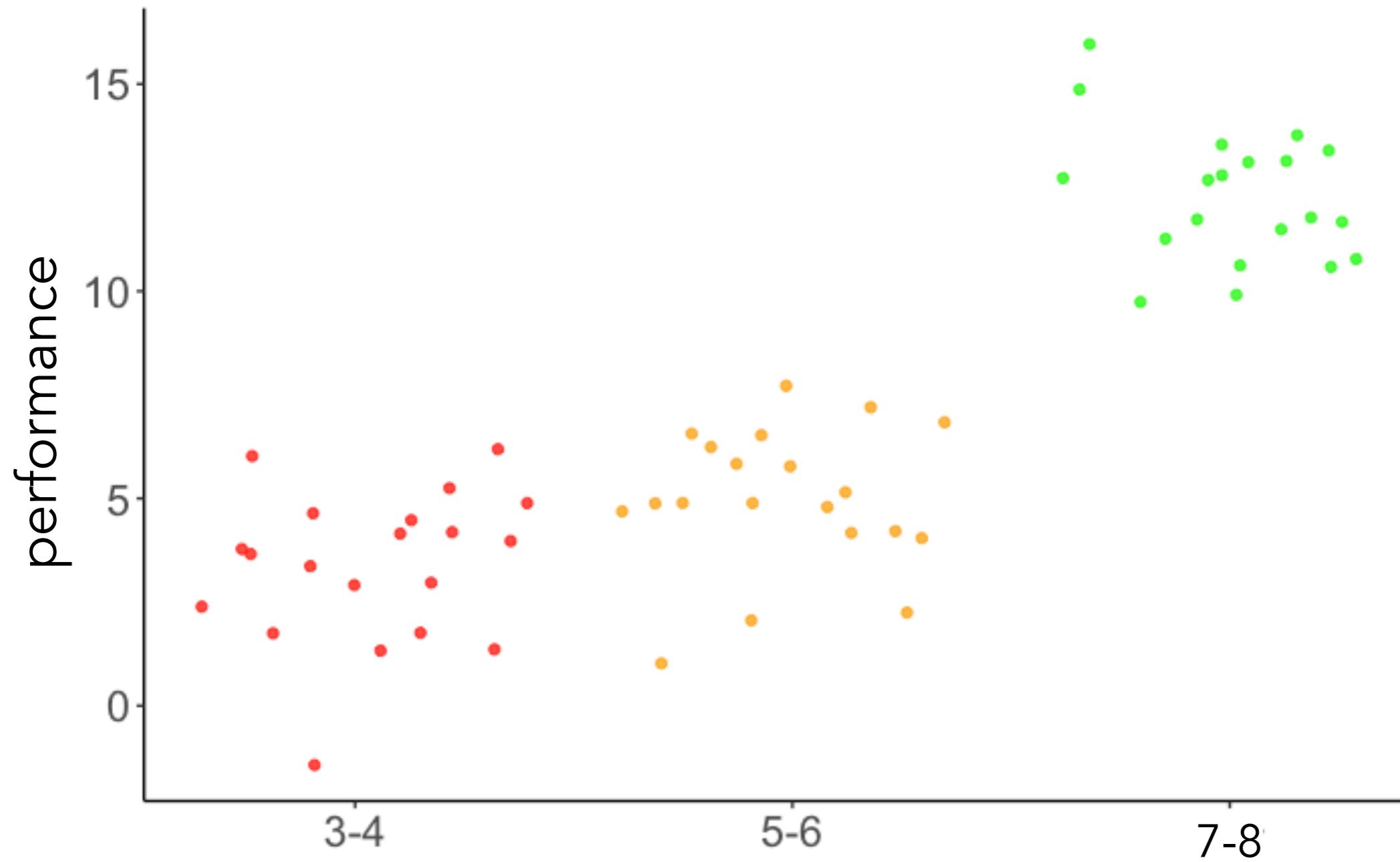
Luckily for me, someone came along and fixed the situation: [emmeans](#). emmeans frames contrasts as a question you pose to a model: you can ask for all pairwise comparisons and get back that. `lm` and `summary` treat the same problem as fitting abstract coefficients, and you are left to answer your own question.

`emmeans` works with `lm`, `glm`, and the Bayesian friends in [brms](#) and [rstanarm](#), so the process is applicable no matter the tool.

And you don't have to learn (much) about contrasts to take advantage of it.

Contrasts

Does performance increase with age?



Data from a hypothetical developmental study

Linear contrasts in R

```
1 library("emmeans") # for calculating contrasts  
2  
3 # fit the linear model  
4 fit = lm(formula = performance ~ group,  
5           data = df.development)
```

fit linear model

Linear contrasts in R

```
1 library("emmeans") # for calculating contrasts  
2  
3 # fit the linear model  
4 fit = lm(formula = performance ~ group,  
5           data = df.development)  
6  
7 # check factor levels  
8 levels(df.development$group) [1] "3-4" "5-6" "7-8"
```

check factor levels before
defining contrasts

Linear contrasts in R

```
1 library("emmeans") # for calculating contrasts
2
3 # fit the linear model
4 fit = lm(formula = performance ~ group,
5           data = df.development)
6
7 # check factor levels
8 levels(df.development$group) [1] "3-4" "5-6" "7-8"
9
10 # define the contrasts of interest
11 contrasts = list(young_vs_old = c(-0.5, -0.5, 1),
12                   three_vs_five = c(-0.5, 0.5, 0)))
```

set up linear contrasts

Linear contrasts in R

```
1 library("emmeans") # for calculating contrasts
2
3 # fit the linear model
4 fit = lm(formula = performance ~ group,
5           data = df.development)
6
7 # check factor levels
8 levels(df.development$group)
9
10 # define the contrasts of interest
11 contrasts = list(young_vs_old = c(-0.5, -0.5, 1),
12                   three_vs_five = c(-0.5, 0.5, 0))
13
14 # compute significance test on contrasts
15 fit %>%
16   emmeans("group",
17           contr = contrasts,
18           adjust = "bonferroni") %>%
19   pluck("contrasts")
```

compute the results

	[1] "3-4" "5-6" "7-8"	contrast	estimate	SE	df	t.ratio	p.value
young_vs_old	16.093541	16.093541	0.4742322	57	33.936	<.0001	
three_vs_five	1.606009	1.606009	0.5475962	57	2.933	0.0097	

P value adjustment: bonferroni method for 2 tests

Linear contrasts in R

```
1 library("emmeans") # for calculating contrasts
2
3 # fit the linear model
4 fit = lm(formula = performance ~ group,
5           data = df.development)
6
7 # check factor levels
8 levels(df.development$group)
9
10 # define the contrasts of interest
11 contrasts = list(young_vs_old = c(-1, -1, 2),
12                   three_vs_five = c(-1, 1, 0))
13
14 # compute significance test on contrasts
15 fit %>%
16   emmeans("group",
17           contr = contrasts,
18           adjust = "bonferroni") %>%
19   pluck("contrasts")
```

hypothesis tests
are the same!

[1] "3-4" "5-6" "7-8"	contrast	estimate	SE	df	t.ratio	p.value
	young_vs_old	32.187	0.948	57	33.936	<.0001
	three_vs_five	0.803	0.274	57	2.933	0.0097

P value adjustment: bonferroni method for 2 tests

Interpreting the coefficients

```
1 fit = lm(formula = performance ~ group,  
2           data = df.development)  
3  
4 # check factor levels  
5 levels(df.development$group)  
6  
7 # define the contrasts of interest  
8 contrasts = list(young_vs_old = c(-1, -1, 2),  
9                   three_vs_five = c(-0.5, 0.5, 0))  
10  
11 # compute estimated marginal means  
12 leastsquare = emmeans(fit, "group")  
13  
14 # run analyses  
15 contrast(leastsquare,  
16            contrasts,  
17            adjust = "bonferroni")
```

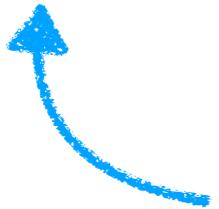
hypothesis tests
are the same!

[1]	"3-4"	"5-6"	"7-8"	contrast	estimate	SE	df	t.ratio	p.value
				young_vs_old	32.187	0.948	57	33.936	<.0001
				three_vs_five	0.803	0.274	57	2.933	0.0097

P value adjustment: bonferroni method for 2 tests

Post hoc tests

```
1 fit = lm(formula = performance ~ group,  
2           data = df.development)  
3  
4 # pairwise differences between all the groups  
5 fit %>%  
6   emmeans(pairwise ~ group) %>%  
7   pluck("contrasts")
```



all pairwise tests between groups

contrast	estimate	SE	df	t.ratio	p.value
3-4 - 5-6	-1.606009	0.5475962	57	-2.933	0.0145
3-4 - 7-8	-16.896546	0.5475962	57	-30.856	<.0001
5-6 - 7-8	-15.290537	0.5475962	57	-27.923	<.0001

P value adjustment: bonferroni method for 3 tests

Post hoc tests

```
1 # fit the model  
2 fit = lm(formula = balance ~ hand + skill,  
3           data = df.poker)  
4  
5 # post hoc tests  
6 fit %>%  
7   emmeans(pairwise ~ hand + skill,  
8             adjust = "bonferroni") %>%  
9   pluck("contrasts")
```

the poker data

contrast	estimate	SE	df	t.ratio	p.value
bad,average - neutral,average	-4.381023	0.6051766	286	-7.239	<.0001
bad,average - good,average	-7.060823	0.6051766	286	-11.667	<.0001
bad,average - bad,expert	-0.740385	0.4896119	286	-1.512	1.0000
bad,average - neutral,expert	-5.121408	0.7611327	286	-6.729	<.0001
bad,average - good,expert	-7.801208	0.7611327	286	-10.249	<.0001
neutral,average - good,average	-2.679800	0.5884403	286	-4.554	0.0001
neutral,average - bad,expert	3.640638	0.7953578	286	4.577	0.0001
neutral,average - neutral,expert	-0.740385	0.4896119	286	-1.512	1.0000
neutral,average - good,expert	-3.420185	0.7654945	286	-4.468	0.0002
good,average - bad,expert	6.320438	0.7953578	286	7.947	<.0001
good,average - neutral,expert	1.939415	0.7654945	286	2.534	0.1774
good,average - good,expert	-0.740385	0.4896119	286	-1.512	1.0000
bad,expert - neutral,expert	-4.381023	0.6051766	286	-7.239	<.0001
bad,expert - good,expert	-7.060823	0.6051766	286	-11.667	<.0001
neutral,expert - good,expert	-2.679800	0.5884403	286	-4.554	0.0001

that's a lot of tests!

... not

P value adjustment: bonferroni method for 15 tests

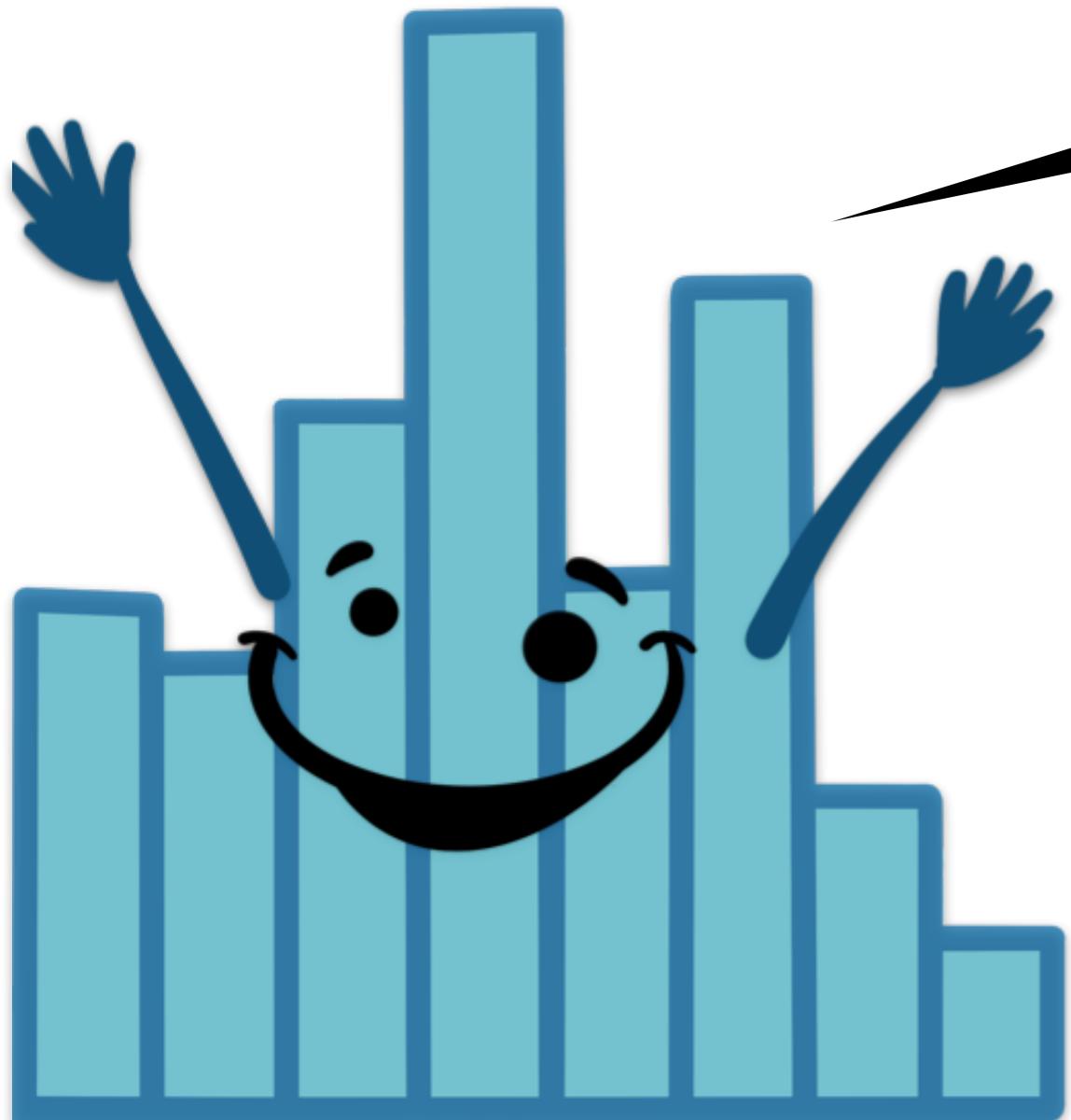
all pairwise tests between groups

Contrasts

- linear contrasts allow us to ask more specific questions of our data
- rather than asking whether any of the group means are significantly different from each other (ANOVA), we can ask questions such as:
 - Does performance increase with age?
 - Is the overall performance in Condition B and C better from the performance in Condition A?

01:00

stretch break!



Power analysis

Making decisions

Type I Error



Type II Error



H_0 : Not pregnant. H_1 : Pregnant.

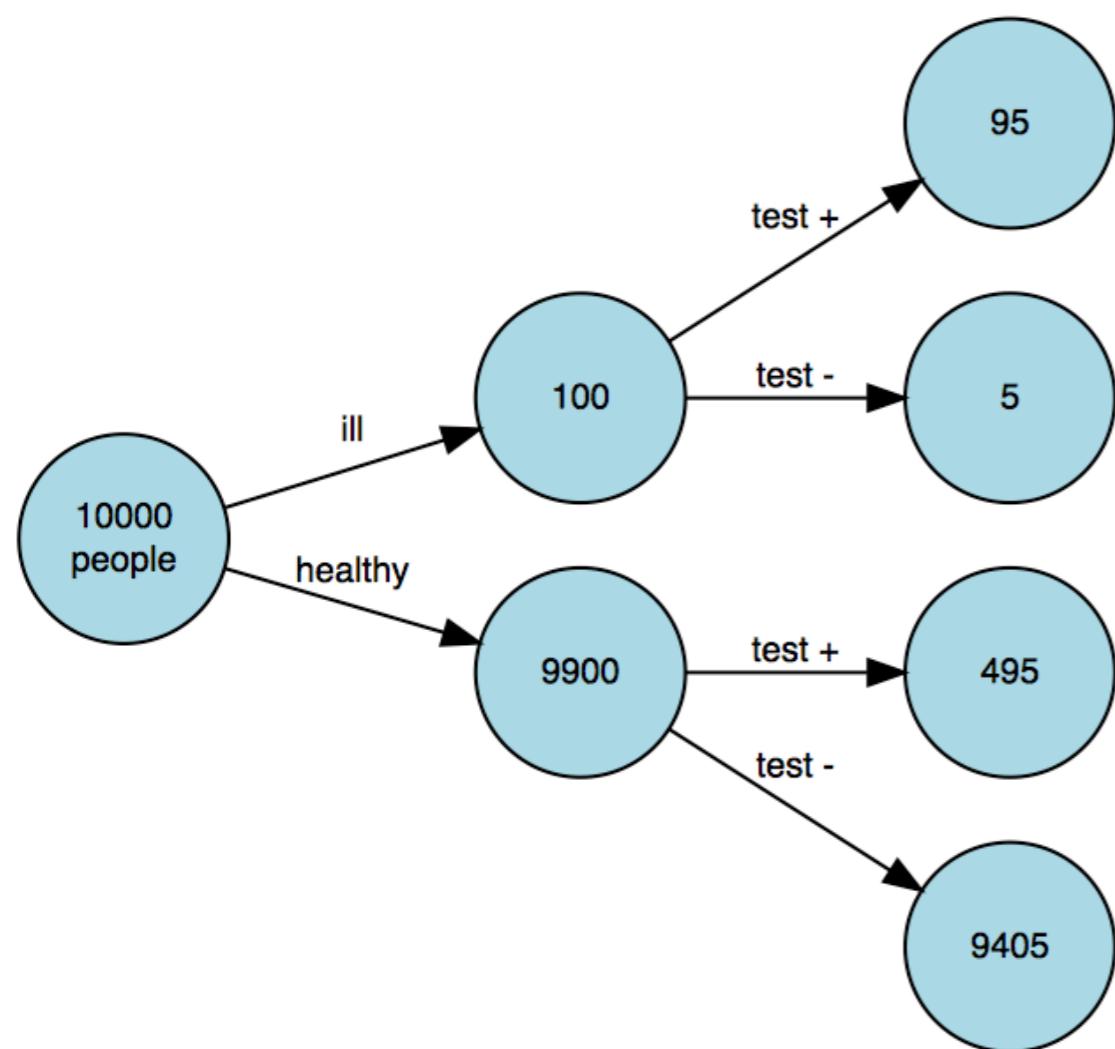
Type I Error: Falsely rejecting the null hypothesis (even though it is true).

Type II Error: Failing to reject the null hypothesis (even though it is false).

Clue guide to probability

H_0 : The person is healthy.

H_1 : The person is ill.



Sensitivity

$p(\text{reject } H_0 | H_1 \text{ is true})$

Power

$1 - \beta$

false negative

Type II error

$p(\text{not reject } H_0 | H_1 \text{ is true})$

β

false positive

Type I error

$p(\text{reject } H_0 | H_0 \text{ is true})$

α

true negative

$p(\text{not reject } H_0 | H_0 \text{ is true})$

Specificity

$1 - \alpha$

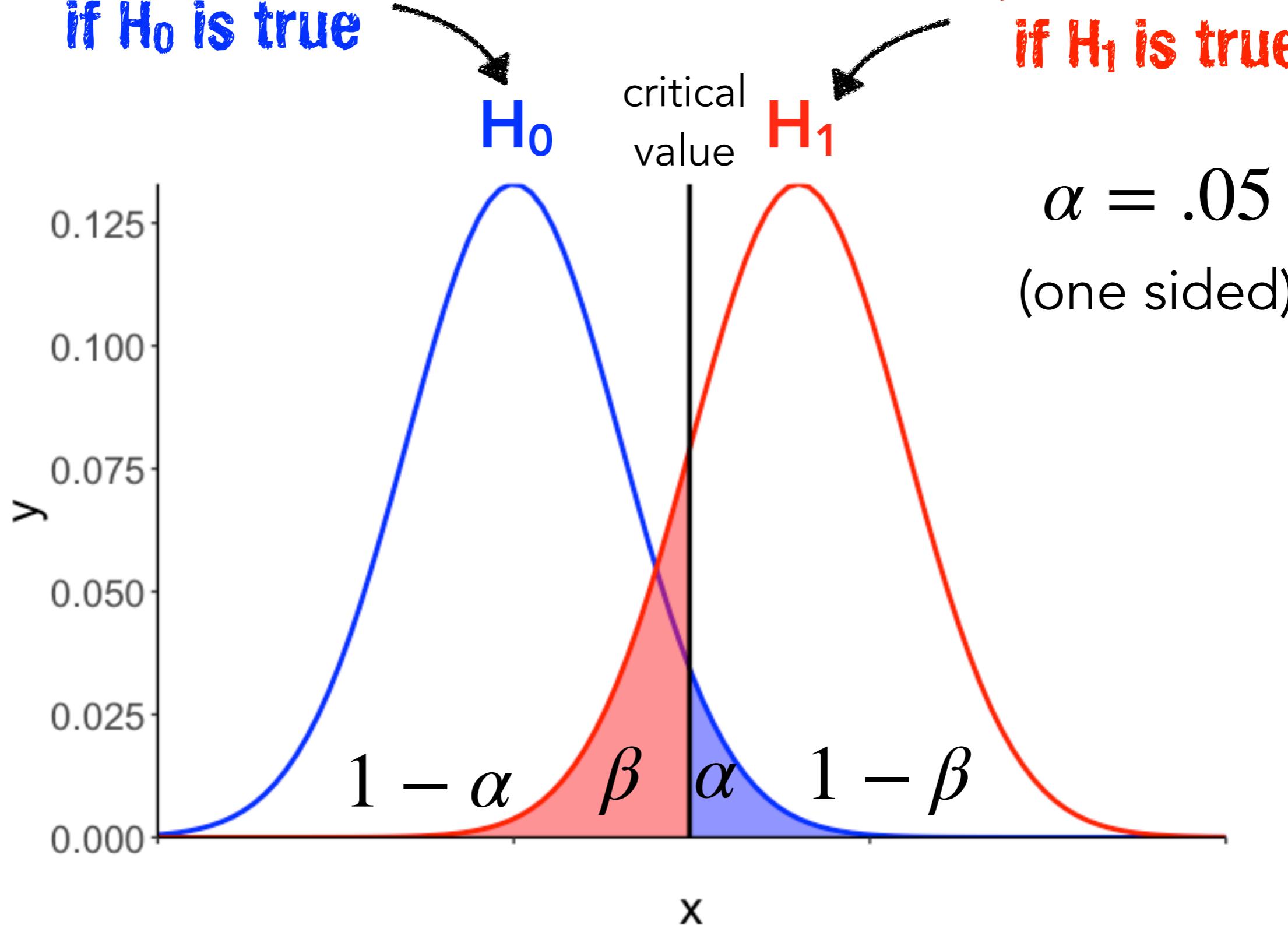
What affects power?

sampling distribution

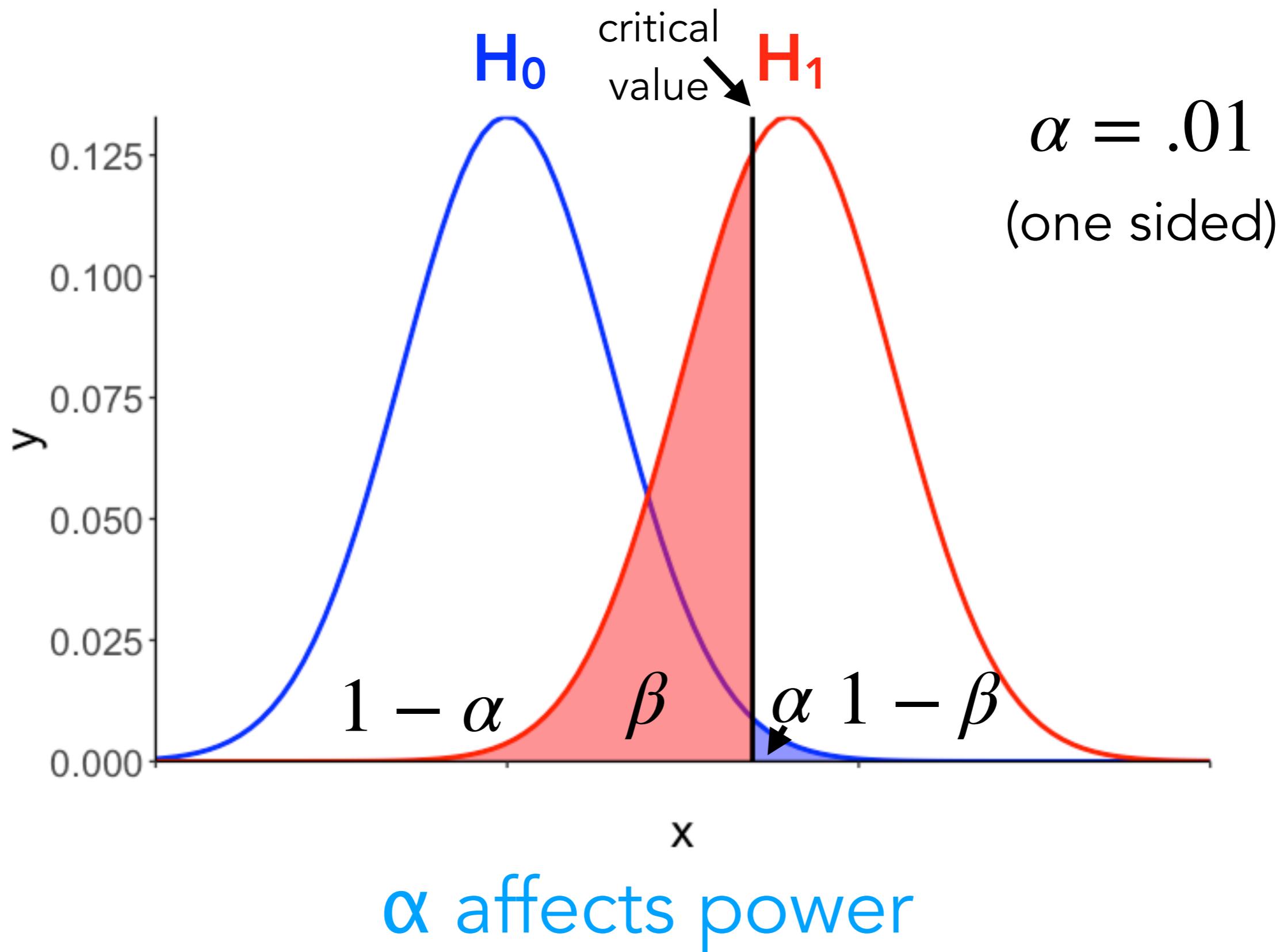
if H_0 is true

sampling distribution

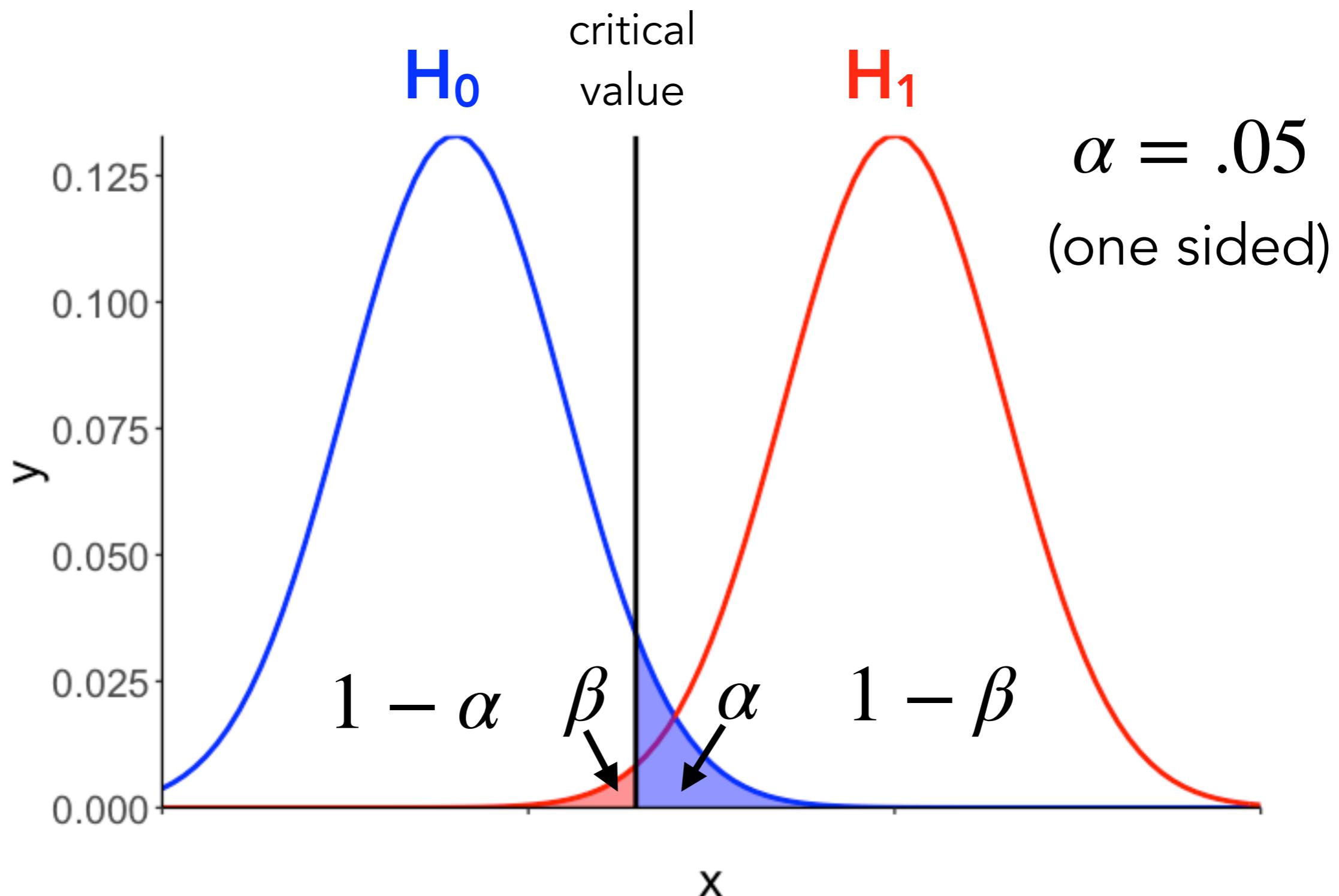
if H_1 is true



What affects power?

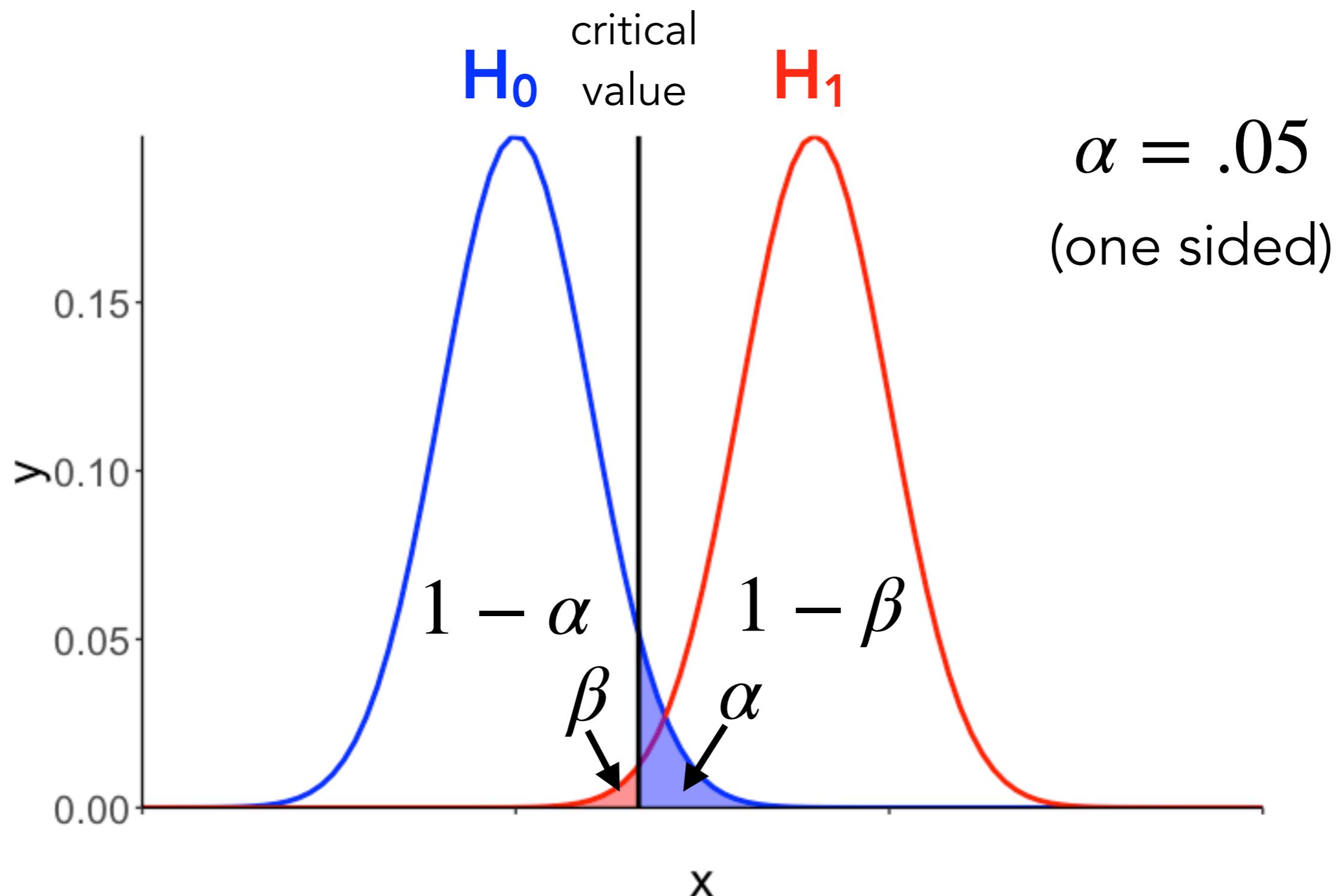


What affects power?



distance between means affects power

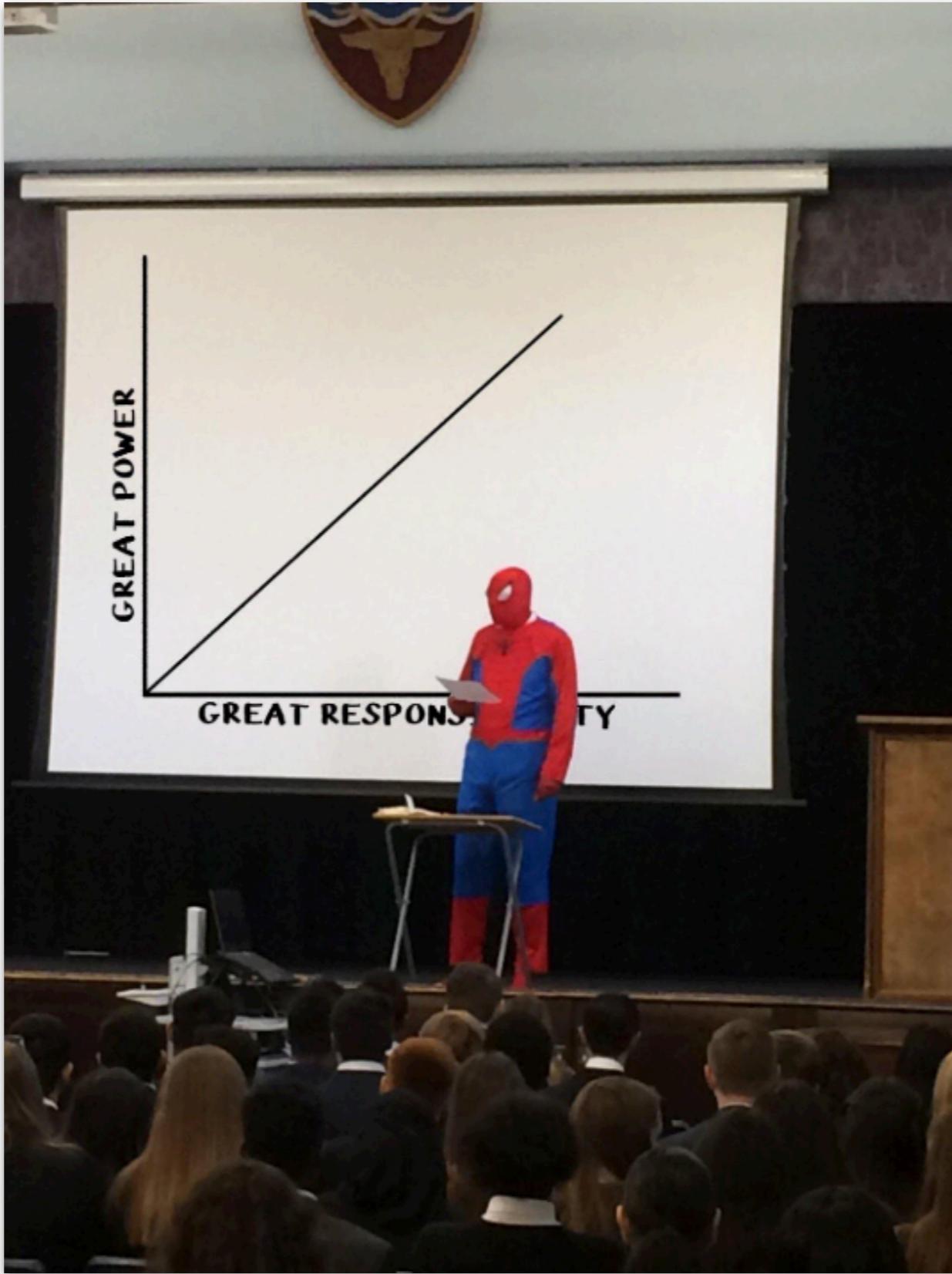
What affects power?



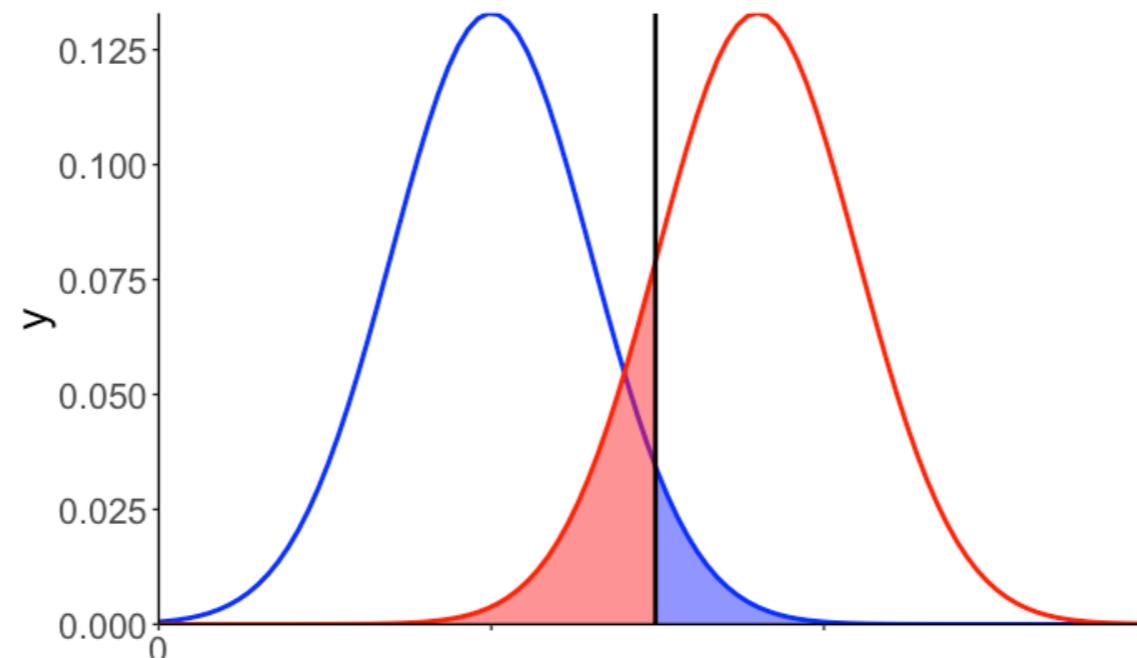
variance affects power

Calculating power

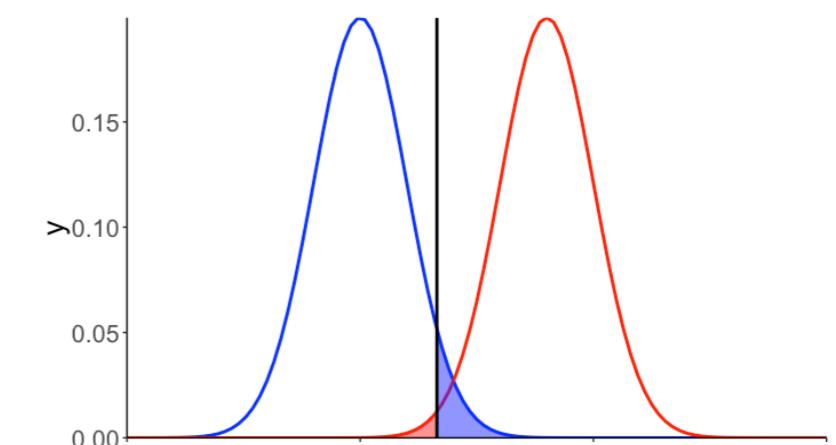
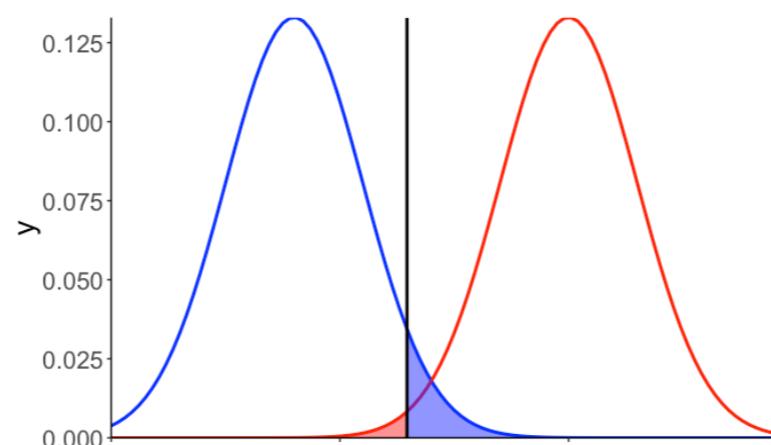
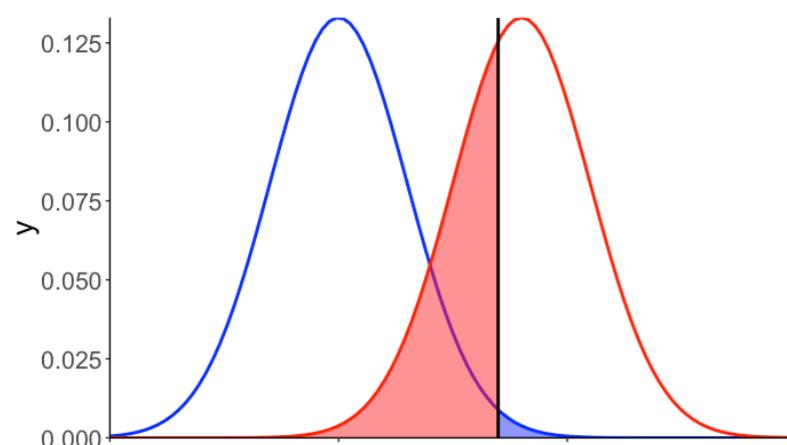
With great power comes ...



The knobs we can turn to affect power



α effect size sample size



Visualization demo

Settings

Solve for? Power Alpha n d

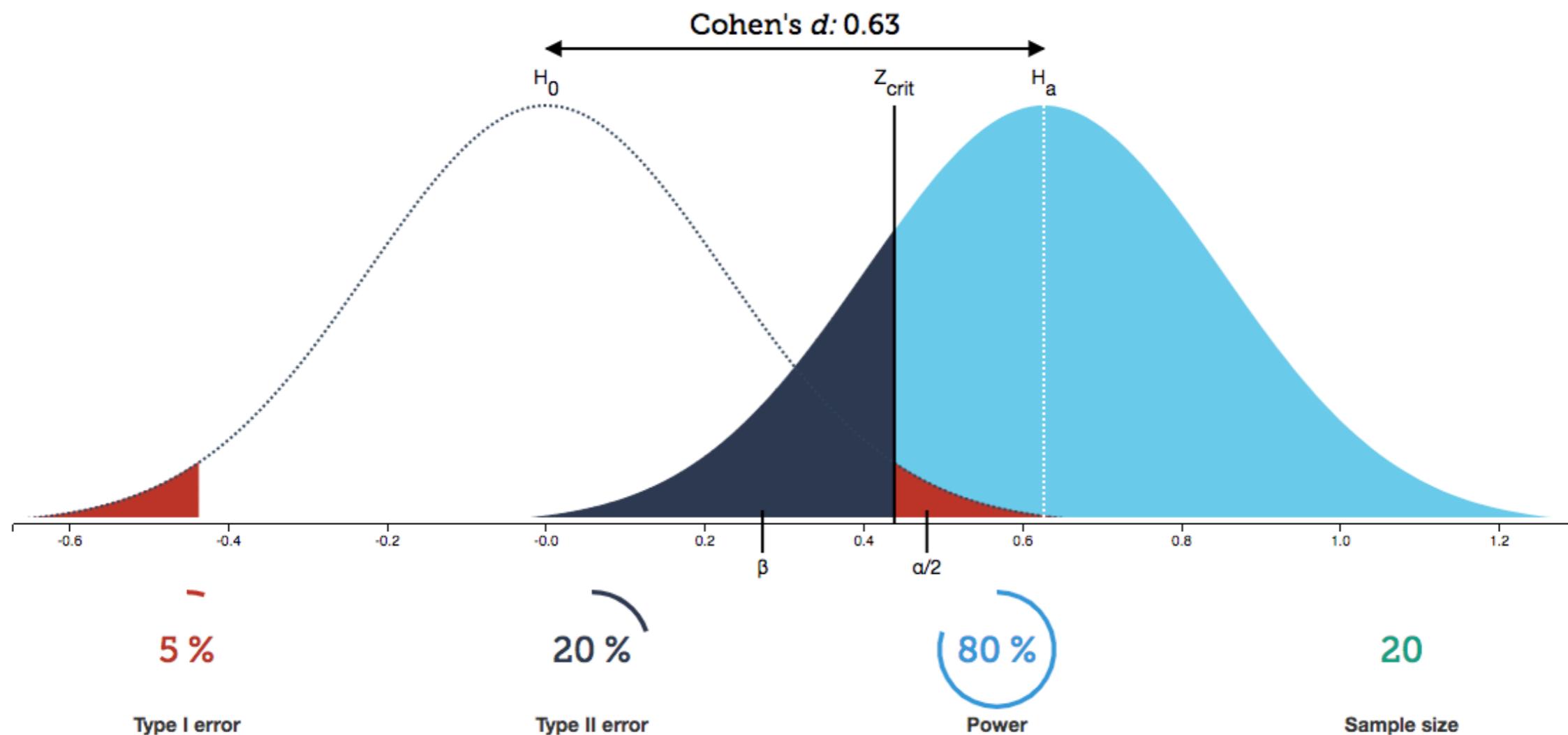
Power ($1-\beta = 0.8$)

Significance level ($\alpha = 0.05$)

Sample size ($n = 20$)

One-tailed Two-tailed

Reset zoom



<https://rpsychologist.com/d3/NHST/>

The **power** of a binary hypothesis test is the probability that the test rejects the null hypothesis (H_0) when a **specific** alternative hypothesis (H_1) is true.

H_0 : Students and non-students have the same balance.

Model C

$$Y_i = \beta_0 + \epsilon_i$$

$$\beta_1 = 0$$

H_1 : Students and non-students have different balances.

Model A

$$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i$$

$$\beta_1 \neq 0$$

We cannot calculate power in this case.
We need a specific alternative hypothesis!

The **power** of a binary hypothesis test is the probability that the test rejects the null hypothesis (H_0) when a **specific** alternative hypothesis (H_1) is true.

H_0 : Students and non-students have the same balance.

Model C

$$Y_i = \beta_0 + \epsilon_i$$

$$\beta_1 = 0$$

H_1 : Students and non-students have different balances.

Model A

$$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i$$

$$\beta_1 = 300$$

We can calculate power in this case (since we have a specific alternative hypothesis)!

Effect sizes

Effect sizes

- a p-value tells us whether we can reject the H_0
- effect sizes is a measure of the strength of the actual effect

**Why can't we just use p-values
as a measure of the effect size?**

$$F = \frac{\text{PRE}/(\text{PA} - \text{PC})}{(1 - \text{PRE})/(n - \text{PA})}$$

PRE = proportional reduction in error

PA = # parameters in the augmented model

PC = # parameters in the compact model

n = sample size

any PRE will become significant if n gets large enough

**statistical vs.
practical significance**

Effect sizes

PRE = proportional reduction in error

Compact model

SSE(C)

Augmented model

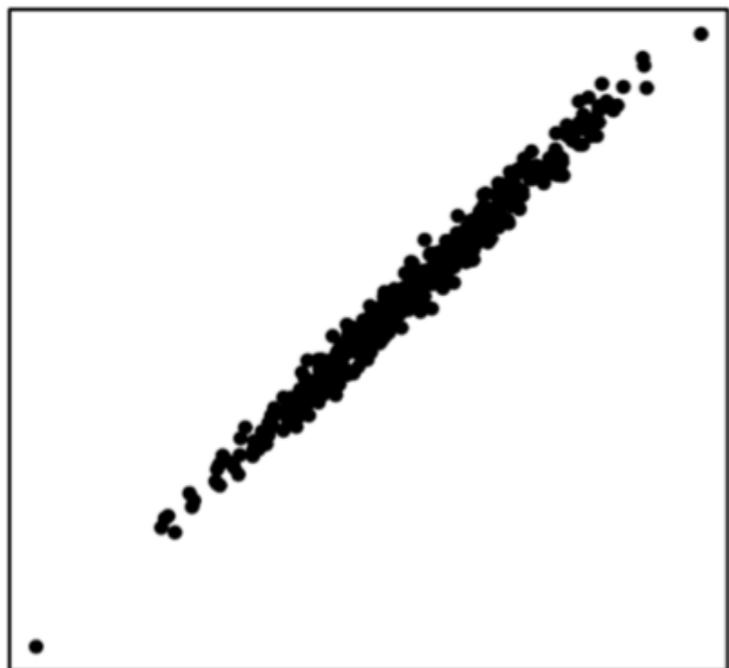
SSE(A)

$$\text{PRE} = 1 - \frac{\text{SSE}(A)}{\text{SSE}(C)}$$

SSE = sum of squared errors

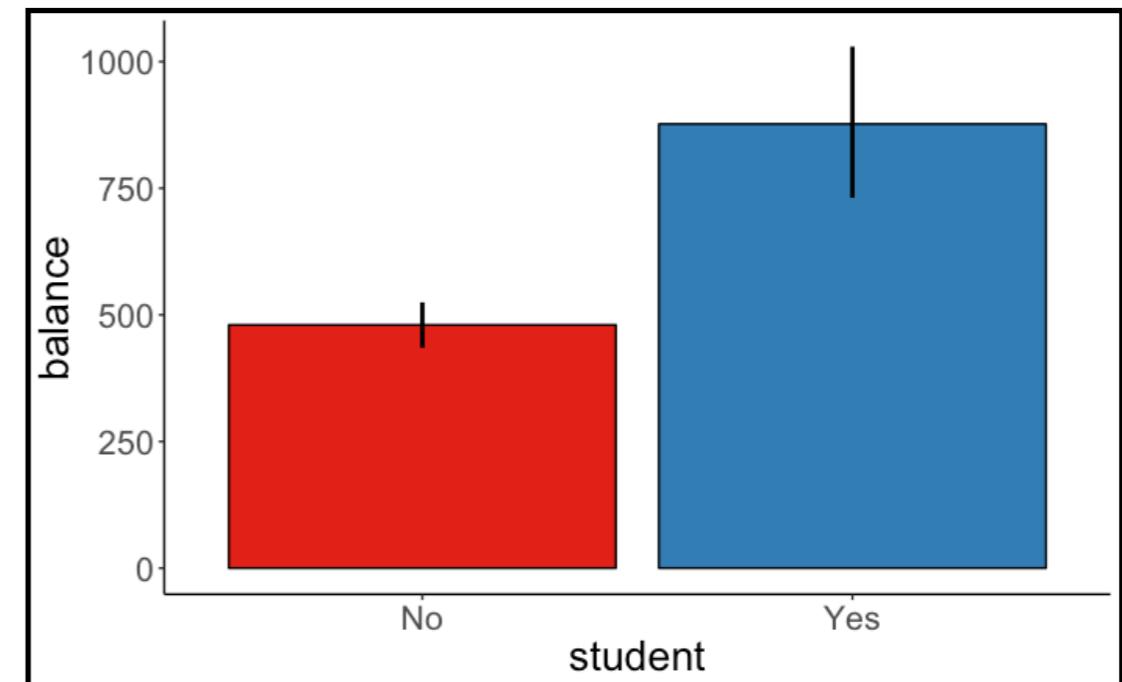
Common effect sizes

Relationships between variables



r correlation

Differences between groups



Cohen's d

Correlation

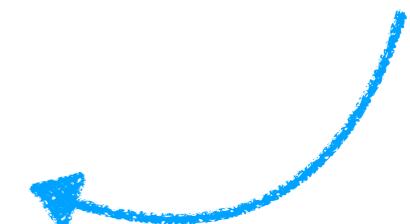
Pearson correlation

$$r(X, Y) = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2} \cdot \sqrt{\sum_{i=1}^n (Y_i - \bar{Y})^2}}$$

Cohen's guidelines for the social sciences

Effect size	r
Small	0.1
Medium	0.3
Large	0.5

depends very
much on the
domain



Cohen's d

- standardized difference between two means

absolute difference between means

$$d = \frac{|\bar{y}_1 - \bar{y}_2|}{s_p}$$

pooled standard variation

$$s_p = \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}}$$

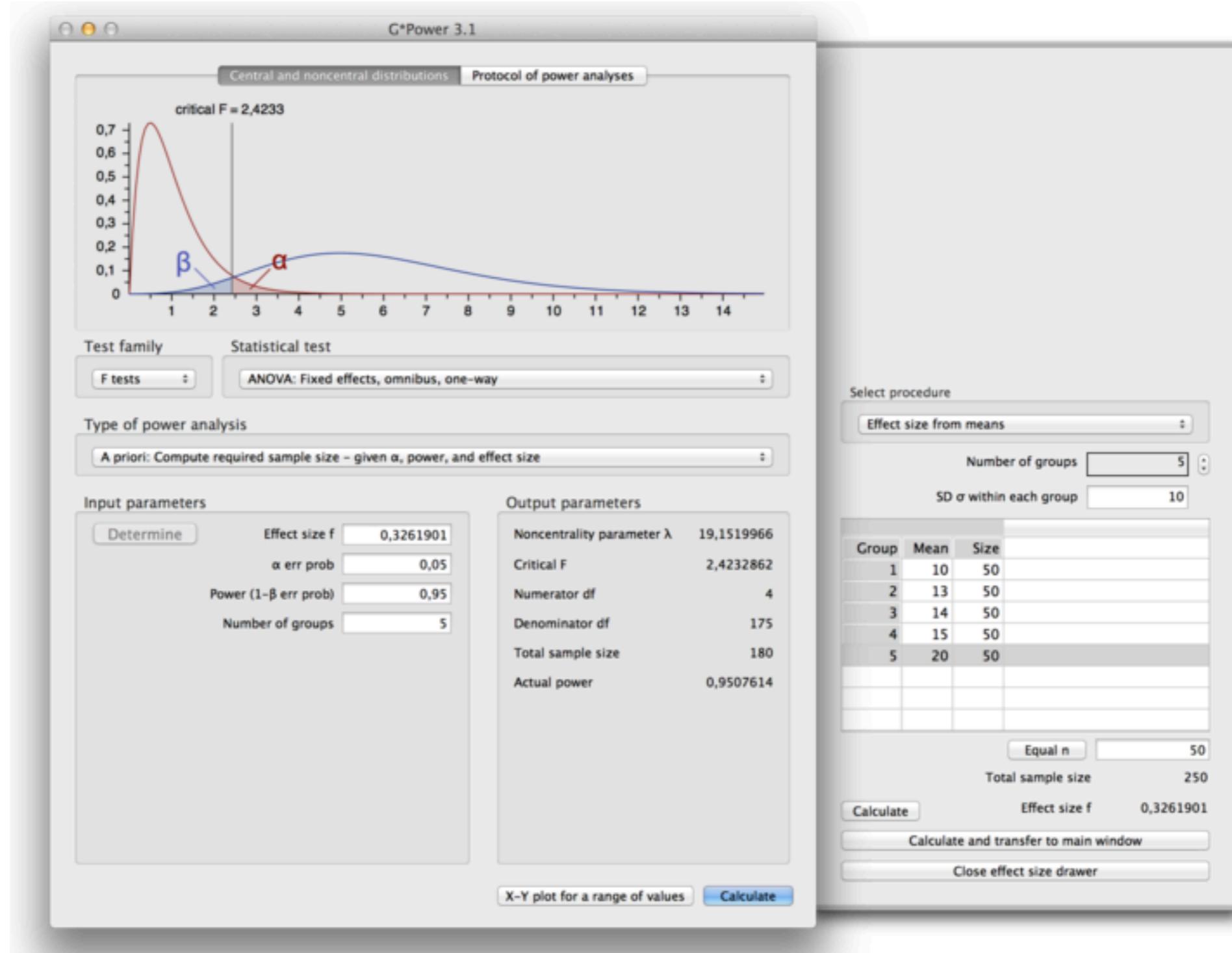
Effect size	d
Very small	0.01
Small	0.20
Medium	0.50
Large	0.80
Very large	1.20
Huge	2.0

Difference between two means in pooled standard deviation

Determining sample size

How many participants do I need to run to have a good chance of detecting a true effect?

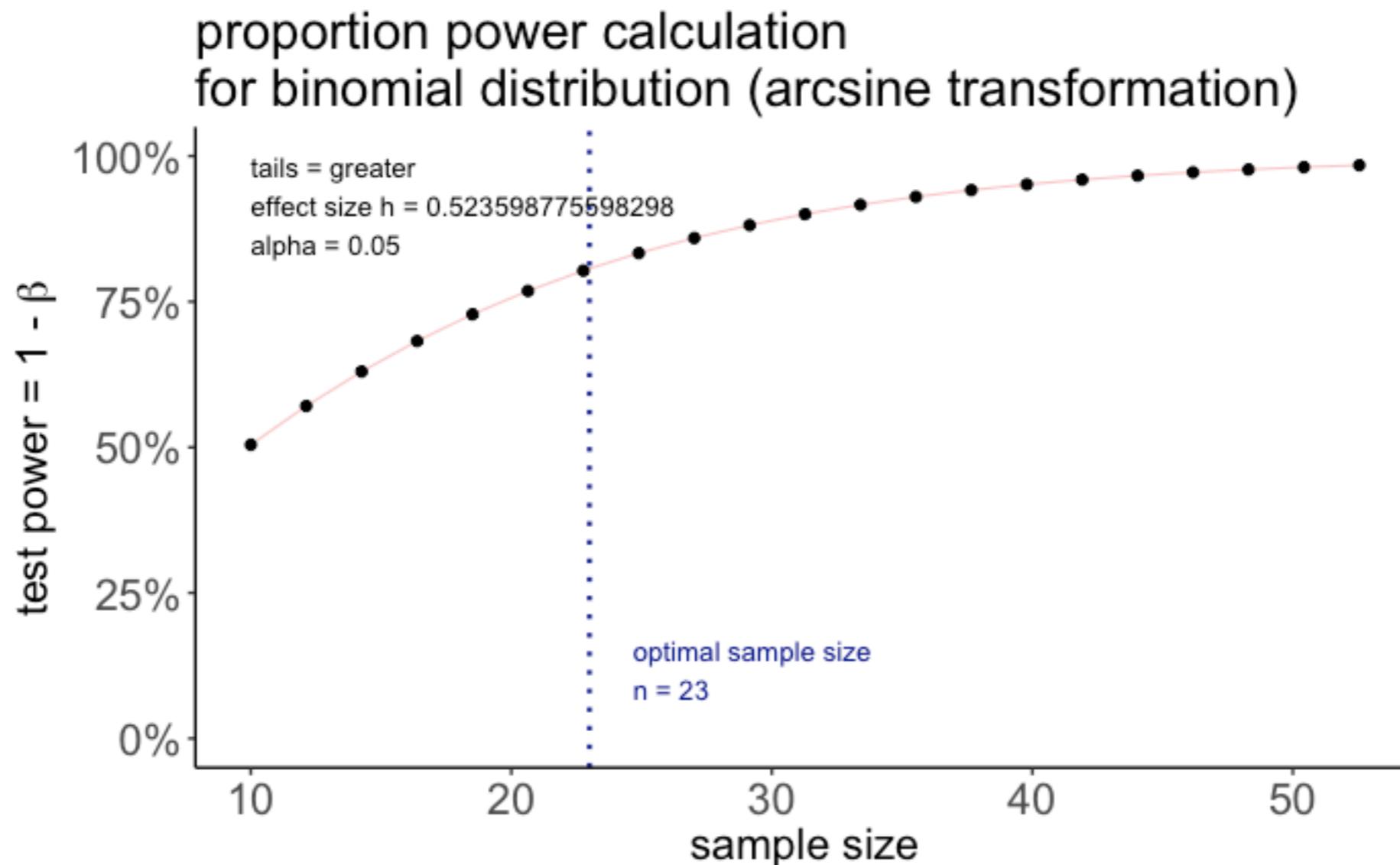
G*Power 3.1: Alternative software for power calculations



<http://www.gpower.hhu.de/>

Example

```
1 library("pwr")
2 pwr.p.test(h = ES.h(p1 = 0.75, p2 = 0.50),
3             sig.level = 0.05,
4             power = 0.80,
5             alternative = "greater") %>%
6   plot()
```



Power simulation recipe

- assume:
 - α , n , effect size
- simulate a large number of data sets of size n with the specified effect size
- for each data set, run a statistical test to calculate the p-value
- determine the probability of rejecting the H_0 (given that H_1 is true)

**Learn about more advanced
simulation techniques in R**

Let's simulate

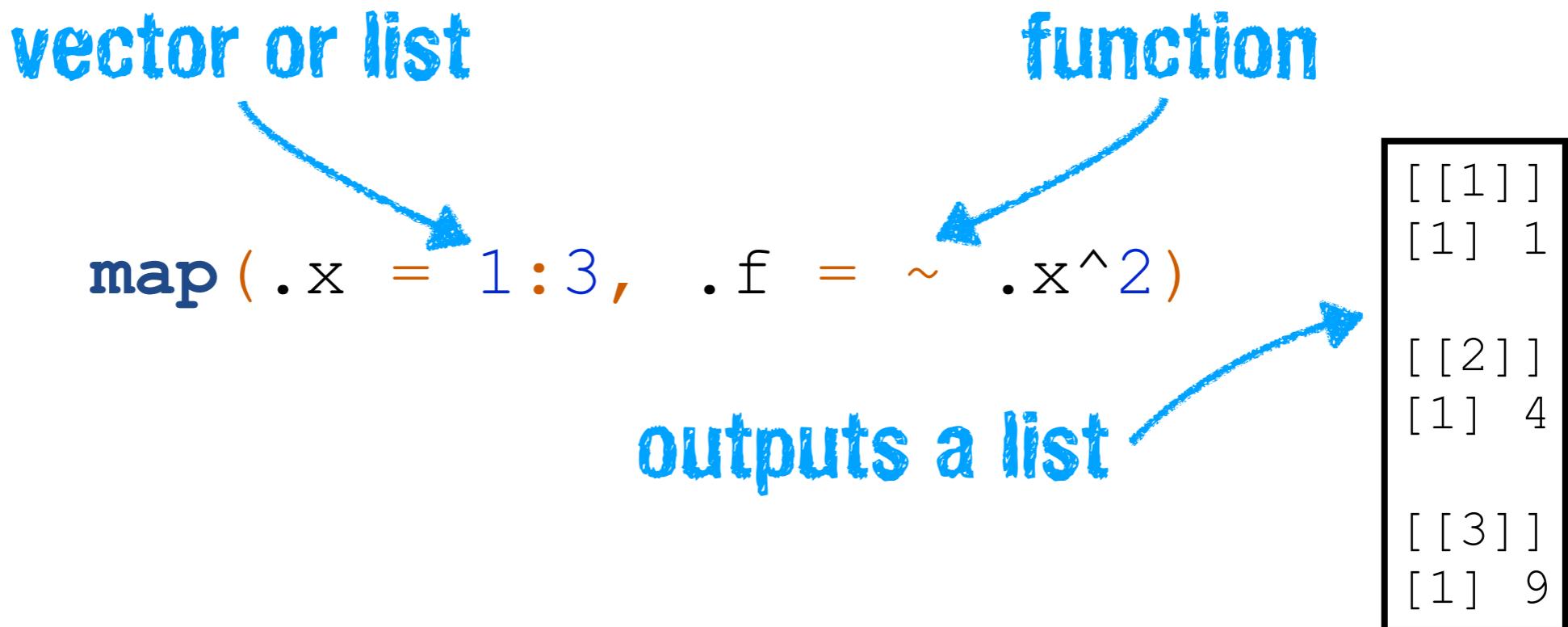
```
library("purrr")
```



automatically loaded with
library("tidyverse")

map ()

map()



- `map(list, function)` applies a function to each element of the list
- it's a unified version of the many different `apply()` functions in base R
- you already know a cousin of `map()`: `replicate()`
- use `map()`, don't write `for () {}` loops!
- it's extremely powerful in combination with data frames

map ()

same same but different

map (.x = 1:3, .f = ~ .x^2)

map (1:3, ~ .x^2)

map (1:3, ~ .^2)

map (.x = 1:3, .f = function (.x) .x^2)

using a function

square = **function**(x) { x^2 }

map (1:3, square)



Studio[®]

time

Plan for today

- Linear contrasts
 - Testing specific hypotheses with linear contrasts
 - emmeans for handling linear contrasts in R
- Power analysis
 - Making decisions
 - Calculating power
 - Effect sizes
 - Determining sample size
- Learn about more advanced simulation techniques in R
 - `map()`
 - list columns: `nest()`, `unnest()`

Feedback

How was the pace of today's class?

much a little just a little much
too too right too too
slow slow

How happy were you with today's class overall?



What did you like about today's class? What could be improved next time?

Thank you!