

Data Science for Biological, Medical and Health Research: Notes for 432

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Built 2018-01-20 16:58:45

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Introduction

These Notes provide a series of examples using R to work through issues that are likely to come up in PQHS/CRSP/MPHP 432.

While these Notes share some of the features of a textbook, they are neither comprehensive nor completely original. The main purpose is to give students in 432 a set of common materials on which to draw during the course. In class, we will sometimes:

- reiterate points made in this document,
- amplify what is here,
- simplify the presentation of things done here,
- use new examples to show some of the same techniques,
- refer to issues not mentioned in this document,

but what we don't (always) do is follow these notes very precisely. We assume instead that you will read the materials and try to learn from them, just as you will attend classes and try to learn from them. We welcome feedback of all kinds on this document or anything else. Just email us at `431-help at case dot edu`, or submit a pull request. Note that we still use `431-help` even though we're now in 432.

What you will mostly find are brief explanations of a key idea or summary, accompanied (most of the time) by R code and a demonstration of the results of applying that code.

Everything you see here is available to you as HTML or PDF. You will also have access to the R Markdown files, which contain the code which generates everything in the document, including all of the R results. We will demonstrate the use of R Markdown (this document is generated with the additional help of an R package called bookdown) and R Studio (the “program” which we use to interface with the R language) in class.

To download the data and R code related to these notes, visit the Data and Code section of the 432 course website.

R Packages used in these notes

Here, we'll load in the packages used in these notes.

```
library(tableone)
library(skimr)
library(magrittr)
library(modelr)
library(broom)
library(tidyverse)
```


Data used in these notes

Here, we'll load in the data sets used in these notes.

```
fakestroke <- read.csv("data/fakestroke.csv") %>% tbl_df
bloodbrain <- read.csv("data/bloodbrain.csv") %>% tbl_df
smartcle1 <- read.csv("data/smartcle1.csv") %>% tbl_df
bonding <- read.csv("data/bonding.csv") %>% tbl_df
cortisol <- read.csv("data/cortisol.csv") %>% tbl_df
```


Chapter 1

Building Table 1

Many scientific articles involve direct comparison of results from various exposures, perhaps treatments. In 431, we studied numerous methods, including various sorts of hypothesis tests, confidence intervals, and descriptive summaries, which can help us to understand and compare outcomes in such a setting. One common approach is to present what's often called Table 1. Table 1 provides a summary of the characteristics of a sample, or of groups of samples, which is most commonly used to help understand the nature of the data being compared.

1.1 Two examples from the *New England Journal of Medicine*

1.1.1 A simple Table 1

Table 1 is especially common in the context of clinical research. Consider the excerpt below, from a January 2015 article in the *New England Journal of Medicine* (Tolaney et al., 2015).

Table 1. Baseline Characteristics of the Patients.*	
Characteristic	Patients (N=406)
	no. (%)
Age group	
<50 yr	132 (32.5)
50–59 yr	137 (33.7)
60–69 yr	96 (23.6)
≥70 yr	41 (10.1)
Sex	
Female	405 (99.8)
Male	1 (0.2)
Race†	
White	351 (86.5)
Black	28 (6.9)
Asian	11 (2.7)
Other	16 (3.9)

This (partial) table reports baseline characteristics on age group, sex and race, describing 406 patients with

HER2-positive¹ invasive breast cancer that began the protocol therapy. Age, sex and race (along with severity of illness) are the most commonly identified characteristics in a Table 1.

In addition to the measures shown in this excerpt, the full Table also includes detailed information on the primary tumor for each patient, including its size, nodal status and histologic grade. Footnotes tell us that the percentages shown are subject to rounding, and may not total 100, and that the race information was self-reported.

1.1.2 A group comparison

A more typical Table 1 involves a group comparison, for example in this excerpt from Roy et al. (2008). This Table 1 describes a multi-center randomized clinical trial comparing two different approaches to caring for patients with heart failure and atrial fibrillation².

Table 1. Baseline Characteristics of the Patients.*		
Variable	Rhythm-Control Group (N = 682)	Rate-Control Group (N = 694)
Male sex (%)	78	85
Age (yr)	66±11	67±11
Body-mass index†	27.8±5.4	28.0±5.1
Nonwhite race (%)‡	16	13
NYHA class III or IV (%)		
At baseline	32	31
During previous 6 mo	76	76
Predominant cardiac diagnosis (%)§		
Coronary artery disease	48	48
Valvular heart disease	5	5
Nonischemic cardiomyopathy	36	39
Congenital heart disease	1	1
Hypertensive heart disease	10	7

The article provides percentages, means and standard deviations across groups, but note that it does not provide p values for the comparison of baseline characteristics. This is a common feature of NEJM reports on randomized clinical trials, where we anticipate that the two groups will be well matched at baseline. Note that the patients in this study were *randomly* assigned to either the rhythm-control group or to the rate-control group, using blocked randomizations stratified by study center.

1.2 The MR CLEAN trial

Berkhemer et al. (2015) reported on the MR CLEAN trial, involving 500 patients with acute ischemic stroke caused by a proximal intracranial arterial occlusion. The trial was conducted at 16 medical centers in the Netherlands, where 233 were randomly assigned to the intervention (intraarterial treatment plus usual care) and 267 to control (usual care alone.) The primary outcome was the modified Rankin scale score at 90 days; this categorical scale measures functional outcome, with scores ranging from 0 (no symptoms) to 6 (death). The fundamental conclusion of Berkhemer et al. (2015) was that in patients with acute ischemic stroke

¹HER2 = human epidermal growth factor receptor type 2. Over-expression of this occurs in 15-20% of invasive breast cancers, and has been associated with poor outcomes.

²The complete Table 1 appears on pages 2668-2669 of Roy et al. (2008), but I have only reproduced the first page and the footnote in this excerpt.

caused by a proximal intracranial occlusion of the anterior circulation, intraarterial treatment administered within 6 hours after stroke onset was effective and safe.

Here's the Table 1 from Berkhemer et al. (2015).

Table 1. Baseline Characteristics of the 500 Patients.*		
Characteristic	Intervention (N = 233)	Control (N = 267)
Age — yr		
Median	65.8	65.7
Interquartile range	54.5–76.0	55.5–76.4
Male sex — no. (%)	135 (57.9)	157 (58.8)
NIHSS score†		
Median (interquartile range)	17 (14–21)	18 (14–22)
Range	3–30	4–38
Location of stroke in left hemisphere — no. (%)	116 (49.8)	153 (57.3)
History of ischemic stroke — no. (%)	29 (12.4)	25 (9.4)
Atrial fibrillation — no. (%)	66 (28.3)	69 (25.8)
Diabetes mellitus — no. (%)	34 (14.6)	34 (12.7)
Prestroke modified Rankin scale score — no. (%)‡		
0	190 (81.5)	214 (80.1)
1	21 (9.0)	29 (10.9)
2	12 (5.2)	13 (4.9)
>2	10 (4.3)	11 (4.1)
Systolic blood pressure — mm Hg§	146±26.0	145±24.4
Treatment with IV alteplase — no. (%)	203 (87.1)	242 (90.6)
Time from stroke onset to start of IV alteplase — min		
Median	85	87
Interquartile range	67–110	65–116
ASPECTS — median (interquartile range)¶	9 (7–10)	9 (8–10)
Intracranial arterial occlusion — no./total no. (%)		
Intracranial ICA	1/233 (0.4)	3/266 (1.1)
ICA with involvement of the M1 middle cerebral artery segment	59/233 (25.3)	75/266 (28.2)
M1 middle cerebral artery segment	154/233 (66.1)	165/266 (62.0)
M2 middle cerebral artery segment	18/233 (7.7)	21/266 (7.9)
A1 or A2 anterior cerebral artery segment	1/233 (0.4)	2/266 (0.8)
Extracranial ICA occlusion — no./total no. (%) **	75/233 (32.2)	70/266 (26.3)
Time from stroke onset to randomization — min††		
Median	204	196
Interquartile range	152–251	149–266
Time from stroke onset to groin puncture — min		
Median	260	NA
Interquartile range	210–313	

The Table was accompanied by the following notes.

- * The intervention group was assigned to intraarterial treatment plus usual care, and the control group was assigned to usual care alone. Plus-minus values are means \pm SD. ICA denotes internal carotid artery, IV intravenous, and NA not applicable.
- † Scores on the National Institutes of Health Stroke Scale (NIHSS) range from 0 to 42, with higher scores indicating more severe neurologic deficits. The NIHSS is a 15-item scale, and values for 30 of the 7500 items were missing (0.4%). The highest number of missing items for a single patient was 6.
- ‡ Scores on the modified Rankin scale of functional disability range from 0 (no symptoms) to 6 (death). A score of 2 or less indicates functional independence.
- § Data on systolic blood pressure at baseline were missing for one patient assigned to the control group.
- ¶ The Alberta Stroke Program Early Computed Tomography Score (ASPECTS) is a measure of the extent of stroke. Scores ranges from 0 to 10, with higher scores indicating fewer early ischemic changes. Scores were not available for four patients assigned to the control group: noncontrast computed tomography was not performed in one patient, and three patients had strokes in the territory of the anterior cerebral artery.
- || Vessel imaging was not performed in one patient in the control group, so the level of occlusion was not known.
- ** Extracranial ICA occlusions were reported by local investigators.
- †† Data were missing for two patients in the intervention group.

1.3 Simulated fakestroke data

Consider the simulated data, available on the Data and Code page of our course website in the `fakestroke.csv` file, which I built to let us mirror the Table 1 for MR CLEAN (Berkhemer et al., 2015). The `fakestroke.csv` file contains the following 18 variables for 500 patients.

Variable	Description
<code>studyid</code>	Study ID # (z001 through z500)
<code>trt</code>	Treatment group (Intervention or Control)
<code>age</code>	Age in years
<code>sex</code>	Male or Female
<code>nihss</code>	NIH Stroke Scale Score (can range from 0-42; higher scores indicate more severe neurological deficits)
<code>location</code>	Stroke Location - Left or Right Hemisphere
<code>hx.isch</code>	History of Ischemic Stroke (Yes/No)
<code>afib</code>	Atrial Fibrillation (1 = Yes, 0 = No)
<code>dm</code>	Diabetes Mellitus (1 = Yes, 0 = No)
<code>mrankin</code>	Pre-stroke modified Rankin scale score (0, 1, 2 or > 2) indicating functional disability - complete range is 0 (no symptoms) to 6 (death)
<code>sbp</code>	Systolic blood pressure, in mm Hg
<code>iv.altep</code>	Treatment with IV alteplase (Yes/No)
<code>time.iv</code>	Time from stroke onset to start of IV alteplase (minutes) if <code>iv.altep=Yes</code>
<code>aspects</code>	Alberta Stroke Program Early Computed Tomography score, which measures extent of stroke from 0 - 10; higher scores indicate fewer early ischemic changes
<code>ia.occlus</code>	Intracranial arterial occlusion, based on vessel imaging - five categories ³
<code>extra.ica</code>	Extracranial ICA occlusion (1 = Yes, 0 = No)
<code>time.rand</code>	Time from stroke onset to study randomization, in minutes
<code>time.punc</code>	Time from stroke onset to groin puncture, in minutes (only if Intervention)

Here's a quick look at the simulated data in `fakestroke`.

³The five categories are Intracranial ICA, ICA with involvement of the M1 middle cerebral artery segment, M1 middle cerebral artery segment, M2 middle cerebral artery segment, A1 or A2 anterior cerebral artery segment

```
fakestroke
# A tibble: 500 x 18
  studyid trt      age sex  nihss location hx.isch afib  dm mrankin
  <fct>   <fct>   <dbl> <fct> <int> <fct>   <fct>  <int> <int> <fct>
1 z001   Control  53.0 Male    21 Right   No        0      0 2
2 z002   Interv~  51.0 Male    23 Left    No        1      0 0
3 z003   Control  68.0 Fema~   11 Right   No        0      0 0
4 z004   Control  28.0 Male    22 Left    No        0      0 0
5 z005   Control  91.0 Male    24 Right   No        0      0 0
6 z006   Control  34.0 Fema~   18 Left    No        0      0 2
7 z007   Interv~  75.0 Male    25 Right   No        0      0 0
8 z008   Control  89.0 Fema~   18 Right   No        0      0 0
9 z009   Control  75.0 Male    25 Left    No        1      0 2
10 z010  Interv~  26.0 Fema~   27 Right   No        0      0 0
# ... with 490 more rows, and 8 more variables: sbp <int>, iv.altep <fct>,
#   time.iv <int>, aspects <int>, ia.occlus <fct>, extra.ica <int>,
#   time.rand <int>, time.punc <int>
```

1.4 Building Table 1 for fakestroke: Attempt 1

Our goal, then, is to take the data in `fakestroke.csv` and use it to generate a Table 1 for the study that compares the 233 patients in the Intervention group to the 267 patients in the Control group, on all of the other variables (except study ID #) available. I'll use the `tableone` package of functions available in R to help me complete this task. We'll make a first attempt, using the `CreateTableOne` function in the `tableone` package. To use the function, we'll need to specify:

- the `vars` or variables we want to place in the rows of our Table 1 (which will include just about everything in the `fakestroke` data except the `studyid` code and the `trt` variable for which we have other plans, and the `time.punc` which applies only to subjects in the Intervention group.)
 - A useful trick here is to use the `dput` function, specifically something like `dput(names(fakestroke))` can be used to generate a list of all of the variables included in the `fakestroke` tibble, and then this can be copied and pasted into the `vars` specification, saving some typing.
- the `strata` which indicates the levels want to use in the columns of our Table 1 (for us, that's `trt`)

```
fs.vars <- c("age", "sex", "nihss", "location",
            "hx.isch", "afib", "dm", "mrainkin", "sbp",
            "iv.altep", "time.iv", "aspects",
            "ia.occlus", "extra.ica", "time.rand")

fs.trt <- c("trt")

att1 <- CreateTableOne(data = fakestroke,
                      vars = fs.vars,
                      strata = fs.trt)

print(att1)
```

	Stratified by trt		p	test
	Control 267	Intervention 233		
n				
age (mean (sd))	65.38 (16.10)	63.93 (18.09)	0.343	
sex = Male (%)	157 (58.8)	135 (57.9)	0.917	
nihss (mean (sd))	18.08 (4.32)	17.97 (5.04)	0.787	
location = Right (%)	114 (42.7)	117 (50.2)	0.111	

hx.isch = Yes (%)	25 (9.4)	29 (12.4)	0.335
afib (mean (sd))	0.26 (0.44)	0.28 (0.45)	0.534
dm (mean (sd))	0.13 (0.33)	0.12 (0.33)	0.923
mrankin (%)			0.922
> 2	11 (4.1)	10 (4.3)	
0	214 (80.1)	190 (81.5)	
1	29 (10.9)	21 (9.0)	
2	13 (4.9)	12 (5.2)	
sbp (mean (sd))	145.00 (24.40)	146.03 (26.00)	0.647
iv.altep = Yes (%)	242 (90.6)	203 (87.1)	0.267
time.iv (mean (sd))	87.96 (26.01)	98.22 (45.48)	0.003
aspects (mean (sd))	8.65 (1.47)	8.35 (1.64)	0.033
ia.occlus (%)			0.795
A1 or A2	2 (0.8)	1 (0.4)	
ICA with M1	75 (28.2)	59 (25.3)	
Intracranial ICA	3 (1.1)	1 (0.4)	
M1	165 (62.0)	154 (66.1)	
M2	21 (7.9)	18 (7.7)	
extra.ica (mean (sd))	0.26 (0.44)	0.32 (0.47)	0.150
time.rand (mean (sd))	213.88 (70.29)	202.51 (57.33)	0.051

1.4.1 Some of this is very useful, and other parts need to be fixed.

1. The 1/0 variables (`afib`, `dm`, `extra.ica`) might be better if they were treated as the factors they are, and reported as the Yes/No variables are reported, with counts and percentages rather than with means and standard deviations.
2. In some cases, we may prefer to re-order the levels of the categorical (factor) variables, particularly the `mrankin` variable, but also the `ia.occlus` variable. It would also be more typical to put the Intervention group to the left and the Control group to the right, so we may need to adjust our `trt` variable's levels accordingly.
3. For each of the quantitative variables (`age`, `nihss`, `sbp`, `time.iv`, `aspects`, `extra.ica`, `time.rand` and `time.punc`) we should make a decision whether a summary with mean and standard deviation is appropriate, or whether we should instead summarize with, say, the median and quartiles. A mean and standard deviation really only yields an appropriate summary when the data are least approximately Normally distributed. This will make the p values a bit more reasonable, too. The `test` column in the first attempt will soon have something useful to tell us.
4. If we'd left in the `time.punc` variable, we'd get some warnings, having to do with the fact that `time.punc` is only relevant to patients in the Intervention group.

1.4.2 fakestroke Cleaning Up Categorical Variables

Let's specify each of the categorical variables as categorical explicitly. This helps the `CreateTableOne` function treat them appropriately, and display them with counts and percentages. This includes all of the 1/0, Yes/No and multi-categorical variables.

```
fs.factorvars <- c("sex", "location", "hx.isch", "afib", "dm",
                  "mrankin", "iv.altep", "ia.occlus", "extra.ica")
```

Then we simply add a `factorVars = fs.factorvars` call to the `CreateTableOne` function.

We also want to re-order some of those categorical variables, so that the levels are more useful to us. Specifically, we want to:

- place Intervention before Control in the `trt` variable,
- reorder the `mrankin` scale as 0, 1, 2, > 2, and

- rearrange the `ia.occlus` variable to the order⁴ presented in Berkhemer et al. (2015).

To accomplish this, we'll use the `fct_relevel` function from the `forcats` package (loaded with the rest of the core tidyverse packages) to reorder our levels manually.

```
fakestroke <- fakestroke %>%
  mutate(trt = fct_relevel(trt, "Intervention", "Control"),
         mrankin = fct_relevel(mrankin, "0", "1", "2", "> 2"),
         ia.occlus = fct_relevel(ia.occlus, "Intracranial ICA",
                                "ICA with M1", "M1", "M2",
                                "A1 or A2"))
```

1.5 fakestroke Table 1: Attempt 2

```
att2 <- CreateTableOne(data = fakestroke,
                      vars = fs.vars,
                      factorVars = fs.factorvars,
                      strata = fs.trt)

print(att2)
```

	Stratified by trt		p	test
	Intervention	Control		
n	233	267		
age (mean (sd))	63.93 (18.09)	65.38 (16.10)	0.343	
sex = Male (%)	135 (57.9)	157 (58.8)	0.917	
nihss (mean (sd))	17.97 (5.04)	18.08 (4.32)	0.787	
location = Right (%)	117 (50.2)	114 (42.7)	0.111	
hx.isch = Yes (%)	29 (12.4)	25 (9.4)	0.335	
afib = 1 (%)	66 (28.3)	69 (25.8)	0.601	
dm = 1 (%)	29 (12.4)	34 (12.7)	1.000	
mrarkin (%)			0.922	
0	190 (81.5)	214 (80.1)		
1	21 (9.0)	29 (10.9)		
2	12 (5.2)	13 (4.9)		
> 2	10 (4.3)	11 (4.1)		
sbp (mean (sd))	146.03 (26.00)	145.00 (24.40)	0.647	
iv.altep = Yes (%)	203 (87.1)	242 (90.6)	0.267	
time.iv (mean (sd))	98.22 (45.48)	87.96 (26.01)	0.003	
aspects (mean (sd))	8.35 (1.64)	8.65 (1.47)	0.033	
ia.occlus (%)			0.795	
Intracranial ICA	1 (0.4)	3 (1.1)		
ICA with M1	59 (25.3)	75 (28.2)		
M1	154 (66.1)	165 (62.0)		
M2	18 (7.7)	21 (7.9)		
A1 or A2	1 (0.4)	2 (0.8)		
extra.ica = 1 (%)	75 (32.2)	70 (26.3)	0.179	
time.rand (mean (sd))	202.51 (57.33)	213.88 (70.29)	0.051	

The categorical data presentation looks much improved.

⁴We might also have considered reordering the `ia.occlus` factor by its frequency, using the `fct_infreq` function

1.5.1 What summaries should we show?

Now, we'll move on to the issue of making a decision about what type of summary to show for the quantitative variables. Since the `fakestroke` data are just simulated and only match the summary statistics of the original results, not the details, we'll adopt the decisions made by Berkhemer et al. (2015), which were to use medians and interquartile ranges to summarize the distributions of all of the continuous variables **except** systolic blood pressure.

- Specifying certain quantitative variables as *non-normal* causes R to show them with medians and the 25th and 75th percentiles, rather than means and standard deviations, and also causes those variables to be tested using non-parametric tests, like the Wilcoxon signed rank test, rather than the t test. The `test` column indicates this with the word `nonnorm`.
 - In real data situations, what should we do? The answer is to look at the data. I would not make the decision as to which approach to take without first plotting (perhaps in a histogram or a Normal Q-Q plot) the observed distributions in each of the two samples, so that I could make a sound decision about whether Normality was a reasonable assumption. If the means and medians are meaningfully different from each other, this is especially important.
 - To be honest, though, if the variable in question is a relatively unimportant covariate and the *p* values for the two approaches are nearly the same, I'm not sure that further investigation is especially important.
- Specifying *exact* tests for certain categorical variables (we'll try this for the `location` and `mrarkin` variables) can be done, and these changes will be noted in the `test` column, as well.
 - In real data situations, I would rarely be concerned about this issue, and often choose Pearson (approximate) options across the board. This is reasonable so long as the number of subjects falling in each category is reasonably large, say above 10. If not, then an exact test may be an improvement.

To accomplish the Table 1, then, we need to specify which variables should be treated as non-Normal in the `print` statement - notice that we don't need to redo the `CreateTableOne` for this change.

```
print(att2,
      nonnormal = c("age", "nihss", "time.iv", "aspects", "time.rand"),
      exact = c("location", "mrarkin"))
```

	Stratified by trt	
	Intervention	Control
n	233	267
age (median [IQR])	65.80 [54.50, 76.00]	65.70 [55.75, 76.20]
sex = Male (%)	135 (57.9)	157 (58.8)
nihss (median [IQR])	17.00 [14.00, 21.00]	18.00 [14.00, 22.00]
location = Right (%)	117 (50.2)	114 (42.7)
hx.isch = Yes (%)	29 (12.4)	25 (9.4)
afib = 1 (%)	66 (28.3)	69 (25.8)
dm = 1 (%)	29 (12.4)	34 (12.7)
mrarkin (%)		
0	190 (81.5)	214 (80.1)
1	21 (9.0)	29 (10.9)
2	12 (5.2)	13 (4.9)
> 2	10 (4.3)	11 (4.1)
sbp (mean (sd))	146.03 (26.00)	145.00 (24.40)
iv.altep = Yes (%)	203 (87.1)	242 (90.6)
time.iv (median [IQR])	85.00 [67.00, 110.00]	87.00 [65.00, 116.00]
aspects (median [IQR])	9.00 [7.00, 10.00]	9.00 [8.00, 10.00]
ia.occlus (%)		
Intracranial ICA	1 (0.4)	3 (1.1)
ICA with M1	59 (25.3)	75 (28.2)

```

M1                      154 (66.1)                      165 (62.0)
M2                      18 ( 7.7)                       21 ( 7.9)
A1 or A2                 1 ( 0.4)                       2 ( 0.8)
extra.ica = 1 (%)       75 (32.2)                      70 (26.3)
time.rand (median [IQR]) 204.00 [152.00, 249.50] 196.00 [149.00, 266.00]

Stratified by trt
p      test
n
age (median [IQR])      0.579 nonnorm
sex = Male (%)          0.917
nihss (median [IQR])    0.453 nonnorm
location = Right (%)    0.106 exact
hx.isch = Yes (%)       0.335
afib = 1 (%)            0.601
dm = 1 (%)              1.000
mrankin (%)             0.917 exact
0
1
2
> 2
sbp (mean (sd))         0.647
iv.altep = Yes (%)      0.267
time.iv (median [IQR])  0.596 nonnorm
aspects (median [IQR])  0.075 nonnorm
ia.occlus (%)           0.795
  Intracranial ICA
  ICA with M1
  M1
  M2
  A1 or A2
extra.ica = 1 (%)       0.179
time.rand (median [IQR]) 0.251 nonnorm

```

1.6 Obtaining a more detailed Summary

If this was a real data set, we'd want to get a more detailed description of the data to make decisions about things like potentially collapsing categories of a variable, or whether or not a normal distribution was useful for a particular continuous variable, etc. You can do this with the `summary` command applied to a created Table 1, which shows, among other things, the effect of changing from normal to non-normal p values for continuous variables, and from approximate to “exact” p values for categorical factors.

Again, as noted above, in a real data situation, we'd want to plot the quantitative variables (within each group) to make a smart decision about whether a t test or Wilcoxon approach is more appropriate.

Note in the summary below that we have some missing values here. Often, we'll present this information within the Table 1, as well.

```
summary(att2)
```

```
### Summary of continuous variables ###
```

```
trt: Intervention
```

```
      n miss p.miss mean sd median p25 p75 min max  skew  kurt
```

age	233	0	0.0	64	18	66	54	76	23	96	-0.34	-0.52
nihss	233	0	0.0	18	5	17	14	21	10	28	0.48	-0.74
sbp	233	0	0.0	146	26	146	129	164	78	214	-0.07	-0.22
time.iv	233	30	12.9	98	45	85	67	110	42	218	1.03	0.08
aspects	233	0	0.0	8	2	9	7	10	5	10	-0.56	-0.98
time.rand	233	2	0.9	203	57	204	152	250	100	300	0.01	-1.16

trt: Control

	n	miss	p.miss	mean	sd	median	p25	p75	min	max	skew	kurt
age	267	0	0.0	65	16	66	56	76	24	94	-0.296	-0.28
nihss	267	0	0.0	18	4	18	14	22	11	25	0.017	-1.24
sbp	267	1	0.4	145	24	145	128	161	82	231	0.156	0.08
time.iv	267	25	9.4	88	26	87	65	116	44	130	0.001	-1.32
aspects	267	4	1.5	9	1	9	8	10	5	10	-1.071	0.36
time.rand	267	0	0.0	214	70	196	149	266	120	360	0.508	-0.93

p-values

	pNormal	pNonNormal
age	0.342813660	0.57856976
nihss	0.787487252	0.45311695
sbp	0.647157646	0.51346132
time.iv	0.003073372	0.59641104
aspects	0.032662901	0.07464683
time.rand	0.050803672	0.25134327

Standardize mean differences

	1 vs 2
age	0.08478764
nihss	0.02405390
sbp	0.04100833
time.iv	0.27691223
aspects	0.19210662
time.rand	0.17720957

=====
 ### Summary of categorical variables ###

trt: Intervention

var	n	miss	p.miss	level	freq	percent	cum.percent
sex	233	0	0.0	Female	98	42.1	42.1
				Male	135	57.9	100.0
location	233	0	0.0	Left	116	49.8	49.8
				Right	117	50.2	100.0
hx.isch	233	0	0.0	No	204	87.6	87.6
				Yes	29	12.4	100.0
afib	233	0	0.0	0	167	71.7	71.7
				1	66	28.3	100.0
dm	233	0	0.0	0	204	87.6	87.6
				1	29	12.4	100.0

mrankin	233	0	0.0		0	190	81.5	81.5
					1	21	9.0	90.6
					2	12	5.2	95.7
					> 2	10	4.3	100.0
iv.altep	233	0	0.0		No	30	12.9	12.9
					Yes	203	87.1	100.0
ia.occlus	233	0	0.0	Intracranial ICA	1	0.4		0.4
				ICA with M1	59	25.3		25.8
				M1	154	66.1		91.8
				M2	18	7.7		99.6
				A1 or A2	1	0.4		100.0
extra.ica	233	0	0.0		0	158	67.8	67.8
					1	75	32.2	100.0

trt: Control								
	var	n	miss	p.miss	level	freq	percent	cum.percent
	sex	267	0	0.0	Female	110	41.2	41.2
					Male	157	58.8	100.0
location	267	0	0.0		Left	153	57.3	57.3
					Right	114	42.7	100.0
hx.isch	267	0	0.0		No	242	90.6	90.6
					Yes	25	9.4	100.0
afib	267	0	0.0		0	198	74.2	74.2
					1	69	25.8	100.0
dm	267	0	0.0		0	233	87.3	87.3
					1	34	12.7	100.0
mrankin	267	0	0.0		0	214	80.1	80.1
					1	29	10.9	91.0
					2	13	4.9	95.9
					> 2	11	4.1	100.0
iv.altep	267	0	0.0		No	25	9.4	9.4
					Yes	242	90.6	100.0
ia.occlus	267	1	0.4	Intracranial ICA	3	1.1		1.1
				ICA with M1	75	28.2		29.3
				M1	165	62.0		91.4
				M2	21	7.9		99.2
				A1 or A2	2	0.8		100.0
extra.ica	267	1	0.4		0	196	73.7	73.7
					1	70	26.3	100.0

```
p-values
      pApprox  pExact
sex      0.9171387 0.8561188
location 0.1113553 0.1056020
hx.isch  0.3352617 0.3124683
afib      0.6009691 0.5460206
dm        1.0000000 1.0000000
mrankin  0.9224798 0.9173657
iv.altep  0.2674968 0.2518374
ia.occlus 0.7945580 0.8189090
extra.ica 0.1793385 0.1667574
```

```
Standardize mean differences
      1 vs 2
sex      0.017479025
location 0.151168444
hx.isch  0.099032275
afib      0.055906317
dm        0.008673478
mrankin  0.062543164
iv.altep  0.111897009
ia.occlus 0.117394890
extra.ica 0.129370206
```

In this case, I have simulated the data to mirror the results in the published Table 1 for this study. In no way have I captured the full range of the real data, or any of the relationships in that data, so it's more important here to see what's available in the analysis, rather than to interpret it closely in the clinical context.

1.7 Exporting the Completed Table 1 from R to Excel or Word

Once you've built the table and are generally satisfied with it, you'll probably want to be able to drop it into Excel or Word for final cleanup.

1.7.1 Approach A: Save and open in Excel

One option is to **save the Table 1** to a `.csv` file, which you can then open directly in Excel. This is the approach I generally use. Note the addition of some `quote`, `noSpaces` and `printToggle` selections here.

```
fs.table1save <- print(att2,
  nonnormal = c("age", "nihss", "time.iv", "aspects", "time.rand"),
  exact = c("location", "mrankin"),
  quote = FALSE, noSpaces = TRUE, printToggle = FALSE)

write.csv(fs.table1save, file = "fs-table1.csv")
```

When I then open the `fs-table1.csv` file in Excel, it looks like this:

	A	B	C	D	E
1		Intervention	Control	p	test
2	n	233	267		
3	age (median [IQR])	65.80 [54.50, 76.00]	65.70 [55.75, 76.20]	0.579	nonnorm
4	sex = Male (%)	135 (57.9)	157 (58.8)	0.917	
5	nihss (median [IQR])	17.00 [14.00, 21.00]	18.00 [14.00, 22.00]	0.453	nonnorm
6	location = Right (%)	117 (50.2)	114 (42.7)	0.111	
7	hx.isch = Yes (%)	29 (12.4)	25 (9.4)	0.335	
8	afib = 1 (%)	66 (28.3)	69 (25.8)	0.601	
9	dm = 1 (%)	29 (12.4)	34 (12.7)	1	
10	mrarkin (%)			0.922	
11		0 190 (81.5)	214 (80.1)		
12		1 21 (9.0)	29 (10.9)		
13		2 12 (5.2)	13 (4.9)		
14	> 2	10 (4.3)	11 (4.1)		
15	sbp (mean (sd))	146.03 (26.00)	145.00 (24.40)	0.647	
16	iv.altep = Yes (%)	203 (87.1)	242 (90.6)	0.267	
17	time.iv (median [IQR])	85.00 [67.00, 110.00]	87.00 [65.00, 116.00]	0.596	nonnorm
18	aspects (median [IQR])	9.00 [7.00, 10.00]	9.00 [8.00, 10.00]	0.075	nonnorm
19	ia.occlus (%)			0.795	
20	Intracranial ICA	1 (0.4)	3 (1.1)		
21	ICA with M1	59 (25.3)	75 (28.2)		
22	M1	154 (66.1)	165 (62.0)		
23	M2	18 (7.7)	21 (7.9)		
24	A1 or A2	1 (0.4)	2 (0.8)		
25	extra.ica = 1 (%)	75 (32.2)	70 (26.3)	0.179	
26	time.rand (median [IQR])	204.00 [152.00, 249.50]	196.00 [149.00, 266.00]	0.251	nonnorm
27	time.punc (median [IQR])	260.00 [212.00, 313.00]	NA [NA, NA]	NA	nonnorm

And from here, I can either drop it directly into Word, or present it as is, or start tweaking it to meet formatting needs.

1.7.2 Approach B: Produce the Table so you can cut and paste it

```
print(att2,
      nonnormal = c("age", "nihss", "time.iv", "aspects", "time.rand"),
      exact = c("location", "mrarkin"),
      quote = TRUE, noSpaces = TRUE)
```

This will look like a mess by itself, but if you:

1. copy and paste that mess into Excel
2. select Text to Columns from the Data menu
3. select Delimited, then Space and select Treat consecutive delimiters as one

you should get something usable again.

Or, in Word,

1. insert the text

2. select the text with your mouse
3. select Insert ... Table ... Convert Text to Table
4. place a quotation mark in the “Other” area under Separate text at ...

After dropping blank columns, the result looks pretty good.

1.8 A Controlled Biological Experiment - The Blood-Brain Barrier

My source for the data and the following explanatory paragraph is page 307 from Ramsey and Schafer (2002). The original data come from Barnett et al. (1995).

The human brain (and that of rats, coincidentally) is protected from the bacteria and toxins that course through the bloodstream by something called the blood-brain barrier. After a method of disrupting the barrier was developed, researchers tested this new mechanism, as follows. A series of 34 rats were inoculated with human lung cancer cells to induce brain tumors. After 9-11 days they were infused with either the barrier disruption (BD) solution or, as a control, a normal saline (NS) solution. Fifteen minutes later, the rats received a standard dose of a particular therapeutic antibody (L6-F(ab')₂). The key measure of the effectiveness of transmission across the brain-blood barrier is the ratio of the antibody concentration in the brain tumor to the antibody concentration in normal tissue outside the brain. The rats were then sacrificed, and the amounts of antibody in the brain tumor and in normal tissue from the liver were measured. The study's primary objective is to determine whether the antibody concentration in the tumor increased when the blood-barrier disruption infusion was given, and if so, by how much?

1.9 The `bloodbrain.csv` file

Consider the data, available on the Data and Code page of our course website in the `bloodbrain.csv` file, which includes the following variables:

Variable	Description
<code>case</code>	identification number for the rat (1 - 34)
<code>brain</code>	an outcome: Brain tumor antibody count (per gram)
<code>liver</code>	an outcome: Liver antibody count (per gram)
<code>tlratio</code>	an outcome: tumor / liver concentration ratio
<code>solution</code>	the treatment: BD (barrier disruption) or NS (normal saline)
<code>sactime</code>	a design variable: Sacrifice time (hours; either 0.5, 3, 24 or 72)
<code>postin</code>	covariate: Days post-inoculation of lung cancer cells (9, 10 or 11)
<code>sex</code>	covariate: M or F
<code>wt.init</code>	covariate: Initial weight (grams)
<code>wt.loss</code>	covariate: Weight loss (grams)
<code>wt.tumor</code>	covariate: Tumor weight (10^{-4} grams)

And here's what the data look like in R.

```
bloodbrain
```

```
# A tibble: 34 x 11
  case brain  liver tlratio solution sactime postin sex  wt.init
<int> <int>  <int>  <dbl> <fct>      <dbl> <int> <fct>  <int>
1     1  41081 1456164 0.0282 BD         0.500     10 F      239
```



```

2      2  44286 1602171  0.0276 BD      0.500      10 F      225
3      3 102926 1601936  0.0642 BD      0.500      10 F      224
4      4  25927 1776411  0.0146 BD      0.500      10 F      184
5      5  42643 1351184  0.0316 BD      0.500      10 F      250
6      6  31342 1790863  0.0175 NS      0.500      10 F      196
7      7  22815 1633386  0.0140 NS      0.500      10 F      200
8      8  16629 1618757  0.0103 NS      0.500      10 F      273
9      9  22315 1567602  0.0142 NS      0.500      10 F      216
10     10 77961 1060057  0.0735 BD      3.00      10 F      267
# ... with 24 more rows, and 2 more variables: wt.loss <dbl>, wt.tumor
#   <int>

```

1.10 A Table 1 for bloodbrain

Barnett et al. (1995) did not provide a Table 1 for these data, so let's build one to compare the two **solutions** (BD vs. NS) on the covariates and outcomes, plus the natural logarithm of the tumor/liver concentration ratio (**tlratio**). We'll opt to treat the sacrifice time (**sactime**) and the days post-inoculation of lung cancer cells (**postin**) as categorical rather than quantitative variables.

```
bloodbrain <- bloodbrain %>%  
  mutate(logTL = log(tlratio))
```

```
dput(names(bloodbrain))
```

```
c("case", "brain", "liver", "tlratio", "solution", "sactime",
  "postin", "sex", "wt.init", "wt.loss", "wt.tumor", "logTL")
```

OK - there's the list of variables we'll need. I'll put the outcomes at the bottom of the table.

```
bb.vars <- c("sactime", "postin", "sex", "wt.init", "wt.loss",
            "wt.tumor", "brain", "liver", "tlratio", "logTL")
```

```
bb.factors <- c("sactime", "sex", "postin")
```

```
bb.att1 <- CreateTableOne(data = bloodbrain,
  vars = bb.vars,
  factorVars = bb.factors,
  strata = c("solution"))
summary(bb.att1)
```

```
### Summary of continuous variables ###
```

solution: BD

	n	miss	p.miss	mean	sd	median	p25	p75	min	max
wt.init	17	0	0	243	3e+01	2e+02	2e+02	3e+02	2e+02	3e+02
wt.loss	17	0	0	3	5e+00	4e+00	1e+00	6e+00	-5e+00	1e+01
wt.tumor	17	0	0	157	8e+01	2e+02	1e+02	2e+02	2e+01	4e+02
brain	17	0	0	56043	3e+04	5e+04	4e+04	8e+04	6e+03	1e+05
liver	17	0	0	672577	7e+05	6e+05	2e+04	1e+06	2e+03	2e+06
tlratio	17	0	0	2	3e+00	1e-01	6e-02	3e+00	1e-02	9e+00
logTL	17	0	0	-1	2e+00	-2e+00	-3e+00	1e+00	-4e+00	2e+00
		skew	kurt							
wt.init		-0.39	0.7							
wt.loss		-0.10	0.2							

```
wt.tumor 0.53 1.0
brain    0.29 -0.6
liver    0.35 -1.7
tlratio  1.58 1.7
logTL    0.08 -1.7
```

```
-----
solution: NS
```

	n	miss	p.miss	mean	sd	median	p25	p75	min	max
wt.init	17	0	0	240	3e+01	2e+02	2e+02	3e+02	2e+02	3e+02
wt.loss	17	0	0	4	4e+00	3e+00	2e+00	7e+00	-4e+00	1e+01
wt.tumor	17	0	0	209	1e+02	2e+02	2e+02	3e+02	3e+01	5e+02
brain	17	0	0	23887	1e+04	2e+04	1e+04	3e+04	1e+03	5e+04
liver	17	0	0	664975	7e+05	7e+05	2e+04	1e+06	9e+02	2e+06
tlratio	17	0	0	1	2e+00	5e-02	3e-02	9e-01	1e-02	7e+00
logTL	17	0	0	-2	2e+00	-3e+00	-3e+00	-7e-02	-5e+00	2e+00

	skew	kurt
wt.init	0.33	-0.48
wt.loss	-0.09	0.08
wt.tumor	0.63	0.77
brain	0.30	-0.35
liver	0.40	-1.56
tlratio	2.27	4.84
logTL	0.27	-1.61

```
p-values
```

	pNormal	pNonNormal
wt.init	0.807308940	0.641940278
wt.loss	0.683756156	0.876749808
wt.tumor	0.151510151	0.190482094
brain	0.001027678	0.002579901
liver	0.974853609	0.904045603
tlratio	0.320501715	0.221425879
logTL	0.351633525	0.221425879

```
Standardize mean differences
```

```
1 vs 2
wt.init 0.08435244
wt.loss 0.14099823
wt.tumor 0.50397184
brain 1.23884159
liver 0.01089667
tlratio 0.34611465
logTL 0.32420504
```

```
=====  
### Summary of categorical variables ###
```

```
solution: BD
```

var	n	miss	p.miss	level	freq	percent	cum.percent
sactime	17	0	0.0	0.5	5	29.4	29.4
				3	4	23.5	52.9
				24	4	23.5	76.5
				72	4	23.5	100.0

```

postin 17    0    0.0    9    1    5.9    5.9
              10   14   82.4   88.2
              11    2   11.8   100.0

sex 17      0    0.0    F   13   76.5   76.5
              M    4   23.5   100.0
-----
solution: NS
  var  n miss p.miss level freq percent cum.percent
sactime 17    0    0.0   0.5    4    23.5    23.5
              3    5    29.4    52.9
              24    4    23.5    76.5
              72    4    23.5   100.0

postin 17    0    0.0    9    2   11.8   11.8
              10   13   76.5   88.2
              11    2   11.8   100.0

sex 17      0    0.0    F   13   76.5   76.5
              M    4   23.5   100.0

```

p-values

```

      pApprox pExact
sactime 0.9739246    1
postin  0.8309504    1
sex      1.0000000    1

```

Standardize mean differences

```

      1 vs 2
sactime 0.1622214
postin  0.2098877
sex      0.0000000

```

Note that, in this particular case, the decisions we make about normality vs. non-normality (for quantitative variables) and the decisions we make about approximate vs. exact testing (for categorical variables) won't actually change the implications of the p values. Each approach gives similar results for each variable. Of course, that's not always true.

1.10.1 Generate final Table 1 for bloodbrain

I'll choose to treat `tlratio` and its logarithm as non-Normal, but otherwise, use t tests, but admittedly, that's an arbitrary decision, really.

```
print(bb.att1, nonnormal = c("tlratio", "logTL"))
```

```

Stratified by solution
      BD      NS
n      17      17
sactime (%)
  0.5      5 (29.4)  4 (23.5)
    3      4 (23.5)  5 (29.4)
   24      4 (23.5)  4 (23.5)

```

72	4 (23.5)	4 (23.5)
postin (%)		
9	1 (5.9)	2 (11.8)
10	14 (82.4)	13 (76.5)
11	2 (11.8)	2 (11.8)
sex = M (%)	4 (23.5)	4 (23.5)
wt.init (mean (sd))	242.82 (27.23)	240.47 (28.54)
wt.loss (mean (sd))	3.34 (4.68)	3.94 (3.88)
wt.tumor (mean (sd))	157.29 (84.00)	208.53 (116.68)
brain (mean (sd))	56043.41 (33675.40)	23887.18 (14610.53)
liver (mean (sd))	672577.35 (694479.58)	664975.47 (700773.13)
tlratio (median [IQR])	0.12 [0.06, 2.84]	0.05 [0.03, 0.94]
logTL (median [IQR])	-2.10 [-2.74, 1.04]	-2.95 [-3.41, -0.07]
Stratified by solution		
	p	test
n		
sactime (%)	0.974	
0.5		
3		
24		
72		
postin (%)	0.831	
9		
10		
11		
sex = M (%)	1.000	
wt.init (mean (sd))	0.807	
wt.loss (mean (sd))	0.684	
wt.tumor (mean (sd))	0.152	
brain (mean (sd))	0.001	
liver (mean (sd))	0.975	
tlratio (median [IQR])	0.221 nonnorm	
logTL (median [IQR])	0.221 nonnorm	

Or, we can get an Excel-readable version, using

```
bb.t1 <- print(bb.att1, nonnormal = c("tlratio", "logTL"), quote = FALSE,
               noSpaces = TRUE, printToggle = FALSE)

write.csv(bb.t1, file = "bb-table1.csv")
```

which, when dropped into Excel, will look like this:

	A	B	C	D	E
1		BD	NS	p	test
2	n	17	17		
3	sex = M (%)	4 (23.5)	4 (23.5)	1	
4	sactime (%)			0.974	
5	0.5	5 (29.4)	4 (23.5)		
6	3	4 (23.5)	5 (29.4)		
7	24	4 (23.5)	4 (23.5)		
8	72	4 (23.5)	4 (23.5)		
9	postin (%)			0.831	
10	9	1 (5.9)	2 (11.8)		
11	10	14 (82.4)	13 (76.5)		
12	11	2 (11.8)	2 (11.8)		
13	wt.init (mean (sd))	242.82 (27.23)	240.47 (28.54)	0.807	
14	wt.loss (mean (sd))	3.34 (4.68)	3.94 (3.88)	0.684	
15	wt.tumor (mean (sd))	157.29 (84.00)	208.53 (116.68)	0.152	
16	brain (mean (sd))	56043.41 (33675.40)	23887.18 (14610.53)	0.001	
17	liver (mean (sd))	672577.35 (694479.58)	664975.47 (700773.13)	0.975	
18	tlratio (median [IQR])	0.12 [0.06, 2.84]	0.05 [0.03, 0.94]	0.221	nonnorm
19	logTL (median [IQR])	-2.10 [-2.74, 1.04]	-2.95 [-3.41, -0.07]	0.221	nonnorm
20					

One thing I would definitely clean up here, in practice, is to change the presentation of the p value for **sex** from 1 to > 0.99 , or just omit it altogether. I'd also drop the **computer-ese** where possible, add units for the measures, round **a lot**, identify the outcomes carefully, and use notes to indicate deviations from the main approach.

1.10.2 A More Finished Version (after Cleanup in Word)

Table 1. Comparing Rats Receiving BD to those Receiving NS on Available Covariates and Design Variables, and Key Outcomes

	Barrier Disruption (BD: treatment)	Normal Saline (NS: control)	p
# of Rats	17	17	
Sex = Male	4 (23.5)	4 (23.5)	-
Sacrifice Time (hours)			0.97
0.5	5 (29.4)	4 (23.5)	
3	4 (23.5)	5 (29.4)	
24	4 (23.5)	4 (23.5)	
72	4 (23.5)	4 (23.5)	
Days post-inoculation of lung cancer cells			0.83
9	1 (5.9)	2 (11.8)	
10	14 (82.4)	13 (76.5)	
11	2 (11.8)	2 (11.8)	
Initial Weight (g)	243 (27)	240 (29)	0.81
Weight Loss (g)	3.3 (4.7)	3.9 (3.9)	0.68
Tumor Weight (10 ⁻⁴ g)	157.3 (84.0)	208.5 (116.7)	0.15
Key Outcomes: mean (sd) unless otherwise indicated			
Brain Tumor Antibody Count (per g)	56,043 (33,675)	23,887 (14,611)	0.001
Liver Antibody Count (per g)	672,577 (694,480)	664,975 (700,773)	0.98
Tumor/Liver Ratio (median [Q25, Q75])	0.12 [0.06, 2.84]	0.05 [0.03, 0.94]	0.22
Natural Log of Tumor/Liver Ratio (median [Q25, Q75])	-2.10 [-2.74, 1.04]	-2.95 [-3.41, -0.07]	0.22

Table 1 Notes:

- Categorical variables are summarized with counts, percentages and p values based on approximate chi-square tests.
- Continuous variables, unless otherwise indicated, are summarized with means, standard deviations and p values based on t tests.
- The Tumor / Liver ratio and its natural logarithm are summarized with the median and quartiles and a p value from a non-parametric (Wilcoxon signed rank) test.

Chapter 2

Linear Regression on a small SMART data set

2.1 BRFSS and SMART

The Centers for Disease Control analyzes Behavioral Risk Factor Surveillance System (BRFSS) survey data for specific metropolitan and micropolitan statistical areas (MMSAs) in a program called the Selected Metropolitan/Micropolitan Area Risk Trends of BRFSS (SMART BRFSS.)

In this work, we will focus on data from the 2016 SMART, and in particular on data from the Cleveland-Elyria, OH, Metropolitan Statistical Area. The purpose of this survey is to provide localized health information that can help public health practitioners identify local emerging health problems, plan and evaluate local responses, and efficiently allocate resources to specific needs.

2.1.1 Key resources

- the full data are available in the form of the 2016 SMART BRFSS MMSA Data, found in a zipped SAS Transport Format file. The data were released in August 2017.
- the MMSA Variable Layout PDF which simply lists the variables included in the data file
- the Calculated Variables PDF which describes the risk factors by data variable names - there is also an online summary matrix of these calculated variables, as well.
- the lengthy 2016 Survey Questions PDF which lists all questions asked as part of the BRFSS in 2016
- the enormous Codebook for the 2016 BRFSS Survey PDF which identifies the variables by name for us.

Later this term, we'll use all of those resources to help construct a more complete data set than we'll study today. I'll also demonstrate how I built the `smartcle1` data set that we'll use in this Chapter.

2.2 The `smartcle1` data: Cookbook

The `smartcle1.csv` data file available on the Data and Code page of our website describes information on 11 variables for 1036 respondents to the BRFSS 2016, who live in the Cleveland-Elyria, OH, Metropolitan Statistical Area. The variables in the `smartcle1.csv` file are listed below, along with (in some cases) the BRFSS items that generate these responses.

Variable	Description
SEQNO	respondent identification number (all begin with 2016)

Variable	Description
physhealth	Now thinking about your physical health, which includes physical illness and injury, for how many days during the past 30 days was your physical health not good?
menthealth	Now thinking about your mental health, which includes stress, depression, and problems with emotions, for how many days during the past 30 days was your mental health not good?
poorhealth	During the past 30 days, for about how many days did poor physical or mental health keep you from doing your usual activities, such as self-care, work, or recreation?
genhealth	Would you say that in general, your health is ... (five categories: Excellent, Very Good, Good, Fair or Poor)
bmi	Body mass index, in kg/m ²
female	Sex, 1 = female, 0 = male
internet30	Have you used the internet in the past 30 days? (1 = yes, 0 = no)
exerany	During the past month, other than your regular job, did you participate in any physical activities or exercises such as running, calisthenics, golf, gardening, or walking for exercise? (1 = yes, 0 = no)
sleephrs	On average, how many hours of sleep do you get in a 24-hour period?
alcdays	How many days during the past 30 days did you have at least one drink of any alcoholic beverage such as beer, wine, a malt beverage or liquor?

```
str(smartcle1)
```

```
Classes 'tbl_df', 'tbl' and 'data.frame':  1036 obs. of  11 variables:
 $ SEQNO      : num  2.02e+09 2.02e+09 2.02e+09 2.02e+09 2.02e+09 ...
 $ physhealth: int   0 0 1 0 5 4 2 2 0 0 ...
 $ menthealth: int   0 0 5 0 0 18 0 3 0 0 ...
 $ poorhealth: int  NA NA 0 NA 0 6 0 0 NA NA ...
 $ genhealth  : Factor w/ 5 levels "1_Excellent",...: 2 1 2 3 1 2 3 3 2 3 ...
 $ bmi        : num   26.7 23.7 26.9 21.7 24.1 ...
 $ female     : int   1 0 0 1 0 0 1 1 0 0 ...
 $ internet30: int   1 1 1 1 1 1 1 1 1 1 ...
 $ exerany    : int   1 1 0 1 1 1 1 1 1 0 ...
 $ sleephrs   : int   6 6 8 9 7 5 9 7 7 7 ...
 $ alcdays    : int   1 4 4 3 2 28 4 2 4 25 ...
```

2.3 smartcle2: Omitting Missing Observations: Complete-Case Analyses

For the purpose of fitting our first few models, we will eliminate the missingness problem, and look only at the *complete cases* in our `smartcle1` data.

To inspect the missingness in our data, we might consider using the `skim` function from the `skimr` package. We'll exclude the respondent identifier code (`SEQNO`) from this summary as uninteresting.

```
skim_with(numeric = list(hist = NULL), integer = list(hist = NULL))
## above line eliminates the sparkline histograms
## it can be commented out when working in the console,
## but I need it to produce the Notes without errors right now
```



```
smartcle1 %>%
  skim(-SEQNO)
```

Skim summary statistics

```
n obs: 1036
n variables: 11
```

Variable type: factor

```
variable missing complete    n n_unique
genhealth      3      1033 1036      5
               top_counts ordered
2_V: 350, 3_G: 344, 1_E: 173, 4_F: 122  FALSE
```

Variable type: integer

```
variable missing complete    n mean  sd p0 p25 median p75 p100
alcdays      46      990 1036 4.65 8.05 0  0      1  4   30
exerany       3      1033 1036 0.76 0.43 0  1      1  1   1
female        0      1036 1036 0.6  0.49 0  0      1  1   1
internet30     6      1030 1036 0.81 0.39 0  1      1  1   1
menthealth    11      1025 1036 2.72 6.82 0  0      0  2   30
physhealth    17      1019 1036 3.97 8.67 0  0      0  2   30
poorhealth   543       493 1036 4.07 8.09 0  0      0  3   30
sleephrs      8      1028 1036 7.02 1.53 1  6      7  8   20
```

Variable type: numeric

```
variable missing complete    n mean  sd  p0 p25 median  p75 p100
bmi          84      952 1036 27.89 6.47 12.71 23.7 26.68 30.53 66.06
```

Now, we'll create a new tibble called `smartcle2` which contains every variable except `poorhealth`, and which includes all respondents with complete data on the variables (other than `poorhealth`). We'll store those observations with complete data in the `smartcle2` tibble.

```
smartcle2 <- smartcle1 %>%
  select(-poorhealth) %>%
  filter(complete.cases(.))
```

```
smartcle2
```

```
# A tibble: 896 x 10
```

```
  SEQNO physhealth menthealth genhealth  bmi female internet30 exerany
  <dbl>   <int>      <int> <fct>    <dbl> <int>      <int>   <int>
1  2.02e9     0         0 2_VeryGo~ 26.7     1         1       1
2  2.02e9     0         0 1_Excell~ 23.7     0         1       1
3  2.02e9     1         5 2_VeryGo~ 26.9     0         1       0
4  2.02e9     0         0 3_Good    21.7     1         1       1
5  2.02e9     5         0 1_Excell~ 24.1     0         1       1
6  2.02e9     4        18 2_VeryGo~ 27.6     0         1       1
7  2.02e9     2         0 3_Good    25.7     1         1       1
8  2.02e9     2         3 3_Good    28.5     1         1       1
9  2.02e9     0         0 2_VeryGo~ 28.6     0         1       1
10 2.02e9     0         0 3_Good    23.1     0         1       0
# ... with 886 more rows, and 2 more variables: sleephrs <int>, alcdays
#   <int>
```

Note that there are only 896 respondents with **complete** data on the 10 variables (excluding `poorhealth`) in the `smartcle2` tibble, as compared to our original `smartcle1` data which described 1036 respondents and

11 variables, but with lots of missing data.

2.4 Summarizing the `smartcle2` data numerically

2.4.1 The New Toy: The `skim` function

```
skim(smartcle2, -SEQNO)
```

Skim summary statistics

n obs: 896

n variables: 10

Variable type: factor

variable	missing	complete	n	n_unique
genhealth	0	896	896	5

top_counts ordered

2_V: 306, 3_G: 295, 1_E: 155, 4_F: 102 FALSE

Variable type: integer

variable	missing	complete	n	mean	sd	p0	p25	median	p75	p100
alcdays	0	896	896	4.83	8.14	0	0	1	5	30
exerany	0	896	896	0.77	0.42	0	1	1	1	1
female	0	896	896	0.58	0.49	0	0	1	1	1
internet30	0	896	896	0.81	0.39	0	1	1	1	1
menthealth	0	896	896	2.69	6.72	0	0	0	2	30
physhealth	0	896	896	3.99	8.64	0	0	0	2	30
sleephrs	0	896	896	7.02	1.48	1	6	7	8	20

Variable type: numeric

variable	missing	complete	n	mean	sd	p0	p25	median	p75	p100
bmi	0	896	896	27.87	6.33	12.71	23.7	26.8	30.53	66.06

2.4.2 The usual summary for a data frame

Of course, we can use the usual `summary` to get some basic information about the data.

```
summary(smartcle2)
```

SEQNO	physhealth	menthealth	genhealth
Min. :2.016e+09	Min. : 0.00	Min. : 0.000	1_Excellent:155
1st Qu.:2.016e+09	1st Qu.: 0.00	1st Qu.: 0.000	2_VeryGood :306
Median :2.016e+09	Median : 0.00	Median : 0.000	3_Good :295
Mean :2.016e+09	Mean : 3.99	Mean : 2.693	4_Fair :102
3rd Qu.:2.016e+09	3rd Qu.: 2.00	3rd Qu.: 2.000	5_Poor : 38
Max. :2.016e+09	Max. :30.00	Max. :30.000	
bmi	female	internet30	exerany
Min. :12.71	Min. :0.0000	Min. :0.0000	Min. :0.0000
1st Qu.:23.70	1st Qu.:0.0000	1st Qu.:1.0000	1st Qu.:1.0000
Median :26.80	Median :1.0000	Median :1.0000	Median :1.0000
Mean :27.87	Mean :0.5848	Mean :0.8147	Mean :0.7667
3rd Qu.:30.53	3rd Qu.:1.0000	3rd Qu.:1.0000	3rd Qu.:1.0000
Max. :66.06	Max. :1.0000	Max. :1.0000	Max. :1.0000

sleephrs	alcdays
Min. : 1.000	Min. : 0.000
1st Qu.: 6.000	1st Qu.: 0.000
Median : 7.000	Median : 1.000
Mean : 7.022	Mean : 4.834
3rd Qu.: 8.000	3rd Qu.: 5.000
Max. : 20.000	Max. : 30.000

2.4.3 The describe function in Hmisc

Or we can use the describe function from the Hmisc package.

```
Hmisc::describe(select(smartcle2, bmi, genhealth, female))
```

```
select(smartcle2, bmi, genhealth, female)
```

```
3 Variables      896 Observations
-----
```

bmi								
	n	missing	distinct	Info	Mean	Gmd	.05	.10
	896	0	467	1	27.87	6.572	20.06	21.23
	.25	.50	.75	.90	.95			
	23.70	26.80	30.53	35.36	39.30			

lowest : 12.71 13.34 14.72 16.22 17.30, highest: 56.89 57.04 60.95 61.84 66.06

```
-----
```

genhealth					
	n	missing	distinct		
	896	0	5		

Value	1_Excellent	2_VeryGood	3_Good	4_Fair	5_Poor
Frequency	155	306	295	102	38
Proportion	0.173	0.342	0.329	0.114	0.042

```
-----
```

female							
	n	missing	distinct	Info	Sum	Mean	Gmd
	896	0	2	0.728	524	0.5848	0.4862

```
-----
```

2.5 Counting as exploratory data analysis

Counting things can be amazingly useful.

2.5.1 How many respondents had exercised in the past 30 days? Did this vary by sex?

```
smartcle2 %>% count(female, exerany) %>% mutate(percent = 100*n / sum(n))
```

```
# A tibble: 4 x 4
  female exerany      n percent
  <int>   <int> <int>   <dbl>
```

1	0	0	64	7.14
2	0	1	308	34.4
3	1	0	145	16.2
4	1	1	379	42.3

so we know now that 42.3% of the subjects in our data were women who exercised. Suppose that instead we want to find the percentage of exercisers within each sex...

```
smartcle2 %>%
  count(female, exerany) %>%
  group_by(female) %>%
  mutate(prob = 100*n / sum(n))
```

```
# A tibble: 4 x 4
# Groups:   female [2]
  female exerany     n  prob
  <int>   <int> <int> <dbl>
1     0       0    64  17.2
2     0       1   308  82.8
3     1       0   145  27.7
4     1       1   379  72.3
```

and now we know that 82.8% of the males exercised at least once in the last 30 days, as compared to 72.3% of the females.

2.5.2 What's the distribution of sleephrs?

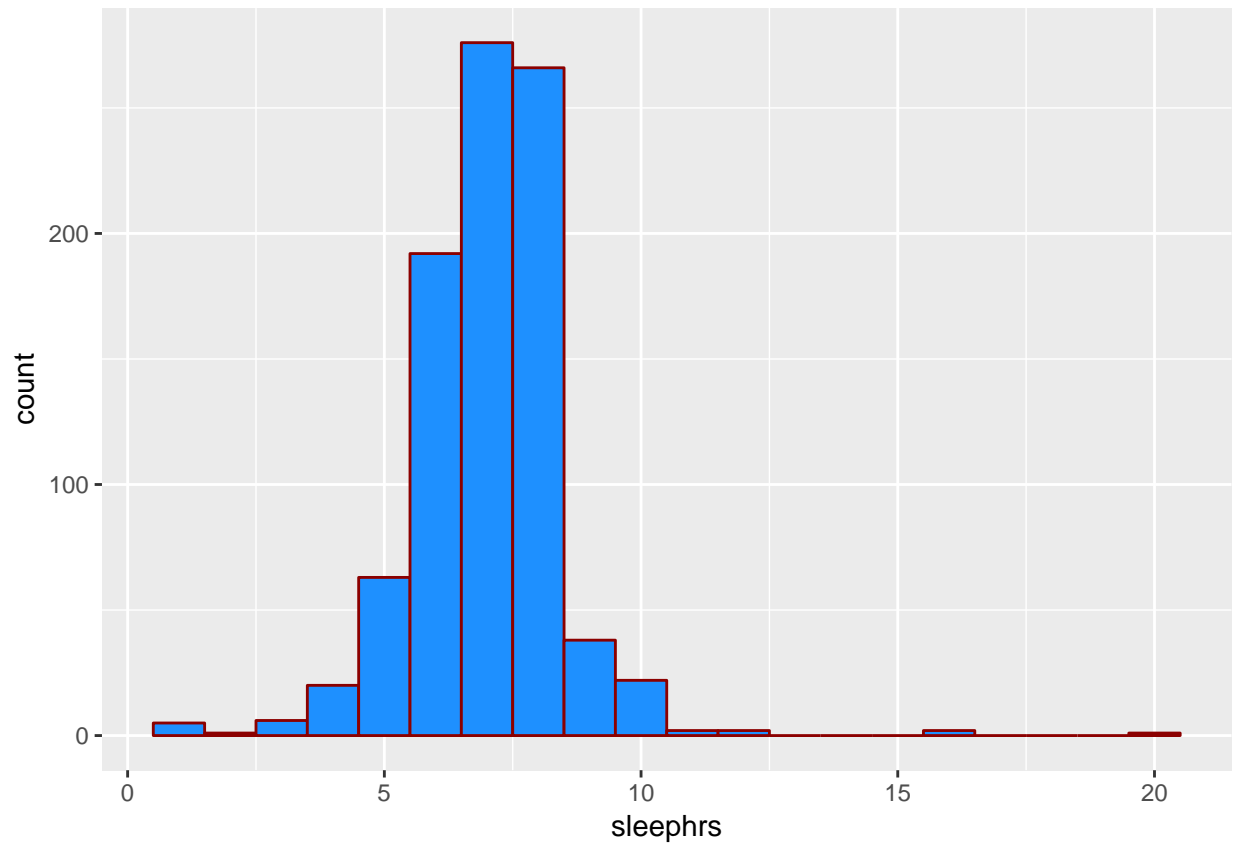
We can count quantitative variables with discrete sets of possible values, like `sleephrs`, which is captured as an integer (that must fall between 0 and 24.)

```
smartcle2 %>% count(sleephrs)
```

```
# A tibble: 14 x 2
  sleephrs     n
  <int> <int>
1       1     5
2       2     1
3       3     6
4       4    20
5       5    63
6       6   192
7       7   276
8       8   266
9       9    38
10      10    22
11      11     2
12      12     2
13      16     2
14      20     1
```

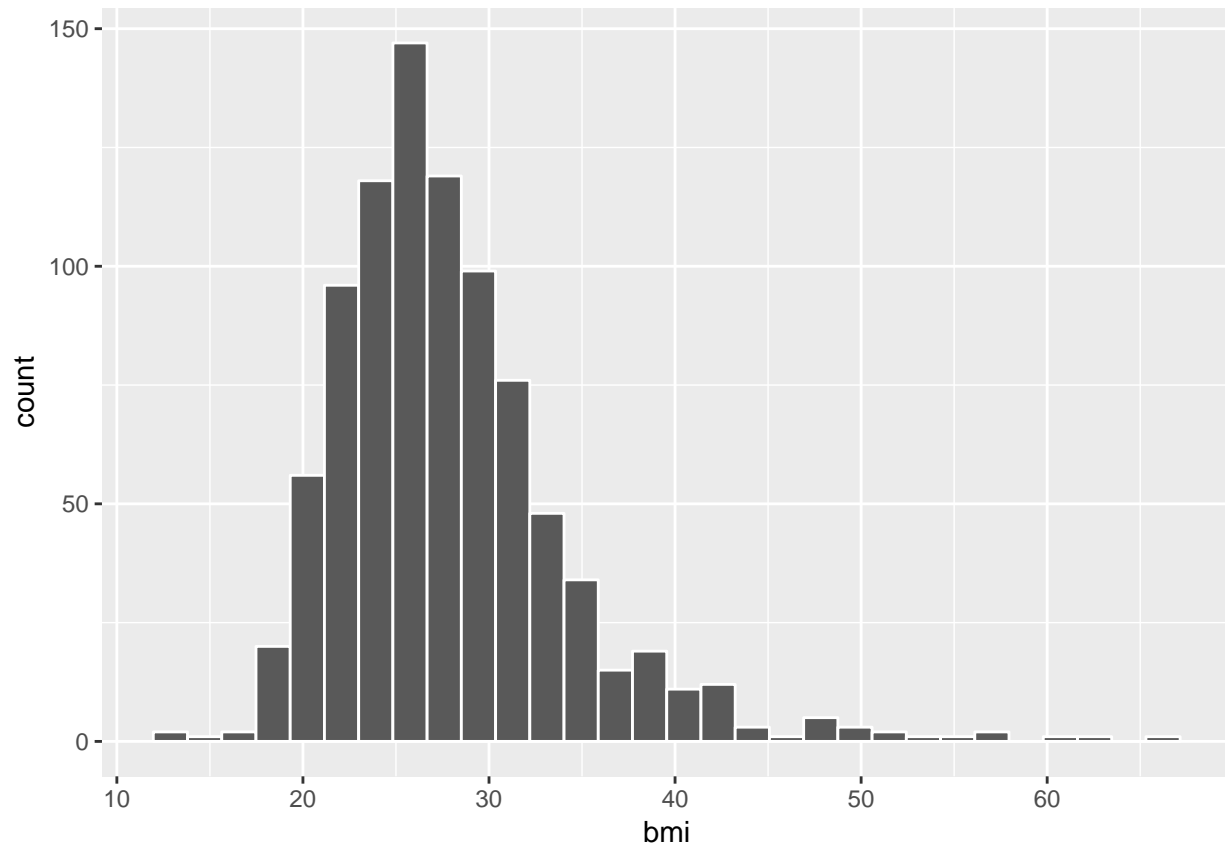
Of course, a natural summary of a quantitative variable like this would be graphical.

```
ggplot(smartcle2, aes(sleephrs)) +
  geom_histogram(binwidth = 1, fill = "dodgerblue", col = "darkred")
```



2.5.3 What's the distribution of BMI?

```
ggplot(smartcle2, aes(bmi)) +  
  geom_histogram(bins = 30, col = "white")
```



2.5.4 How many of the respondents have a BMI below 30?

```
smartcle2 %>% count(bmi < 30) %>% mutate(proportion = n / sum(n))
```

```
# A tibble: 2 x 3
  `bmi < 30`      n proportion
  <lgl>         <int>     <dbl>
1 F           253     0.282
2 T           643     0.718
```

2.5.5 How many of the respondents who have a BMI < 30 exercised?

```
smartcle2 %>% count(exerany, bmi < 30) %>%
  group_by(exerany) %>%
  mutate(percent = 100*n/sum(n))
```

```
# A tibble: 4 x 4
# Groups:   exerany [2]
  exerany `bmi < 30`      n percent
  <int> <lgl>         <int>     <dbl>
1      0 F           88     42.1
2      0 T          121     57.9
3      1 F          165     24.0
4      1 T          522     76.0
```

2.5.6 Is obesity associated with sex, in these data?

```
smartcle2 %>% count(female, bmi < 30) %>%
  group_by(female) %>%
  mutate(percent = 100*n/sum(n))
```

```
# A tibble: 4 x 4
# Groups: female [2]
  female `bmi < 30`      n percent
  <int> <lgl>      <int> <dbl>
1     0 F         105    28.2
2     0 T         267    71.8
3     1 F         148    28.2
4     1 T         376    71.8
```

2.5.7 Comparing sleephrs summaries by obesity status

Can we compare the `sleephrs` means, medians and 75th percentiles for respondents whose BMI is below 30 to the respondents whose BMI is not?

```
smartcle2 %>%
  group_by(bmi < 30) %>%
  summarize(mean(sleephrs), median(sleephrs),
            q75 = quantile(sleephrs, 0.75))
```

```
# A tibble: 2 x 4
  `bmi < 30` `mean(sleephrs)` `median(sleephrs)` q75
  <lgl>      <dbl>              <int> <dbl>
1 F         6.93              7 8.00
2 T         7.06              7 8.00
```

2.5.8 The skim function within a pipe

The `skim` function works within pipes and with the other `tidyverse` functions.

```
smartcle2 %>%
  group_by(exerany) %>%
  skim(bmi, sleephrs)
```

```
Skim summary statistics
n obs: 896
n variables: 10
group variables: exerany
```

```
Variable type: integer
exerany variable missing complete  n mean  sd p0 p25 median p75 p100
0 sleephrs 0 209 209 7 1.85 1 6 7 8 20
1 sleephrs 0 687 687 7.03 1.34 1 6 7 8 16
```

```
Variable type: numeric
exerany variable missing complete  n mean  sd p0 p25 median p75
0 bmi 0 209 209 29.57 7.46 18 24.11 28.49 33.13
1 bmi 0 687 687 27.35 5.84 12.71 23.7 26.52 29.81
p100
```

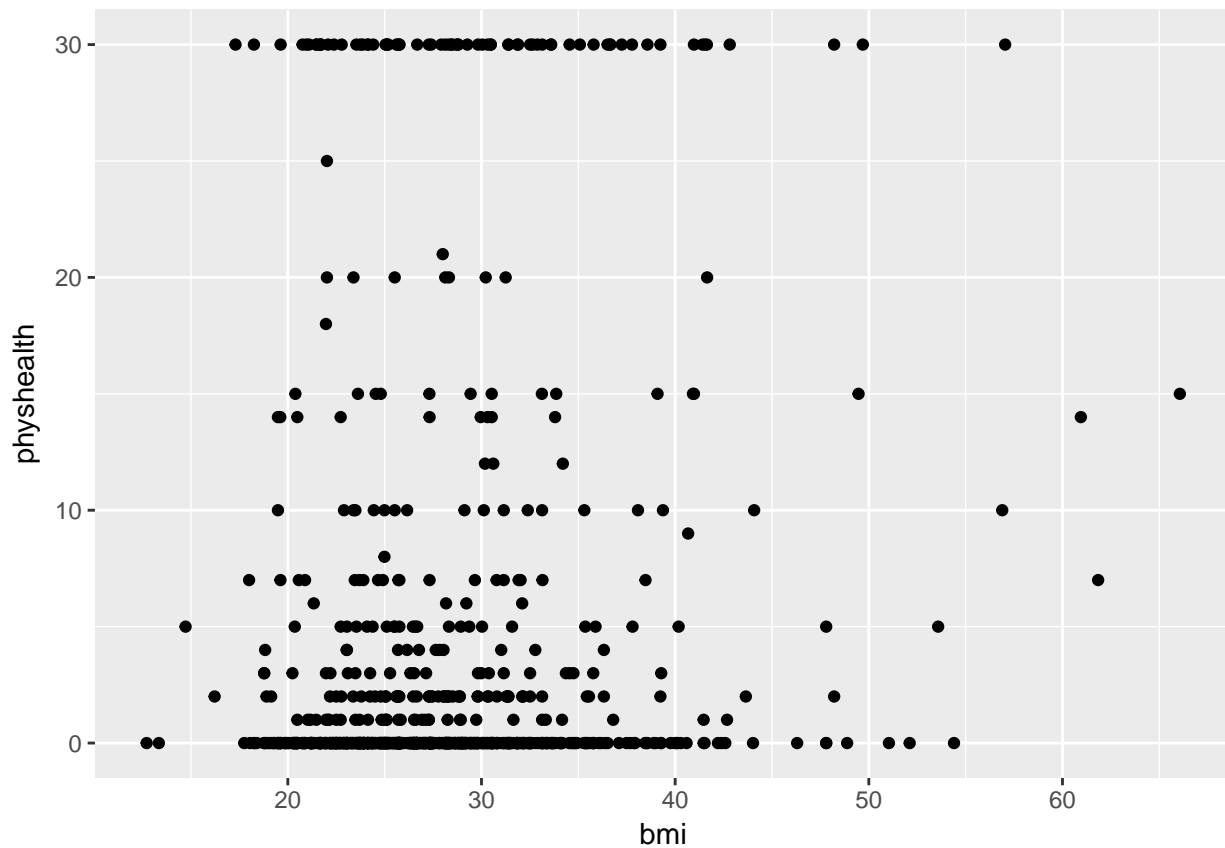
66.06

60.95

2.6 First Modeling Attempt: Can bmi predict physhealth?

We'll start with an effort to predict `physhealth` using `bmi`. A natural graph would be a scatterplot.

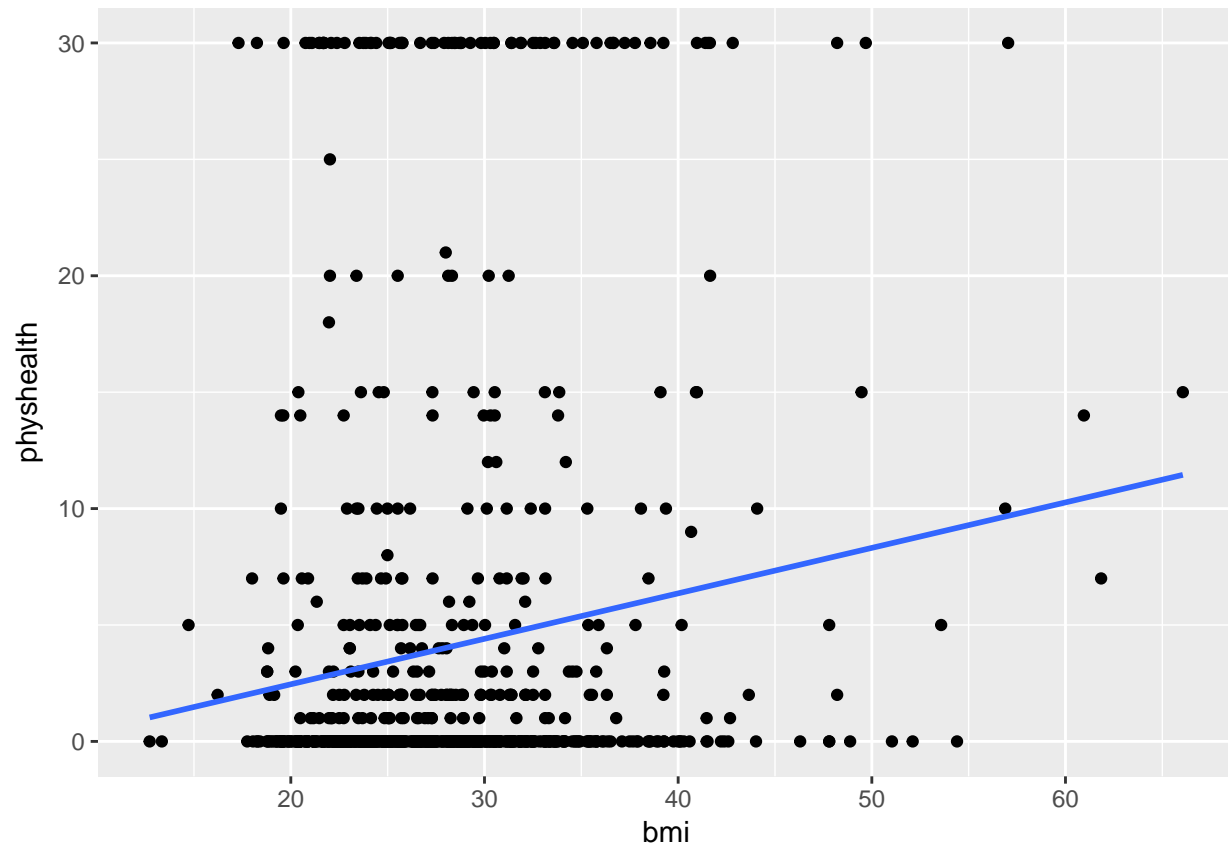
```
ggplot(data = smartcle2, aes(x = bmi, y = physhealth)) +  
  geom_point()
```



A good question to ask ourselves here might be: “In what BMI range can we make a reasonable prediction of `physhealth`?”

Now, we might take the plot above and add a simple linear model ...

```
ggplot(data = smartcle2, aes(x = bmi, y = physhealth)) +  
  geom_point() +  
  geom_smooth(method = "lm", se = FALSE)
```

which shows the same least squares regression model that we can fit with the `lm` command.

2.6.1 Fitting a Simple Regression Model

```
model_A <- lm(physhealth ~ bmi, data = smartcle2)
```

```
model_A
```

Call:

```
lm(formula = physhealth ~ bmi, data = smartcle2)
```

Coefficients:

```
(Intercept)      bmi
   -1.4514      0.1953
```

```
summary(model_A)
```

Call:

```
lm(formula = physhealth ~ bmi, data = smartcle2)
```

Residuals:

```
      Min      1Q  Median      3Q      Max
-9.171 -4.057 -3.193 -1.576 28.073
```

Coefficients:

```

      Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.45143    1.29185  -1.124    0.262
bmi          0.19527    0.04521   4.319 1.74e-05 ***
---

```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 8.556 on 894 degrees of freedom

Multiple R-squared: 0.02044, Adjusted R-squared: 0.01934

F-statistic: 18.65 on 1 and 894 DF, p-value: 1.742e-05

```
confint(model_A, level = 0.95)
```

```

      2.5 %    97.5 %
(Intercept) -3.9868457 1.0839862
bmi          0.1065409 0.2840068

```

The model coefficients can be obtained by printing the model object, and the `summary` function provides several useful descriptions of the model's residuals, its statistical significance, and quality of fit.

2.6.2 Model Summary for a Simple (One-Predictor) Regression

The fitted model predicts `physhealth` with the equation $-1.45 + 0.195 \cdot \text{bmi}$, as we can read off from the model coefficients.

Each of the 896 respondents included in the `smartcle2` data makes a contribution to this model.

2.6.2.1 Residuals

Suppose Harry is one of the people in that group, and Harry's data is `bmi = 20`, and `physhealth = 3`.

- Harry's *observed* value of `physhealth` is just the value we have in the data for them, in this case, observed `physhealth = 3` for Harry.
- Harry's *fitted* or *predicted* `physhealth` value is the result of calculating $-1.45 + 0.195 \cdot \text{bmi}$ for Harry. So, if Harry's BMI was 20, then Harry's predicted `physhealth` value is $-1.45 + (0.195)(20) = 2.45$.
- The *residual* for Harry is then his *observed* outcome minus his *fitted* outcome, so Harry has a residual of $3 - 2.45 = 0.55$.
- Graphically, a residual represents vertical distance between the observed point and the fitted regression line.
- Points above the regression line will have positive residuals, and points below the regression line will have negative residuals. Points on the line have zero residuals.

The residuals are summarized at the top of the `summary` output for linear model.

- The mean residual will always be zero in an ordinary least squares model, but a five number summary of the residuals is provided by the summary, as is an estimated standard deviation of the residuals (called here the Residual standard error.)
- In the `smartcle2` data, the minimum residual was -9.17, so for one subject, the observed value was 9.17 days smaller than the predicted value. This means that the prediction was 9.17 days too large for that subject.
- Similarly, the maximum residual was 28.07 days, so for one subject the prediction was 28.07 days too small. Not a strong performance.
- In a least squares model, the residuals are assumed to follow a Normal distribution, with mean zero, and standard deviation (for the `smartcle2` data) of about 8.6 days. Thus, by the definition of a Normal distribution, we'd expect
- about 68% of the residuals to be between -8.6 and +8.6 days,

- about 95% of the residuals to be between -17.2 and +17.2 days,
- about all (99.7%) of the residuals to be between -25.8 and +25.8 days.

2.6.2.2 Coefficients section

The `summary` for a linear model shows Estimates, Standard Errors, t values and p values for each coefficient fit.

- The Estimates are the point estimates of the intercept and slope of `bmi` in our model.
- In this case, our estimated slope is 0.195, which implies that if Harry's BMI is 20 and Sally's BMI is 21, we predict that Sally's `physhealth` will be 0.195 days larger than Harry's.
- The Standard Errors are also provided for each estimate. We can create rough 95% confidence intervals by adding and subtracting two standard errors from each coefficient, or we can get a slightly more accurate answer with the `confint` function.
- Here, the 95% confidence interval for the slope of `bmi` is estimated to be (0.11, 0.28). This is a good measure of the uncertainty in the slope that is captured by our model. We are 95% confident in the process of building this interval, but this doesn't mean we're 95% sure that the true slope is actually in that interval.

Also available are a t value (just the Estimate divided by the Standard Error) and the appropriate p value for testing the null hypothesis that the true value of the coefficient is 0 against a two-tailed alternative.

- If a slope coefficient is statistically significantly different from 0, this implies that 0 will not be part of the uncertainty interval obtained through `confint`.
- If the slope was zero, it would suggest that `bmi` would add no predictive value to the model. But that's unlikely here.

If the `bmi` slope coefficient is associated with a small p value, as in the case of our `model_A`, it suggests that the model including `bmi` is statistically significantly better at predicting `physhealth` than the model without `bmi`.

- Without `bmi` our `model_A` would become an *intercept-only* model, in this case, which would predict the mean `physhealth` for everyone, regardless of any other information.

2.6.2.3 Model Fit Summaries

The `summary` of a linear model also displays:

- The residual standard error and associated degrees of freedom for the residuals.
- For a simple (one-predictor) least regression like this, the residual degrees of freedom will be the sample size minus 2.
- The multiple R-squared (or coefficient of determination)
- This is interpreted as the proportion of variation in the outcome (`physhealth`) accounted for by the model, and will always fall between 0 and 1 as a result.
- Our `model_A` accounts for a mere 2% of the variation in `physhealth`.
- The Adjusted R-squared value "adjusts" for the size of our model in terms of the number of coefficients included in the model.
- The adjusted R-squared will always be less than the Multiple R-squared.
- We still hope to find models with relatively large adjusted R^2 values.
- In particular, we hope to find models where the adjusted R^2 isn't substantially less than the Multiple R-squared.
- The adjusted R-squared is usually a better estimate of likely performance of our model in new data than is the Multiple R-squared.
- The adjusted R-squared result is no longer interpretable as a proportion of anything - in fact, it can fall below 0.

- We can obtain the adjusted R^2 from the raw R^2 , the number of observations N and the number of predictors p included in the model, as follows:

$$R_{adj}^2 = 1 - \frac{(1 - R^2)(N - 1)}{N - p - 1},$$

- The F statistic and p value from a global ANOVA test of the model.
 - Obtaining a statistically significant result here is usually pretty straightforward, since the comparison is between our model, and a model which simply predicts the mean value of the outcome for everyone.
 - In a simple (one-predictor) linear regression like this, the t statistic for the slope is just the square root of the F statistic, and the resulting p values for the slope's t test and for the global F test will be identical.
- To see the complete ANOVA F test for this model, we can run `anova(model_A)`.

```
anova(model_A)
```

Analysis of Variance Table

Response: physhealth

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
bmi	1	1366	1365.5	18.655	1.742e-05 ***
Residuals	894	65441	73.2		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

2.6.3 Using the broom package

The `broom` package has three functions of particular use in a linear regression model:

2.6.3.1 The tidy function

`tidy` builds a data frame/tibble containing information about the coefficients in the model, their standard errors, t statistics and p values.

```
tidy(model_A)
```

	term	estimate	std.error	statistic	p.value
1	(Intercept)	-1.4514298	1.29185199	-1.123526	2.615156e-01
2	bmi	0.1952739	0.04521145	4.319125	1.741859e-05

2.6.3.2 The glance function

`glance` builds a data frame/tibble containing summary statistics about the model, including

- the (raw) multiple R^2 and adjusted R^2
- `sigma` which is the residual standard error
- the F statistic, `p.value` model df and `df.residual` associated with the global ANOVA test, plus
- several statistics that will be useful in comparing models down the line:
- the model's log likelihood function value, `logLik`
- the model's Akaike's Information Criterion value, `AIC`
- the model's Bayesian Information Criterion value, `BIC`
- and the model's `deviance` statistic

```
glance(model_A)
```

```
      r.squared adj.r.squared   sigma statistic      p.value df    logLik
1 0.02044019    0.01934449 8.555737  18.65484 1.741859e-05  2 -3193.723
      AIC      BIC deviance df.residual
1 6393.446 6407.84 65441.36          894
```

2.6.3.3 The augment function

`augment` builds a data frame/tibble which adds fitted values, residuals and other diagnostic summaries that describe each observation to the original data used to fit the model, and this includes

- `.fitted` and `.resid`, the fitted and residual values, in addition to
- `.hat`, the leverage value for this observation
- `.cooks`, the Cook's distance measure of *influence* for this observation
- `.stdresid`, the standardized residual (think of this as a z-score - a measure of the residual divided by its associated standard deviation `.sigma`)
- and `se.fit` which will help us generate prediction intervals for the model downstream

Note that each of the new columns begins with `.` to avoid overwriting any data.

```
head(augment(model_A))
```

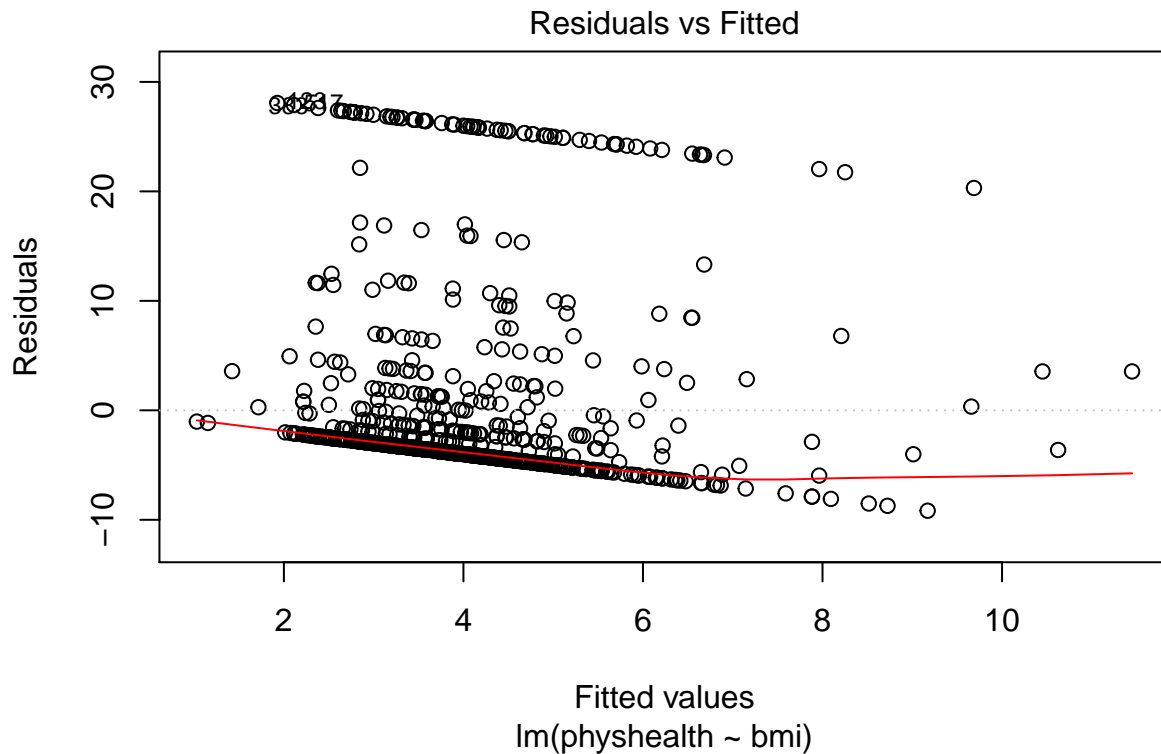
```
  physhealth  bmi .fitted .se.fit .resid .hat .sigma
1          0 26.69 3.760430 0.2907252 -3.76043009 0.001154651 8.559600
2          0 23.70 3.176561 0.3422908 -3.17656119 0.001600574 8.559865
3          1 26.92 3.805343 0.2890054 -2.80534308 0.001141030 8.560010
4          0 21.66 2.778202 0.4005101 -2.77820248 0.002191352 8.560020
5          5 24.09 3.252718 0.3329154  1.74728200 0.001514095 8.560326
6          4 27.64 3.945940 0.2860087  0.05405972 0.001117490 8.560526
      .cooks .std.resid
1 1.117852e-04 -0.439775451
2 1.106717e-04 -0.371575999
3 6.147744e-05 -0.328077528
4 1.160381e-04 -0.325074461
5 3.167016e-05  0.204378225
6 2.235722e-08  0.006322069
```

For more on the `broom` package, you may want to look at this vignette.

2.6.4 How does the model do? (Residuals vs. Fitted Values)

- Remember that the R^2 value was about 2%.

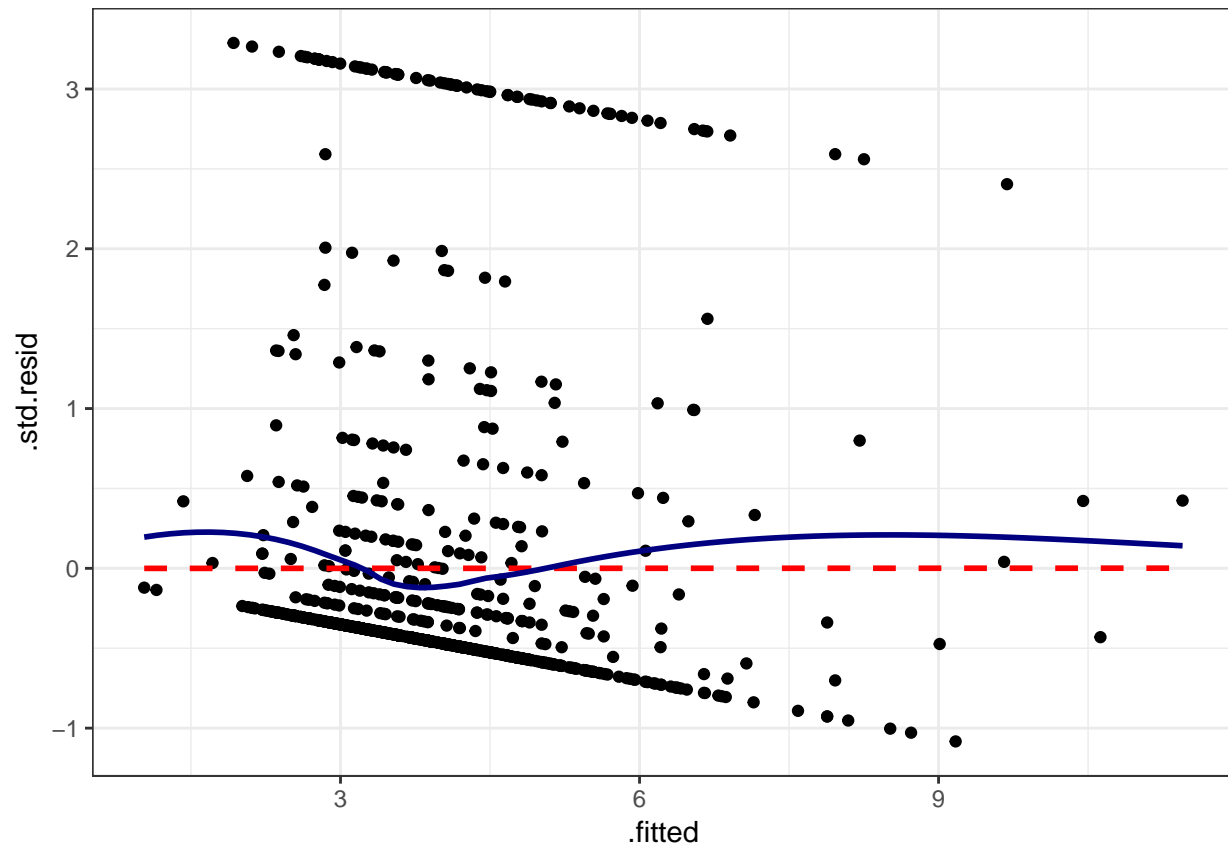
```
plot(model_A, which = 1)
```



This is a plot of residuals vs. fitted values. The goal here is for this plot to look like a random scatter of points, perhaps like a “fuzzy football”, and that’s **not** what we have. Why?

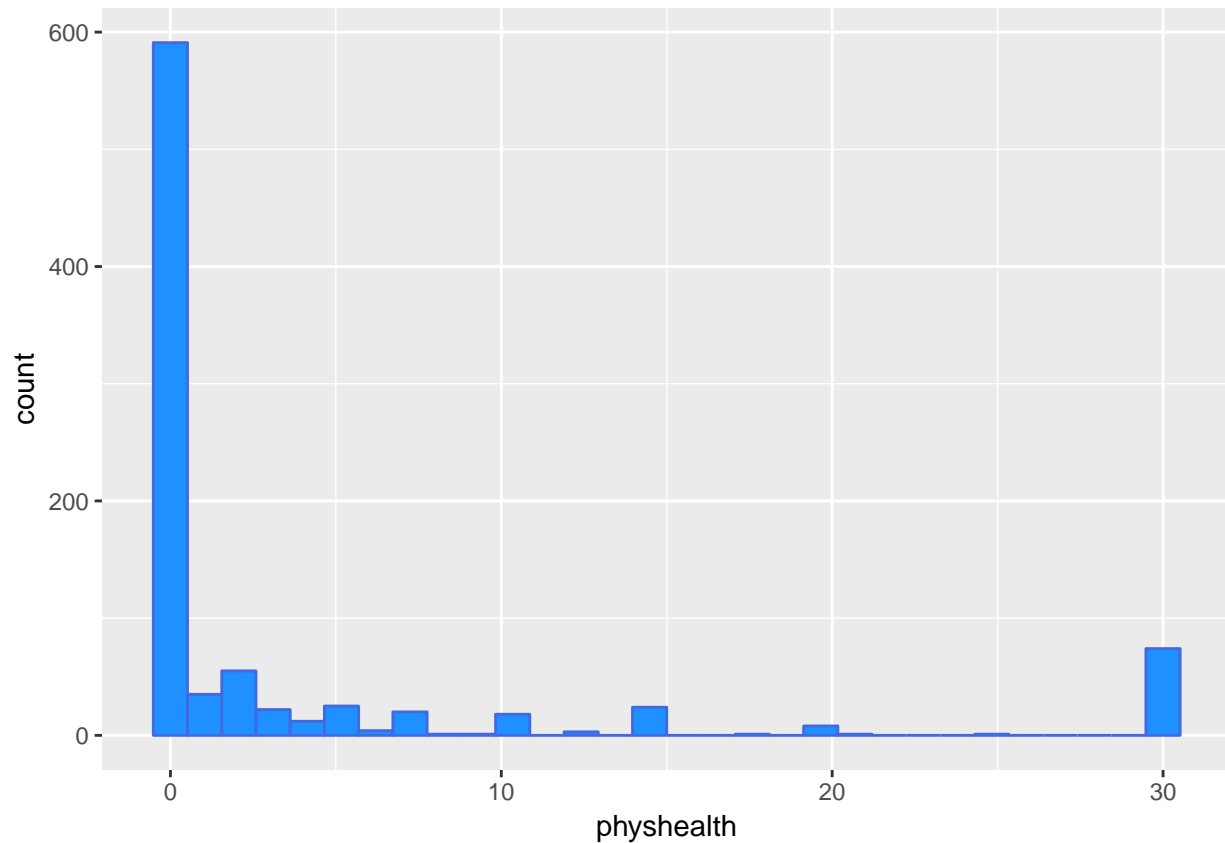
If you prefer, here’s a `ggplot2` version of a similar plot, now looking at standardized residuals instead of raw residuals, and adding a loess smooth and a linear fit to the result.

```
ggplot(augment(model_A), aes(x = .fitted, y = .std.resid)) +
  geom_point() +
  geom_smooth(method = "lm", se = FALSE, col = "red", linetype = "dashed") +
  geom_smooth(method = "loess", se = FALSE, col = "navy") +
  theme_bw()
```



The problem we're having here becomes, I think, a little more obvious if we look at what we're predicting. Does `physhealth` look like a good candidate for a linear model?

```
ggplot(smartcle2, aes(x = physhealth)) +  
  geom_histogram(bins = 30, fill = "dodgerblue", color = "royalblue")
```



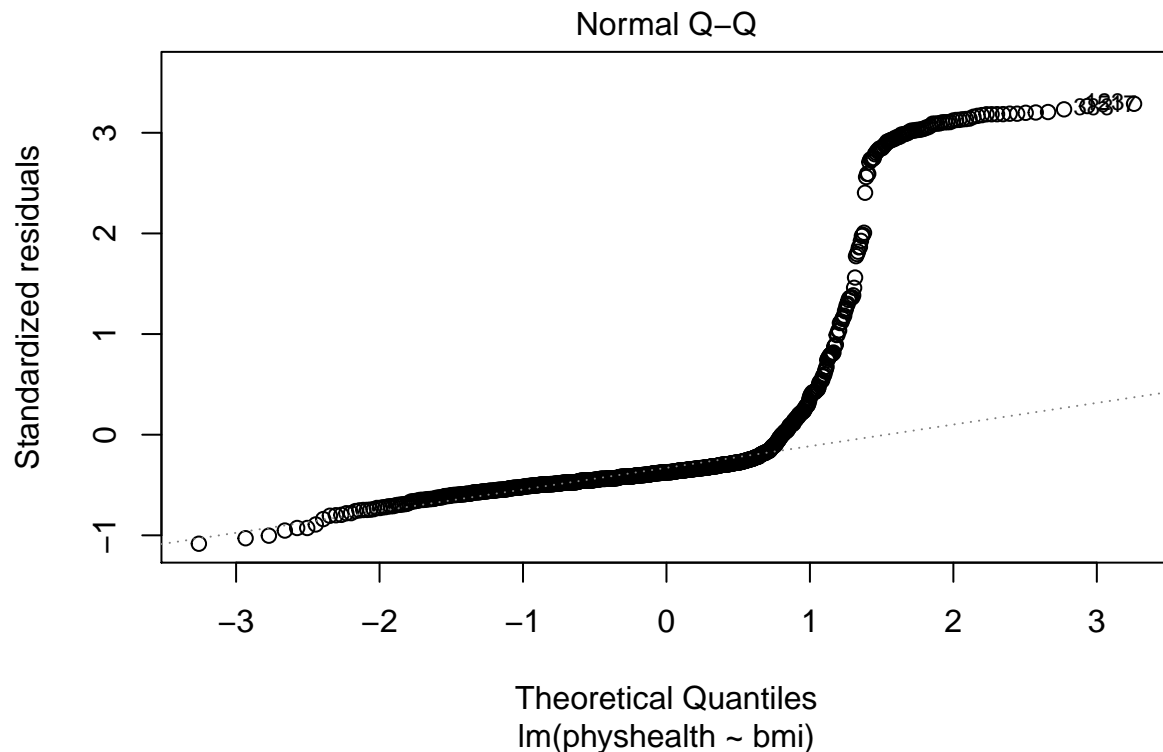
```
smartcle2 %>% count(physhealth == 0, physhealth == 30)
```

```
# A tibble: 3 x 3
  `physhealth == 0` `physhealth == 30`   n
  <lgl>             <lgl>             <int>
1 F                F                231
2 F                T                 74
3 T                F                591
```

No matter what model we fit, if we are predicting **physhealth**, and most of the data are values of 0 and 30, we have limited variation in our outcome, and so our linear model will be somewhat questionable just on that basis.

A normal Q-Q plot of the standardized residuals for our **model_A** shows this problem, too.

```
plot(model_A, which = 2)
```

We’re going to need a method to deal with this sort of outcome, that has both a floor and a ceiling. We’ll get there eventually, but linear regression alone doesn’t look promising.

All right, so that didn’t go anywhere great. Let’s try again, with a new outcome.

2.7 A New Small Study: Predicting BMI

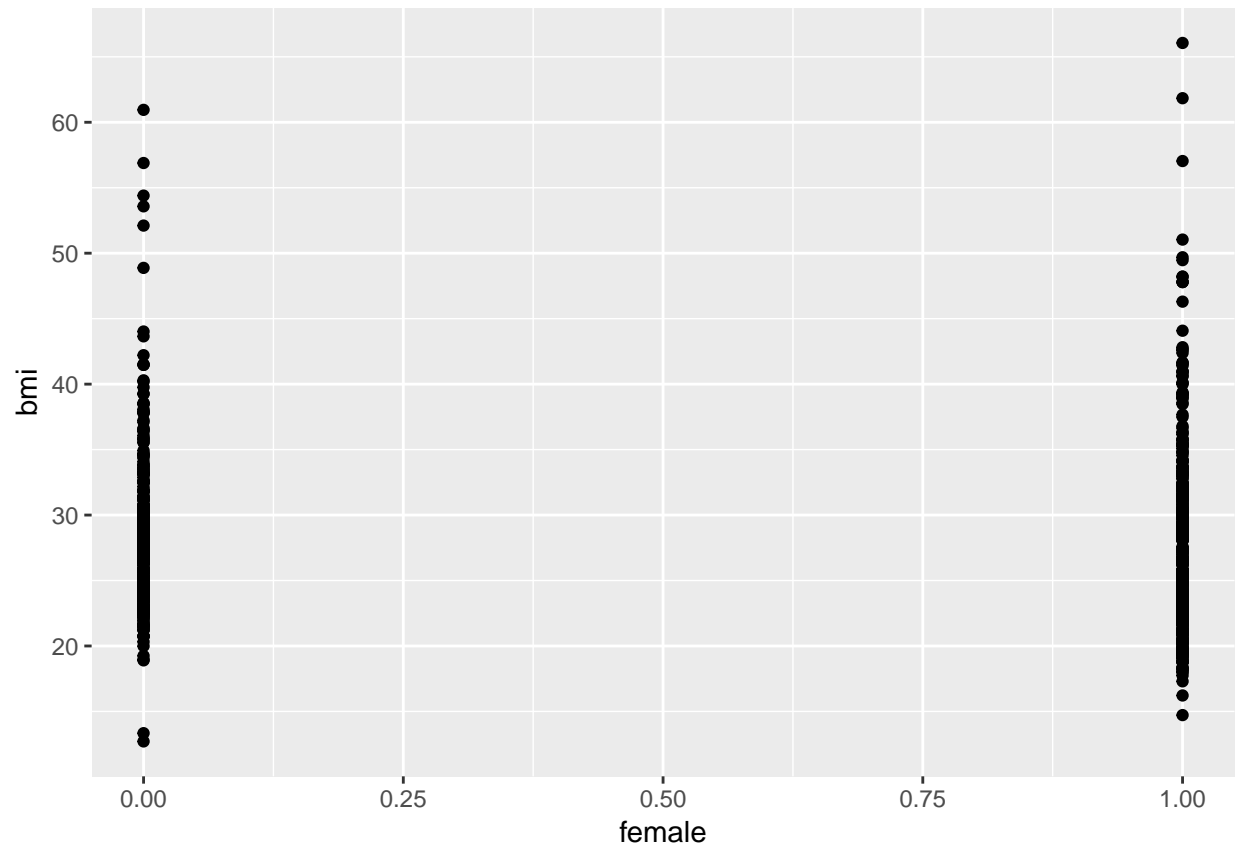
We’ll begin by investigating the problem of predicting `bmi`, at first with just three regression inputs: `sex`, `exerany` and `sleephrs`, in our new `smartcle2` data set.

- The outcome of interest is `bmi`.
- Inputs to the regression model are:
 - `female` = 1 if the subject is female, and 0 if they are male
 - `exerany` = 1 if the subject exercised in the past 30 days, and 0 if they didn’t
 - `sleephrs` = hours slept in a typical 24-hour period (treated as quantitative)

2.7.1 Does `female` predict `bmi` well?

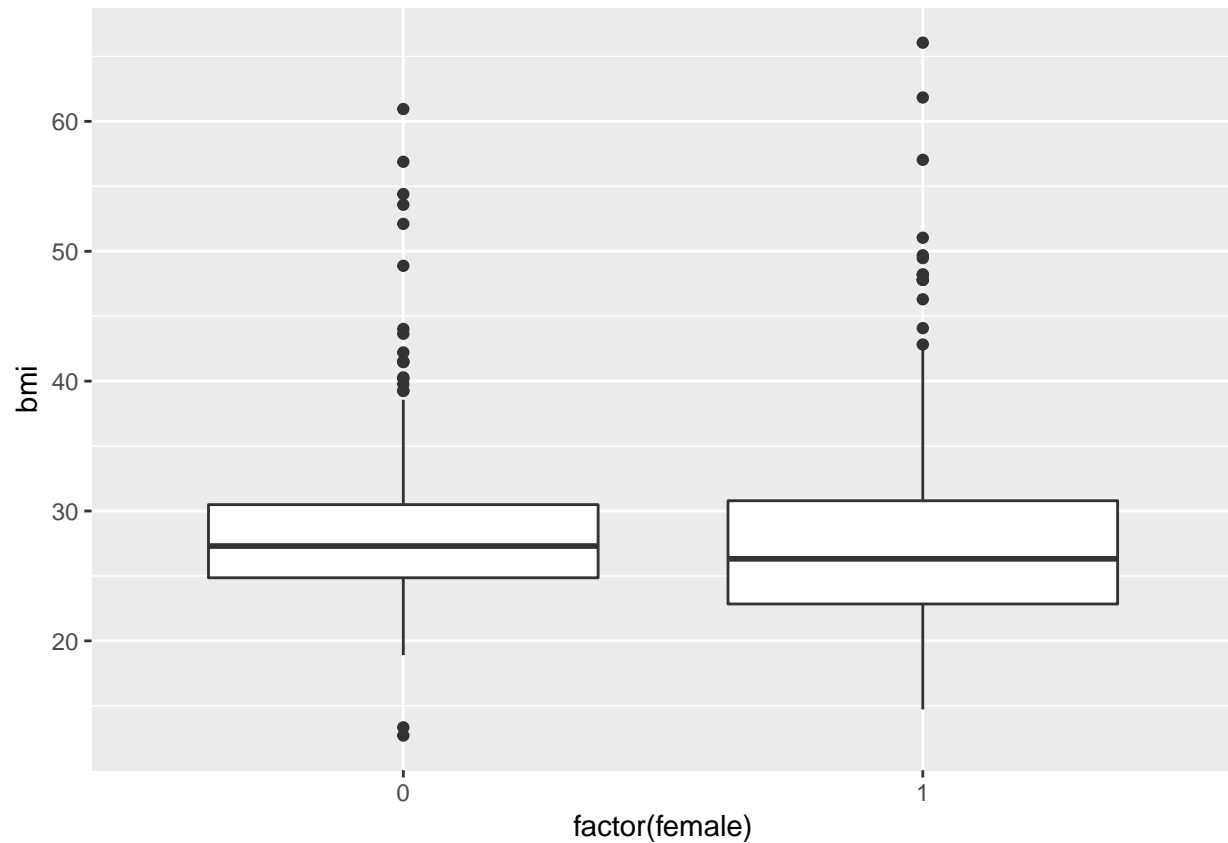
2.7.1.1 Graphical Assessment

```
ggplot(smartcle2, aes(x = female, y = bmi)) +  
  geom_point()
```



Not so helpful. We should probably specify that `female` is a factor, and try another plotting approach.

```
ggplot(smartcle2, aes(x = factor(female), y = bmi)) +  
  geom_boxplot()
```



The median BMI looks a little higher for males. Let's see if a model reflects that.

2.8 c2_m1: A simple t-test model

```
c2_m1 <- lm(bmi ~ female, data = smartcle2)
c2_m1
```

Call:

```
lm(formula = bmi ~ female, data = smartcle2)
```

Coefficients:

(Intercept)	female
28.3600	-0.8457

```
summary(c2_m1)
```

Call:

```
lm(formula = bmi ~ female, data = smartcle2)
```

Residuals:

Min	1Q	Median	3Q	Max
-15.650	-4.129	-1.080	2.727	38.546

Coefficients:

```

      Estimate Std. Error t value Pr(>|t|)
(Intercept)  28.3600     0.3274  86.613   <2e-16 ***
female       -0.8457     0.4282  -1.975   0.0485 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 6.315 on 894 degrees of freedom
Multiple R-squared:  0.004345, Adjusted R-squared:  0.003231
F-statistic: 3.902 on 1 and 894 DF, p-value: 0.04855

```

```
confint(c2_m1)
```

```

      2.5 %      97.5 %
(Intercept) 27.717372 29.00262801
female      -1.686052 -0.00539878

```

The model suggests, based on these 896 subjects, that

- our best prediction for males is $\text{BMI} = 28.36 \text{ kg/m}^2$, and
- our best prediction for females is $\text{BMI} = 28.36 - 0.85 = 27.51 \text{ kg/m}^2$.
- the mean difference between females and males is -0.85 kg/m^2 in BMI
- a 95% confidence (uncertainty) interval for that mean female - male difference in BMI ranges from -1.69 to -0.01
- the model accounts for 0.4% of the variation in BMI, so that knowing the respondent's sex does very little to reduce the size of the prediction errors as compared to an intercept only model that would predict the overall mean (regardless of sex) for all subjects.
- the model makes some enormous errors, with one subject being predicted to have a BMI 38 points lower than his/her actual BMI.

Note that this simple regression model just gives us the t-test.

```
t.test(bmi ~ female, var.equal = TRUE, data = smartcle2)
```

Two Sample t-test

```

data:  bmi by female
t = 1.9752, df = 894, p-value = 0.04855
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
 0.00539878 1.68605160
sample estimates:
mean in group 0 mean in group 1
    28.36000      27.51427

```

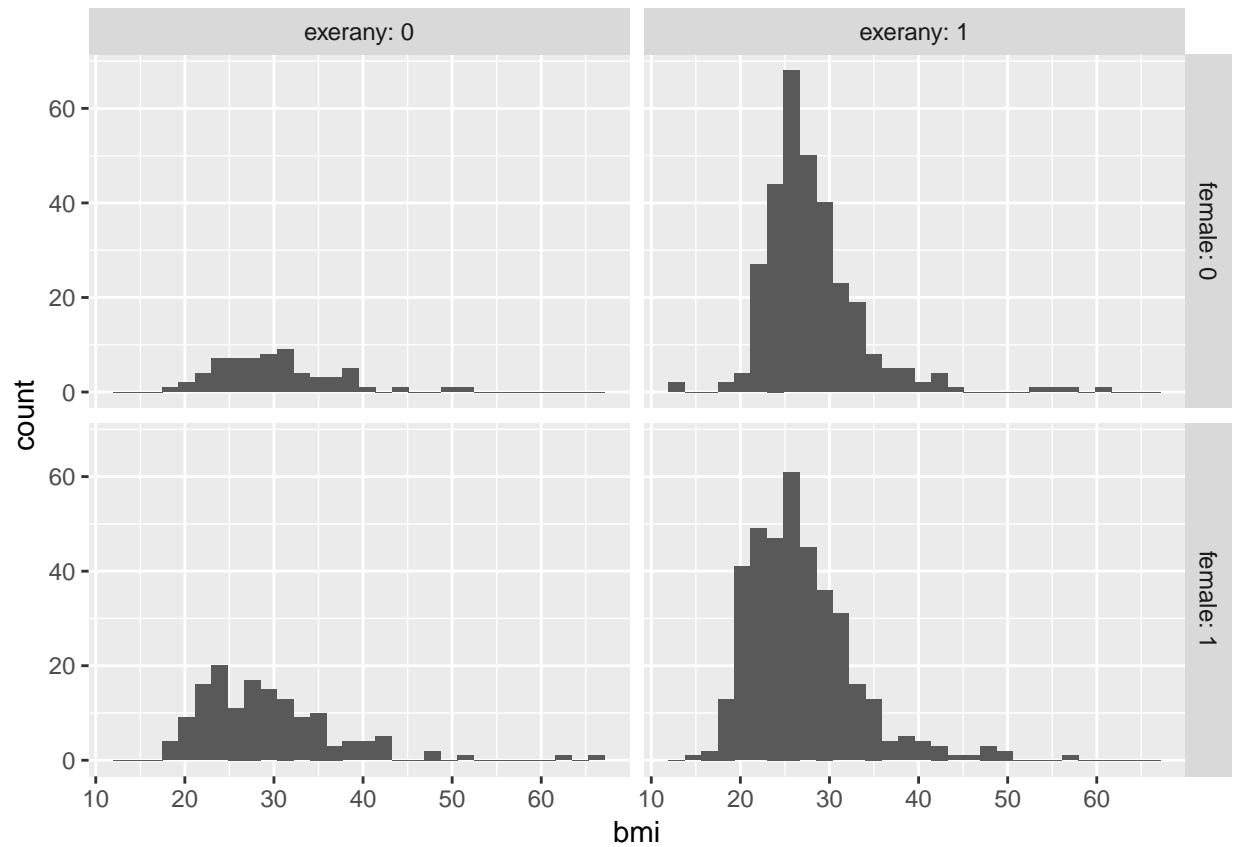
2.9 c2_m2: Adding another predictor (two-way ANOVA without interaction)

When we add in the information about `exerany` to our original model, we might first picture the data. We could look at separate histograms,

```

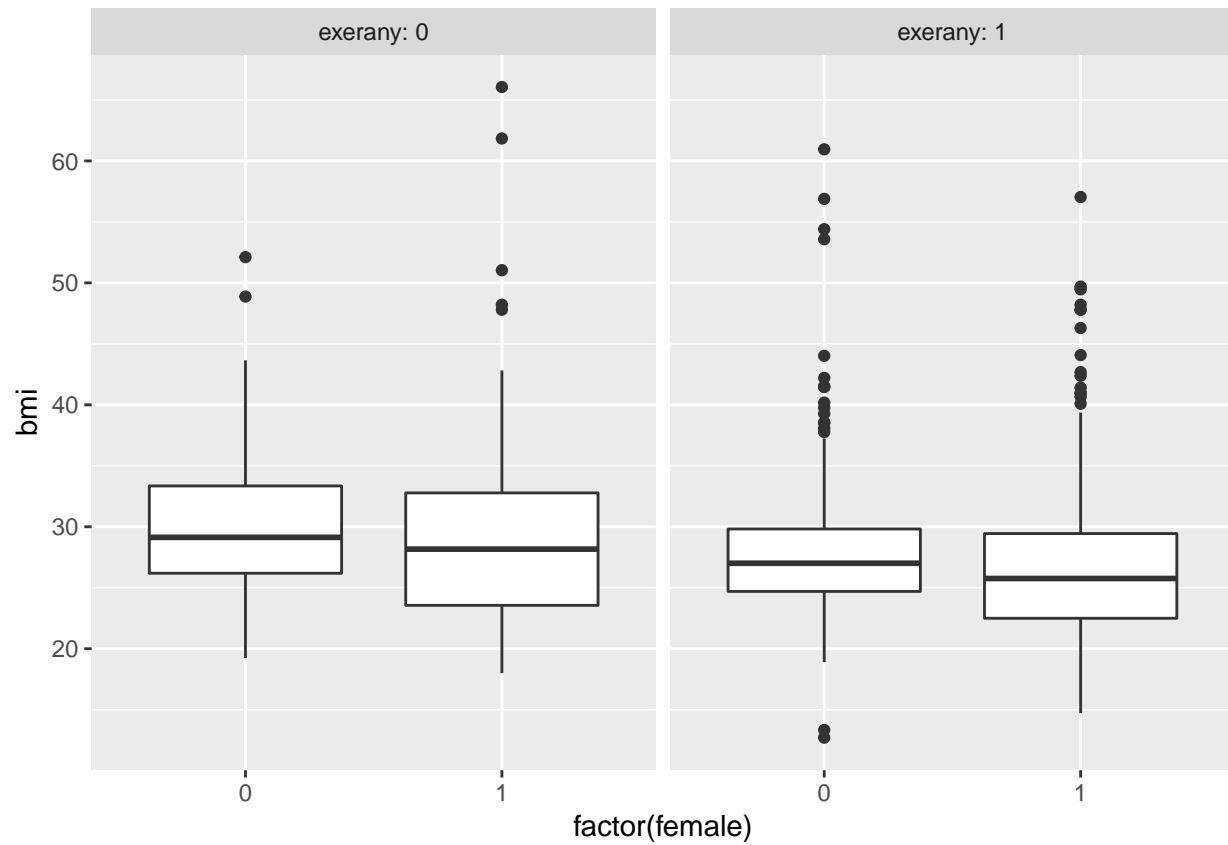
ggplot(smartcle2, aes(x = bmi)) +
  geom_histogram(bins = 30) +
  facet_grid(female ~ exerany, labeller = label_both)

```

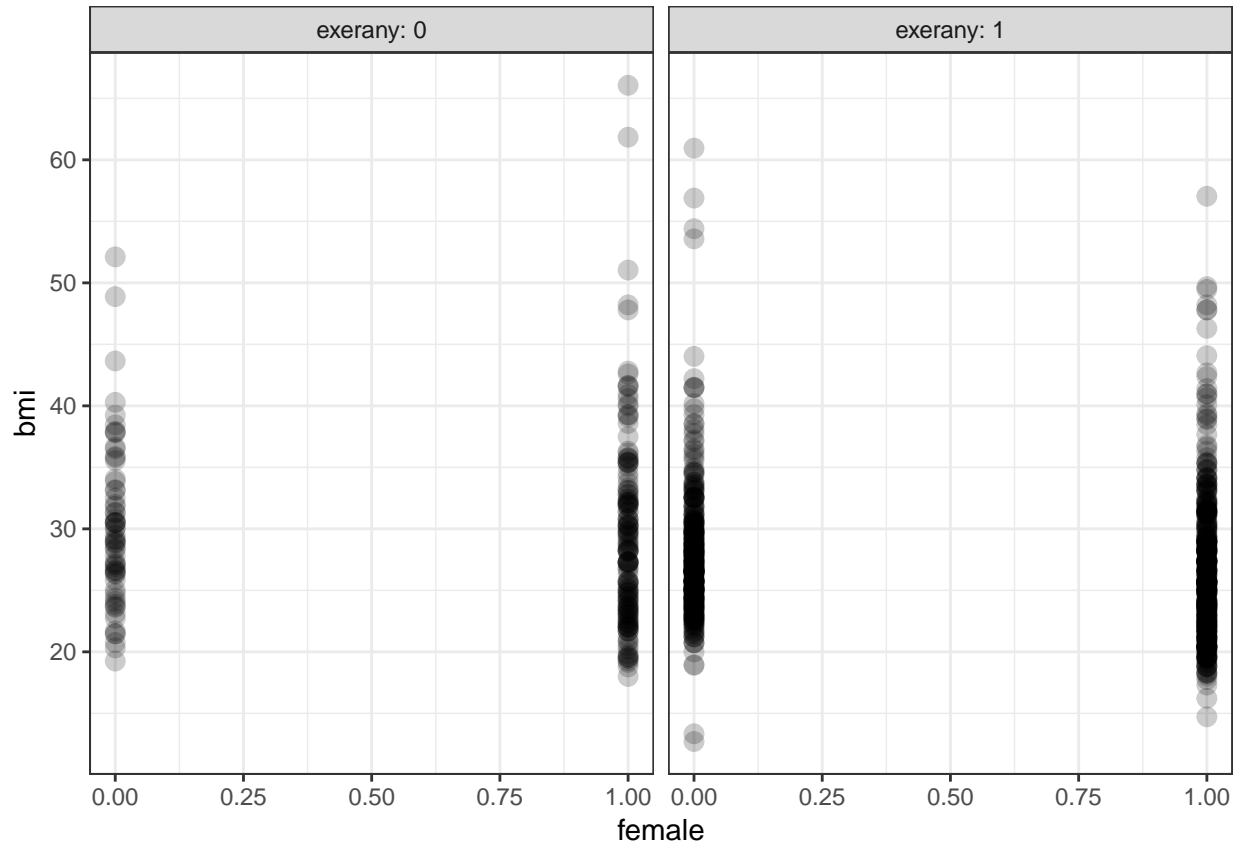


or maybe boxplots?

```
ggplot(smartcle2, aes(x = factor(female), y = bmi)) +
  geom_boxplot() +
  facet_wrap(~ exerany, labeller = label_both)
```



```
ggplot(smartcle2, aes(x = female, y = bmi)) +
  geom_point(size = 3, alpha = 0.2) +
  theme_bw() +
  facet_wrap(~ exerany, labeller = label_both)
```



OK. Let's try fitting a model.

```
c2_m2 <- lm(bmi ~ female + exerany, data = smartcle2)
c2_m2
```

Call:

```
lm(formula = bmi ~ female + exerany, data = smartcle2)
```

Coefficients:

(Intercept)	female	exerany
30.334	-1.095	-2.384

This new model predicts only four predicted values:

- $\text{bmi} = 30.334$ if the subject is male and did not exercise (so $\text{female} = 0$ and $\text{exerany} = 0$)
- $\text{bmi} = 30.334 - 1.095 = 29.239$ if the subject is female and did not exercise ($\text{female} = 1$ and $\text{exerany} = 0$)
- $\text{bmi} = 30.334 - 2.384 = 27.950$ if the subject is male and exercised (so $\text{female} = 0$ and $\text{exerany} = 1$), and, finally
- $\text{bmi} = 30.334 - 1.095 - 2.384 = 26.855$ if the subject is female and exercised (so both female and $\text{exerany} = 1$).

For those who did not exercise, the model is:

- $\text{bmi} = 30.334 - 1.095 \text{ female}$

and for those who did exercise, the model is:

- $\text{bmi} = 27.95 - 1.095 \text{ female}$

Only the intercept of the `bmi-female` model changes depending on `exerany`.

```
summary(c2_m2)
```

Call:

```
lm(formula = bmi ~ female + exerany, data = smartcle2)
```

Residuals:

Min	1Q	Median	3Q	Max
-15.240	-4.091	-1.095	2.602	36.822

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	30.3335	0.5231	57.99	< 2e-16 ***
female	-1.0952	0.4262	-2.57	0.0103 *
exerany	-2.3836	0.4965	-4.80	1.86e-06 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6.239 on 893 degrees of freedom

Multiple R-squared: 0.02939, Adjusted R-squared: 0.02722

F-statistic: 13.52 on 2 and 893 DF, p-value: 1.641e-06

```
confint(c2_m2)
```

	2.5 %	97.5 %
(Intercept)	29.306846	31.3602182
female	-1.931629	-0.2588299
exerany	-3.358156	-1.4090777

The slopes of both `female` and `exerany` have confidence intervals that are completely below zero, indicating that both `female` sex and `exerany` appear to be associated with reductions in `bmi`.

The R^2 value suggests that just under 3% of the variation in `bmi` is accounted for by this ANOVA model.

In fact, this regression (on two binary indicator variables) is simply a two-way ANOVA model without an interaction term.

```
anova(c2_m2)
```

Analysis of Variance Table

Response: bmi

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
female	1	156	155.61	3.9977	0.04586 *
exerany	1	897	896.93	23.0435	1.856e-06 ***
Residuals	893	34759	38.92		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

2.10 c2_m3: Adding the interaction term (Two-way ANOVA with interaction)

Suppose we want to let the effect of `female` vary depending on the `exerany` status. Then we need to incorporate an interaction term in our model.


```
c2_m3 <- lm(bmi ~ female * exerany, data = smartcle2)
c2_m3
```

Call:

```
lm(formula = bmi ~ female * exerany, data = smartcle2)
```

Coefficients:

(Intercept)	female	exerany	female:exerany
30.1359	-0.8104	-2.1450	-0.3592

So, for example, for a male who exercises, this model predicts

- $\text{bmi} = 30.136 - 0.810 (0) - 2.145 (1) - 0.359 (0)(1) = 30.136 - 2.145 = 27.991$

And for a female who exercises, the model predicts

- $\text{bmi} = 30.136 - 0.810 (1) - 2.145 (1) - 0.359 (1)(1) = 30.136 - 0.810 - 2.145 - 0.359 = 26.822$

For those who did not exercise, the model is:

- $\text{bmi} = 30.136 - 0.81 \text{ female}$

But for those who did exercise, the model is:

- $\text{bmi} = (30.136 - 2.145) + (-0.810 + (-0.359)) \text{ female}$, or ,,
- $\text{bmi} = 27.991 - 1.169 \text{ female}$

Now, both the slope and the intercept of the **bmi-female** model change depending on **exerany**.

```
summary(c2_m3)
```

Call:

```
lm(formula = bmi ~ female * exerany, data = smartcle2)
```

Residuals:

Min	1Q	Median	3Q	Max
-15.281	-4.101	-1.061	2.566	36.734

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	30.1359	0.7802	38.624	<2e-16 ***
female	-0.8104	0.9367	-0.865	0.3872
exerany	-2.1450	0.8575	-2.501	0.0125 *
female:exerany	-0.3592	1.0520	-0.341	0.7328

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6.242 on 892 degrees of freedom

Multiple R-squared: 0.02952, Adjusted R-squared: 0.02625

F-statistic: 9.044 on 3 and 892 DF, p-value: 6.669e-06

```
confint(c2_m3)
```

	2.5 %	97.5 %
(Intercept)	28.604610	31.6672650
female	-2.648893	1.0280526
exerany	-3.827886	-0.4620407
female:exerany	-2.423994	1.7055248

In fact, this regression (on two binary indicator variables and a product term) is simply a two-way ANOVA model with an interaction term.

```
anova(c2_m3)
```

Analysis of Variance Table

Response: bmi

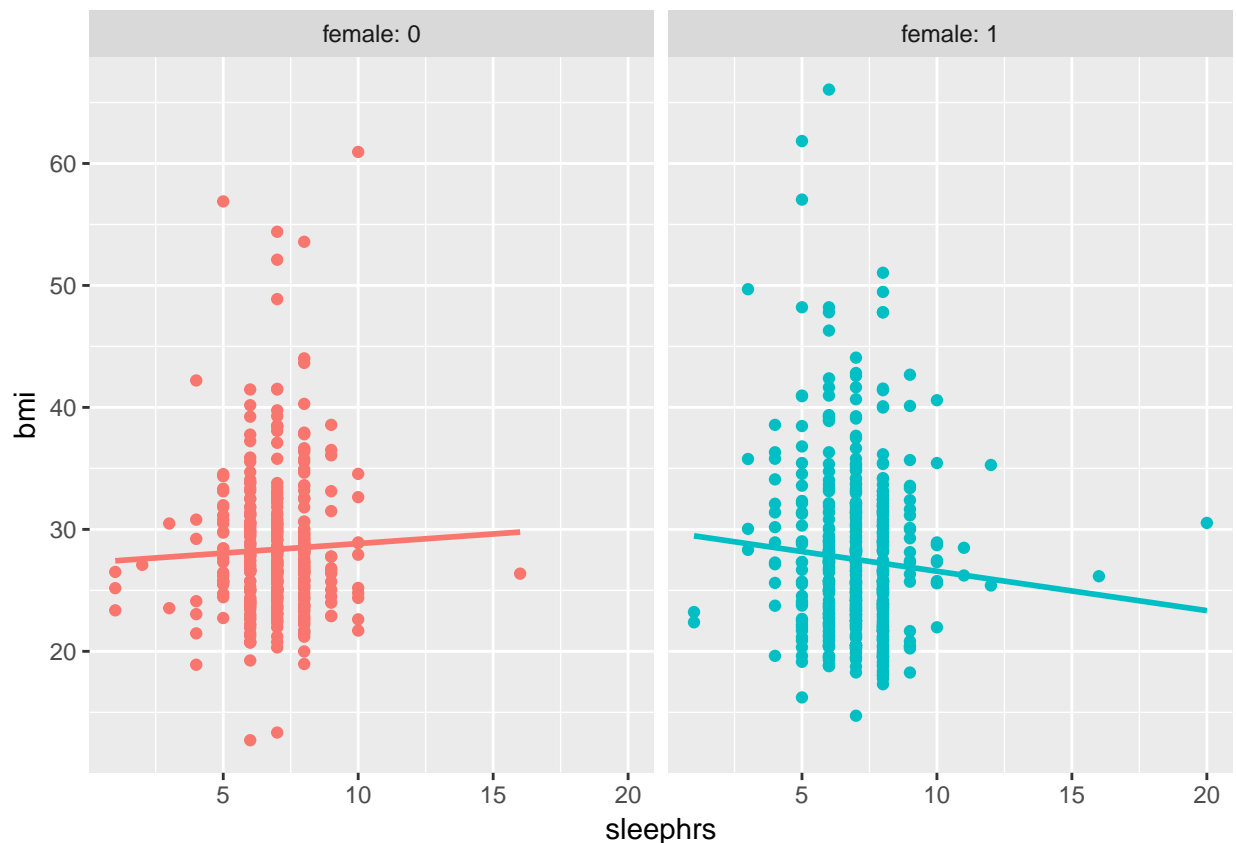
	Df	Sum Sq	Mean Sq	F value	Pr(>F)
female	1	156	155.61	3.9938	0.04597 *
exerany	1	897	896.93	23.0207	1.878e-06 ***
female:exerany	1	5	4.54	0.1166	0.73283
Residuals	892	34754	38.96		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

The interaction term doesn't change very much here. Its uncertainty interval includes zero, and the overall model still accounts for just under 3% of the variation in bmi.

2.11 c2_m4: Using female and sleephrs in a model for bmi

```
ggplot(smartcle2, aes(x = sleephrs, y = bmi, color = factor(female))) +
  geom_point() +
  guides(col = FALSE) +
  geom_smooth(method = "lm", se = FALSE) +
  facet_wrap(~ female, labeller = label_both)
```



Does the difference in slopes of `bmi` and `sleephrs` for males and females appear to be substantial and important?

```
c2_m4 <- lm(bmi ~ female * sleephrs, data = smartc1e2)

summary(c2_m4)
```

Call:

```
lm(formula = bmi ~ female * sleephrs, data = smartc1e2)
```

Residuals:

```
      Min       1Q   Median       3Q      Max
-15.498  -4.179  -1.035   2.830  38.204
```

Coefficients:

```
              Estimate Std. Error t value Pr(>|t|)
(Intercept)    27.2661     1.6320  16.707  <2e-16 ***
female          2.5263     2.0975   1.204    0.229
sleephrs        0.1569     0.2294   0.684    0.494
female:sleephrs -0.4797     0.2931  -1.636    0.102
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 6.31 on 892 degrees of freedom

Multiple R-squared: 0.008341, Adjusted R-squared: 0.005006

F-statistic: 2.501 on 3 and 892 DF, p-value: 0.05818

Does it seem as though the addition of `sleephrs` has improved our model substantially over a model with `female` alone (which, you recall, was `c2_m1`)?

Since the `c2_m4` model contains the `c2_m1` model's predictors as a subset and the outcome is the same for each model, we consider the models *nested* and have some extra tools available to compare them.

- I might start by looking at the basic summaries for each model.

```
glance(c2_m4)
```

```
      r.squared adj.r.squared   sigma statistic    p.value df    logLik
1 0.008341404   0.005006229 6.309685    2.50104 0.05818038  4 -2919.873
      AIC      BIC deviance df.residual
1 5849.747 5873.736 35512.42         892
```

```
glance(c2_m1)
```

```
      r.squared adj.r.squared   sigma statistic    p.value df    logLik
1 0.004345169   0.003231461 6.31531    3.901534 0.04854928  2 -2921.675
      AIC      BIC deviance df.residual
1 5849.35 5863.744 35655.53         894
```

- The R^2 is twice as large for the model with `sleephrs`, but still very tiny.
- The p value for the global ANOVA test is actually less significant in `c2_m4` than in `c2_m1`.
- Smaller AIC and smaller BIC statistics are more desirable. Here, there's little to choose from, but `c2_m1` is a little better on each standard.
- We might also consider a significance test by looking at an ANOVA model comparison. This is only appropriate because `c2_m1` is nested in `c2_m4`.

```
anova(c2_m4, c2_m1)
```

Analysis of Variance Table

```

Model 1: bmi ~ female * sleephrs
Model 2: bmi ~ female
      Res.Df  RSS Df Sum of Sq    F Pr(>F)
1      892 35512
2      894 35656 -2    -143.11 1.7973 0.1663

```

The addition of the `sleephrs` term picked up 143 in the sum of squares column, at a cost of two degrees of freedom, yielding a p value of 0.166, suggesting that this isn't a significant improvement over the model that just did a t -test on `female`.

2.12 c2_m5: What if we add more variables?

We can boost our R^2 a bit, to over 5%, by adding in two new variables, related to whether or not the subject (in the past 30 days) used the internet, and on how many days the subject drank alcoholic beverages.

```

c2_m5 <- lm(bmi ~ female + exerany + sleephrs + internet30 + alcdays,
            data = smartcle2)
summary(c2_m5)

```

Call:

```
lm(formula = bmi ~ female + exerany + sleephrs + internet30 +
    alcdays, data = smartcle2)
```

Residuals:

```

      Min       1Q   Median       3Q      Max
-16.147  -3.997  -0.856   2.487  35.965

```

Coefficients:

```

              Estimate Std. Error t value Pr(>|t|)
(Intercept) 30.84066     1.18458  26.035 < 2e-16 ***
female      -1.28801     0.42805  -3.009  0.0027 **
exerany      -2.42161     0.49853  -4.858 1.40e-06 ***
sleephrs     -0.14118     0.13988  -1.009  0.3131
internet30    1.38916     0.54252   2.561  0.0106 *
alcdays      -0.10460     0.02595  -4.030 6.04e-05 ***
---

```

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 6.174 on 890 degrees of freedom

Multiple R-squared: 0.05258, Adjusted R-squared: 0.04726

F-statistic: 9.879 on 5 and 890 DF, p-value: 3.304e-09

1. Here's the ANOVA for this model. What can we study with this?

```
anova(c2_m5)
```

Analysis of Variance Table

Response: bmi

```

      Df Sum Sq Mean Sq F value    Pr(>F)
female  1    156   155.61   4.0818  0.04365 *
exerany  1    897   896.93  23.5283 1.453e-06 ***
sleephrs  1     33    32.90   0.8631  0.35313

```

```
internet30  1    178  178.33  4.6779  0.03082 *
alcdays     1    619  619.26 16.2443 6.044e-05 ***
Residuals  890  33928   38.12
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

2. Consider the revised output below. Now what can we study?

```
anova(lm(bmi ~ exerany + internet30 + alcdays + female + sleephrs,
         data = smartcle2))
```

Analysis of Variance Table

```
Response: bmi
      Df Sum Sq Mean Sq F value    Pr(>F)
exerany  1    795   795.46  20.8664 5.618e-06 ***
internet30  1    212   211.95   5.5599 0.0185925 *
alcdays    1    486   486.03  12.7496 0.0003752 ***
female     1    351   350.75   9.2010 0.0024891 **
sleephrs   1     39    38.83   1.0186 0.3131176
Residuals 890  33928   38.12
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

3. What does the output below let us conclude?

```
anova(lm(bmi ~ exerany + internet30 + alcdays + female + sleephrs,
         data = smartcle2),
      lm(bmi ~ exerany + female + alcdays,
         data = smartcle2))
```

Analysis of Variance Table

```
Model 1: bmi ~ exerany + internet30 + alcdays + female + sleephrs
Model 2: bmi ~ exerany + female + alcdays
  Res.Df  RSS Df Sum of Sq    F Pr(>F)
1     890 33928
2     892 34221 -2    -293.2  3.8456 0.02173 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

4. What does it mean for the models to be “nested”?

2.13 c2_m6: Would adding self-reported health help?

And we can do even a bit better than that by adding in a multi-categorical measure: self-reported general health.

```
c2_m6 <- lm(bmi ~ female + exerany + sleephrs + internet30 + alcdays + genhealth,
           data = smartcle2)
summary(c2_m6)
```

Call:

```
lm(formula = bmi ~ female + exerany + sleephrs + internet30 +
    alcdays + genhealth, data = smartcle2)
```

Residuals:

Min	1Q	Median	3Q	Max
-16.331	-3.813	-0.838	2.679	34.166

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	26.49498	1.31121	20.206	< 2e-16	***
female	-0.85520	0.41969	-2.038	0.041879	*
exerany	-1.61968	0.50541	-3.205	0.001400	**
sleephrs	-0.12719	0.13613	-0.934	0.350368	
internet30	2.02498	0.53898	3.757	0.000183	***
alcdays	-0.08431	0.02537	-3.324	0.000925	***
genhealth2_VeryGood	2.10537	0.59408	3.544	0.000415	***
genhealth3_Good	4.08245	0.60739	6.721	3.22e-11	***
genhealth4_Fair	4.99213	0.80178	6.226	7.37e-10	***
genhealth5_Poor	3.11025	1.12614	2.762	0.005866	**

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.993 on 886 degrees of freedom

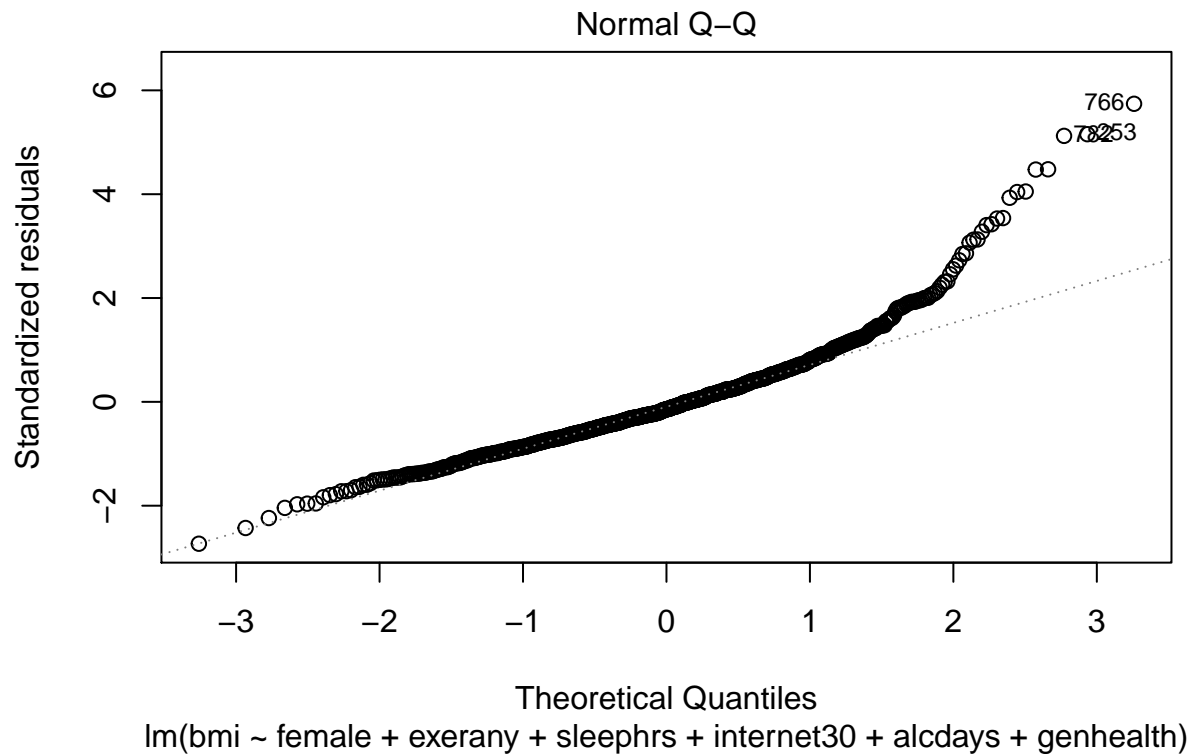
Multiple R-squared: 0.1115, Adjusted R-squared: 0.1024

F-statistic: 12.35 on 9 and 886 DF, p-value: < 2.2e-16

1. If Harry and Marty have the same values of `female`, `exerany`, `sleephrs`, `internet30` and `alcdays`, but Harry rates his health as Good, and Marty rates his as Fair, then what is the difference in the predictions? Who is predicted to have a larger BMI, and by how much?

2. What does this normal probability plot of the residuals suggest?

```
plot(c2_m6, which = 2)
```



2.14 c2_m7: What if we added days of work missed?

```
c2_m7 <- lm(bmi ~ female + exerany + sleephrs + internet30 + alcdays +
             genhealth + physhealth + menthealth,
             data = smartcle2)
summary(c2_m7)
```

Call:

```
lm(formula = bmi ~ female + exerany + sleephrs + internet30 +
    alcdays + genhealth + physhealth + menthealth, data = smartcle2)
```

Residuals:

Min	1Q	Median	3Q	Max
-16.060	-3.804	-0.890	2.794	33.972

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	25.88208	1.31854	19.629	< 2e-16 ***
female	-0.96435	0.41908	-2.301	0.021616 *
exerany	-1.43171	0.50635	-2.828	0.004797 **
sleephrs	-0.08033	0.13624	-0.590	0.555583
internet30	2.00267	0.53759	3.725	0.000207 ***
alcdays	-0.07997	0.02528	-3.163	0.001614 **

```

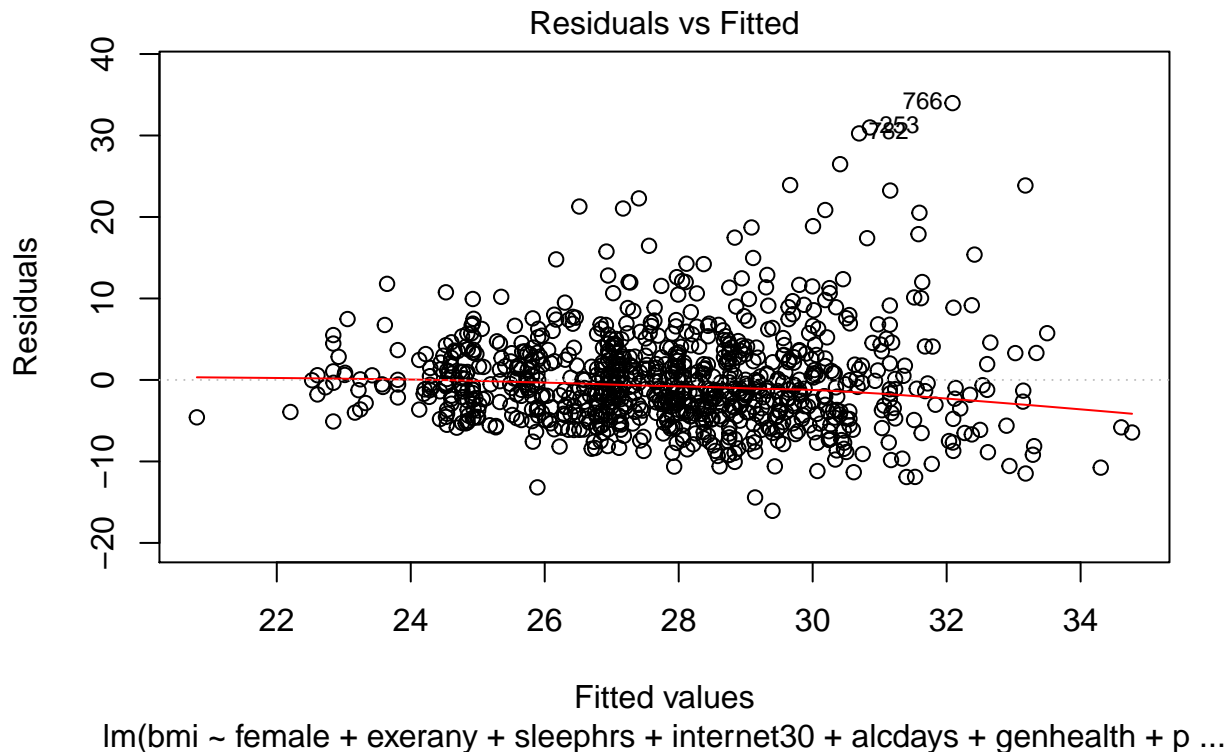
genhealth2_VeryGood  2.09533    0.59238    3.537 0.000425 ***
genhealth3_Good      3.90949    0.60788    6.431 2.07e-10 ***
genhealth4_Fair      4.27152    0.83986    5.086 4.47e-07 ***
genhealth5_Poor      1.26021    1.31556    0.958 0.338361
physhealth           0.06088    0.03005    2.026 0.043064 *
menthealth           0.06636    0.03177    2.089 0.037021 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.964 on 884 degrees of freedom
Multiple R-squared:  0.1219,    Adjusted R-squared:  0.111
F-statistic: 11.16 on 11 and 884 DF,  p-value: < 2.2e-16

```

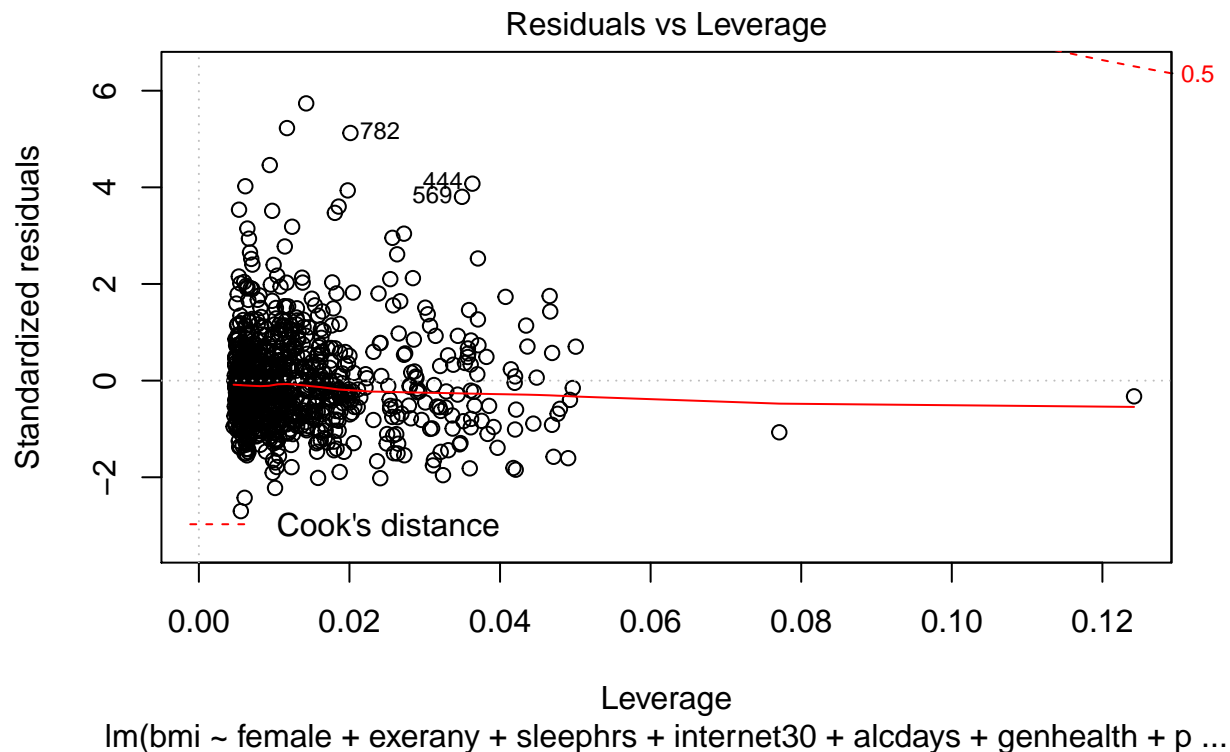
1. How do the assumptions behind this model look?

```
plot(c2_m7, which = 1)
```



2. What can we conclude from the plot below?

```
plot(c2_m7, which = 5)
```

2.15 (DRAFT material) How might we validate this model?

Here's some early code for that issue, which is built on some material by David Robinson at <https://rpubs.com/dgrtwo/cv-modelr>

This bit of code performs what is called *10-crossfold separation*. In words, this approach splits the 896 observations in our data into 10 exclusive partitions of about 90% into a training sample, and the remaining 10% in a test sample. The next part of the code maps a modeling step to the training data, and then fits the resulting model on the test data using the **broom** package's **augment** function.

I've selected the variables in this case so that the model we'll fit is the **m2_c7** model we've been looking at, although there are several ways to accomplish this.

```
set.seed(4320118)

models <- smartcle2 %>%
  select(bmi, female, exerany, sleephrs,
         internet30, alcdays, genhealth) %>%
  crossv_kfold(k = 10) %>%
  mutate(model = map(train, ~ lm(bmi ~ ., data = .)))

predictions <- models %>%
  unnest(map2(model, test, ~ augment(.x, newdata = .y)))

predictions
```

```
# A tibble: 896 x 10
  .id    bmi female exerany sleephrs internet30 alcdays genhealth
  <chr> <dbl> <int> <int> <int> <int> <int> <fct>
1 01    24.1     0     1     7     1     2 1_Excellent
2 01    36.4     0     1     8     1     0 4_Fair
3 01    32.1     1     0     4     1     5 2_VeryGood
4 01    27.3     0     1     8     1     0 1_Excellent
5 01    28.0     0     1     7     1     4 2_VeryGood
6 01    22.5     1     1     7     1     3 2_VeryGood
7 01    26.3     0     1     7     1     1 1_Excellent
8 01    22.4     0     1     8     1     4 1_Excellent
9 01    19.3     1     0     6     1     0 3_Good
10 01    24.2     1     0     6     0     0 3_Good
# ... with 886 more rows, and 2 more variables: .fitted <dbl>, .se.fit
# <dbl>
```

The results are a set of predictions based on the splits into training and test groups (remember there are 10 of them, indexed by `.id`) that describe the complete set of 896 respondents again.

What this lets us now do is calculate the root Mean Squared Prediction Error (RMSE) and Mean Absolute Prediction Error (MAE) for this model (the `c2_m7` model) across these observations, and also to compare that error to a model that simply predicts the mean `bmi` across all patients (the `intercept only` model.) In practice, we could consider two distinct models in doing this work.

```
predictions %>%
  summarize(RMSE_c2_m7 = sqrt(mean((bmi - .fitted) ^2)),
            MAE_c2_m7 = mean(abs(bmi - .fitted)),
            RMSE_interceptonly = sqrt(mean((bmi - mean(bmi))^2)),
            MAE_interceptonly = mean(abs(bmi - mean(bmi))))
```

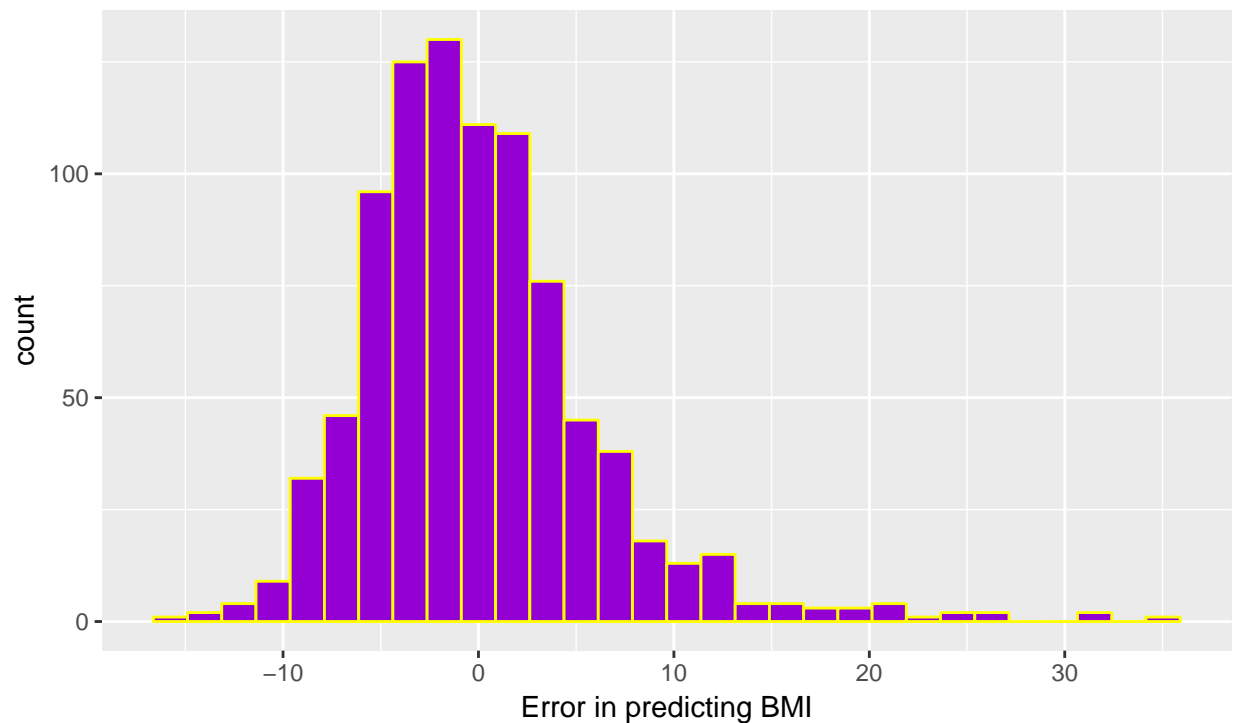
```
# A tibble: 1 x 4
  RMSE_c2_m7 MAE_c2_m7 RMSE_interceptonly MAE_interceptonly
  <dbl>      <dbl>      <dbl>      <dbl>
1    6.03      4.40      6.32      4.59
```

Another thing we could do with this tibble of predictions we have created is to graph the size of the prediction errors (observed `bmi` minus predicted values in `.fitted`) that our modeling approach makes.

```
predictions %>%
  mutate(errors = bmi - .fitted) %>%
  ggplot(., aes(x = errors)) +
  geom_histogram(bins = 30, fill = "darkviolet", col = "yellow") +
  labs(title = "Cross-Validated Errors in Prediction of BMI",
       subtitle = "Using a model (`c2_m7`) including 6 regression inputs",
       caption = "SMART BRFSS 2016 data for Cleveland-Elyria MMSA, n = 896",
       x = "Error in predicting BMI")
```

Cross-Validated Errors in Prediction of BMI

Using a model (`c2_m7``) including 6 regression inputs



SMART BRFSS 2016 data for Cleveland–Elyria MMSA, $n = 896$

2.16 Coming Soon ...

1. Would stepwise regression help us build a better model for `bmi`?
 - Is there a better approach for variable selection? What's this I hear about “best subsets”, for example?
2. How should we think about potential transformations of these predictors?
 - What's a Spearman rho-squared plot, and how might it help us decide how to spend degrees of freedom on non-linear terms better?
3. How do we deal with missing data in fitting and evaluating a linear regression model if we don't actually want to drop all of the incomplete cases?
4. How can we use the `ols` tool in the `rms` package to fit regression models?
5. How can we use the tools in the `arm` package to fit and evaluate regression models?

Chapter 3

Two-Factor Analysis of Variance and Interactions

3.1 The bonding data: A Designed Dental Experiment

The `bonding` data describe a designed experiment into the properties of four different resin types (`resin = A, B, C, D`) and two different curing light sources (`light = Halogen, LED`) as they relate to the resulting bonding strength (measured in MPa¹) on the surface of teeth. The source is Kim (2014).

The experiment involved making measurements of bonding strength under a total of 80 experimental setups, or runs, with 10 runs completed at each of the eight combinations of a light source and a resin type. The data are gathered in the `bonding.csv` file.

```
bonding
```

```
# A tibble: 80 x 4
  run_ID light  resin strength
  <fct>  <fct>  <fct>    <dbl>
1 R101   LED    B        12.8
2 R102   Halogen B        22.2
3 R103   Halogen B        24.6
4 R104   LED    A        17.0
5 R105   LED    C        32.2
6 R106   Halogen B        27.1
7 R107   LED    A        23.4
8 R108   Halogen A        23.5
9 R109   Halogen D        37.3
10 R110  Halogen A        19.7
# ... with 70 more rows
```

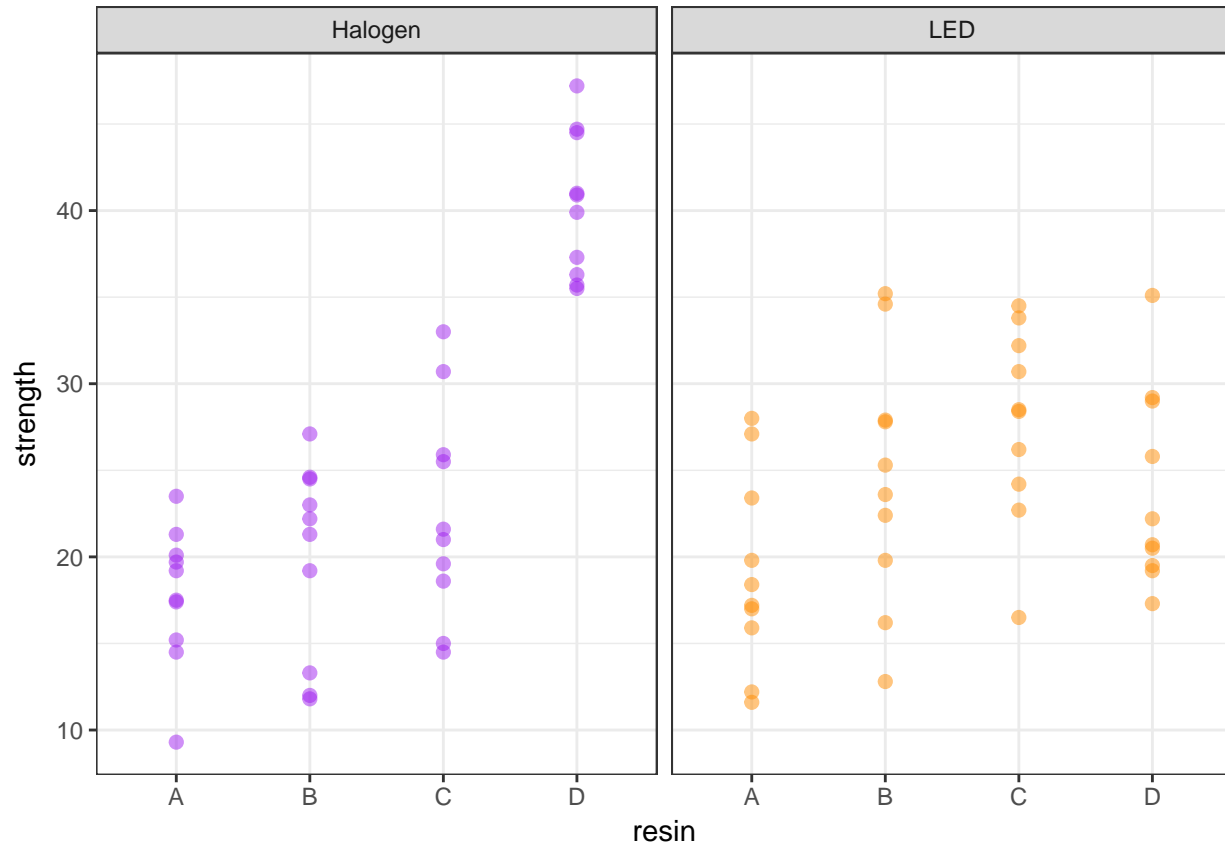
3.1.1 Looking at the Data

We can look at the distribution of the `strength` values at the combinations of `light` and `resin`, with a plot like this one...

```
ggplot(bonding, aes(x = resin, y = strength, color = light)) +
  geom_point(size = 2, alpha = 0.5) +
```

¹The MPa is defined as the failure load (in Newtons) divided by the entire bonded area, in mm².

```
facet_wrap(~ light) +
guides(color = FALSE) +
scale_color_manual(values = c("purple", "darkorange")) +
theme_bw()
```



3.2 A Means Plot (with standard deviations) to check for interaction

Sometimes, we'll instead look at a plot simply of the means (and, often, the standard deviations) of **strength** at each combination of **light** and **resin**. We'll start by building up a data set with the summaries we want to plot.

```
bond.sum <- bonding %>%
  group_by(resin, light) %>%
  summarize(mean.str = mean(strength), sd.str = sd(strength))
```

```
bond.sum
```

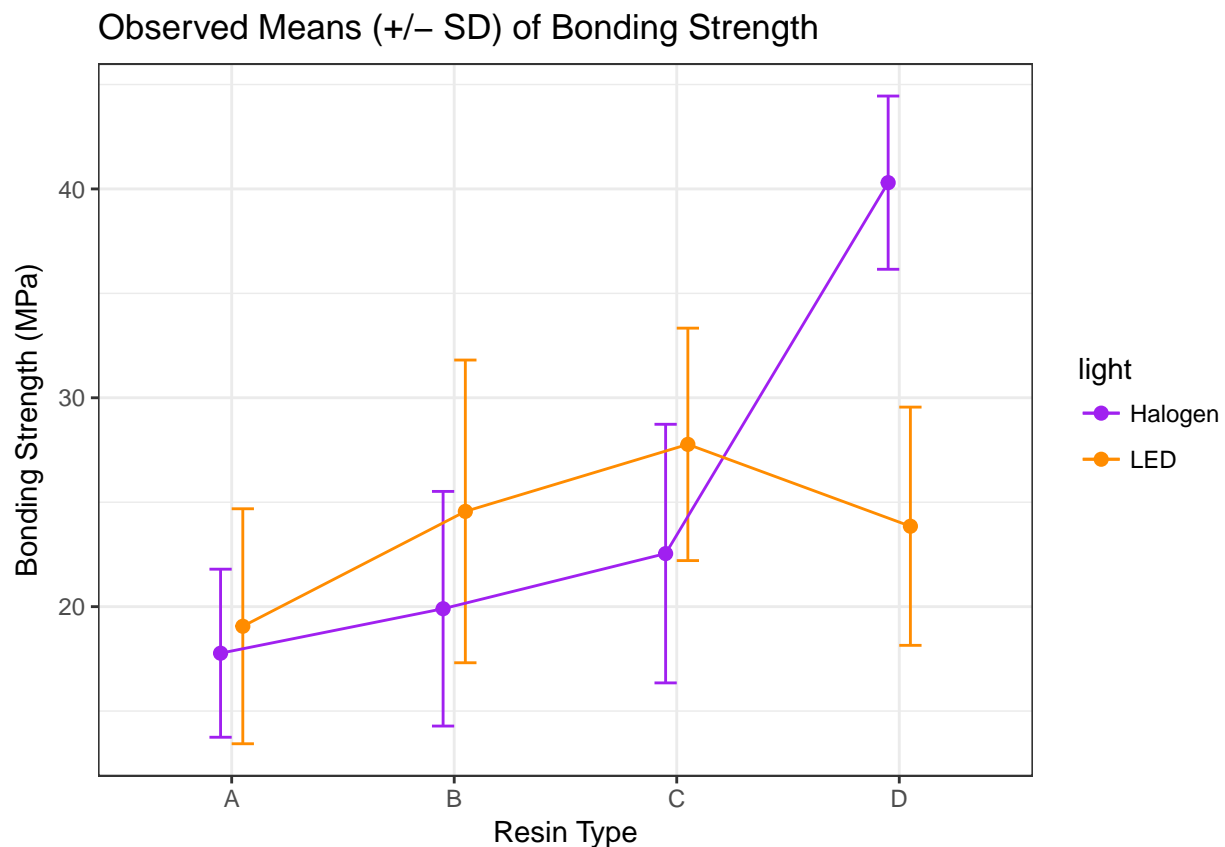
```
# A tibble: 8 x 4
# Groups:   resin [?]
  resin light  mean.str sd.str
  <fct> <fct>    <dbl> <dbl>
1 A     Halogen  17.8   4.02
2 A     LED      19.1   5.63
3 B     Halogen  19.9   5.62
```

4	B	LED	24.6	7.25
5	C	Halogen	22.5	6.19
6	C	LED	27.8	5.56
7	D	Halogen	40.3	4.15
8	D	LED	23.8	5.70

Now, we'll use this new data set to plot the means and standard deviations of **strength** at each combination of **resin** and **light**.

```
## The error bars will overlap unless we adjust the position.
pd <- position_dodge(0.2) # move them .1 to the left and right

ggplot(bond.sum, aes(x = resin, y = mean.str, col = light)) +
  geom_errorbar(aes(ymin = mean.str - sd.str,
                    ymax = mean.str + sd.str),
                width = 0.2, position = pd) +
  geom_point(size = 2, position = pd) +
  geom_line(aes(group = light), position = pd) +
  scale_color_manual(values = c("purple", "darkorange")) +
  theme_bw() +
  labs(y = "Bonding Strength (MPa)", x = "Resin Type",
       title = "Observed Means (+/- SD) of Bonding Strength")
```



Is there evidence of a meaningful interaction between the resin type and the **light** source on the bonding strength in this plot?

- Sure. A meaningful interaction just means that the strength associated with different **resin** types depends on the **light** source.

- With LED light, it appears that resin C leads to the strongest bonding strength.
- With Halogen light, though, it seems that resin D is substantially stronger.
- Note that the lines we see here connecting the light sources aren't in parallel (as they would be if we had zero interaction between resin and light), but rather, they cross.

3.2.1 Skimming the data after grouping by resin and light

We might want to look at a numerical summary of the strengths within these groups, too.

```
bonding %>%
  group_by(resin, light) %>%
  skim(strength)
```

Skim summary statistics

```
n obs: 80
n variables: 4
group variables: resin, light
```

Variable type: numeric

resin	light	variable	missing	complete	n	mean	sd	p0	p25	median
A	Halogen	strength	0	10	10	17.77	4.02	9.3	15.75	18.35
A	LED	strength	0	10	10	19.06	5.63	11.6	16.18	17.8
B	Halogen	strength	0	10	10	19.9	5.62	11.8	14.78	21.75
B	LED	strength	0	10	10	24.56	7.25	12.8	20.45	24.45
C	Halogen	strength	0	10	10	22.54	6.19	14.5	18.85	21.3
C	LED	strength	0	10	10	27.77	5.56	16.5	24.7	28.45
D	Halogen	strength	0	10	10	40.3	4.15	35.5	36.55	40.4
D	LED	strength	0	10	10	23.85	5.7	17.3	19.75	21.45

p75	p100
20	23.5
22.5	28
24.12	27.1
27.87	35.2
25.8	33
31.83	34.5
43.62	47.2
28.2	35.1

3.3 Fitting the Two-Way ANOVA model with Interaction

```
c3_m1 <- lm(strength ~ resin * light, data = bonding)
summary(c3_m1)
```

Call:

```
lm(formula = strength ~ resin * light, data = bonding)
```

Residuals:

Min	1Q	Median	3Q	Max
-11.760	-3.663	-0.320	3.697	11.250

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	17.770	1.771	10.033	2.57e-15	***
resinB	2.130	2.505	0.850	0.3979	
resinC	4.770	2.505	1.904	0.0609	.
resinD	22.530	2.505	8.995	2.13e-13	***
lightLED	1.290	2.505	0.515	0.6081	
resinB:lightLED	3.370	3.542	0.951	0.3446	
resinC:lightLED	3.940	3.542	1.112	0.2697	
resinD:lightLED	-17.740	3.542	-5.008	3.78e-06	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 5.601 on 72 degrees of freedom

Multiple R-squared: 0.6149, Adjusted R-squared: 0.5775

F-statistic: 16.42 on 7 and 72 DF, p-value: 9.801e-13

3.3.1 The ANOVA table for our model

In a two-way ANOVA model, we begin by assessing the interaction term. If it's important, then our best model is the model including the interaction. If it's not important, we will often move on to consider a new model, fit without an interaction.

The ANOVA table is especially helpful in this case, because it lets us look specifically at the interaction effect.

```
anova(c3_m1)
```

Analysis of Variance Table

Response: strength

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
resin	3	1999.72	666.57	21.2499	5.792e-10 ***
light	1	34.72	34.72	1.1067	0.2963
resin:light	3	1571.96	523.99	16.7043	2.457e-08 ***
Residuals	72	2258.52	31.37		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

3.3.2 Is the interaction important?

In this case, the interaction:

- is evident in the means plot, and
- is highly statistically significant, and
- accounts for a sizeable fraction (27%) of the overall variation

$$\eta_{interaction}^2 = \frac{SS(\text{resin:light})}{SS(\text{Total})} = \frac{1571.96}{1999.72 + 34.72 + 1571.96 + 2258.52} = 0.268$$

If the interaction were *either* large or significant we would be inclined to keep it in the model. In this case, it's both, so there's no real reason to remove it.

3.3.3 Interpreting the Interaction

Recall the model equation, which is:

```
c3_m1
```

Call:

```
lm(formula = strength ~ resin * light, data = bonding)
```

Coefficients:

(Intercept)	resinB	resinC	resinD
17.77	2.13	4.77	22.53
lightLED	resinB:lightLED	resinC:lightLED	resinD:lightLED
1.29	3.37	3.94	-17.74

so we have:

$$strength = 17.77 + 2.13resinB + 4.77resinC + 22.53resinD + 1.29lightLED + 3.37resinB*lightLED + 3.94resinC*lightLED - 17.74resinD*lightLED$$

So, if `light` = Halogen, our equation is:

$$strength = 17.77 + 2.13resinB + 4.77resinC + 22.53resinD$$

And if `light` = LED, our equation is:

$$strength = 19.06 + 5.50resinB + 8.71resinC + 4.79resinD$$

Note that both the intercept and the slopes change as a result of the interaction. The model yields a different prediction for every possible combination of a `resin` type and a `light` source.

3.4 Comparing Individual Combinations of `resin` and `light`

To make comparisons between individual combinations of a `resin` type and a `light` source, using something like Tukey's HSD approach for multiple comparisons, we first refit the model using the `aov` structure, rather than `lm`.

```
c3m1_aov <- aov(strength ~ resin * light, data = bonding)
```

```
summary(c3m1_aov)
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
resin	3	1999.7	666.6	21.250	5.79e-10 ***
light	1	34.7	34.7	1.107	0.296
resin:light	3	1572.0	524.0	16.704	2.46e-08 ***
Residuals	72	2258.5	31.4		

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

And now, we can obtain Tukey HSD comparisons (which will maintain an overall 95% family-wise confidence level) across the `resin` types, the `light` sources, and the combinations, with the `TukeyHSD` command. This approach is only completely appropriate if these comparisons are pre-planned, and if the design is balanced (as this is, with the same sample size for each combination of a `light` source and `resin` type.)

TukeyHSD(c3m1_aov)

Tukey multiple comparisons of means
95% family-wise confidence level

Fit: aov(formula = strength ~ resin * light, data = bonding)

\$resin

	diff	lwr	upr	p adj
B-A	3.815	-0.843129	8.473129	0.1461960
C-A	6.740	2.081871	11.398129	0.0016436
D-A	13.660	9.001871	18.318129	0.0000000
C-B	2.925	-1.733129	7.583129	0.3568373
D-B	9.845	5.186871	14.503129	0.0000026
D-C	6.920	2.261871	11.578129	0.0011731

\$light

	diff	lwr	upr	p adj
LED-Halogen	-1.3175	-3.814042	1.179042	0.2963128

\$`resin:light`

	diff	lwr	upr	p adj
B:Halogen-A:Halogen	2.13	-5.68928258	9.949283	0.9893515
C:Halogen-A:Halogen	4.77	-3.04928258	12.589283	0.5525230
D:Halogen-A:Halogen	22.53	14.71071742	30.349283	0.0000000
A:LED-A:Halogen	1.29	-6.52928258	9.109283	0.9995485
B:LED-A:Halogen	6.79	-1.02928258	14.609283	0.1361092
C:LED-A:Halogen	10.00	2.18071742	17.819283	0.0037074
D:LED-A:Halogen	6.08	-1.73928258	13.899283	0.2443200
C:Halogen-B:Halogen	2.64	-5.17928258	10.459283	0.9640100
D:Halogen-B:Halogen	20.40	12.58071742	28.219283	0.0000000
A:LED-B:Halogen	-0.84	-8.65928258	6.979283	0.9999747
B:LED-B:Halogen	4.66	-3.15928258	12.479283	0.5818695
C:LED-B:Halogen	7.87	0.05071742	15.689283	0.0473914
D:LED-B:Halogen	3.95	-3.86928258	11.769283	0.7621860
D:Halogen-C:Halogen	17.76	9.94071742	25.579283	0.0000000
A:LED-C:Halogen	-3.48	-11.29928258	4.339283	0.8591455
B:LED-C:Halogen	2.02	-5.79928258	9.839283	0.9922412
C:LED-C:Halogen	5.23	-2.58928258	13.049283	0.4323859
D:LED-C:Halogen	1.31	-6.50928258	9.129283	0.9995004
A:LED-D:Halogen	-21.24	-29.05928258	-13.420717	0.0000000
B:LED-D:Halogen	-15.74	-23.55928258	-7.920717	0.0000006
C:LED-D:Halogen	-12.53	-20.34928258	-4.710717	0.0001014
D:LED-D:Halogen	-16.45	-24.26928258	-8.630717	0.0000002
B:LED-A:LED	5.50	-2.31928258	13.319283	0.3665620
C:LED-A:LED	8.71	0.89071742	16.529283	0.0185285
D:LED-A:LED	4.79	-3.02928258	12.609283	0.5471915
C:LED-B:LED	3.21	-4.60928258	11.029283	0.9027236
D:LED-B:LED	-0.71	-8.52928258	7.109283	0.9999920
D:LED-C:LED	-3.92	-11.73928258	3.899283	0.7690762

One conclusion from this is that the combination of D and Halogen is significantly stronger than each of the other seven combinations.

3.5 The bonding model without Interaction

It seems incorrect in this situation to fit a model without the interaction term, but we'll do so just so you can see what's involved.

```
c3_m2 <- lm(strength ~ resin + light, data = bonding)

summary(c3_m2)
```

Call:

```
lm(formula = strength ~ resin + light, data = bonding)
```

Residuals:

Min	1Q	Median	3Q	Max
-14.1163	-4.9531	0.1187	4.4613	14.4663

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	19.074	1.787	10.676	< 2e-16 ***
resinB	3.815	2.260	1.688	0.09555 .
resinC	6.740	2.260	2.982	0.00386 **
resinD	13.660	2.260	6.044	5.39e-08 ***
lightLED	-1.317	1.598	-0.824	0.41229

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.147 on 75 degrees of freedom

Multiple R-squared: 0.3469, Adjusted R-squared: 0.312

F-statistic: 9.958 on 4 and 75 DF, p-value: 1.616e-06

In the no-interaction model, if light = Halogen, our equation is:

$$strength = 19.07 + 3.82resinB + 6.74resinC + 13.66resinD$$

And if light = LED, our equation is:

$$strength = 17.75 + 3.82resinB + 6.74resinC + 13.66resinD$$

So, in the no-interaction model, only the intercept changes.

```
anova(c3_m2)
```

Analysis of Variance Table

Response: strength

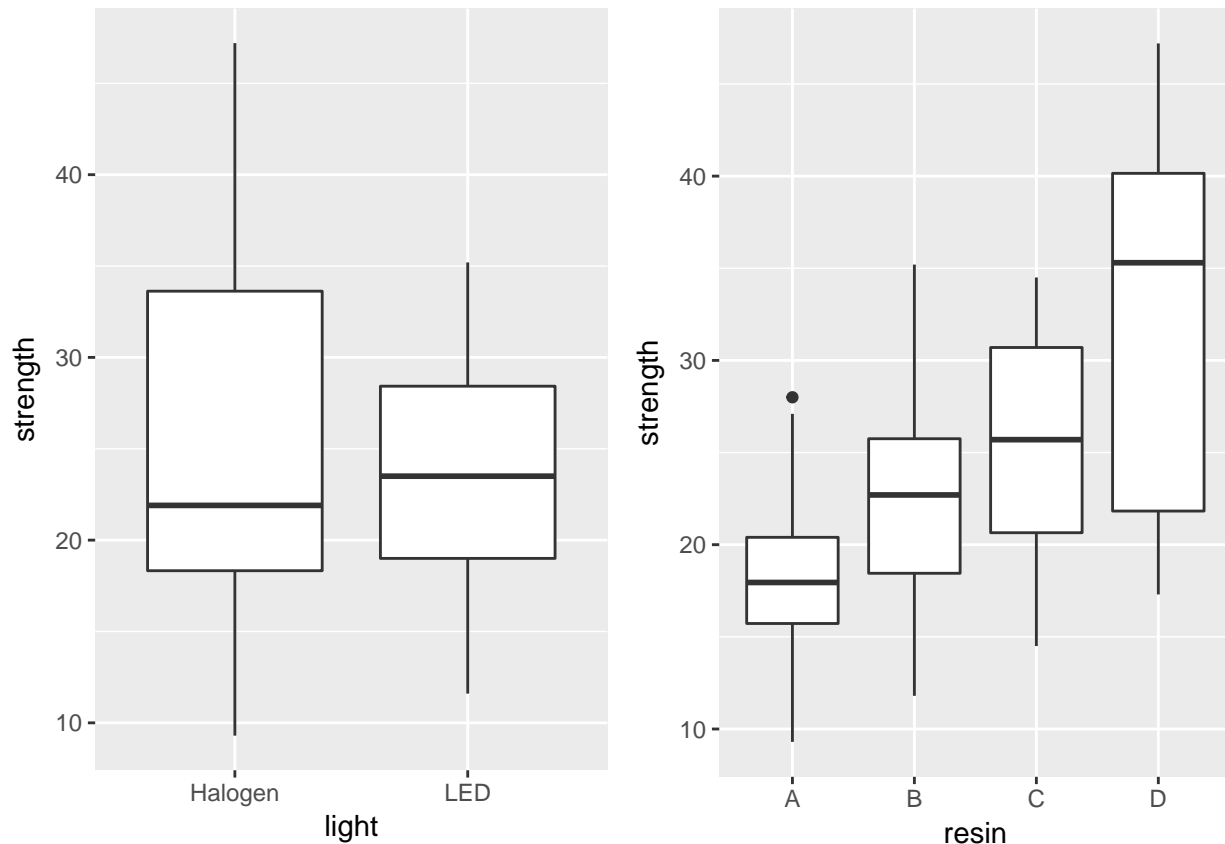
	Df	Sum Sq	Mean Sq	F value	Pr(>F)
resin	3	1999.7	666.57	13.0514	6.036e-07 ***
light	1	34.7	34.72	0.6797	0.4123
Residuals	75	3830.5	51.07		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

And, it appears, if we ignore the interaction, then resin type has a significant impact on strength but light source doesn't. This is a bit clearer, when we look at boxplots of the separated light and resin groups.

```
p1 <- ggplot(bonding, aes(x = light, y = strength)) +
  geom_boxplot()
p2 <- ggplot(bonding, aes(x = resin, y = strength)) +
  geom_boxplot()

gridExtra::grid.arrange(p1, p2, nrow = 1)
```



3.6 cortisol: A Hypothetical Clinical Trial

156 adults who complained of problems with a high-stress lifestyle were enrolled in a hypothetical clinical trial of the effectiveness of a behavioral intervention designed to help reduce stress levels, as measured by salivary cortisol.

The subjects were randomly assigned to one of three intervention groups (usual care, low dose, and high dose.) The “low dose” subjects received a one-week intervention with a follow-up at week 5. The “high dose” subjects received a more intensive three-week intervention, with follow up at week 5.

Since cortisol levels rise and fall with circadian rhythms, the cortisol measurements were taken just after rising for all subjects. These measurements were taken at baseline, and again at five weeks. The difference (baseline - week 5) in cortisol level (in micrograms / l) serves as the primary outcome.

3.6.1 Codebook and Raw Data for cortisol

The data are gathered in the `cortisol` data set. Included are:

Variable	Description
subject	subject identification code
interv	intervention group (UC = usual care, Low, High)
waist	waist circumference at baseline (in inches)
sex	male or female
cort.1	salivary cortisol level (microg/l) week 1
cort.5	salivary cortisol level (microg/l) week 5

```
cortisol
```

```
# A tibble: 156 x 6
```

```
  subject interv waist sex  cort.1 cort.5
    <int> <fct> <dbl> <fct> <dbl> <dbl>
1     1001 UC    48.3 M     13.4  13.3
2     1002 Low   58.3 M     17.8  16.6
3     1003 High  43.0 M     14.4  12.7
4     1004 Low   44.9 M      9.00  9.80
5     1005 High  46.1 M     14.2  14.2
6     1006 UC    41.3 M     14.8  15.1
7     1007 Low   51.0 F     13.7  16.0
8     1008 UC    42.0 F     17.3  18.7
9     1009 Low   24.7 F     15.3  15.8
10    1010 Low   59.4 M     12.4  11.7
```

```
# ... with 146 more rows
```

3.6.2 Creating a factor combining sex and waist

Next, we'll put the `waist` and `sex` data in the `cortisol` example together. We want to build a second categorical variable (called `fat_est`) combining this information, to indicate “healthy” vs. “unhealthy” levels of fat around the waist.

- Male subjects whose waist circumference is 40 inches or more, and
- Female subjects whose waist circumference is 35 inches or more, will fall in the “unhealthy” group.

```
cortisol <- cortisol %>%
  mutate(
    fat_est = factor(case_when(
      sex == "M" & waist >= 40 ~ "unhealthy",
      sex == "F" & waist >= 35 ~ "unhealthy",
      TRUE ~ "healthy")),
    cort_diff = cort.1 - cort.5)

summary(cortisol)
```

subject	interv	waist	sex	cort.1
Min. :1001	High:53	Min. :20.80	F:83	Min. : 6.000
1st Qu.:1040	Low :52	1st Qu.:33.27	M:73	1st Qu.: 9.675
Median :1078	UC :51	Median :40.35		Median :12.400
Mean :1078		Mean :40.42		Mean :12.686
3rd Qu.:1117		3rd Qu.:47.77		3rd Qu.:16.025
Max. :1156		Max. :59.90		Max. :19.000
cort.5	fat_est	cort_diff		
Min. : 4.2	healthy : 56	Min. : -2.3000		
1st Qu.: 9.6	unhealthy:100	1st Qu.: -0.5000		

Median :12.6	Median : 0.2000
Mean :12.4	Mean : 0.2821
3rd Qu.:15.7	3rd Qu.: 1.2000
Max. :19.7	Max. : 2.0000

3.7 A Means Plot for the cortisol trial (with standard errors)

Again, we'll start by building up a data set with the summaries we want to plot.

```
cort.sum <- cortisol %>%
  group_by(interv, fat_est) %>%
  summarize(mean.cort = mean(cort_diff),
            se.cort = sd(cort_diff)/sqrt(n()))

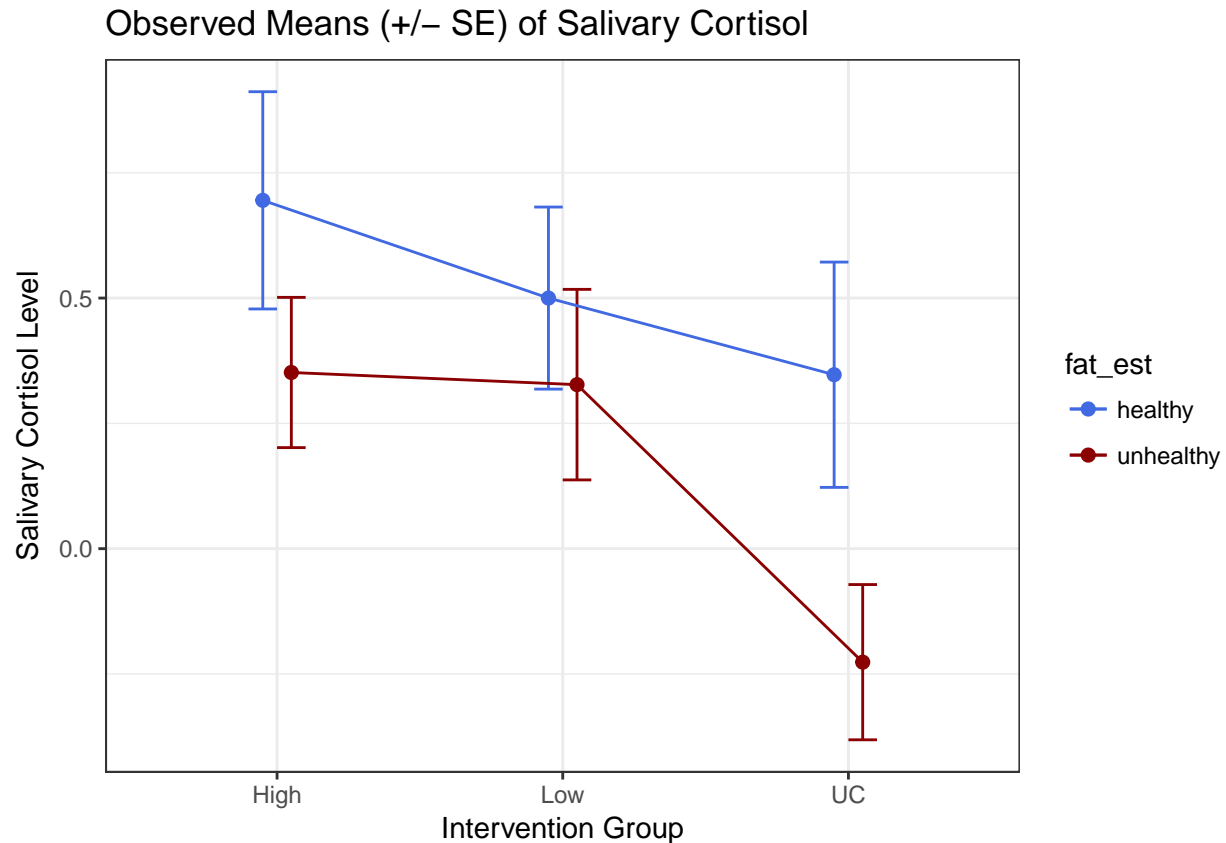
cort.sum
```

```
# A tibble: 6 x 4
# Groups:   interv [?]
  interv fat_est mean.cort se.cort
  <fct>   <fct>      <dbl>  <dbl>
1 High   healthy      0.695  0.217
2 High   unhealthy    0.352  0.150
3 Low    healthy      0.500  0.182
4 Low    unhealthy    0.327  0.190
5 UC     healthy      0.347  0.225
6 UC     unhealthy    -0.226  0.155
```

Now, we'll use this new data set to plot the means and standard errors.

```
## The error bars will overlap unless we adjust the position.
pd <- position_dodge(0.2) # move them .1 to the left and right

ggplot(cort.sum, aes(x = interv, y = mean.cort, col = fat_est)) +
  geom_errorbar(aes(ymin = mean.cort - se.cort,
                    ymax = mean.cort + se.cort),
                width = 0.2, position = pd) +
  geom_point(size = 2, position = pd) +
  geom_line(aes(group = fat_est), position = pd) +
  scale_color_manual(values = c("royalblue", "darkred")) +
  theme_bw() +
  labs(y = "Salivary Cortisol Level", x = "Intervention Group",
       title = "Observed Means (+/- SE) of Salivary Cortisol")
```



3.8 A Two-Way ANOVA model for cortisol with Interaction

```
c3_m3 <- lm(cort_diff ~ interv * fat_est, data = cortisol)
anova(c3_m3)
```

Analysis of Variance Table

Response: cort_diff

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
interv	2	7.847	3.9235	4.4698	0.01301 *
fat_est	1	4.614	4.6139	5.2564	0.02326 *
interv:fat_est	2	0.943	0.4715	0.5371	0.58554
Residuals	150	131.666	0.8778		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Does it seem like we need the interaction term in this case?

```
summary(c3_m3)
```

Call:

```
lm(formula = cort_diff ~ interv * fat_est, data = cortisol)
```

Residuals:


```

      Min      1Q   Median      3Q      Max
-2.62727 -0.75702  0.08636  0.84848  2.12647

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)      0.6950     0.2095   3.317  0.00114 **
intervLow        -0.1950     0.3001  -0.650  0.51689
intervUC         -0.3479     0.3091  -1.126  0.26206
fat_estunhealthy -0.3435     0.2655  -1.294  0.19774
intervLow:fat_estunhealthy  0.1708     0.3785   0.451  0.65256
intervUC:fat_estunhealthy -0.2300     0.3846  -0.598  0.55068
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.9369 on 150 degrees of freedom
Multiple R-squared:  0.0924,    Adjusted R-squared:  0.06214
F-statistic: 3.054 on 5 and 150 DF,  p-value: 0.01179

```

How do you reconcile the apparent difference in significance levels between this regression summary and the ANOVA table above?

3.9 A Two-Way ANOVA model for cortisol without Interaction

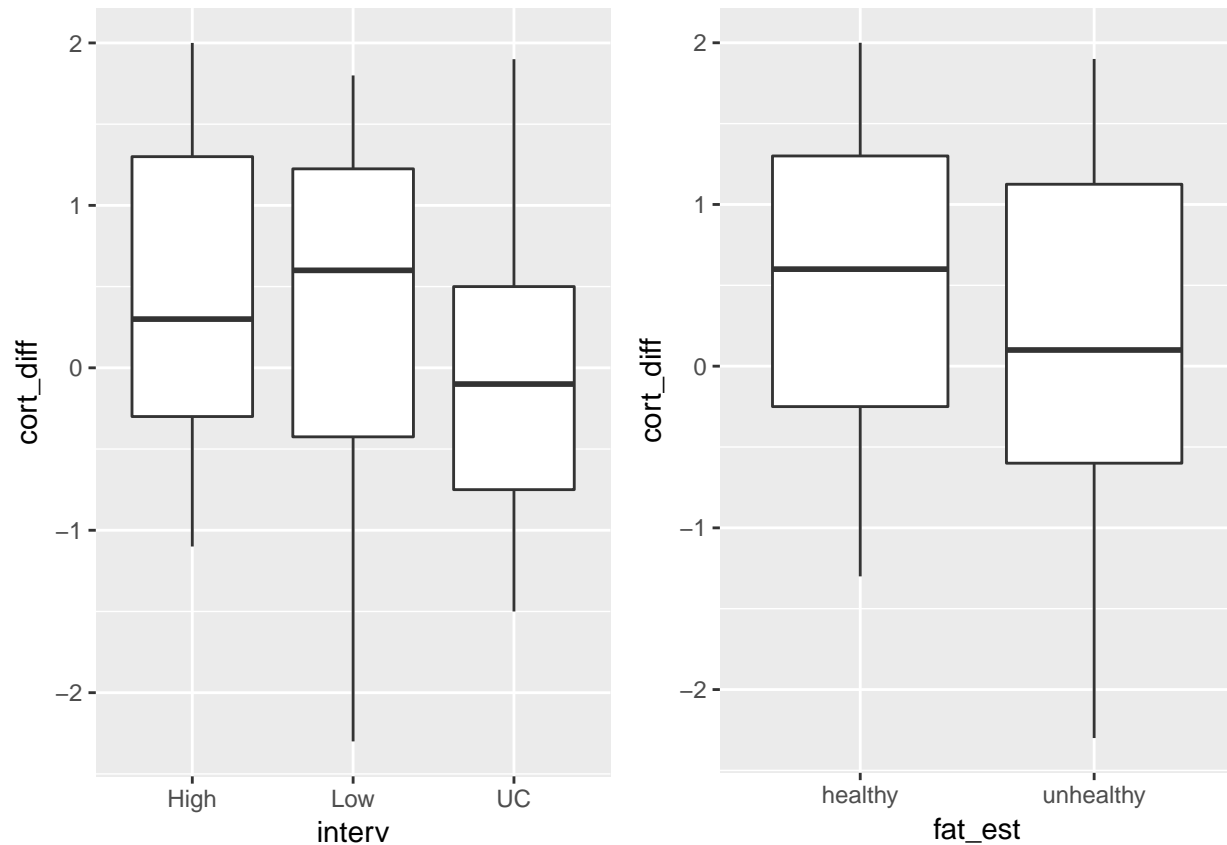
3.9.1 The Graph

```

p1 <- ggplot(cortisol, aes(x = interv, y = cort_diff)) +
  geom_boxplot()
p2 <- ggplot(cortisol, aes(x = fat_est, y = cort_diff)) +
  geom_boxplot()

gridExtra::grid.arrange(p1, p2, nrow = 1)

```



3.9.2 The ANOVA Model

```
c3_m4 <- lm(cort_diff ~ interv + fat_est, data = cortisol)
```

```
anova(c3_m4)
```

Analysis of Variance Table

Response: cort_diff

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
interv	2	7.847	3.9235	4.4972	0.01266 *
fat_est	1	4.614	4.6139	5.2886	0.02283 *
Residuals	152	132.609	0.8724		

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

How do these results compare to those we saw in the model with interaction?

3.9.3 The Regression Summary

```
summary(c3_m4)
```

Call:

```
lm(formula = cort_diff ~ interv + fat_est, data = cortisol)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-2.55929	-0.74527	0.05457	0.86456	2.05489

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)	
(Intercept)	0.70452	0.16093	4.378	2.22e-05	***
intervLow	-0.08645	0.18232	-0.474	0.63606	
intervUC	-0.50063	0.18334	-2.731	0.00707	**
fat_estunhealthy	-0.35878	0.15601	-2.300	0.02283	*

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.934 on 152 degrees of freedom
Multiple R-squared: 0.0859, Adjusted R-squared: 0.06785
F-statistic: 4.761 on 3 and 152 DF, p-value: 0.00335

3.9.4 Tukey HSD Comparisons

Without the interaction term, we can make direct comparisons between levels of the intervention, and between levels of the fat_est variable. This is probably best done here in a Tukey HSD comparison.

```
TukeyHSD(aov(cort_diff ~ interv + fat_est, data = cortisol))
```

```
Tukey multiple comparisons of means
 95% family-wise confidence level
```

```
Fit: aov(formula = cort_diff ~ interv + fat_est, data = cortisol)
```

```
$interv
      diff      lwr      upr    p adj
Low-High -0.09074746 -0.5222655  0.34077063 0.8724916
UC-High  -0.51642619 -0.9500745 -0.08277793 0.0150150
UC-Low   -0.42567873 -0.8613670  0.01000948 0.0570728
```

```
$fat_est
      diff      lwr      upr    p adj
unhealthy-healthy -0.3582443 -0.6662455 -0.05024305 0.0229266
```

What conclusions can we draw, at a 5% significance level?

Bibliography

- Barnett, P. A., Roman-Golstein, S., Ramsey, F., et al. (1995). Differential permeability and quantitative mr imaging of a human lung carcinoma brain xenograft in the nude rat. *American Journal of Pathology*, 146(2):436–449.
- Berkhemer, O. A., Fransen, P. S. S., Buemer, D., et al. (2015). A randomized trial of intraarterial treatment for acute ischemic stroke. *New England Journal of Medicine*, 372:11–20.
- Kim, H.-Y. (2014). Statistical notes for clinical researchers: Two-way analysis of variance (anova) - exploring possible interaction between factors. *Restorative Dentistry & Endodontics*, 39(2):143–147.
- Ramsey, F. L. and Schafer, D. W. (2002). *The Statistical Sleuth: A Course in Methods of Data Analysis*. Duxbury, Pacific Grove, CA, second edition.
- Roy, D., Talajic, M., Nattel, S., et al. (2008). Rhythm control versus rate control for atrial fibrillation and heart failure. *New England Journal of Medicine*, 358:2667–2677.
- Tolaney, S. M., Barry, W. T., Chau, T. D., et al. (2015). Adjuvant paclitaxel and trastuzumab for node-negative, her2-positive breast cancer. *New England Journal of Medicine*, 372:134–141.