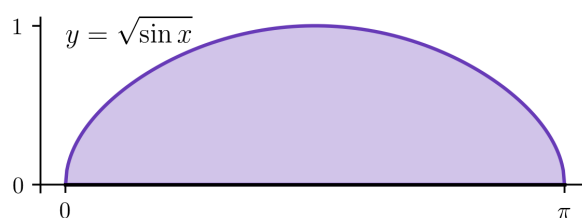


# The Disk and Washer Methods

We practice setting up calculations related to the disk and washer methods

**Example 1.** Suppose the region below the graph  $y = \sqrt{\sin x}$  and above the  $x$ -axis between  $x = 0$  and  $x = \pi$  is revolved around the  $x$ -axis. Compute the volume of the resulting solid.



- Because the axis of rotation lies perfectly along the boundary of the region, the (disk ✓/ washer) method can be used.
- The radius  $R$  is the length of a (horizontal/ vertical ✓) extending from the axis to the graph  $y = \sqrt{\sin x}$ .
- Thus we know that the radius  $R$  must equal

**Multiple Choice:**

- (a)  $R(x) = \sqrt{\sin x} - 0 = \sqrt{\sin x}$  ✓
- (b)  $R(y) = \arcsin y^2 - 0 = \arcsin y^2$

- We conclude that

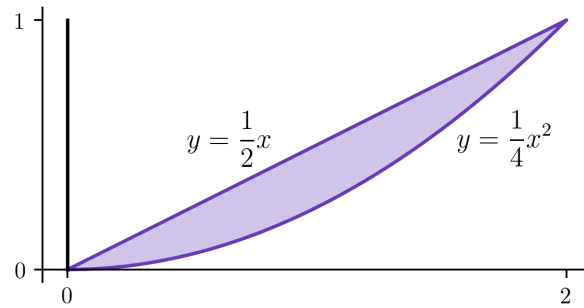
$$V = \int_0^\pi \pi \left( \sqrt{\sin x} \right)^2 dx = 2\pi.$$

**Example 2.** Suppose the region between the graphs  $y = x/2$  and  $y = x^2/4$  is revolved around the axis  $x = 0$ . Compute the volume of the resulting solid.

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Learning outcomes:  
Author(s): Philip T. Gressman

The Disk and Washer Methods



- Because the axis of rotation does not lie along the boundary of the region, the (disk/ washer ✓) method can be used.
- In this case, radius will equal the length of a (horizontal ✓/ vertical) extending from the axis to the graphs  $y = x/2$  and  $y = x^2/4$ .
- **Multiple Choice:**
  - (a)  $R_{\text{outer}}(x) = x/2$  and  $r_{\text{inner}}(x) = x^2/4$
  - (b)  $R_{\text{outer}}(y) = 2\sqrt{y}$  and  $r_{\text{inner}}(y) = 2y$  ✓
- We conclude that

$$V = \int_0^1 \pi \left[ \left( 2\sqrt{y} \right)^2 - \left( 2y \right)^2 \right] dy = \frac{2\pi}{3}.$$