



The  
University  
Of  
Sheffield.

# Accelerating Road Network Simulations using GPUs

---

Peter Heywood

The University of Sheffield

# Table of contents

1. Road Network Simulation
2. GPU Accelerated *Microscopic* Simulation
3. GPU Accelerated *Macroscopic* Simulation
4. Summary

# Road Network Simulation

---

# Road Network Simulation

- Global transport demand is increasing [4]
- Many constraints on transport networks
- Simulation can improve use of limited resources
  - Planning
  - Management



CC BY 2.0 Highways England  
<https://www.flickr.com/photos/highwaysagency/9950013283/>

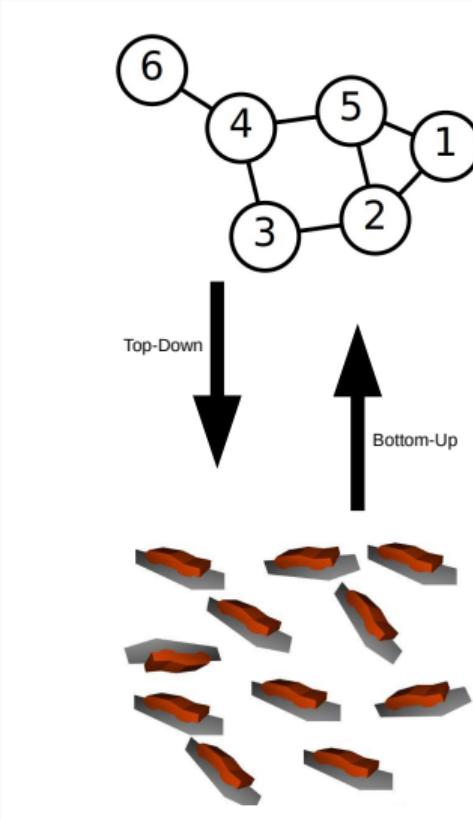
# Road Network Simulation

- Simulations are becoming more computationally expensive
  - **Larger** - City-scale, National-scale
  - **More Complex** - CAVs, Smart Motorways, ...
  - **More Permutations** - weather, demand, ...
- **Better than real-time** simulations required for active management
- Performance is limiting the use of simulation [1]
- **Need higher performance simulators!**



# Road Network Simulation Categories

- **Macroscopic** Simulation
  - Top-Down
  - High level, flow simulation
- **Mesoscopic** Simulation
  - Mid-level
  - Fine-grained macrosimulation or Platoons/groups
- **Microscopic** Simulation
  - Bottom-Up
  - Low level, individual vehicles



# Graphics Processing Units (GPUs)

- Massively parallel, many-core co-processors
- Data-parallel algorithms and data structure
  - Possibly very different to CPU
- Suitable for all scales of road network simulation
  - Different degrees of parallelism expressed
  - Different levels of performance improvement



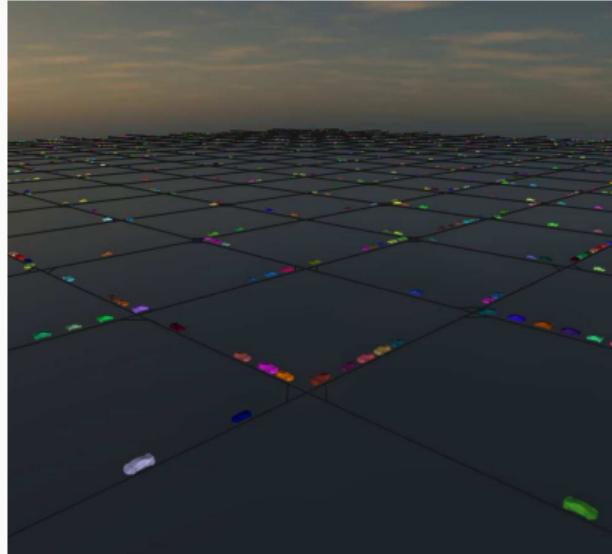
NVIDIA DGX-2

## GPU Accelerated *Microscopic* Simulation

---

# Microscopic Simulation

- Bottom-up Simulations
- Individual vehicles
- Agent Based Modelling (ABM) [6]
  - Intuitive descriptions of behaviour and interactions
    - with other vehicles
    - with the environment
  - Complex behaviour emerges from simple rules
- **Very computationally expensive**
- Large volume of data required and generated

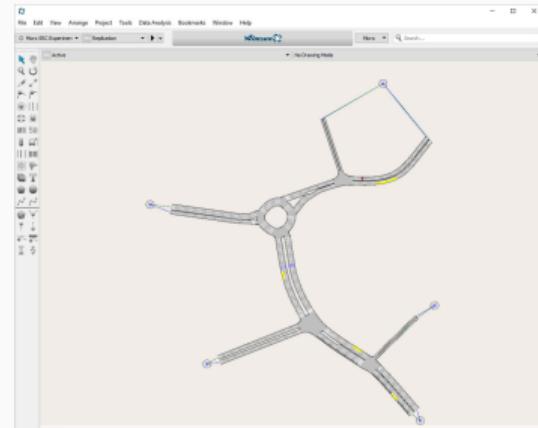


FLAME GPU Road Network Microscopic  
Simulation

# Our Aims

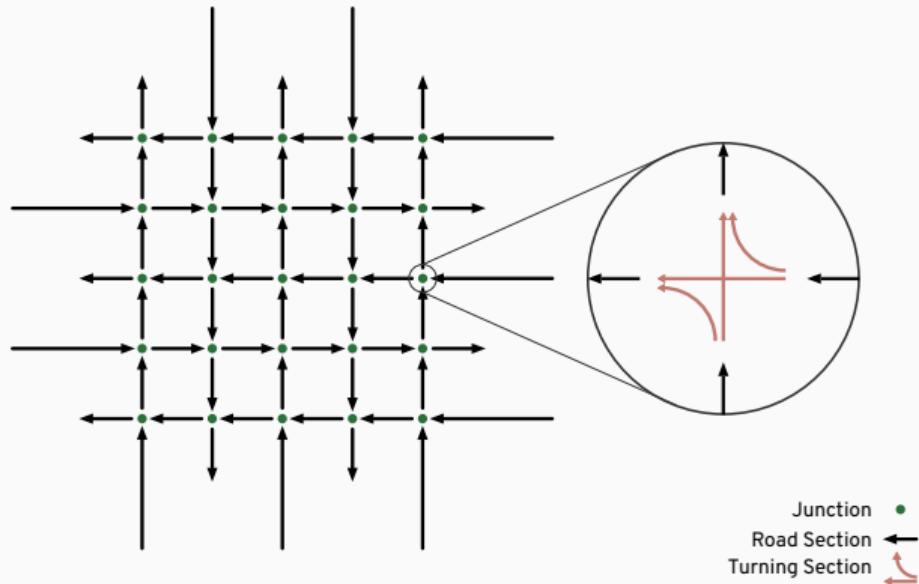
## Aims

- Demonstrate GPUs are suitable and performant
  - Implement a subset of models from commercial tool
  - Cross-validate GPU implementation
  - Benchmark using a scalable model
- **Aimsun [2]**
  - Commercial, multi-core CPU, microscopic simulator
  - Used globally within the transport industry
  - Can simulate a broad array of transport networks and infrastructure



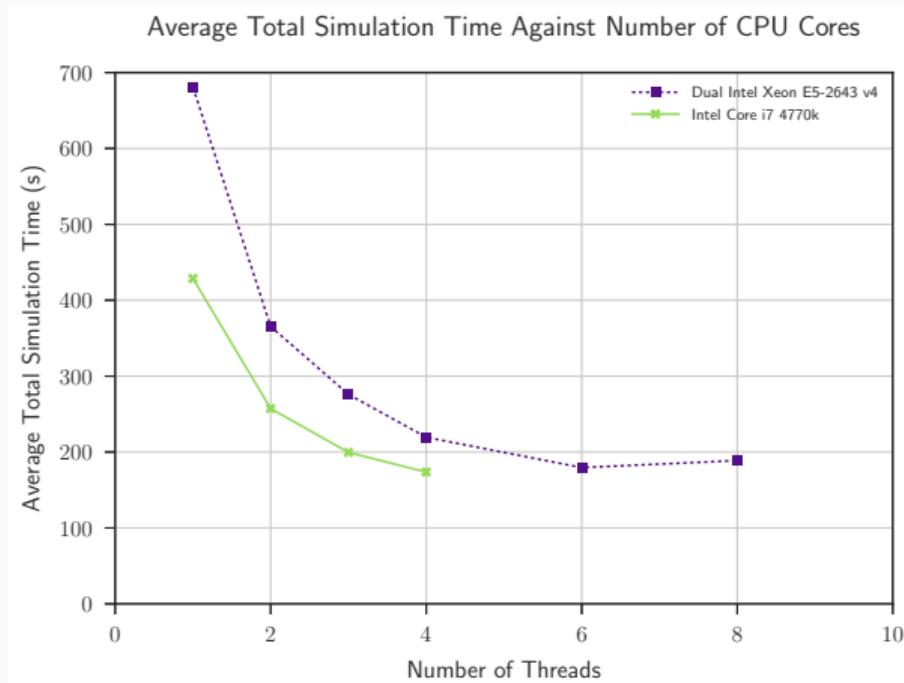
# Procedurally Generated Network

- Manhattan-style grid network
- Single lane, one-way roads
- Stop-signs at junctions
- Entrances and Exits at the edge of the simulated grid



# Aimsun 8.1 CPU Performance

- Single size of grid network
- 3 repetitions
- **Diminishing Returns** from additional cores



## Models and Functionality

- Gipps' Car Following Model [9, 14]
- Aimsun Gap Acceptance Model [2]
- Turning Probability based Routing [13]
- Simulated Vehicle Detectors [13]
- Constant Vehicle Arrival [13]

### Gipps' Car Following Model

$$v_{free}(n, t + \tau) \leq v(n, t) + 2.5a(n)\tau(1 - v(n, t)/V(n))(0.025 + v(n, t)/V_t(n))^{\frac{1}{2}}$$

$$v_{safe}(n, t + \tau) \leq d(n)\tau + \sqrt{d(n)^2\tau^2 - d(n)(2[x(n-1, t) - s(n-1) - x(n, t)] - v(n, t)\tau - \frac{v(n-1, t)^2}{\hat{d}(n)})}$$

$$v(n, t + \tau) = \min \left\{ v_{free}(n, t + \tau), v_{safe}(n, t + \tau) \right\}$$

# FLAME GPU

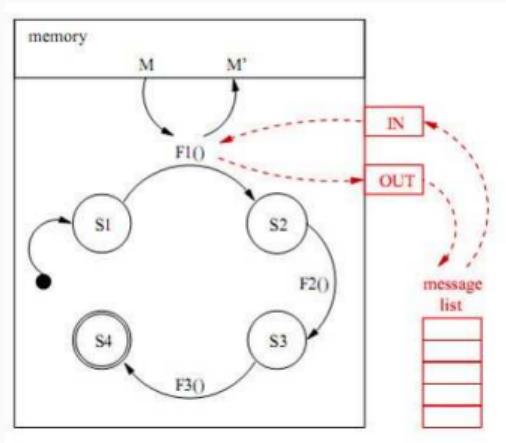
- Flexible Large-scale Agent Modelling Environment for the GPU [11]
- Template-based simulation environment for high performance simulation
- Agents represented as X-Machines
  - with *message lists* for communication
- Abstracts the CUDA programming model away from the user
  - I.e. A modeller writes an XML file and simple C/C++ code



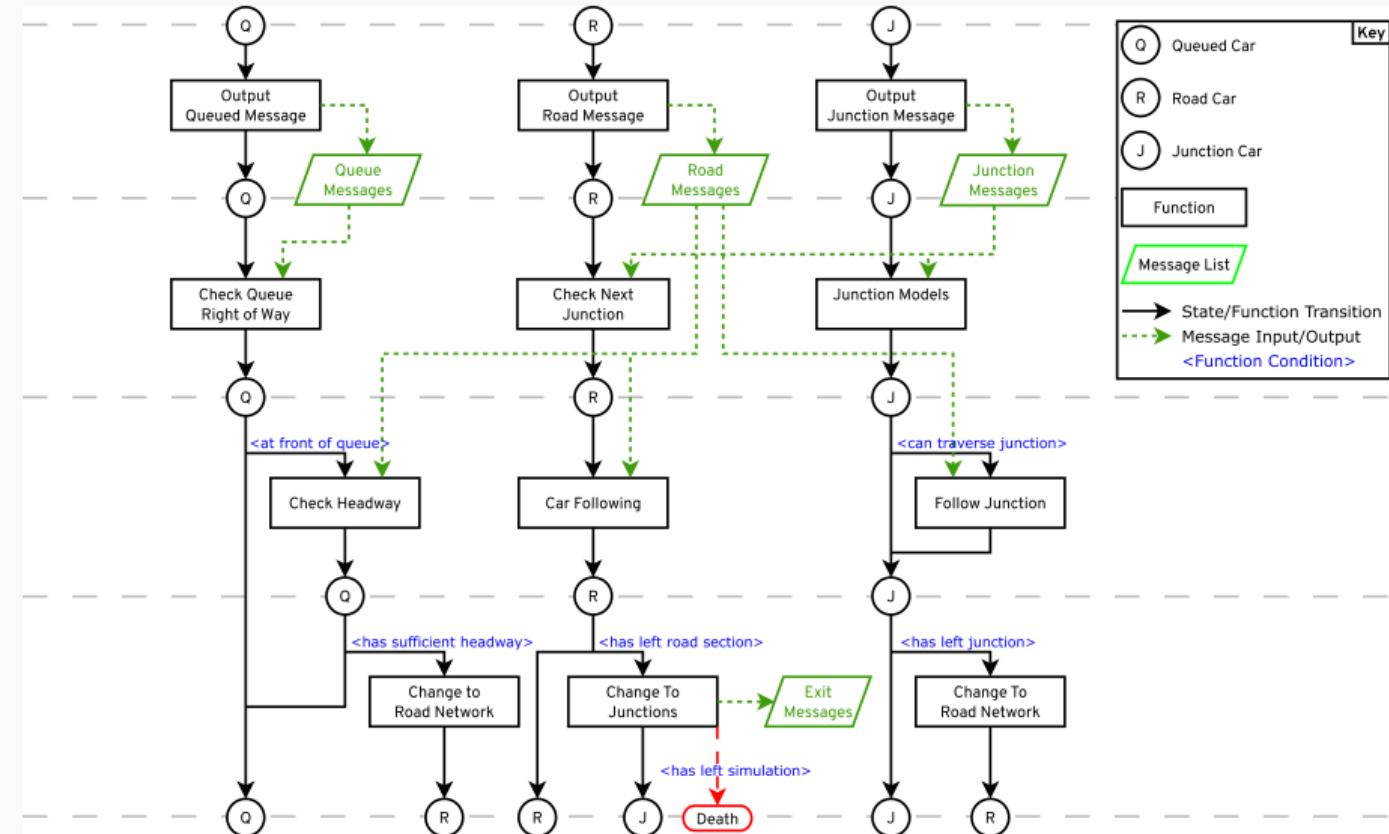
[flamegpu.com](http://flamegpu.com)

[github.com/flamegpu](https://github.com/flamegpu)

- State-based representation minimises divergence
- SoA per state list - improves data access pattern
- Message lists avoid race-conditions
  - Natural synchronisation barriers
- Reduce global reads via shared memory



# FLAME GPU Road Network Simulation State Diagram

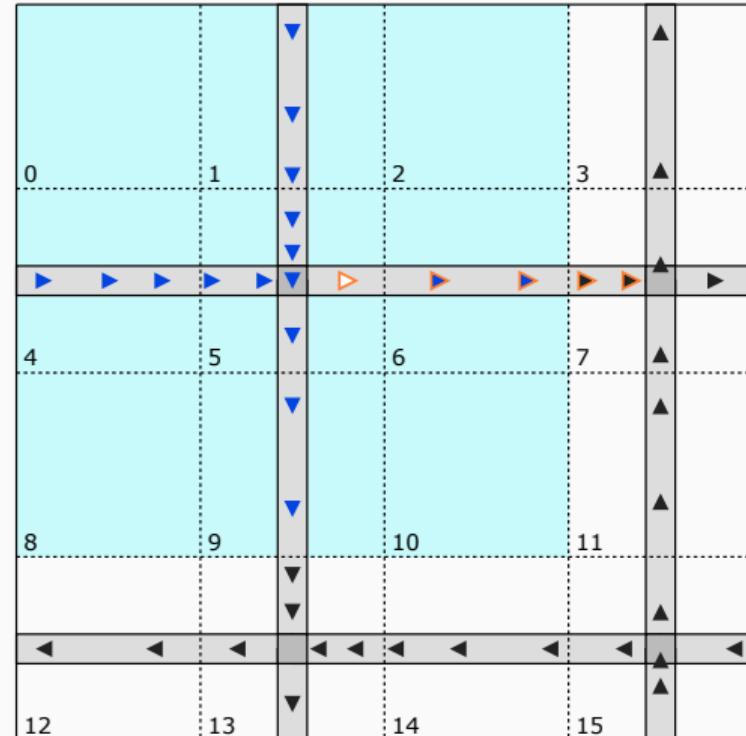


- Message lists enable high performance memory access pattern
  - avoids issues with concurrent access to agent memory
- Typically the performance-limiting factor in large-scale simulations
- Specialisation for typical communication patterns [12]
  - All-to-All
  - Discrete Partitioned Messaging (2D Cellular Automata)
  - Spatially Partitioned Messaging (2D & 3D Continuous Agents)
- Non-optimal for road network models

# On-Graph Communication

- Communication between vehicles is based on the transport network
- I.e. Gipps' car following model only involves the lead vehicle
- Associate messages to the graph data structure
- Reduce the number of messages to be iterated
  - by accessing messages from the relevant edge(s) or vertices

Communication	Messages
All-to-All	42
Spatial	18
Graph	5



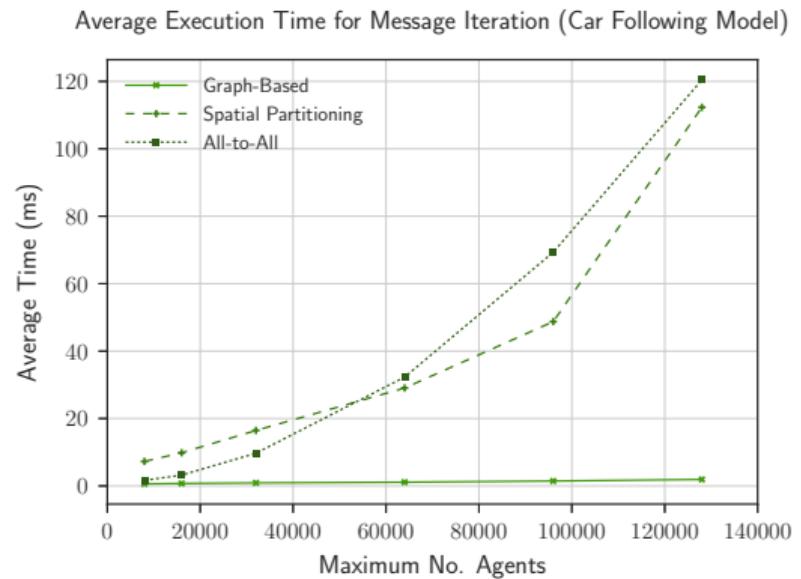
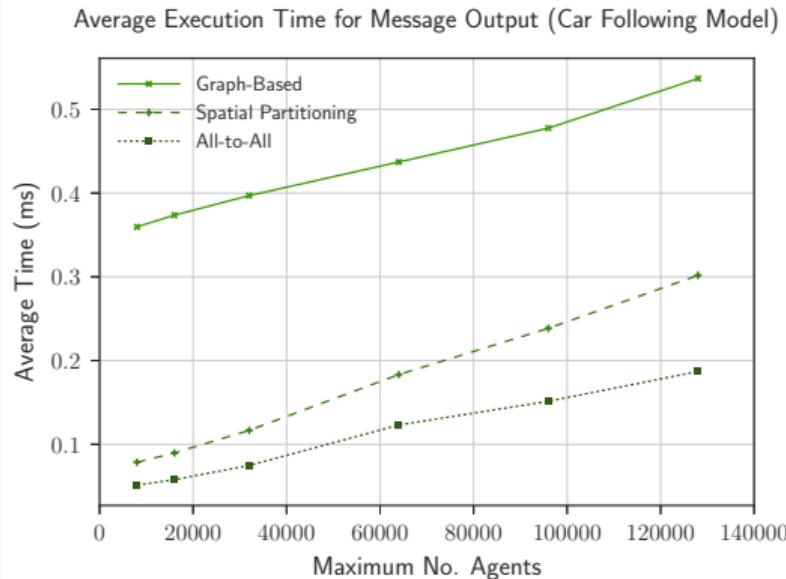
Example highlighting FLAME GPU Communication strategies

## On-Graph Communication

- Compressed Sparse Row (CSR) representation of graph
- Messages contain edge or vertex index
- Sort message list based on edge (or vertex) index
  - *Counting Sort*
  - Shared-memory atomics
  - Builds data structure to access messages whilst sorting
- Can access a single edge, or use the CSR to explore the message-list
- Available in the next release of FLAME GPU (1.5)

# On-Graph Communication Performance

- Measured performance of message list output and input for car-following
- Higher output cost, **much** cheaper message input cost.



# Performance Benchmarking

1. Scale population and environment
2. Scale population for fixed size environment
  - 3 repetitions
  - 1 hour of simulated time
  - Multiple hardware configurations

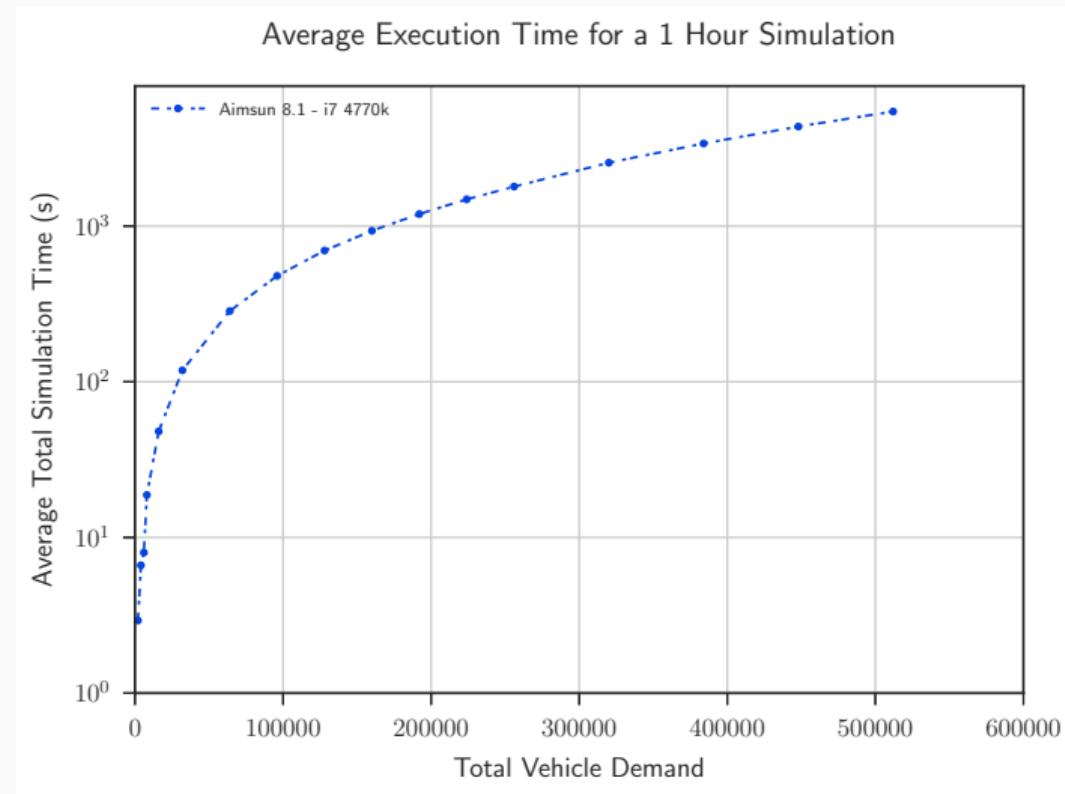
## Workstation

- Windows and Linux
- i7 4770k (4 Cores)
- GTX 1080
- Titan X (Pascal)
- Titan V

## Nvidia DGX-1

- Linux
- 2x Xeon E5 2698 v4 (20 cores each)
- 8x Tesla P100

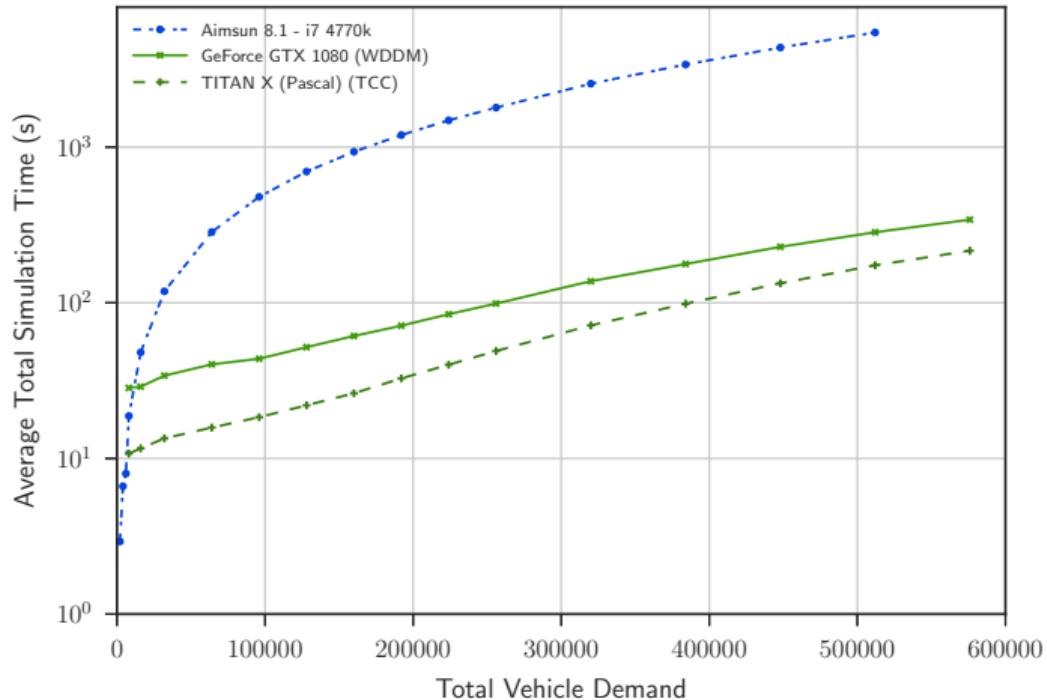
# Scale Population and Environment



- 0.5 Million Vehicles:
- CPU - Windows
  - 5447s

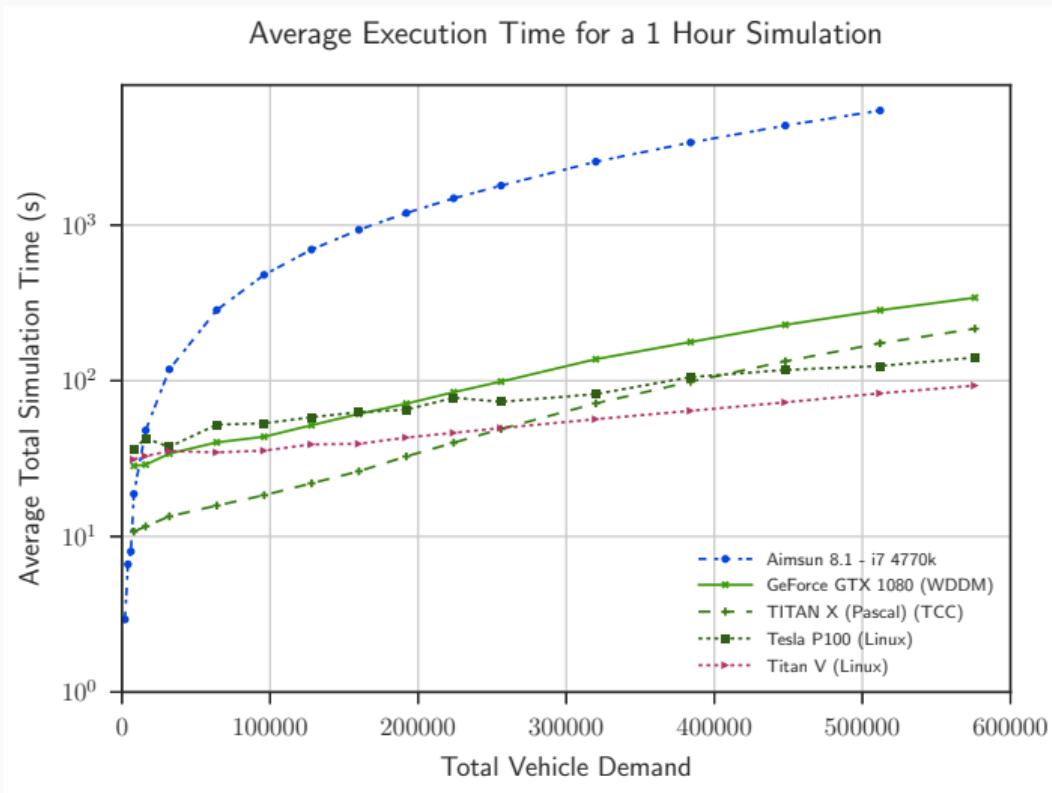
# Scale Population and Environment

Average Execution Time for a 1 Hour Simulation



- 0.5 Million Vehicles:
  - CPU - Windows
    - 5447s
  - GPU - Windows
    - 174.2s
    - 31x speed up  
(Titan X (Pascal))

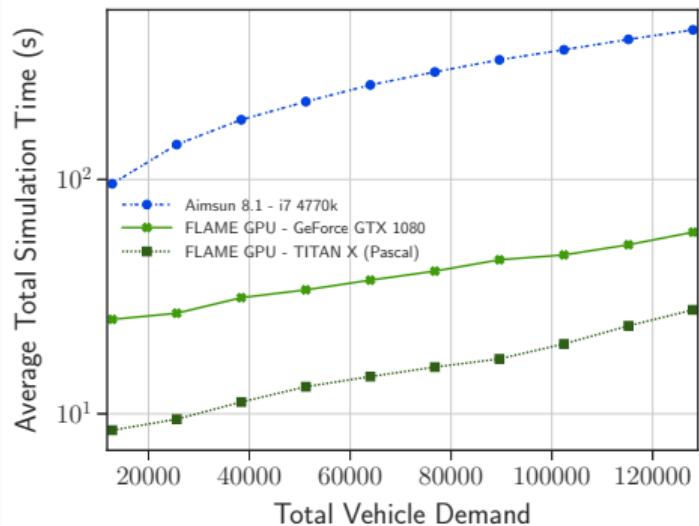
# Scale Population and Environment



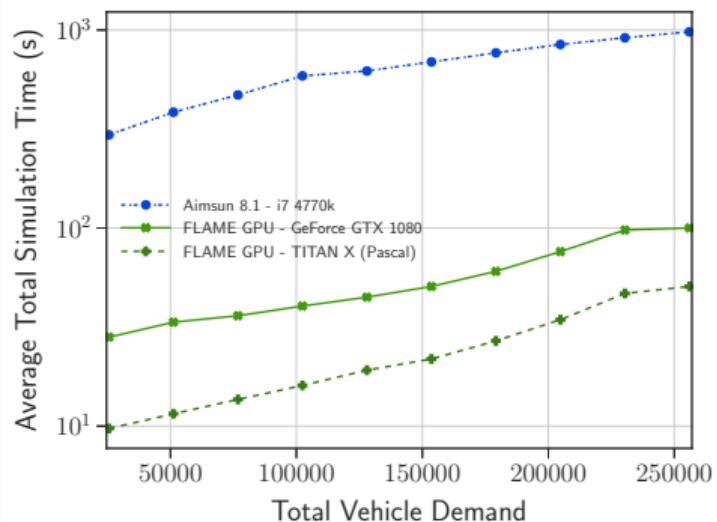
- 0.5 Million Vehicles:
  - CPU - Windows
    - 5447s
  - GPU - Windows
    - 174.2s
    - 31x speed up  
(Titan X (Pascal))
  - GPU - Linux
    - 82.04s
    - **66x speed up**  
(Titan V)

# Scale Population for Fixed Environment

Average Simulation Time as Flow is Increased Grid Size 64



Average Simulation Time as Flow is Increased Grid Size 128



## GPU Accelerated *Macroscopic* Simulation

---

# Macroscopic Simulation

- Top-Down Simulations
- Models networks as flows on roads (i.e pipes)
- High level of abstraction from reality
- Relatively long time steps
  - Misses short-term events
- Low data requirements
- Lower computational cost
  - But still expensive for large scale simulations

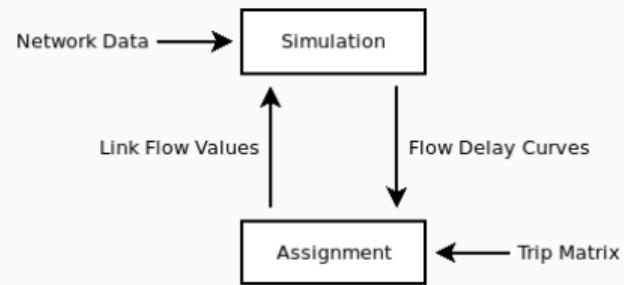


- Simulation and Assignment of Traffic to Urban Road Networks [16]
- Commercial, multi-core CPU software
- Originally Developed in the 1970s
- Used by companies and governments for (mostly) planning
  - Highways England, Transport for London (TfL), ...
- Fortran 77 with OpenMP



# SATURN Simulation-Assignment Loop

- Iterative equilibrium-based algorithm of Assignment and Simulation
  - Wardrop's Equilibrium [17]
- **Assignment Phase**
  - Network + Demand Matrix -> Flow-per-edge
  - Vehicles types are considered independently (*User Classes*)
    - Cars, Taxis, Buses, HGVs, ...
  - Trip Matrix contains many *Origins* and *Destinations*
    - Known as *Zones* or *Centroids*



Assignment-Simulation Loop in SATURN [16]

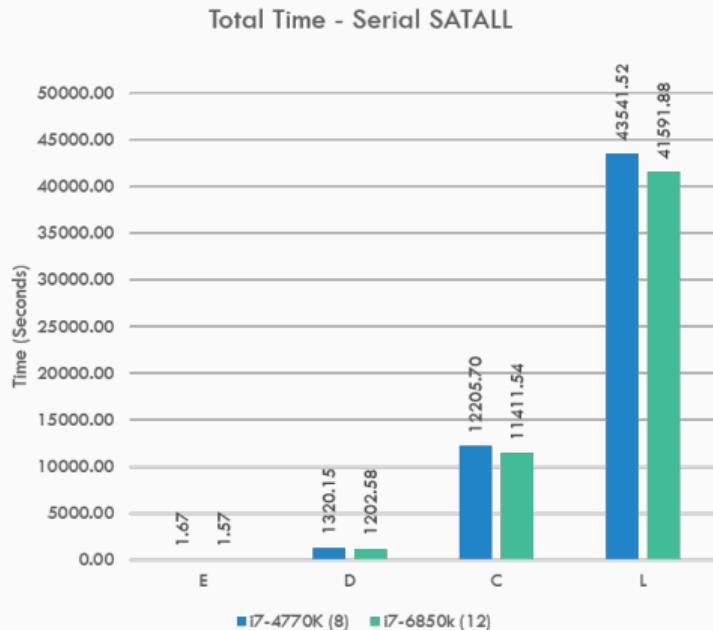
# SATURN Models

- Road networks are very sparse graphs
  - Preprocessing step to create a denser representation
  - Referred to as “*Spider Network*”
    - Contraction Hierarchies
- These are **very sparse** graphs, even when preprocessed
- Range of scales from *tiny* to *very very large*

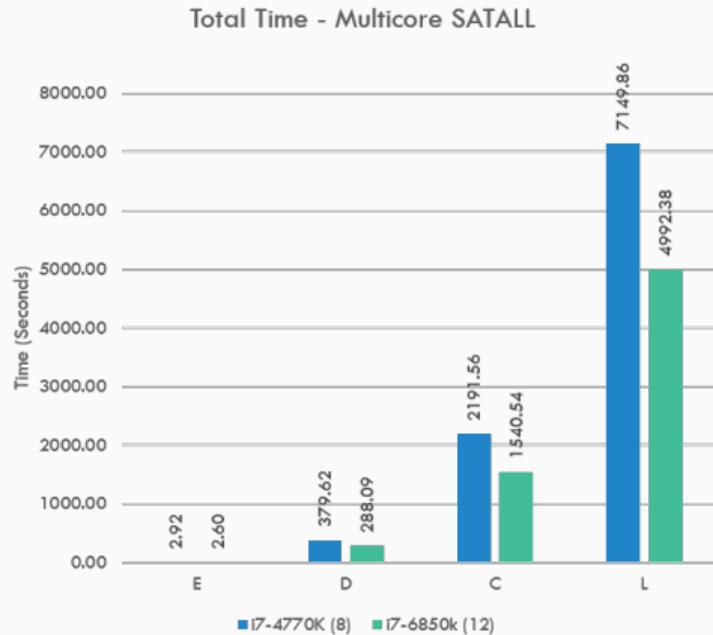
Model	Size	User Classes	Centroids	Vertices	Edges
E	Town	2	12	17	74
D	Small City	13	547	2700	25385
C	Large City	5	2548	15179	132600
L	Metropolitan	5	5194	18427	192711

# CPU Performance - Serial and OpenMP

## Single Core CPU

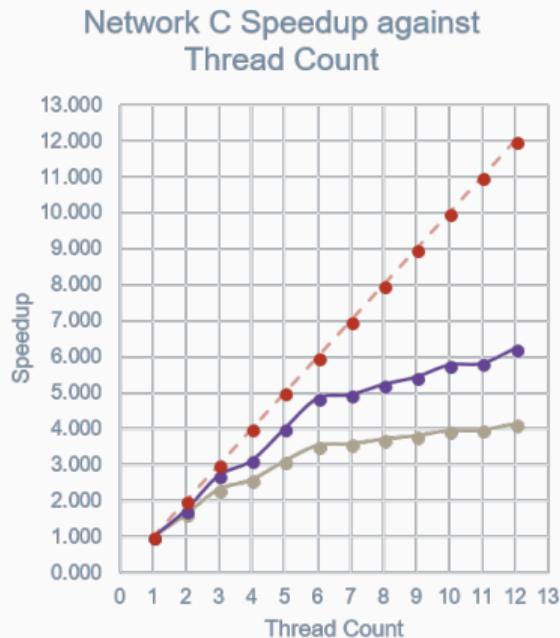


## Multi-Core CPU

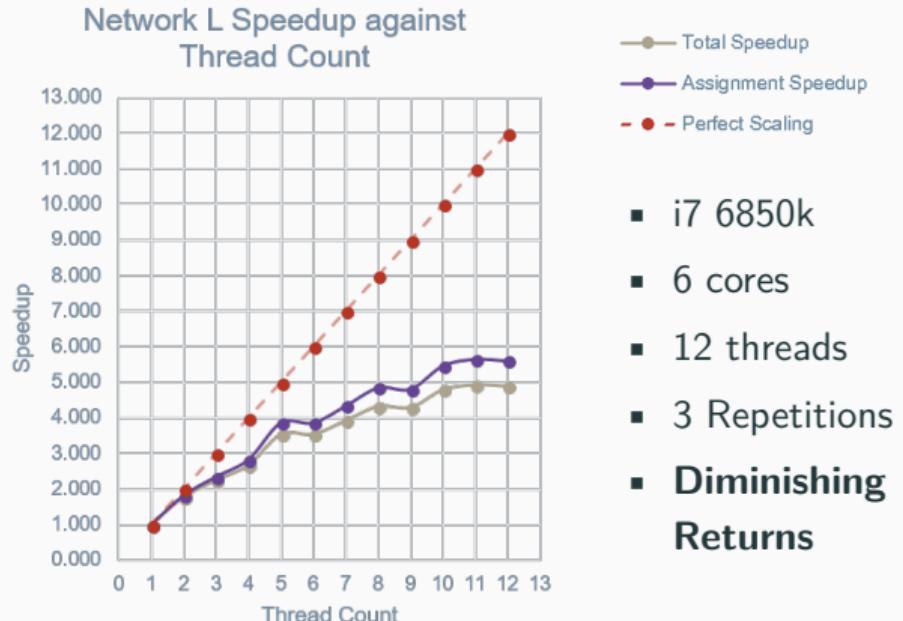


# CPU OpenMP Scaling

## Single Core CPU

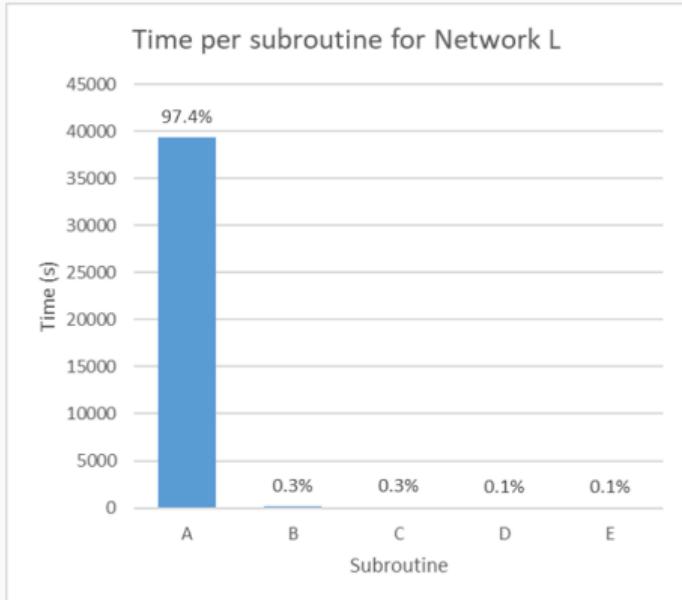


## Multi-Core CPU



# SATURN Profiling - Serial

- Serial version of SATALL
- Largest available model (L)
  - London + surrounding area
- > 11 Hour Runtime
- 97.4% in a single subroutine
- Computes shortest paths for an origin centroid
  - Accumulates flow for each trip from the origin
- Most time spent calculating paths



- **Single Source Shortest Path (SSSP)**
  - Uses the D'Esopo-Pape algorithm [10]
    - An efficient, *highly-serial* algorithm
    - Algorithmic decision in the 1970s, due to benchmarking at the time [15]
    - A modern implementation of Dijkstra's algorithm [5, 8] is up to 50% faster
- **Flow Accumulation**
  - Trace all routes from an origin to destination zones
  - Update per-edge flow value at each step
  - Double precision to avoid numerical precision loss
- Calculated per-origin centroid, per-userclass, at each iteration

# GPU Shortest Path Algorithm

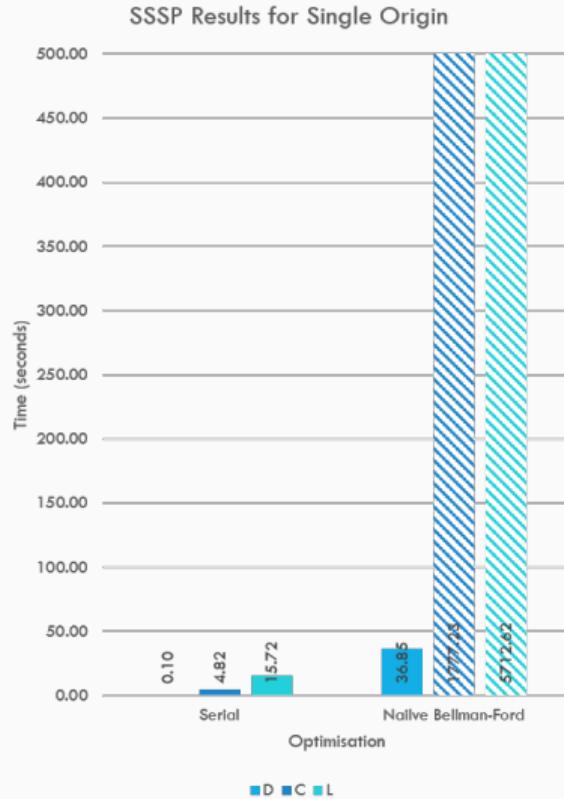
- Need data-parallel algorithms for the GPU
  - Sacrifice efficiency to enable parallelism
  - More work, but in parallel

## Bellman-Ford Algorithm [3, 7]

- For up to  $|v| - 1$  iterations
  - For each Edge in the network
  - If the edge is a cheaper route to the destination node, update the route.
- Significant changes required to provide a performance improvement for road networks vs Dijkstra or D'Esopo-Pape

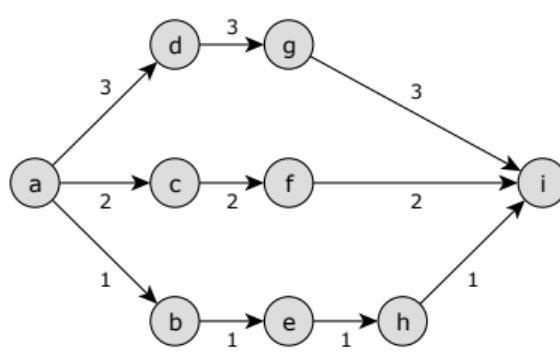
# Initial GPU Implementation

- Naive version of the Bellman-Ford Algorithm
- **Much, Much, Much, Much Slower...**
- 364x slower
- Inefficient use of compute
- Inefficient data transfer
- **Lots of unnecessary work**



# Multiple Source Bellman-Ford

- *Frontier-based* implementation of Bellman-Ford
- Solve for **multiple origins** concurrently
- Threads co-operate to balance work-load
- Solve for **multiple independent user-classes** concurrently

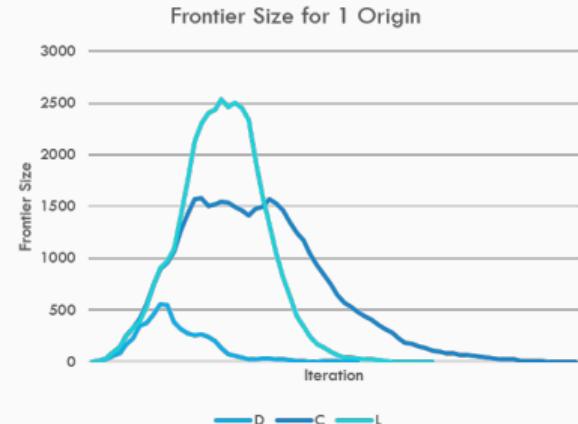


Iteration	Frontier Vertices
0	a
1	b c d
2	e f g
3	h i
4	i
5	

# Origin-Vertex Frontier

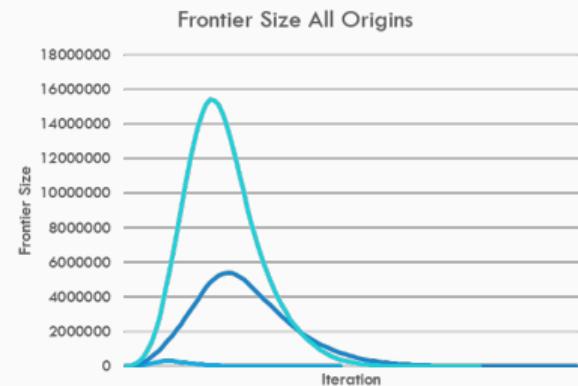
## Vertex Frontier

- Tracks which vertices could cause an update
  - Increases efficiency, but decreases parallelism
- Not enough work
  - Latency bound, Low number of threads (< 2500 for network L)



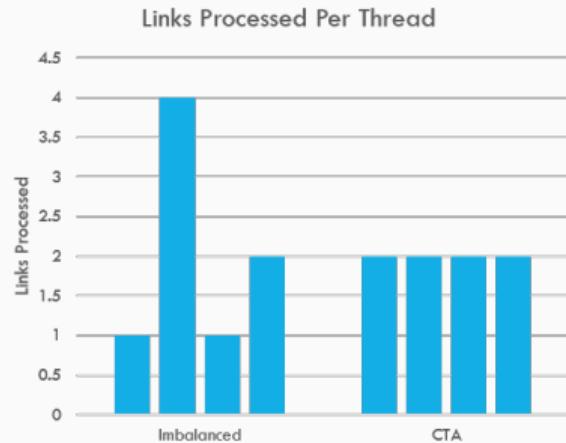
## Origin-Vertex Frontier

- Multiple origins concurrently
- Track which origin each frontier vertex belongs to
  - Increases parallelism
  - Significantly increases memory requirements



# Block-level Load Balancing

- Number of edges per vertex varies
  - Co-operative Thread Array (CTA)
  - Threads in a block collectively work on the same portion of the origin-vertex frontier
  - Balances work load across threads (and warps) in the block
  - Improved L2 bandwidth 4.8x (148GB/s to 716GB/s)
  - CUDA 9.0 introduces Cooperative Groups API

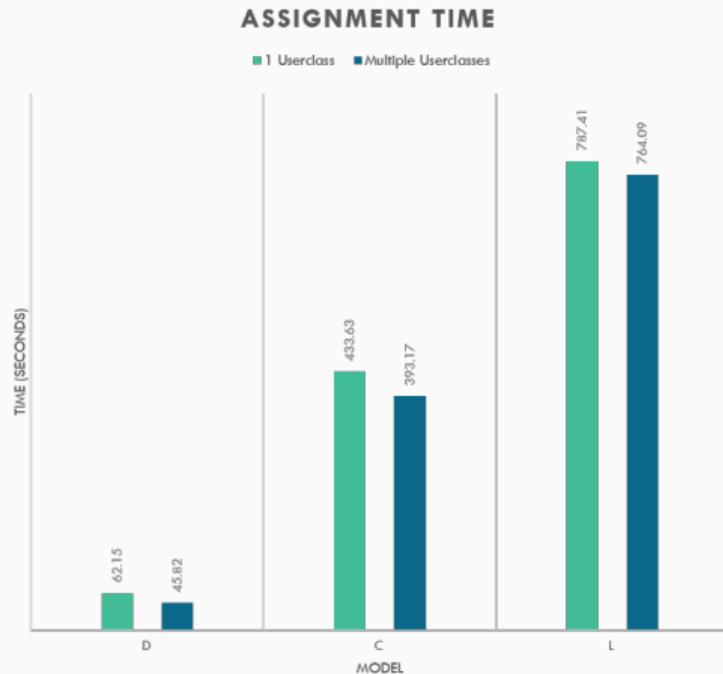


## Flow Accumulation

- For each trip from origin to destination:
  - Trace the shortest path, atomically updating per-link flow
- Good performance on Pascal and Volta
- **But** `atomicAdd(double)` not available on Maxwell and older
  - `atomicCAS` implementation very slow due to high *atomic contention*
  - Complex workaround:
    - Device-wide sort
    - Block-wide key-value reduction
    - Single global `atomicAdd` per edge in the block
  - Faster the naive algorithm on Maxwell, but slower than Pascal

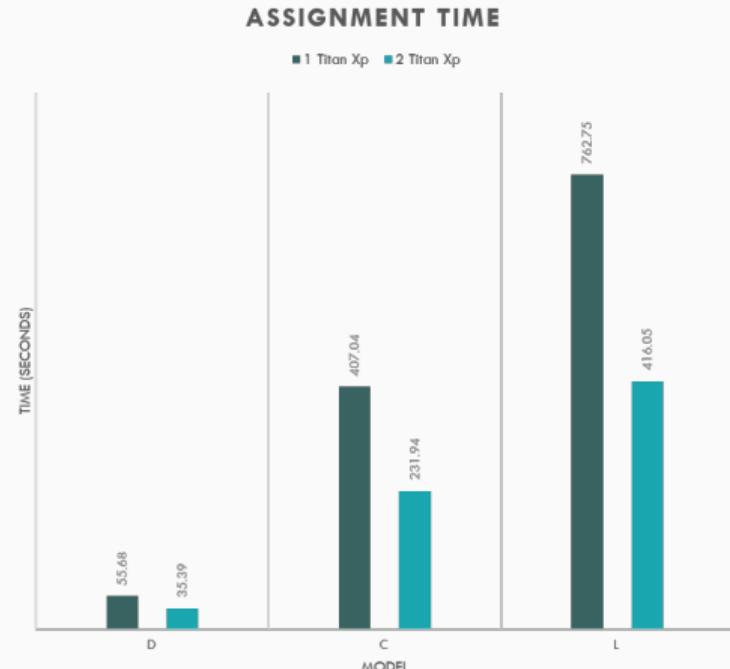
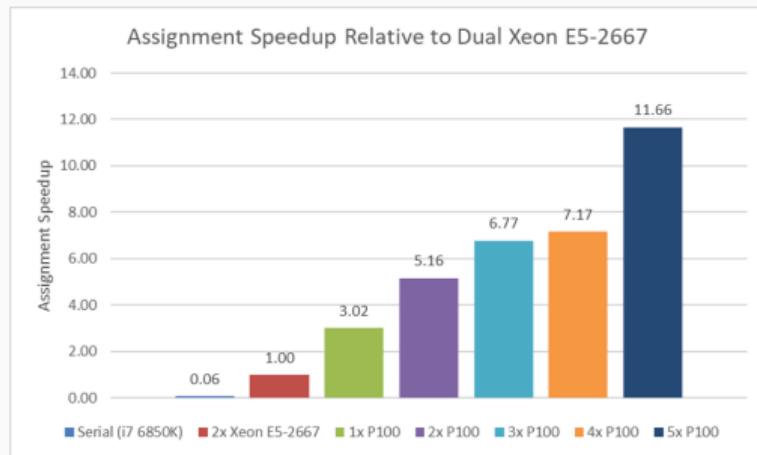
# Multiple User Classes

- User classes can be processed independently
- CUDA stream per user-class
- Increases parallelism
- Not a significant speed up
  - Serialisation when device oversubscribed
- *Enables the use of Multiple GPUs*

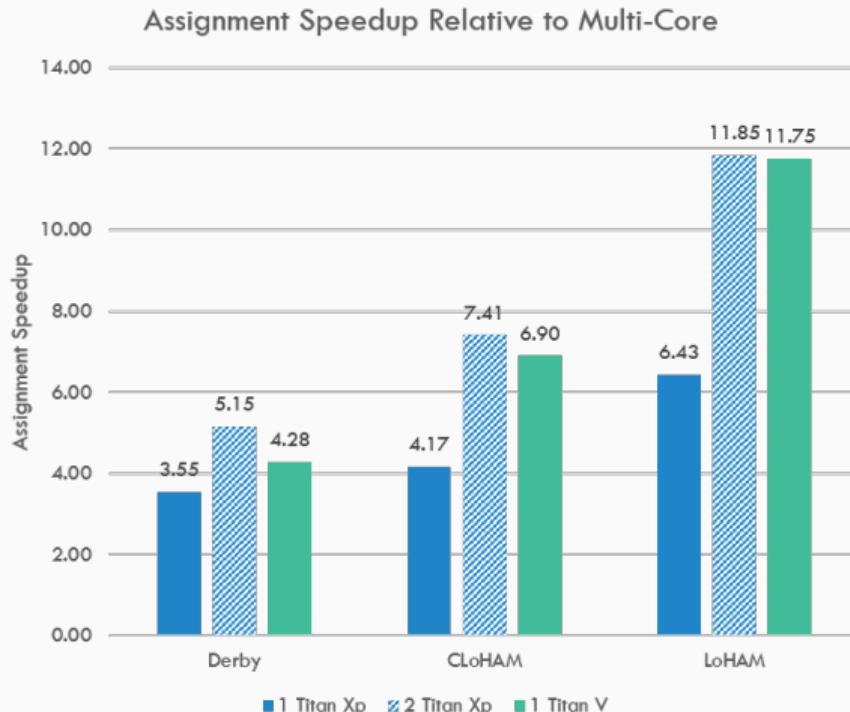


# Multiple GPUs

- Distribute user classes between GPUs
- Imbalanced workload between devices
  - Only assign whole user classes



# Volta GPU Architecture



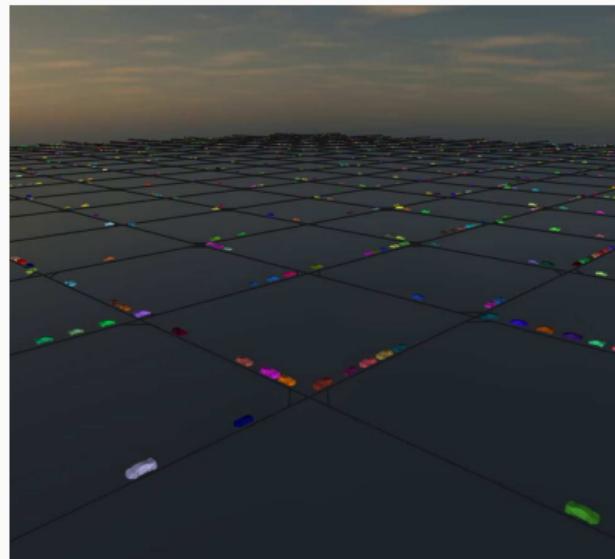
- Up to 80% performance improvement vs 1 Titan Xp
- Speed up relative to 6 core i7
- No source code changes
  - Other than updating libraries (CUB) and CUDA version.

## Summary

---

# Conclusion

- Microscopic Simulation
  - Up to 66x speed up using a Titan V
  - Real-time-ratio of 39x for up to 576000 vehicles
- Macroscopic Assignment
  - Up to 11.7x speed up on 1 Titan V vs 6 core i7
  - Up to 11.8x speed up on 5 P100 vs 2 CPUs
- More simulations in less time
- Large simulations feasible
- Better-than-real-time microsimulation of 0.5 million vehicles is achievable



# Thank You

## Supported By

- DfT Transport Technology Research Innovation Grant (T-TRIG July 2016)
- EPSRC fellowship "Accelerating Scientific Discovery with Accelerated Computing" (EP/N018869/1)
- Support from Atkins, STFC, TSC & Aimsun

## Contact

- p.heywood@sheffield.ac.uk
- @ptheywood
- ptheywood.uk
- rse.shef.ac.uk

## More Information

"Data-parallel agent-based microscopic road network simulation using graphics processing units"

<https://doi.org/10.1016/j.simp.2017.11.002>

## References i

- [1] C. Antoniou, J. Barcelò, M. Brackstone, H. Celikoglu, B. Ciuffo, V. Punzo, P. Sykes, T. Toledo, P. Vortisch, and P. Wagner.  
Traffic simulation: Case for guidelines.  
2014.
- [2] J. Barceló and J. Casas.  
Dynamic network simulation with aimsun.  
In *Simulation approaches in transportation analysis*, pages 57–98. Springer, 2005.
- [3] R. Bellman.  
On a routing problem.  
*Quarterly of applied mathematics*, pages 87–90, 1958.
- [4] Department for Transport.  
Road traffic forecasts 2015.  
[https://www.gov.uk/government/uploads/system/uploads/attachment\\_data/file/260700/road-transport-forecasts-2013-extended-version.pdf](https://www.gov.uk/government/uploads/system/uploads/attachment_data/file/260700/road-transport-forecasts-2013-extended-version.pdf), Mar. 2015.
- [5] E. W. Dijkstra.  
A note on two problems in connexion with graphs.  
*Numerische mathematik*, 1(1):269–271, 1959.

## References ii

- [6] G. Eliasson.  
Modeling the experimentally organized economy, 1991.
- [7] L. R. Ford Jr.  
Network flow theory.  
Technical report, DTIC Document, 1956.
- [8] M. L. Fredman and R. E. Tarjan.  
Fibonacci heaps and their uses in improved network optimization algorithms.  
*Journal of the ACM (JACM)*, 34(3):596–615, 1987.
- [9] P. Gipps.  
A behavioural car-following model for computer simulation.  
*Transportation Research Part B: Methodological*, 15(2):105–111, 1981.
- [10] U. Pape.  
Implementation and efficiency of Moore-algorithms for the shortest route problem.  
*Mathematical Programming*, 7(1):212–222, 1974.
- [11] P. Richmond.  
Flame gpu technical report and user guide (cs-11-03).  
Technical report, Technical report, Department of Computer Science, University of Sheffield, 2011.

## References iii

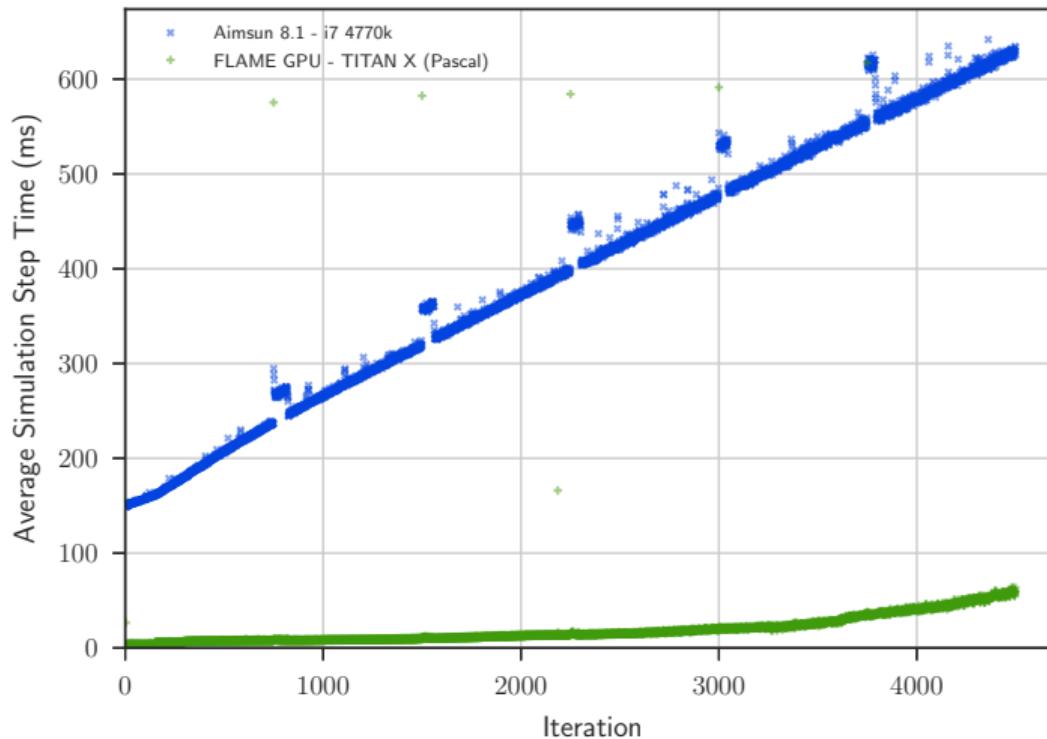
- [12] P. Richmond and D. Romano.  
Template-driven agent-based modeling and simulation with cuda.  
*GPU Computing Gems Emerald Edition, Applications of GPU Computing Series*, pages 313–324, 2011.
- [13] Transport Simulation Systems.  
*Aimsun 8 Dynamic Simulators Users' Manual*, 2014.
- [14] M. Treiber, A. Hennecke, and D. Helbing.  
Congested traffic states in empirical observations and microscopic simulations.  
*Physical review E*, 62(2):1805, 2000.
- [15] D. Van Vliet.  
Improved shortest path algorithms for transport networks.  
*Transportation Research*, 12(1):7–20, 1978.
- [16] D. Van Vliet.  
SATURN - a modern assignment model.  
*Traffic Engineering & Control*, 23(HS-034 256), 1982.
- [17] J. G. Wardrop.  
Some theoretical aspects of road traffic research.  
*Proceedings of the institution of civil engineers*, 1(3):325–362, 1952.

# Backup Slides

Backup Slides

# Microsimulation: Runtime per Iteration

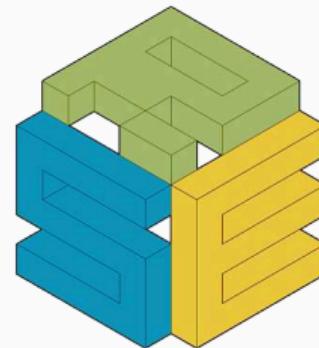
Average Simulation Step Time for a 1 Hour Simulation for a 256x256 Grid



- Population grows as time progresses
- Anomalous values correlate with detector outputs
- Every 800 iterations (10 minutes)

# About Me

- MComp Computer Science & Artificial Intelligence at Sheffield (2010-2014)
- PhD Student at Sheffield (2014 - 2018)
- Research Software Engineer (RSE) and PhD Candidate at Sheffield (2018-2021)



Research  
Software  
Engineering  
Sheffield.