

Topic 3

Day 1

1) $X \sim N(a, \sigma^2)$, $Y \sim N(0, 1)$

Can Y be expressed as a function of X ?

$$Y = \frac{X - a}{\sigma}$$

2) Can X be expressed as a function of Y ?

$$X = \sigma Y + a$$

3) Define the cumulative distribution function $F: \mathbb{R} \rightarrow [0, 1]$

$F(x) = P(X \leq x)$ - i.e. the probability that X takes a value less than or equal to x .
 Note: x can be negative and 0 (negative ∞)

4) $F'(x) = f(x)$

5) $P(a < x < b) = P(X \in (a, b)) = F(b) - F(a)$

Day 4 $X \sim R.p$, $p \in (0, 1)$

6) $f(x) = \begin{cases} 1-p, & x=0 \\ p, & x=1 \end{cases}$ $F(x) = \begin{cases} 0, & x < 0 \\ 1-p, & 0 \leq x < 1 \\ 1, & x \geq 1 \end{cases}$

