

# Trabalho de Grafos

## Parte 3

Fluxo máximo (com Ford Fulkerson)

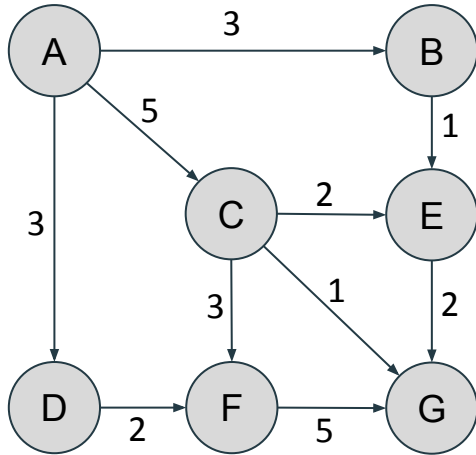
# Código

Linguagem:



Algoritmo implementado de 2 formas.

# Ford Fulkerson V1 (Duplicar grafo)



Estrutura:

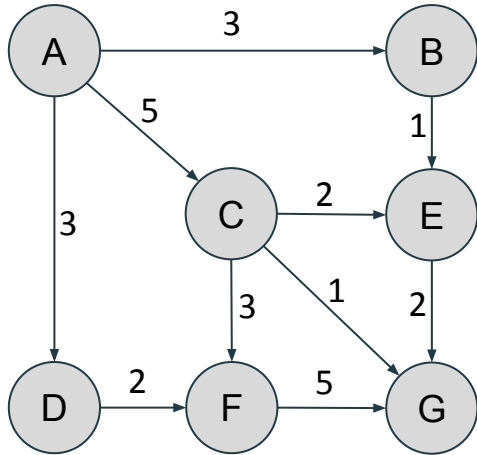
```
5  type Edge struct {  
6      origin uint32  
7      dest   uint32  
8      weight float64  
9      comp   *Edge  
10 }
```

```
lista_adjacencia [][]*Edge
```

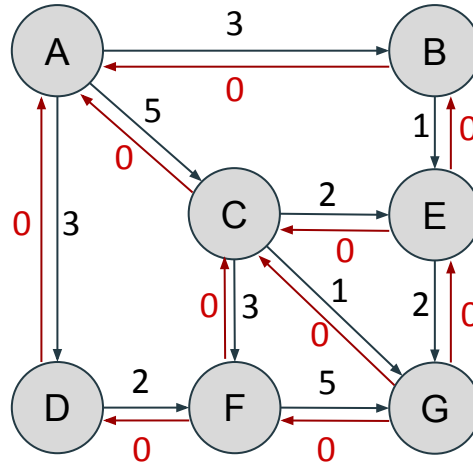
```
lista_adjacencia = [  
1: [&Edge, &Edge, ...],  
2: [&Edge, ...],  
...  
]
```

# Ford Fulkerson V1 (Duplicar grafo)

Original:



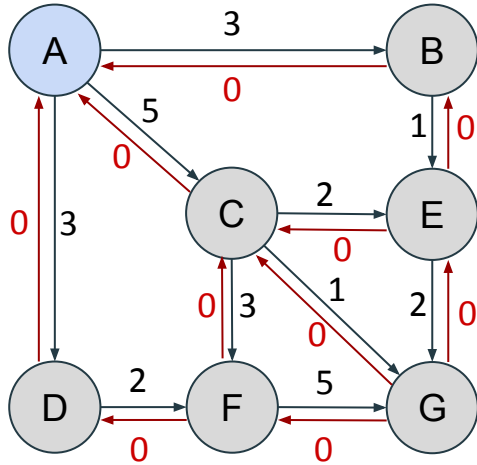
Residual:



```
correlacao_de_arestas[][2]*Edge
```

```
correlacao_de_arestas = [  
    (&original, &residual),  
    (&original, &residual),  
    ...  
]
```

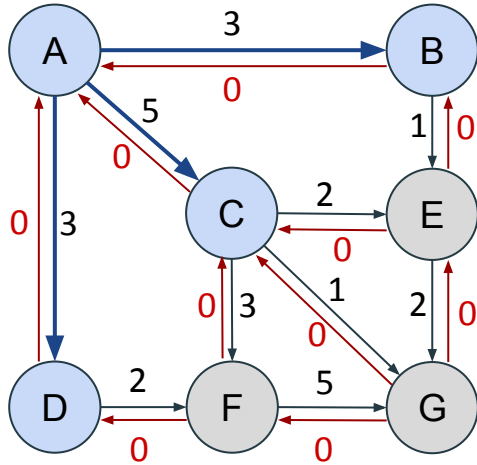
# Ford Fulkerson V1 (BFS)



```
5  type Edge struct {  
6      origin uint32  
7      dest   uint32  
8      weight float64  
9      comp   *Edge  
10 }
```

pais:	A	B	C	D	E	F	G
aresta	[	x,	nil,	nil,	nil,	nil,	nil]

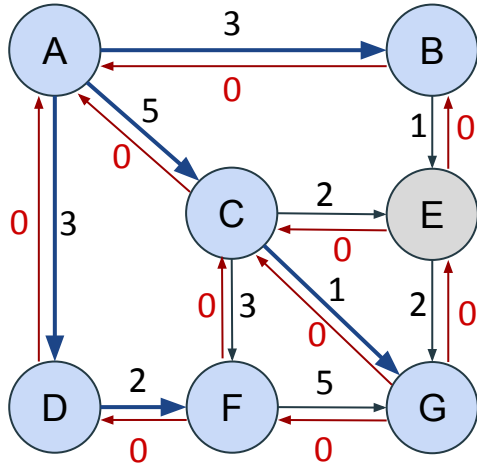
# Ford Fulkerson V1 (BFS)



```
5  type Edge struct {  
6      origin uint32  
7      dest   uint32  
8      weight float64  
9      comp   *Edge  
10 }
```

pais:	A	B	C	D	E	F	G	
aresta	[	x,	&e,	&e,	&e,	nil,	nil,	nil]

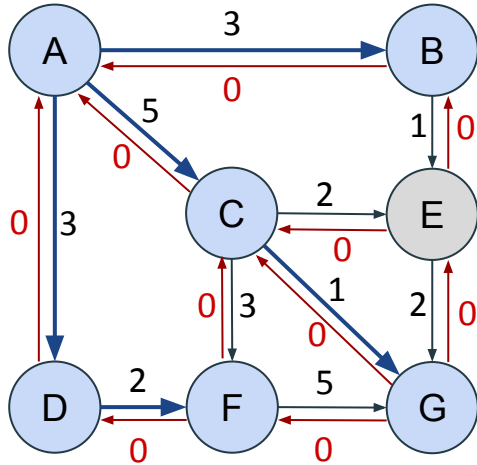
# Ford Fulkerson V1 (BFS)



```
5  type Edge struct {  
6      origin uint32  
7      dest   uint32  
8      weight float64  
9      comp   *Edge  
10 }
```

pais:	A	B	C	D	E	F	G	
aresta	[	x,	&e,	&e,	&e,	nil,	&e,	&e]

# Ford Fulkerson V1 (BFS)

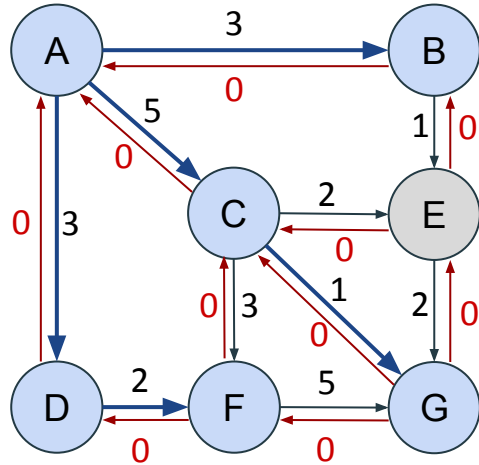


origin	C
dest	G
weight	1
comp	&edge

pais:	A	B	C	D	E	F	G
aresta	[ x,	&e,	&e,	&e,	nil,	&e,	&e]



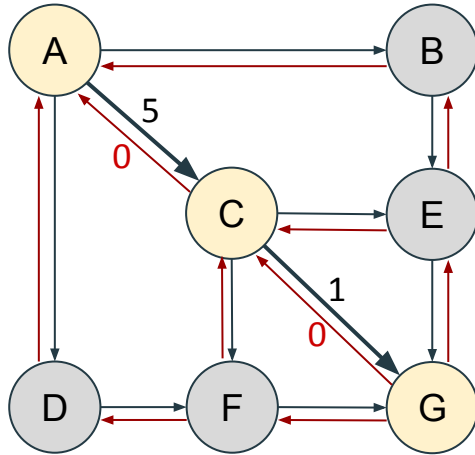
# Ford Fulkerson V1 (BFS)



origin	A
dest	C
weight	5
comp	&edge

pais:	A	B	C	D	E	F	G
aresta	[ x,	&e,	&e,	&e,	nil,	&e,	&e]

# Ford Fulkerson V1 (Atualizar residual)

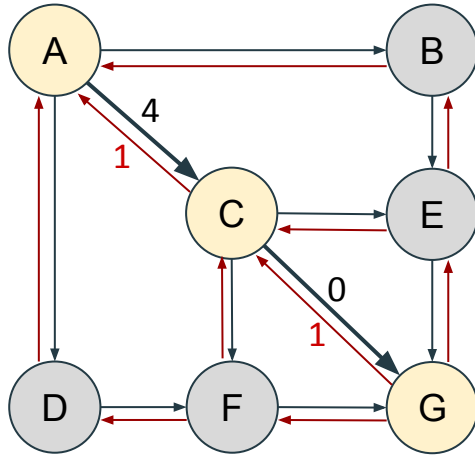


origin	A
dest	C
weight	5
comp	&edge

origin	C
dest	G
weight	1
comp	&edge

pais:	A	B	C	D	E	F	G	
aresta	[	x,	&e,	&e,	&e,	nil,	&e,	&e]

# Ford Fulkerson V1 (Atualizar residual)

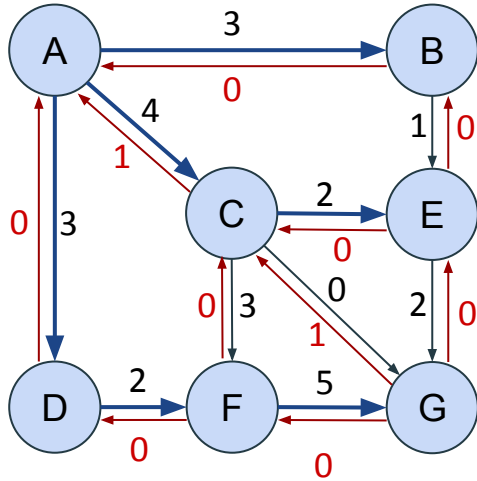


origin	A
dest	C
weight	4
comp	&edge

origin	C
dest	G
weight	0
comp	&edge

pais:	A	B	C	D	E	F	G	
aresta	[	x,	&e,	&e,	&e,	nil,	&e,	&e]

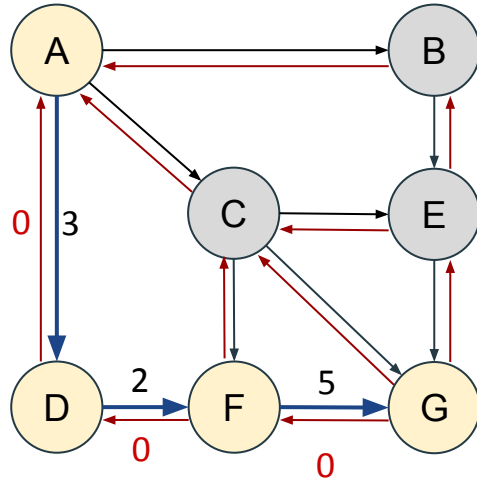
# Ford Fulkerson V1 (BFS)



```
5  type Edge struct {  
6      origin uint32  
7      dest   uint32  
8      weight float64  
9      comp   *Edge  
10 }
```

pais:	A	B	C	D	E	F	G
aresta	[ x,	&e,	&e,	&e,	&e,	&e,	&e]

# Ford Fulkerson V1 (BFS)



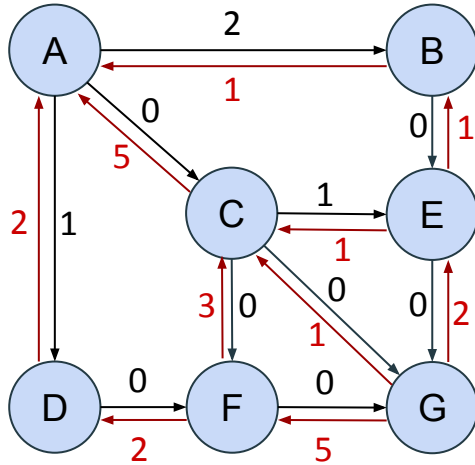
origin	A
dest	D
weight	3
comp	&edge

origin	D
dest	F
weight	2
comp	&edge

origin	F
dest	G
weight	5
comp	&edge

pais:	A	B	C	D	E	F	G
aresta	[ x,	&e,	&e,	&e,	nil,	&e,	&e]

# Ford Fulkerson V1 (BFS)

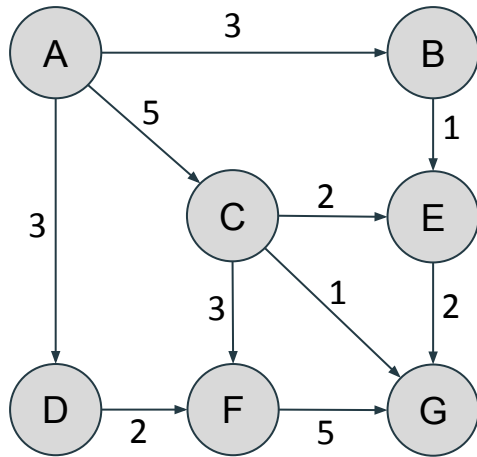


```
5  type Edge struct {  
6      origin uint32  
7      dest   uint32  
8      weight float64  
9      comp   *Edge  
10 }
```

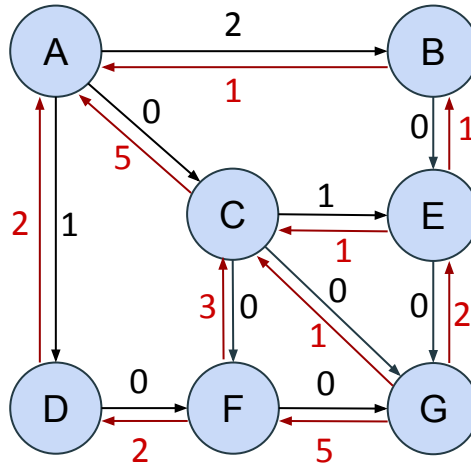
pais:	A	B	C	D	E	F	G
aresta	[ x,	&e,	&e,	&e,	&e,	&e,	&e]

# Ford Fulkerson V1 (Encontrando fluxos)

Original:



Residual:

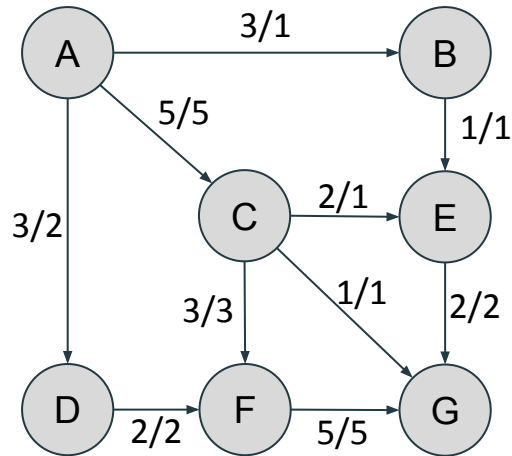


```
correlacao_de_arestas [][]*Edge  
  
correlacao_de_arestas = [  
    (&original, &residual),  
    (&original, &residual),  
    ...  
]
```

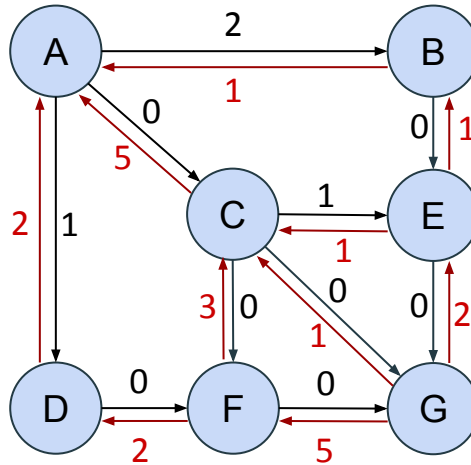
```
13 type EdgeFlow struct {  
14     edge *Edge  
15     flow float64  
16 }
```

# Ford Fulkerson V1 (Encontrando fluxos)

Original:



Residual:



```
correlacao_de_arestas [][]*Edge  
  
correlacao_de_arestas = [  
    (&original, &residual),  
    (&original, &residual),  
    ...  
]
```

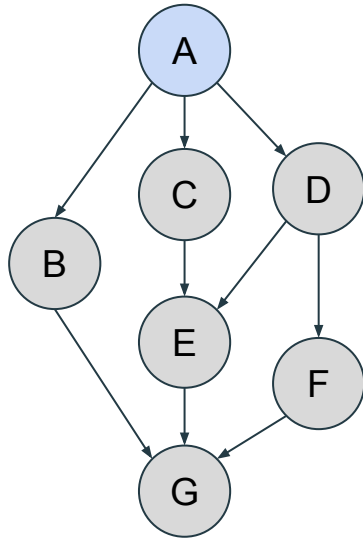
```
13 type EdgeFlow struct {  
14     edge *Edge  
15     flow float64  
16 }
```



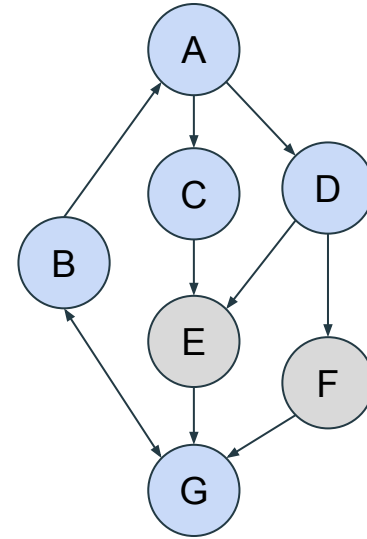
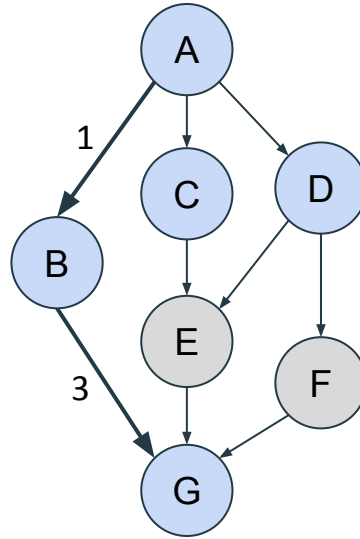
# Resultados

Grafos	grafo 1	grafo 2	grafo 3	grafo 4	grafo 5	grafo 6	grafo 7	grafo 8
<b>Fluxo máximo (entre vértices 1 e 2)</b>	284	276820	291	253278	618	548517	611	5382665
<b>Tempo médio de execução (Versão 1)</b>	0.0044s (4.4ms)	0.0078s (7.8ms)	0.0795s (79.5ms)	0.1365s (135ms)	4.39314s	8.00897s	44.97805s	114.2085s (1m54s)

# Melhorias (lista de visitados/pais)

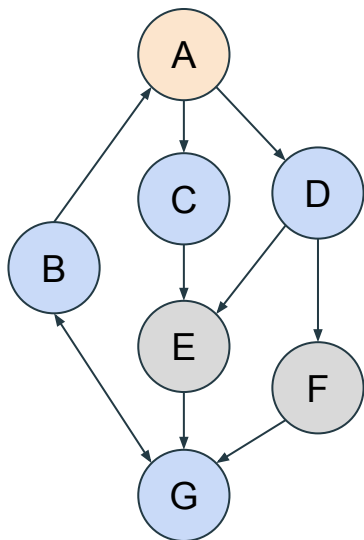


visitados:	A	B	C	D	E	F	G								
aresta	[	1	,	0	,	0	,	0	,	0	,	0	,	0	]

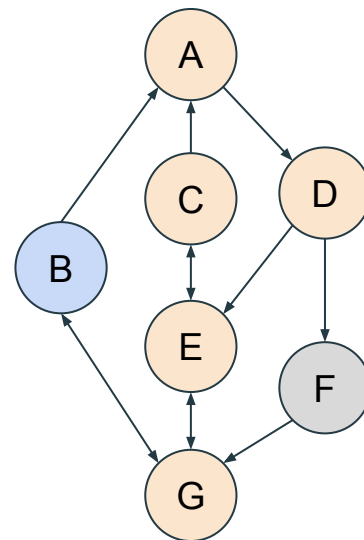
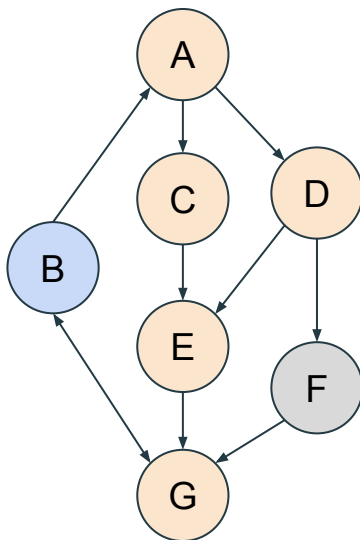


visitados:	A	B	C	D	E	F	G										
aresta	[	1	,	1	,	1	,	1	,	0	,	0	,	0	,	1	]

# Melhorias (lista de visitados/pais)

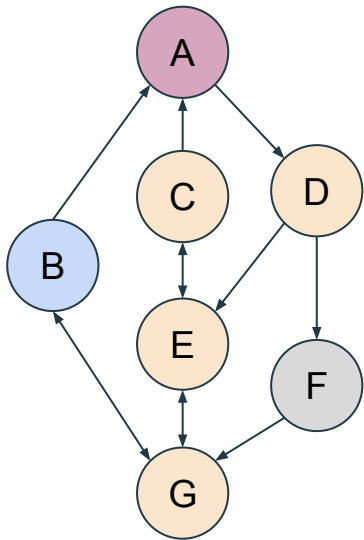


visitados:	A	B	C	D	E	F	G								
aresta	[	2	,	1	,	1	,	1	,	0	,	0	,	1	]

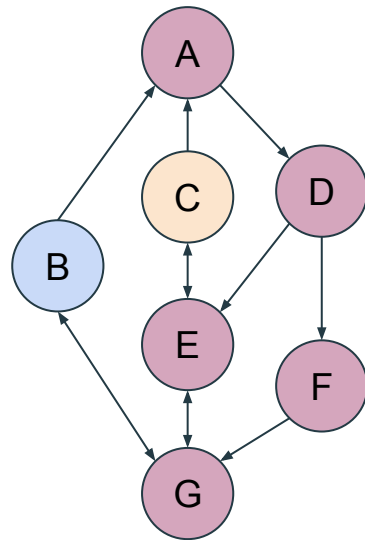
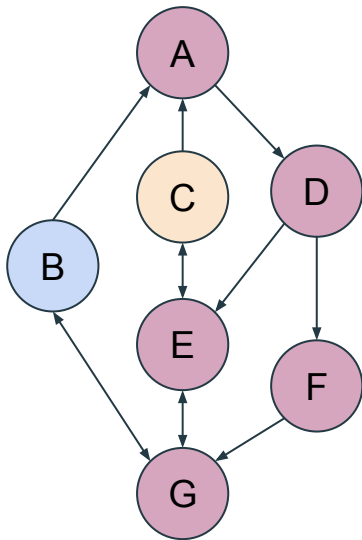


visitados:	A	B	C	D	E	F	G								
aresta	[	2	,	1	,	2	,	2	,	2	,	0	,	2	]

# Melhorias (lista de visitados/pais)

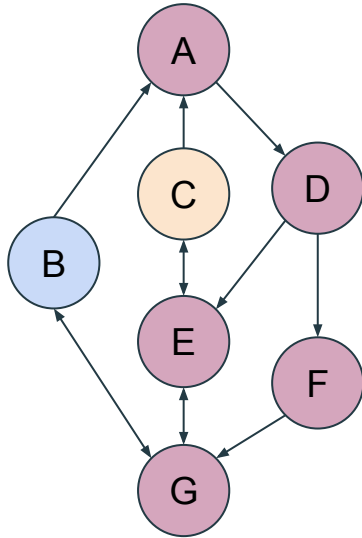


visitados:	A	B	C	D	E	F	G
aresta	[	3,	1,	2,	2,	2,	0, 2]



visitados:	A	B	C	D	E	F	G
aresta	[	3,	1,	2,	3,	3,	3, 3]

# Melhorias (lista de visitados/pais)

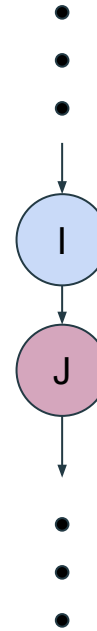
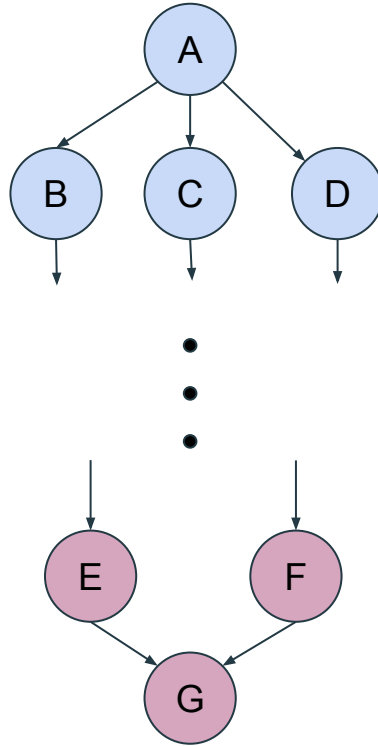
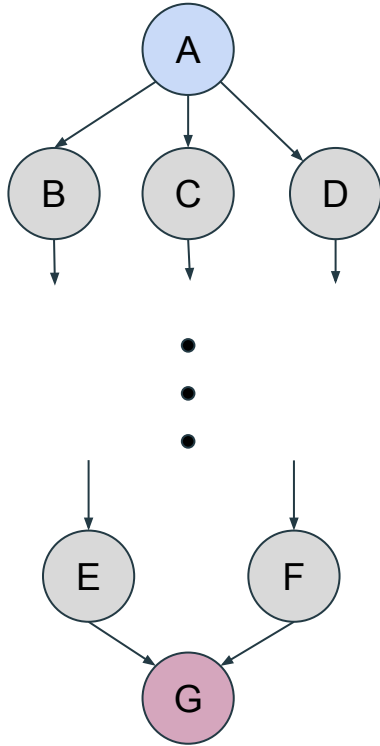


```
type Father struct {  
    edge *Edge  
    treeID uint64  
}
```

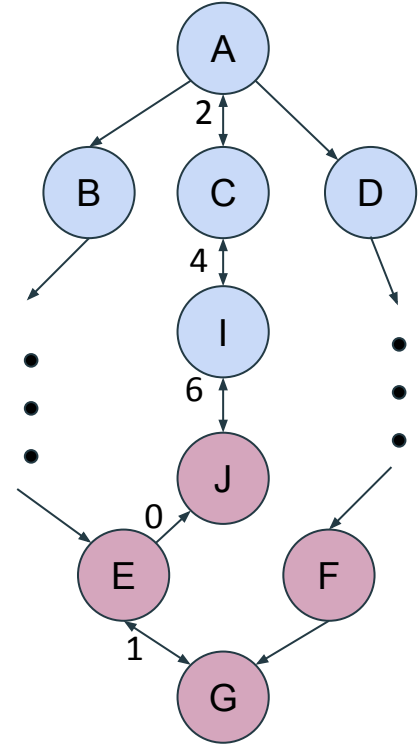
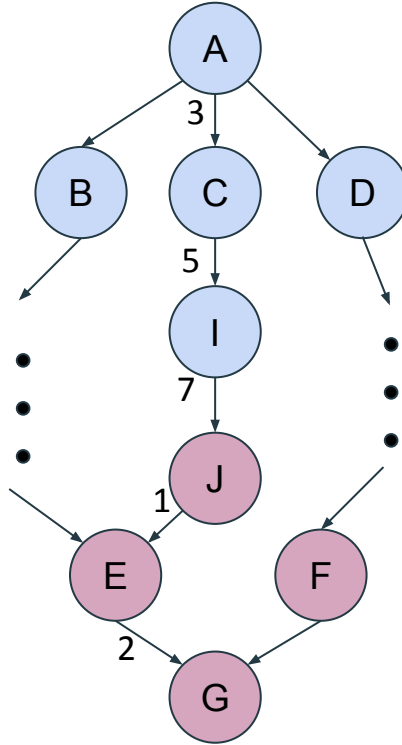
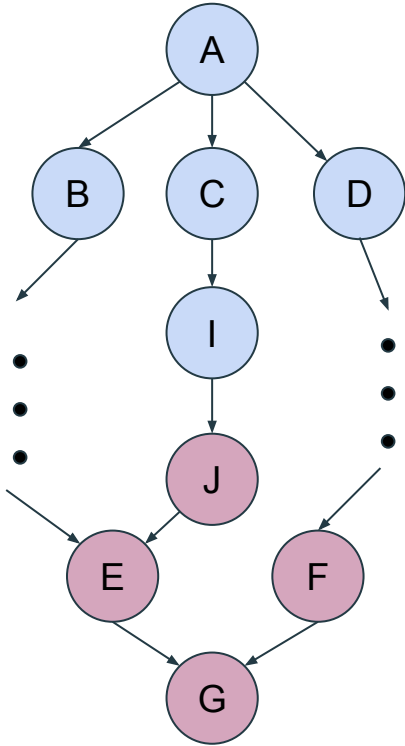
pais:	A	B	C	D	E	F	G
aresta	[ x,	&e,	&e,	&e,	&e,	&e,	&e]

visitados:	A	B	C	D	E	F	G
aresta	[ 3,	1,	2,	3,	3,	3,	3]

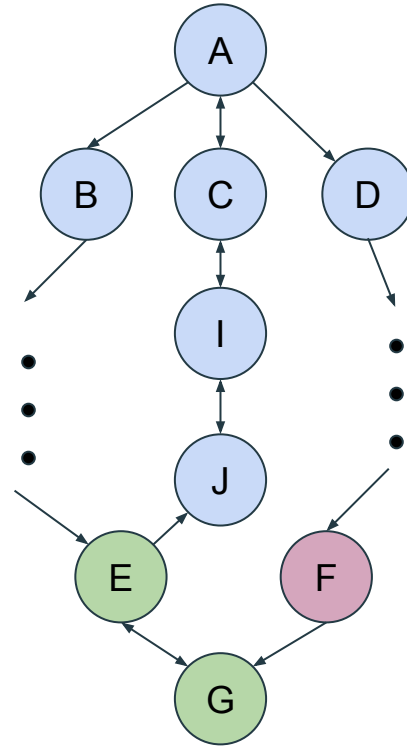
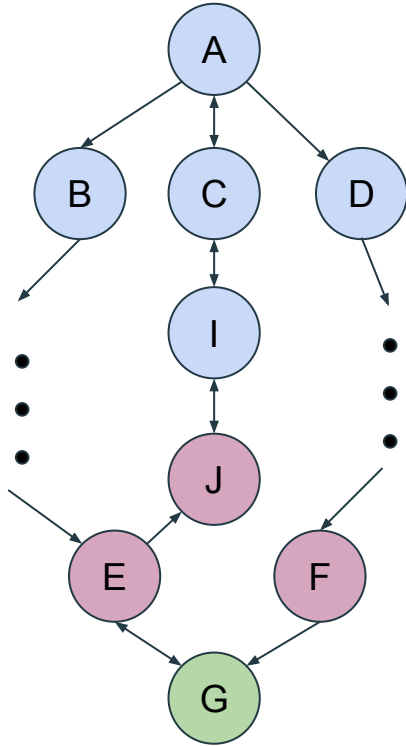
# Melhorias (2 BFS)



# Melhorias (2 BFS)



## Melhorias (2 BFS)





# Resultados

Grafos	grafo 1	grafo 2	grafo 3	grafo 4	grafo 5	grafo 6	grafo 7	grafo 8
<b>Fluxo máximo (entre vértices 1 e 2)</b>	284	276820	291	253278	618	548517	611	5382665
<b>Tempo médio de execução (Versão 1)</b>	0.0044s (4.4ms)	0.0078s (7.8ms)	0.0795s (79.5ms)	0.1365s (135ms)	4.393s	8.009s	44.98s	114.21s (1m54s)
<b>Tempo médio de execução (Versão 2)</b>	0.0017s (1.7ms)	0.0016s (1.6ms)	0.0228s (22.8ms)	0.0238s (23.8ms)	0.472s	0.639s	8.96s	9.43s
<b>Ganho de velocidade (vezes mais rápido)</b>	2.59x	4.88x	3.49x	5.74x	9.31x	12.53x	5.02x	12.11x