Introduction
What is Cryptography
How does Linear Algebra and Encryption connected?
The fundamental example of Encryption
AES - Advanced Encryption Standard
Conclusion

Cryptography and the World of the Mystery

Ismail Kably & Duc Phan

June 6, 2018



Table of Contents

- Introduction
- What is Cryptography
- 3 How does Linear Algebra and Encryption connected?
- 4 The fundamental example of Encryption
- 5 AES Advanced Encryption Standard
- **6** Conclusion

What we are going to do?

Let's explore the world of encryption!



What is cryptography?

- Cryptography or cryptology is the practice and study of techniques for secure communication in the presence of third parties called adversaries.
- More generally, cryptography is about constructing and analyzing protocols that prevent third parties or the public from reading private messages.

Introduction
What is Cryptography
How does Linear Algebra and Encryption connected?
The fundamental example of Encryption
AES - Advanced Encryption Standard
Conclusion

The link between Linear Algebra and Encryption

Because many types of encryption Matrix use the Math behind matrices to encrypt, Linear Algebra is required for Encryption and Decryption!

Is it complicated?

- The idea behind encryption is not hard to understand at all!
- Cipher matrix can be as simple as a 3x3 matrix composed of random integers that represent the characters in the plain-text.

Introduction
What is Cryptography
How does Linear Algebra and Encryption connected?
The fundamental example of Encryption
AES - Advanced Encryption Standard
Conclusion

A simple encryption method

Let's take a look at a simple encryption type :D

Say, I want to encrypt the word "MATH"

The general Idea

- Convert a plain-text to a matrix
- ② Encrypt the matrix
- Oecrypt the encrypted matrix

Plain-text to Matrix

Each character in plain-text must be denoted with a **numerical** value and placed into a matrix.

Α	В	С	D	Е	F	G	Н	1	J	K	L	М	N	0	Р	Q	R	s	Т	U	٧	w	Х	Υ	Z
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26

Plain-text to Matrix

The numerical values are then separated into vectors, such that:

- The number of rows of each vector is equivalent to the numbers of rows of the cipher matrix.
- **5** Values are placed one at a time, going down a row for each value.
- Vectors are filled one to another.
- 1 The remaining empty entries in the last vector is filled with space.



Plain-text to Matrix

The vectors are then **augmented** to form a **plain-text matrix**.



The plain-text matrix is then **multiplied** by another **cipher-matrix** to create the **encrypted matrix**.

Let's take a look at this

$$C \times P = E$$

$$\iff C^{-1} \times C \times P = C^{-1} \times E$$

$$\iff P = C^{-1} \times E$$

First, we need to find the **inverse** of the **cipher-matrix**.

The inverted matrix is then multiplied with the cipher-text matrix. The product is the original plain-text matrix.

The plain-text can be found by splitting the products into vectors



And then use the **numerical rules** to convert the **numbers** back into their **letter forms**.



What is Cryptography
How does Linear Algebra and Encryption connected?
The fundamental example of Encryption
AES - Advanced Encryption Standard

More advanced encryption

Let's take a look at AES, a more secure encryption type!

AES - ...

AES - Advanced Encryption Standard - is:

- a symmetric encryption algorithm.
- very powerful.
- widely used in software and hardware throughout the world!

The general Process

- AES operates on 4x4 matrix.
- Each character in the plain-text is denoted with a corresponding numerical value

An example

Let's take a look at an example to understand the process

We'll encrypt and decrypt the plain-text:

"Come here I got cash"

From text to plain-text matrix

Just like in the last example, we use the same rules to convert the text into a matrix.

C _{0,0}	O _{0,1}	m _{0,2}	e _{0,3}
h _{1,0}	e _{1,1}	r _{1,2}	e _{1,3}
I _{2,0}	g _{2,1}	O _{2,2}	t _{2,3}
C _{3,0}	a _{3,1}	S _{3,2}	h _{3,3}

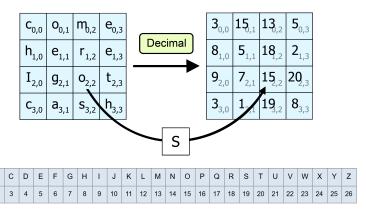
В

2

1

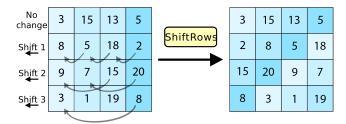
Conversion Plain-text to Numerical Matrix

Then, we convert the plain-text into its corresponding numerical matrix



Shifting rows

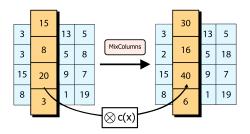
- First row is unchanged
- Second row is shifted to the left 1 time
- Third row is shifted to the left 2 times
- Fourth row is shifted to the left 3 times



Mixing the columns

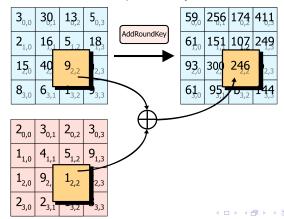
The four decimals in each column are transformed using a linear transformation

In this example, we'll scale the second column by 2



Adding round keys

We then multiply the matrix by another randomly generated invertible matrix, which is the private key



Sending and Deciphering

After encrypting the matrix, it is now secure to be sent to the recipient(s).

To decrypting, we can decipher the message using the private key that contains all the operation backward!

Conclusion

- Encryption plays an essential role in securing our private data.
- The examples use Linear Algebra to handle the Math, but there can be other methods!

Introduction
What is Cryptography
How does Linear Algebra and Encryption connected?
The fundamental example of Encryption
AES - Advanced Encryption Standard
Conclusion

Thank you very much for watching!