## **Problems and Applications**

Consider the regression of average hourly earnings AHE (in dollars) on Age (in years) and several binary variables for characteristics such as sex, education, and region of employment:

$$\widehat{AHE} = 0.33 + 10.42 \, College - 4.57 \, Female + 0.61 \, Age + 0.74 \, Northeast - 1.54 \, Midwest - 0.44 \, South$$

$$R^2 = 0.185, \quad SER = 12.01, \quad n = 7178$$

- a. Do there appear to be important regional differences?
- b. Why is the regressor West omitted from the regression? What would happen if it were included?
- c. Juanita is a 28-year-old female college graduate from the South. Jennifer is a 28-year-old female college graduate from the Midwest. Calculate the expected difference in earnings between Juanita and Jennifer.

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b. Why is the regressor West omitted from the regression? What would happen if it were included?

The regressor West is omitted to avoid perfect multicollinearity. Perfect multicollinearity would arise because the data is divided into exactly 4 groups: West, Midwest, Northeast, and South. Since the 4 categories are exchaustive and mutually exclusive, by construction, they add up to 1 for every observation in the dataset. This is known as the "dummy variable trap". Perfect multicollinearity among regressors is usually easy to detect. Some software will produce an error, others will drop one of the perfectly multicollinear regressors and issue a warning. Imperfect multicollinearity is another issue, much less easy to deal with.

## **Problems and Applications**

a. Do there appear to be important regional differences?

Since the variables for West is omitted from the regression, it is the reference group to which the other regional variables can be compared to. On average, and controlling for other variables in the regression, workers in the Northeast earn \$0.74 more per hour than workers in the West; while workers in the Midwest earn \$1.54 less than workers in the West; and workers in the South earn \$0.44 less than workers in the West.

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c. Juanita is a 28-year-old female college graduate from the South. Jennifer is a 28-year-old female college graduate from the Midwest. Calculate the expected difference in earnings between Juanita and Jennifer.

The expected difference in earnings between Juanita and Jennifer is:

$$AHE_{\mathsf{Juanita}} - AHE_{\mathsf{Jennifer}}$$

$$= (AHE|College = 1, Female = 1, Age = 28,$$

$$Northeast = 0, Midwest = 0, South = 1)$$

$$- (AHE|College = 1, Female = 1, Age = 28,$$

$$Northeast = 0, Midwest = 1, South = 0)$$

$$= (-0.44) - (-1.54)$$

$$= + 1.10$$

The expected difference in earnings between Juanita and Jennifer, based on the information used in the regression, is \$1.10 per hour.