# UCLA Math Circle

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#### Abstract

More problems on modular arithmetic to accompany the UCLA Math Circle Intermediate-2 for Summer Session 2020, August 9nd.

#### More Problems on Modular Arithmetic

### Problem 1

Calculate  $3^{31} \pmod{7}$ .

### Problem 2

Calculate 2<sup>35</sup> (mod 7)

#### Problem 3

The remainder of  $2^{1000}$  divided by 13.

## Problem 4

Solve  $x^{103} \equiv 4 \pmod{11}$ .

# Problem 5

If a googolplex is  $10^{10^{100}}$ , what day of the week will it be a googolplex days from now? (Today is Sunday)

## Problem 6

Find all positive integers x such that  $2^{2^x+1}+2$  is divisible by 17.