

FORMULAZIONE COMPLETA

VARIABLES: $X_{pq}^i \rightarrow$ node i used for VNF i on SFC p
 $B \rightarrow$ bandwidth $D \rightarrow$ delay
 $R^w \rightarrow$ node resource w

MINIMIZE:

$$\begin{aligned} \text{cost} = & \sum_i \sum_p \sum_{\substack{q \neq q_{\text{usr}} \\ q \neq q_{\text{mtr}}}} \sum_w X_{pq}^i \cdot R_{pq}^w \cdot C_i^w + \quad \# \text{ nodes} \\ & + \sum_{\substack{i, j \\ i \neq j}} \sum_p \sum_{\substack{q \\ q \neq q_{\text{usr}}}} \sum_{\substack{q' \\ q' \neq q_{\text{mtr}}}} X_{pq}^i \cdot X_{pq'+1}^j \cdot B_p \cdot C_{ij} \quad \# \text{ links} \\ & + \sum_p \sum_q C_{pq} \quad (?) \quad \# \text{ embedding cost} \end{aligned}$$

CONSTRAINTS

$$1) \quad \forall i \quad \sum_p \sum_{\substack{q \neq q_{\text{usr}} \\ q \neq q_{\text{mtr}}}} \sum_w X_{pq}^i \cdot R_{pq}^w \leq \max(R_i^w) \quad \# \text{ node res}$$

$$2) \quad \forall i, j \mid i \neq j \quad \sum_p \sum_{\substack{q \neq q_{\text{usr}} \\ q \neq q_{\text{mtr}}}} \sum_{\substack{q' \\ q' \neq q_{\text{mtr}}}} X_{pq}^i \cdot X_{pq'+1}^j \cdot B_p \leq \max(B_{ij}) \quad \# \text{ link BW}$$

$$3) \quad \forall p \quad \sum_{\substack{i, j \\ i \neq j}} \sum_{\substack{q \\ q \neq q_{\text{usr}}}} \sum_{\substack{q' \\ q' \neq q_{\text{mtr}}}} X_{pq}^i \cdot X_{pq'+1}^j \cdot D_{ij} \leq D_p \quad \# \text{ link delay}$$

$$4) \quad \forall p, q \quad \sum_i X_{pq}^i = 1 \quad \# \text{ one node for every function}$$

$$5) \quad \forall p \quad \sum_q \sum_{\substack{i, j \\ i \neq j}} \sum_{\substack{q' \\ q' \neq q_{\text{mtr}}}} X_{pq}^i \cdot X_{pq'+1}^j = \text{LEN}(p) - 1 \quad \# \text{ all links of chain are chosen}$$

$$6) \quad \forall_{p,q} \quad \sum_{\substack{i,j \\ i \neq j}} X'_{pq} X''_{pq+1} = 1$$

NOTES

1) $B_{ij} = 0$ IF i, j NOT CONNECTED

2) $D_{ij} \rightarrow \infty$ IF i, j NOT CONNECTED

QUADRATIC DISCONTINUOUS
CANNOT BE EXPRESSED
AS QUBO !!!

FORMULATIONS INCOMPETITIVE (LINK BASED)

VARIABLES: y_{pq}^{ij} → LINK ij IS USED FOR GIVING FLOW
 VALUE q TO $q+1$

$B \rightarrow$ BANDWIDTH

$D \rightarrow$ DELAY

$R^w \rightarrow$ NODE RESOURCE w

MINIMIZE:

→ CONSTANT PER UNIT OF
 AN EDGE FLOW

$$\begin{aligned} \text{COST} = & \sum_{i,j} \sum_{p,q} \sum_{\substack{q \neq q_{\text{max}} \\ q \neq q_{\text{min}}}} y_{pq}^{ij} \cdot R_{pq}^w \cdot C_{ij}^w + \quad \# \text{ LINKS} \\ & + \sum_{i,j} \sum_{p,q} \sum_{\substack{q \neq q_{\text{max}} \\ q \neq q_{\text{min}}}} y_{pq}^{ij} \cdot B_p \cdot C_{ij} \quad \# \text{ LINKS} \\ & + \sum_p \sum_q C_{pq} \quad (?) \quad \# \text{ EMBOSSING COST} \end{aligned}$$

CONSTRAINTS

$$1) \forall w, j \sum_{i \neq j} \sum_{p,q} \sum_{\substack{q \neq q_{\text{max}} \\ q \neq q_{\text{min}}}} y_{pq}^{ij} R_{pq}^w \leq \text{MAX}(R_i^w) \quad \# \text{ NODE RES}$$

$$2) \forall i, j | i \neq j \sum_{p,q} \sum_{\substack{q \neq q_{\text{max}} \\ q \neq q_{\text{min}}}} y_{pq}^{ij} B_p \leq \text{MAX}(B_{i,j}) \quad \# \text{ LINK RES}$$

$$3) \forall p \sum_{i,j} \sum_{\substack{q \neq q_{\text{max}} \\ q \neq q_{\text{min}}}} y_{pq}^{ij} D_{ij} \leq D_p \quad \# \text{ LINK DELAY}$$

$$4) \forall_{\substack{p,q \\ q \neq q_{\text{max}} \\ q \neq q_{\text{min}}}} \sum_{i,j \neq i} y_{pq}^{ij} = 1 \quad \# \text{ ONE NODE FOR GIVING FUNCTION}$$

$$5) \forall_p \sum_q \sum_{i,j \neq i} y_{pq}^{ij} = \text{LEN}(p) - 1 \quad \text{ALL LINKS OF CHAIN ARE PRESENT}$$

$$6) \quad \forall_{p,q} \quad \sum_{i \in S} \sum_{j \in T} y_{pq}^{ij} = 1 \quad \text{ONLY ONE LINK BETWEEN TWO VARS}$$

NOTES

- EQUAZIONE 5) NON FORZA UNA DUE
STESSA CATEGORIA AD ESSERE COMPLETI !!

↳ DIFFICILE AGGIUNGERE COME
CONSTRAINT CHE SIA QUADRATICO

LINK FORMULATION (NEW)

VARIABLES

L_{pq}^{ij} → LINK $i \rightarrow j$ IS USED FOR VNF CONNECTION $q \rightarrow q+1$ OF CHAIN p

q_0 → FIRST FUNCTION ASSIGNED TO ENTRY NODE

q_L → FIRST FUNCTION ASSIGNED TO EXIT NODE

B_p → BANDWIDTH

R^w → NODE RESOURCE w

D → DELAY

C^w → UNIT COST OF RESOURCE w

↳ $L_{pq_L}^{ij}$ DOES NOT NOT

$T(i) \mid i \in \text{NODES} \rightarrow \{ \text{SOURCE}, \text{ENTRY}, \text{EXIT} \}$

MINIMIZE:

$$\text{COST} = \sum_i \sum_j \sum_p \sum_q \sum_w L_{pq}^{ij} \cdot R_{pq}^w \cdot C_j^w \quad \# \text{ NODE COST}$$

$i \neq j$
 $T(i) = \text{SOURCE}, \quad q \neq q_0$
 $T(j) = \text{SINK}, \quad q = q_L$

$$+ \sum_i \sum_j \sum_p \sum_q L_{pq}^{ij} \cdot B_p \cdot C_{ij} \quad \# \text{ LINK COST}$$

$i \neq j$
 $q \neq q_L$

$$+ \sum_p \sum_q C_{pq} \rightarrow \text{NODES NOT MATTER FOR QURSO} \quad \# \text{ EMISORING COST}$$

CONSTRAINTS

$$\Rightarrow \forall x, w \sum_j \sum_p \sum_q L_{pq}^{ij} R_{pq}^w \leq \max_i (R_i^w) \quad \# \text{ nodes } n = S$$

$$2) \forall i, j \mid i \neq j \quad \sum_p \sum_{\substack{q \\ q \neq p}} L_{pq}^{i,j} B_p \leq \max(B_{i,j}) \quad \neq \text{LINK BANDWIDTH}$$

$$3) \forall p \sum_{i \neq j} \sum_{q \neq p} L_{pq}^{ij} D_{ij} \in D_p \quad \# \text{ LINK}_{D_{pq}}$$

4) $\forall p, q$
 $q \neq q_L$

$$\sum_i \sum_j L_{pq}^{ij} = 1$$

* EXACTLY ONE LINK FOR
every $q \rightarrow q+1$

5) $\forall p \sum_{q=q_0} \sum_{i \neq j} \sum_{p \neq q} L^{ij} = \text{LEN}(p) - 1$ # LENGTH OF CHAIN IS FIXED

6) $\forall_{j,p,q} \sum_x L^{xj}_{pq} - \sum_K L^{Kj}_{pq+1} = 0$ \nexists COMMUNITY AND ORIGIN OF VME CLANKS.

COMMONS

A) IF ROWS $i \neq j$ CONSTRAINTS MAYBE YOU CAN
PUT CONSECUTIVE VNF_n ON SAME NODE

B) L_{pq}^{ij} WHERE $type(i) = entry$ ($type(j) = exit$) AND
 $q \neq q_0$ ($q \neq q_{L-1}$) DOS NOT EXIST