

Projections and clusterings

Formation IA biodiversité

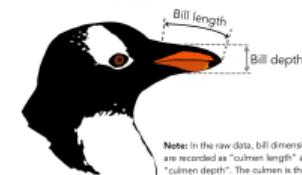
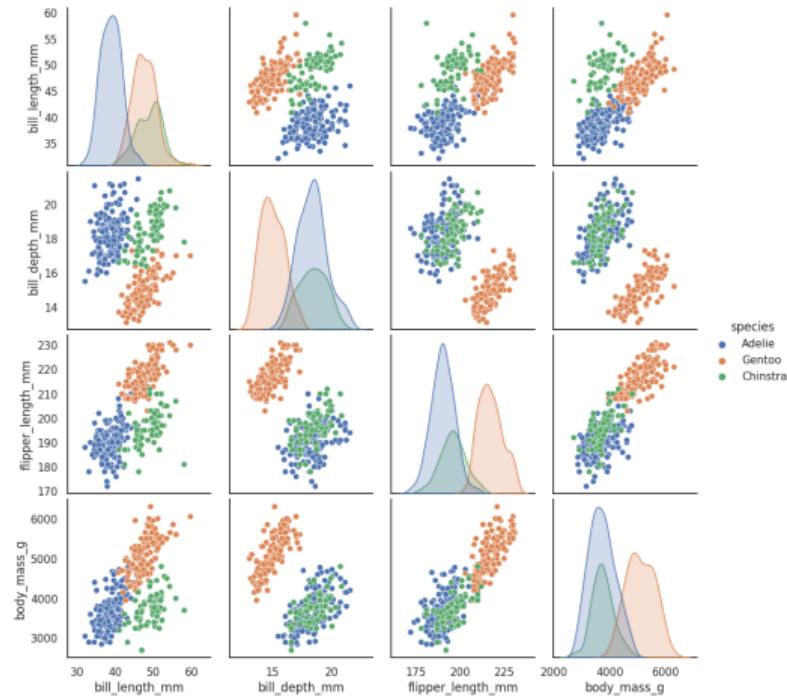
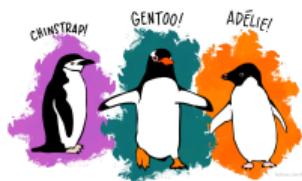
Paul Tresson

May 13, 2025

UMR AMAP

Introduction

Visualize what is happening in higher dimensions



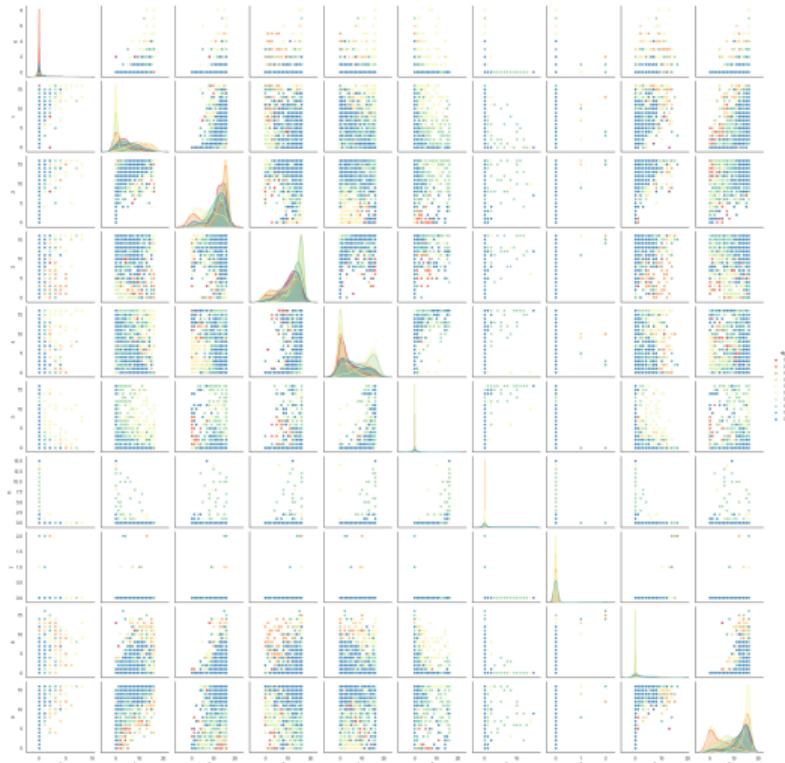
Note: In the raw data, bill dimensions are recorded as "culmen length" and "culmen depth". The culmen is the dorsal ridge atop the bill.

Visualize what is happening in higher dimensions

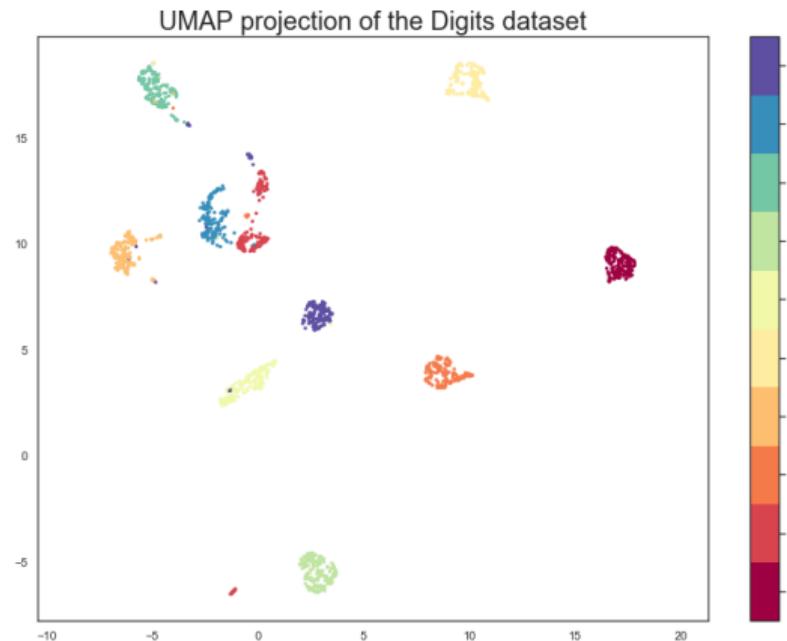
A 10x10 grid of numbers from 0 to 9, arranged in a specific pattern that forms a 3D cube's surface when visualized in 3D space. The pattern is as follows:

0	0	8	5	4	5	0	2	1	9
1	1	4	3	0	4	1	2	5	4
2	2	1	6	5	3	2	0	7	3
3	3	7	2	8	5	6	4	9	6
4	4	2	9	6	4	7	3	8	7
5	5	0	1	5	2	0	9	6	0
6	6	6	7	6	0	4	8	3	5
7	7	1	6	4	1	1	4	7	9
8	8	8	0	4	6	7	5	2	6
9	9	9	9	8	9	8	7	5	3

Visualize what is happening in higher dimensions



Visualize what is happening in higher dimensions

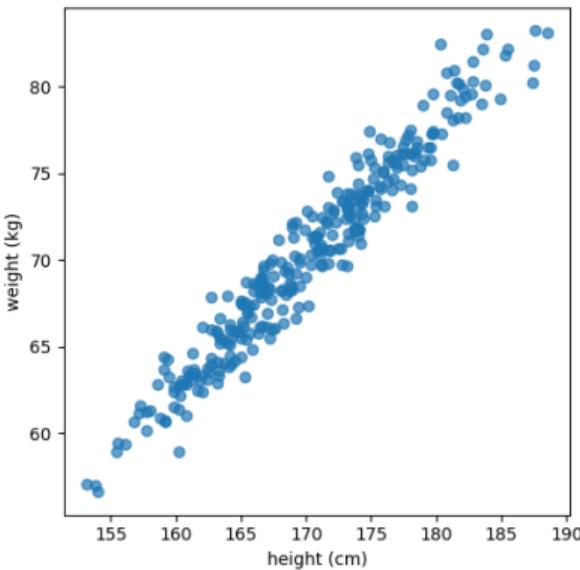


Projections

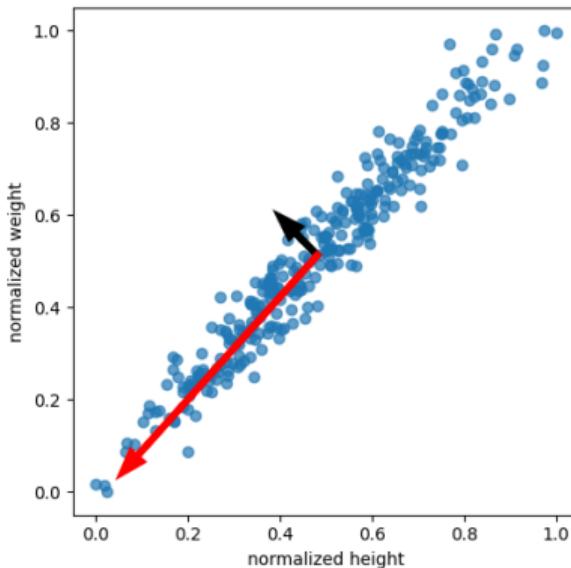
Projections

PCA

PCA



PCA



PCA calculation

$$X = \begin{bmatrix} x_1 & y_1 \\ x_2 & y_2 \\ x_3 & y_3 \\ \dots & \dots \end{bmatrix}$$

PCA calculation

$$C = \frac{1}{n-1} X^T X$$

PCA calculation

$$C = \begin{bmatrix} \sigma_x^2 & \sigma_{xy} \\ \sigma_{yx} & \sigma_y^2 \end{bmatrix}$$

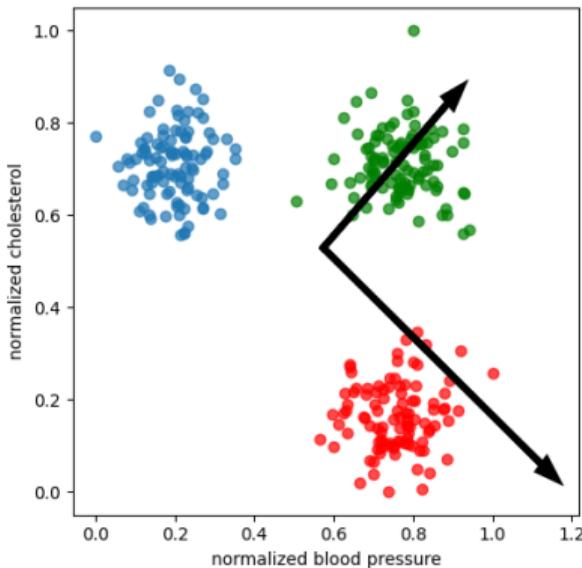
PCA calculation

$$Cv = \lambda v$$
$$\begin{bmatrix} \sigma_x^2 & \sigma_{xy} \\ \sigma_{yx} & \sigma_y^2 \end{bmatrix} \begin{bmatrix} v_x \\ v_y \end{bmatrix} = \lambda \begin{bmatrix} v_x \\ v_y \end{bmatrix}$$

PCA calculation

$$P = \begin{bmatrix} v_x & v_y \end{bmatrix}$$

PCA



PCA advantages and drawbacks

Advantages

- fast

Drawbacks

PCA advantages and drawbacks

Advantages

- fast
- scales well

Drawbacks

PCA advantages and drawbacks

Advantages

- fast
- scales well
- explanatory

Drawbacks

PCA advantages and drawbacks

Advantages

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Drawbacks

- **not suited for non-linear data**

Non linear data

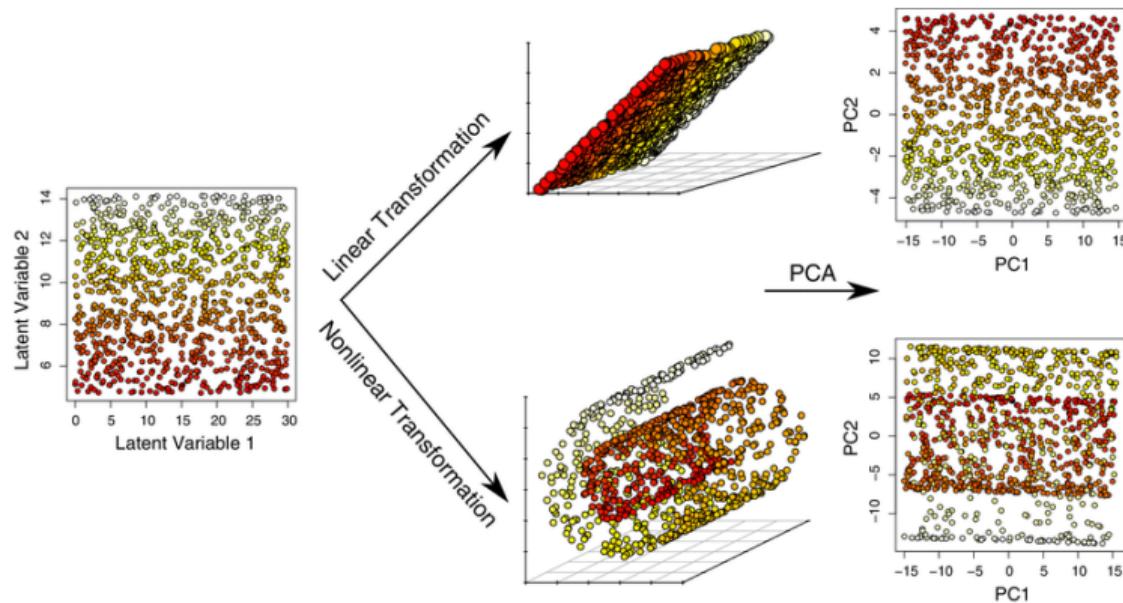


Figure from Du, 2019

Projections

UMAP

How to work with non linear data

1. Find a good representation of the data in high dimension
2. Fit a good representation of in low dimension

- **SNE** (Stochastic Neighbor Embedding) Hinton and Roweis, 2002

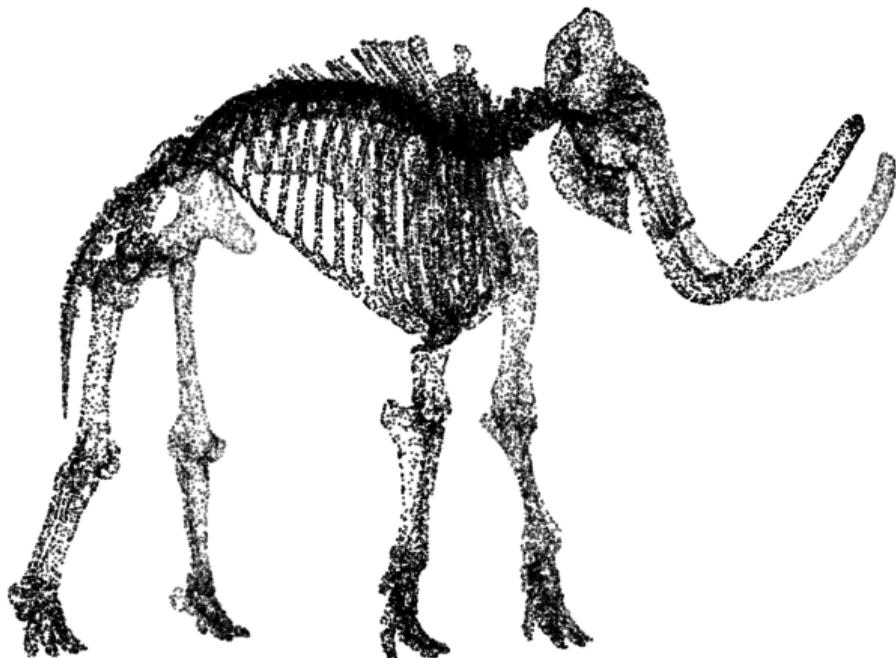
- **SNE** (Stochastic Neighbor Embedding) Hinton and Roweis, 2002
- **T-SNE** (T-distributed SNE) Van der Maaten and Hinton, 2008

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- **UMAP** (Uniform Manifold Approximation and Projection) McInnes et al., 2018

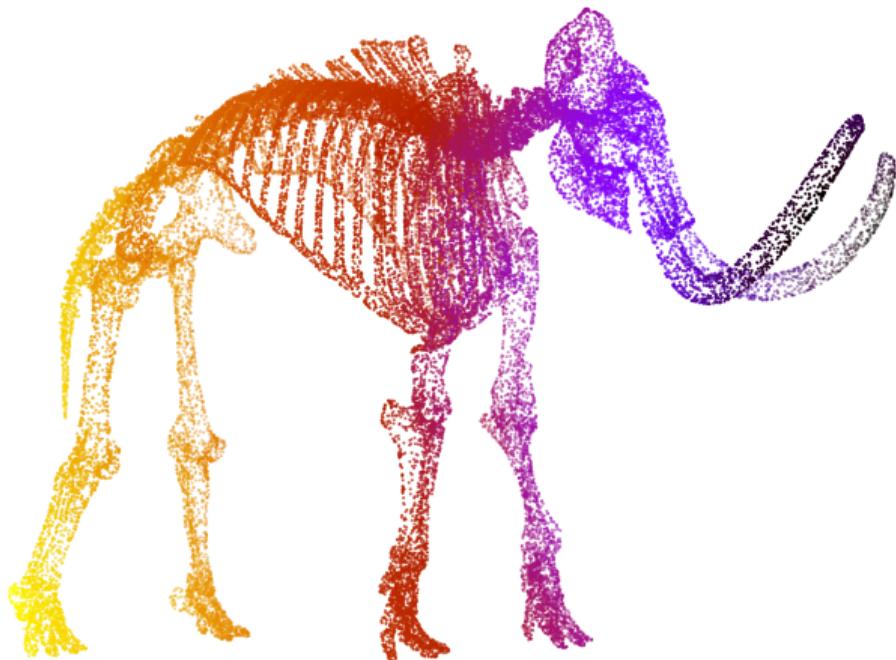
UMAP : Finding high dimension graph

UMAP : Fitting low dimensional representation

Mammoth example



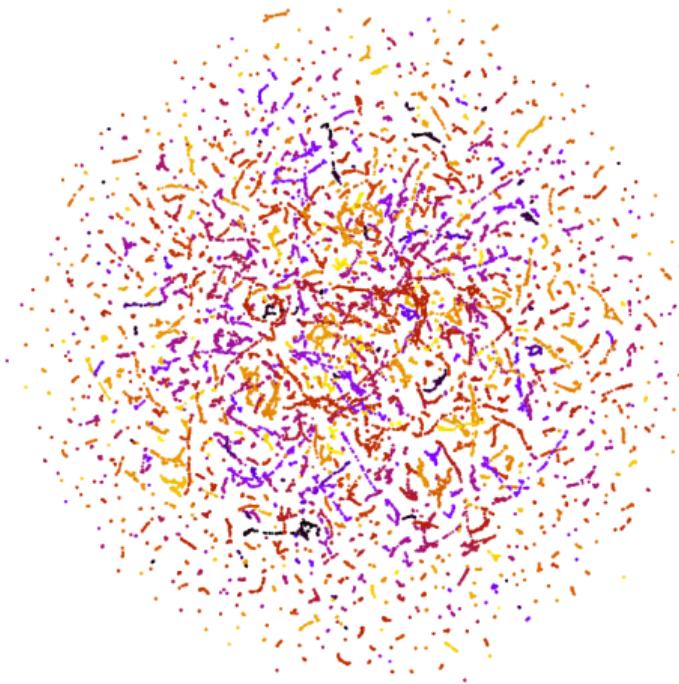
Mammoth example



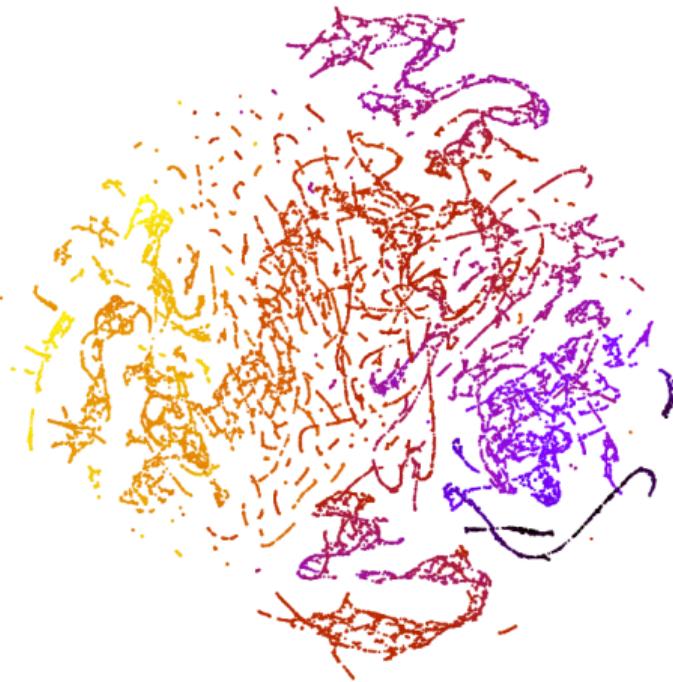
Mammoth example



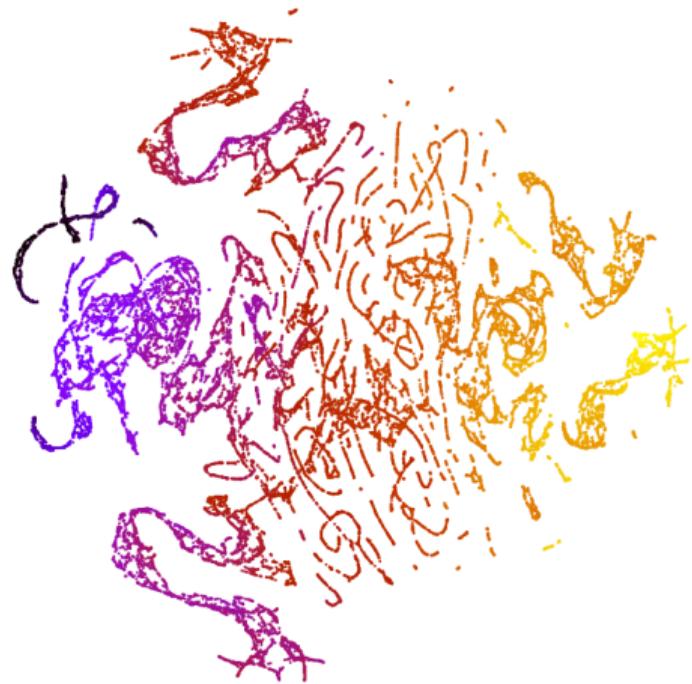
Mammoth example



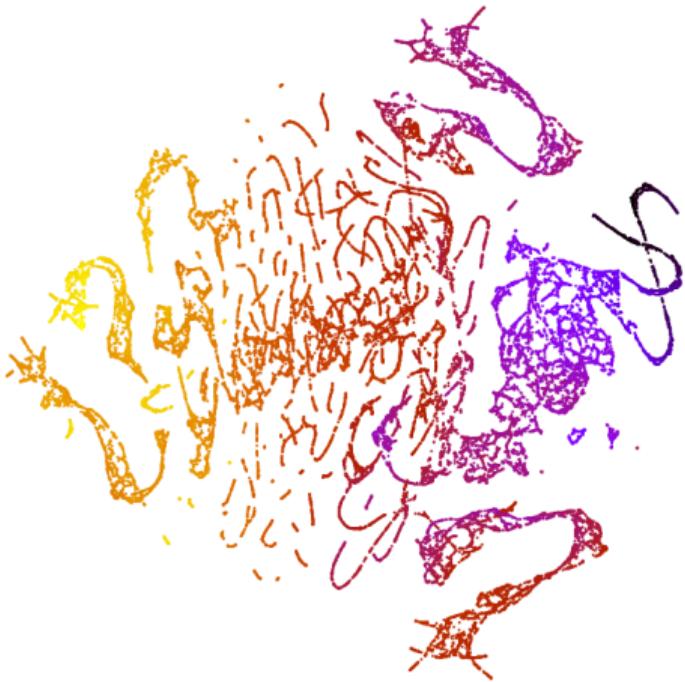
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Mammoth example



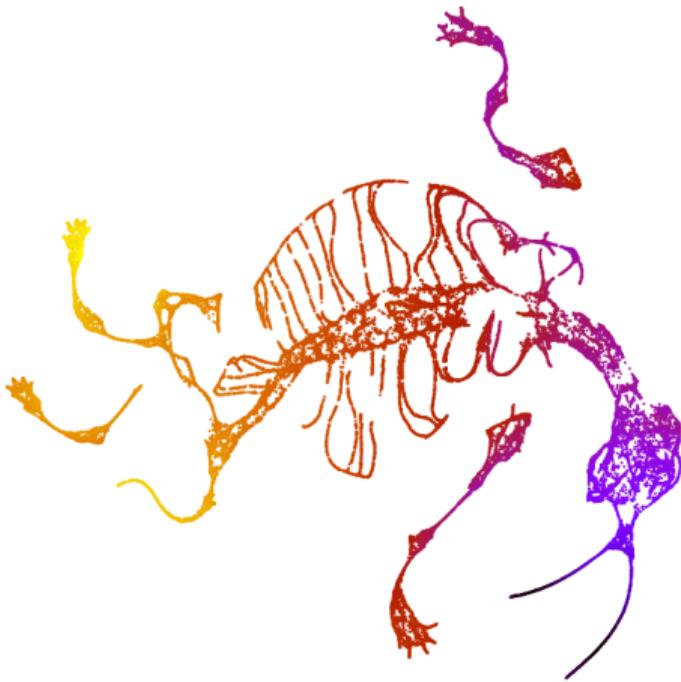
Mammoth example



Mammoth example



Mammoth example



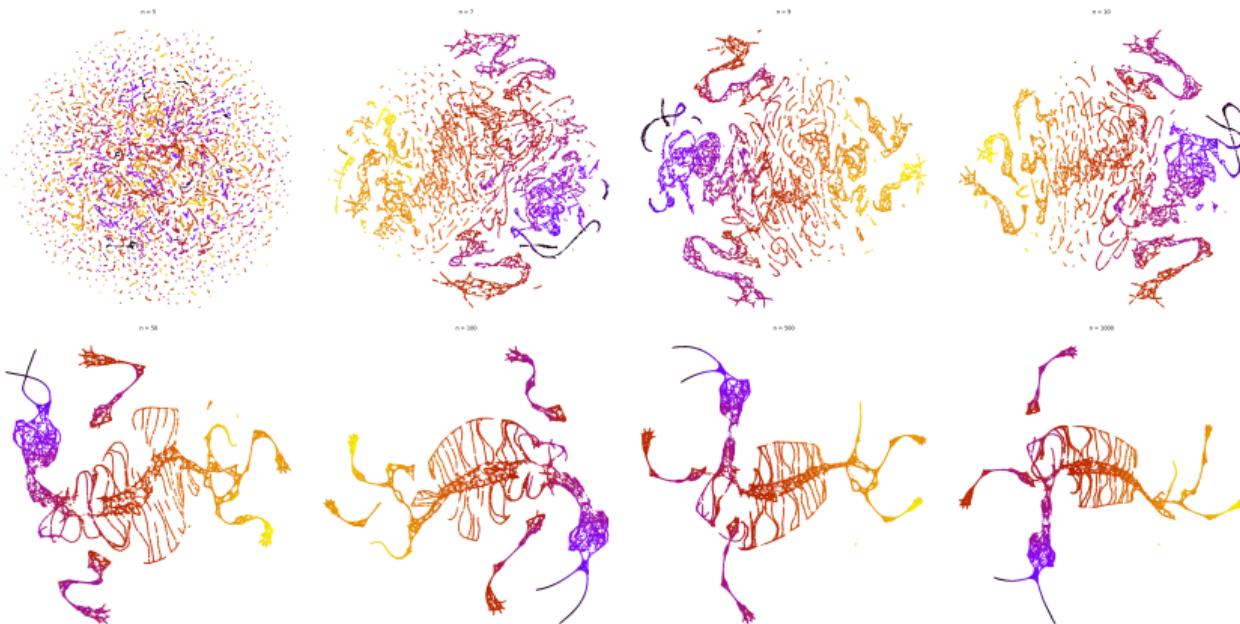
Mammoth example



Mammoth example



Mammoth example



UMAP vs. T-SNE

UMAP

- graph theory, fuzzy logic

T-SNE

- probabilities

UMAP vs. T-SNE

UMAP

- graph theory, fuzzy logic
- deterministic initialization

T-SNE

- probabilities
- random initialization

UMAP vs. T-SNE

UMAP

- graph theory, fuzzy logic
- determinist initialization
- \log_2 similarity scores

T-SNE

- probabilities
- random initialization
- gaussian distribution similarity

UMAP vs. T-SNE

UMAP

- graph theory, fuzzy logic
 - determinist initialization
 - \log_2 similarity scores
 - update by pairs
- scales well for large datasets

T-SNE

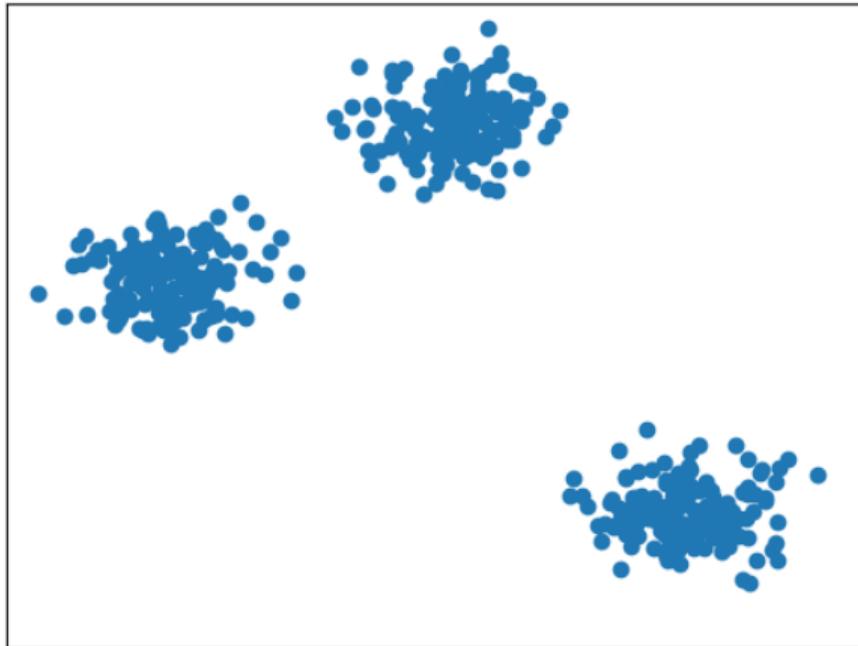
- probabilities
 - random initialization
 - gaussian distribution similarity
 - update all points
- scales less

Clustering

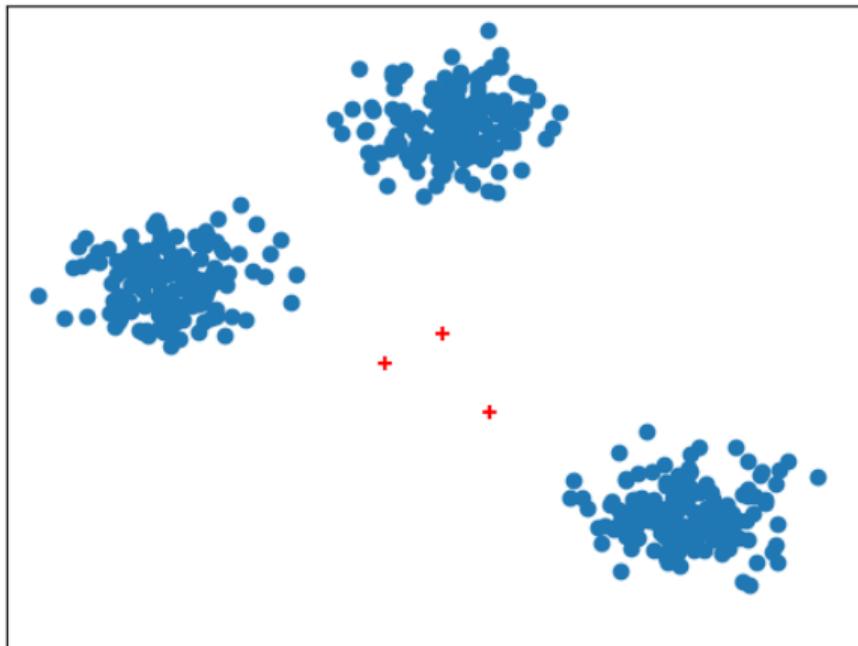
Clustering

K-means

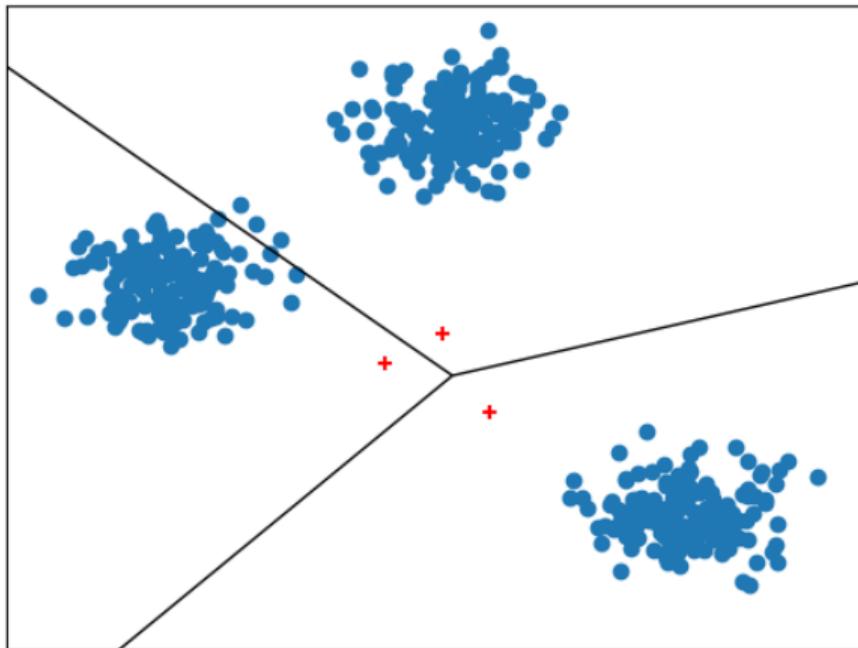
K-means



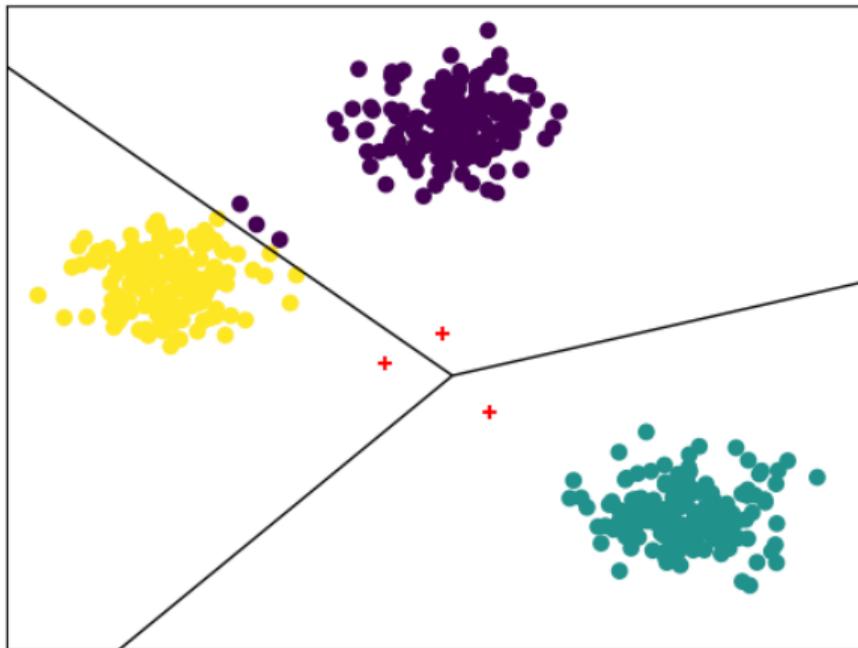
K-means



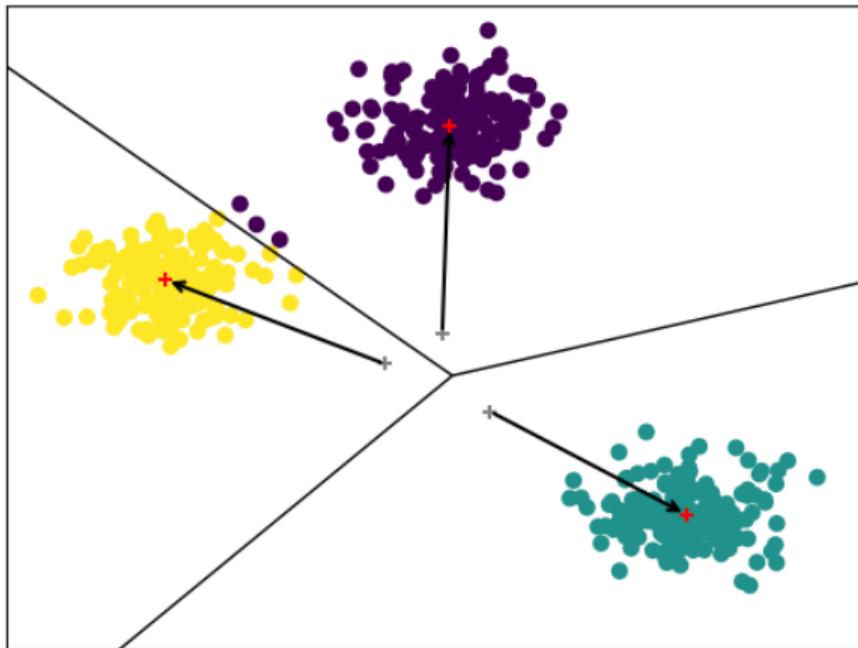
K-means



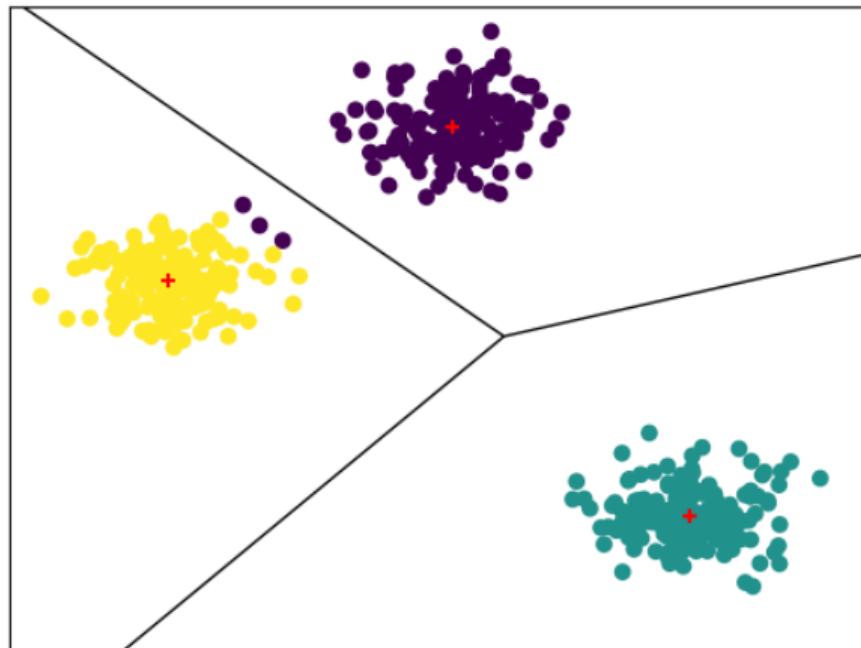
K-means



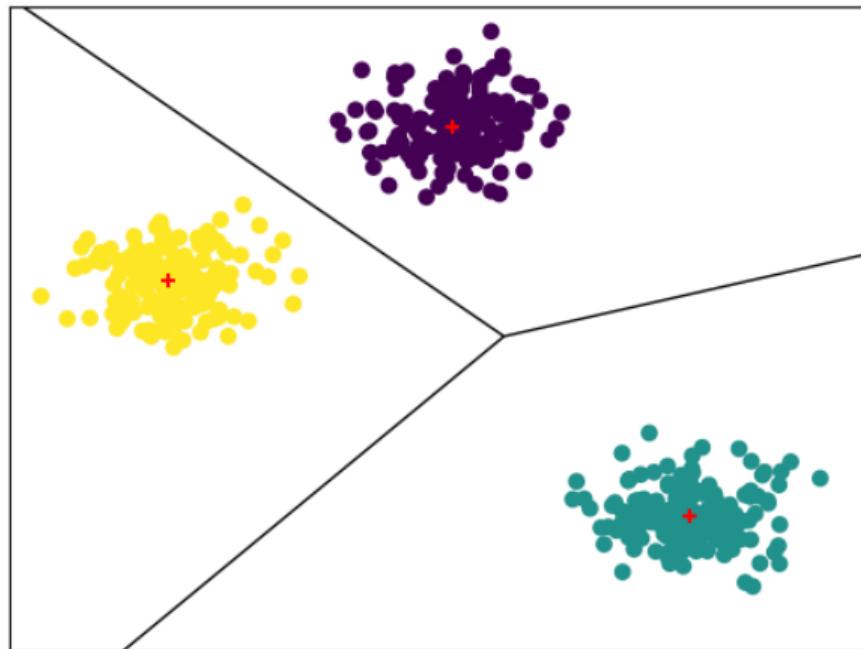
K-means



K-means



K-means



Determine the good K ? Elbow method

K-means advantages and drawbacks

Advantages

- fast

Drawbacks

K-means advantages and drawbacks

Advantages

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- scales well

Drawbacks

K-means advantages and drawbacks

Advantages

- fast
- scales well
- converges well

Drawbacks

K-means advantages and drawbacks

Advantages

- fast
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- robust

Drawbacks

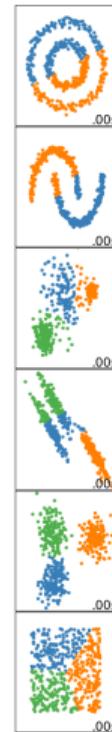
K-means advantages and drawbacks

Advantages

- fast
- scales well
- converges well
- robust

Drawbacks

- **not suited for non-linear data**



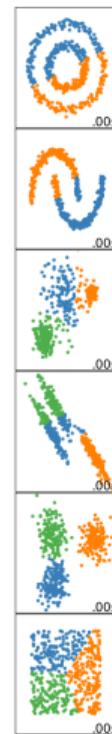
K-means advantages and drawbacks

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Drawbacks

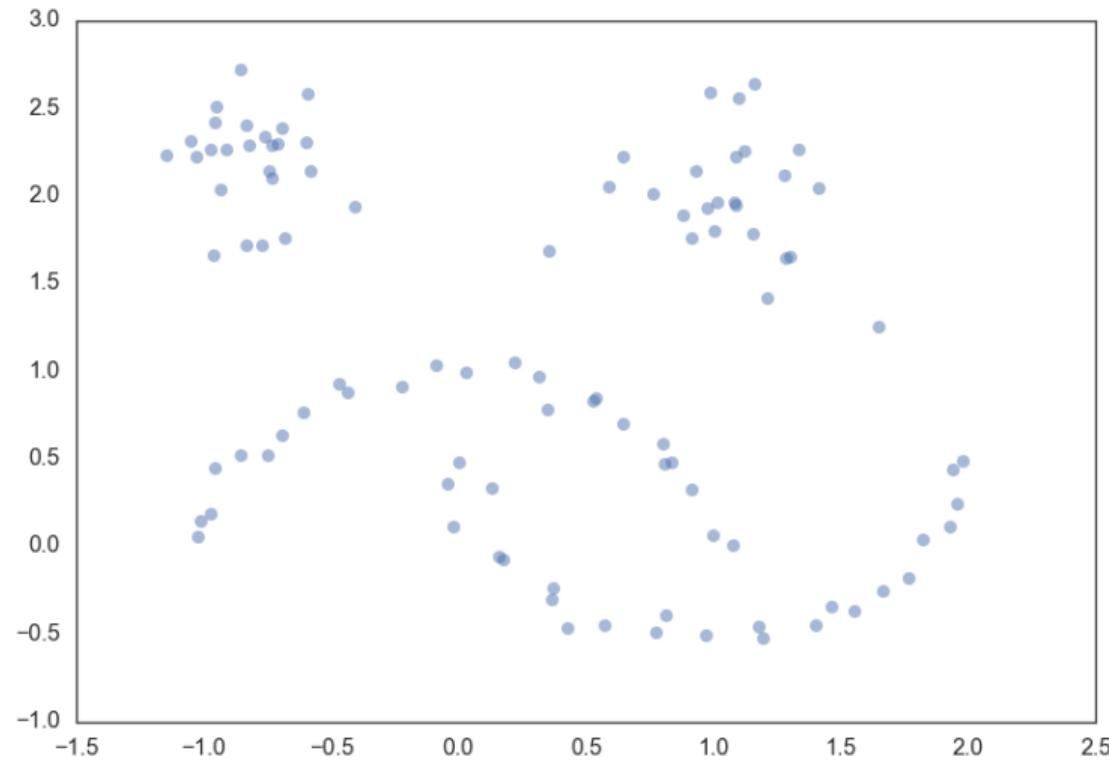
- **not suited for non-linear data**
→ Density based clustering



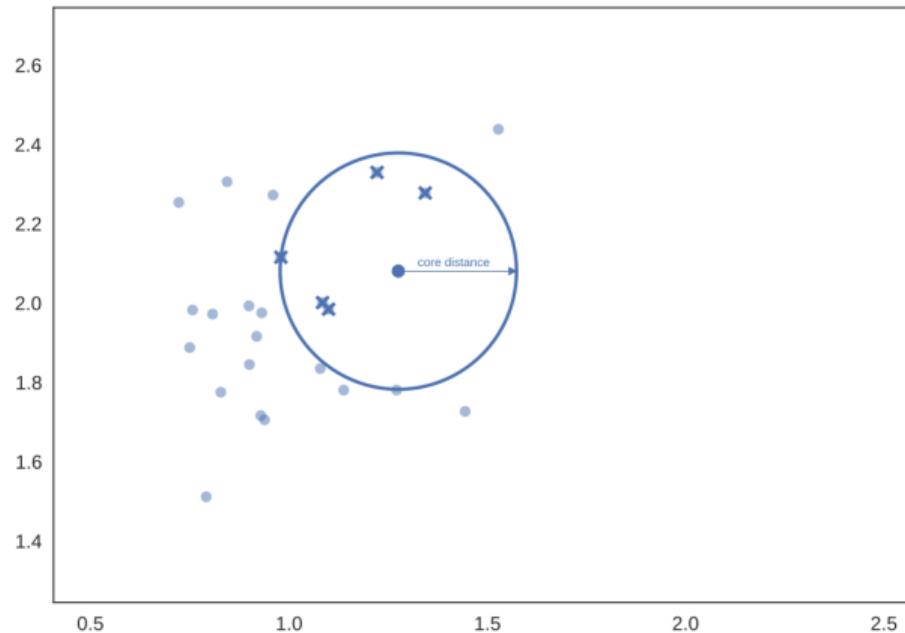
Clustering

HDBSCAN

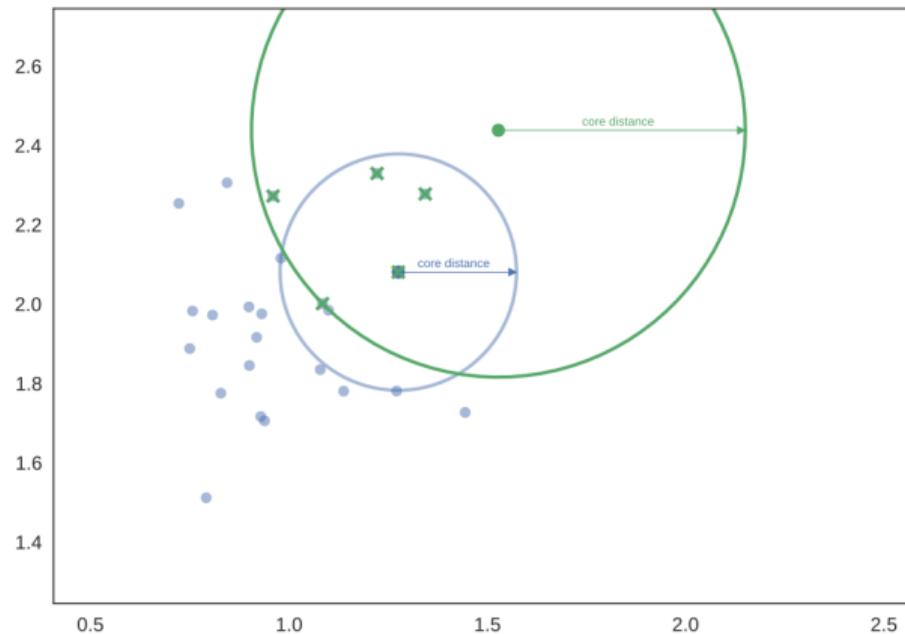
HDBSCAN



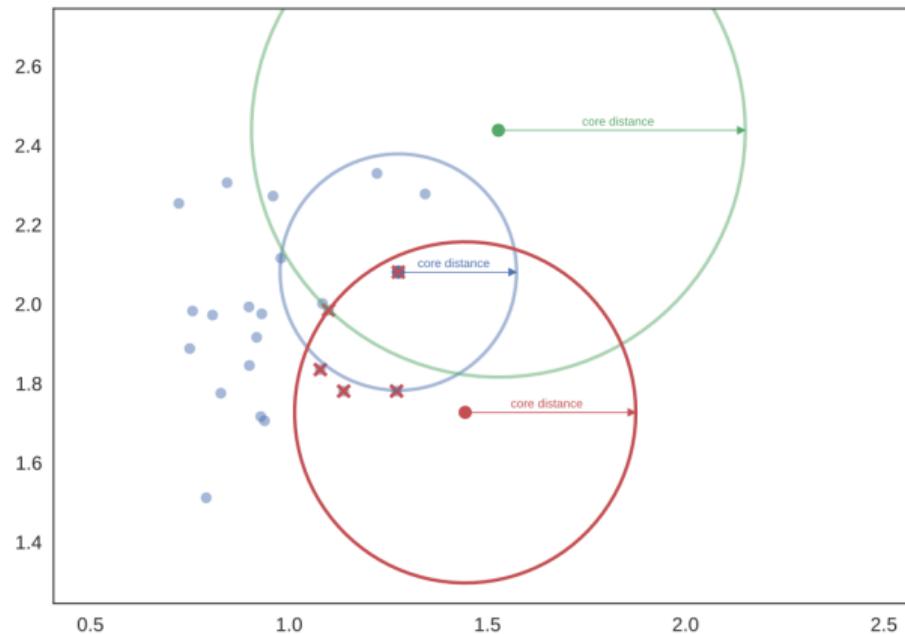
HDBSCAN



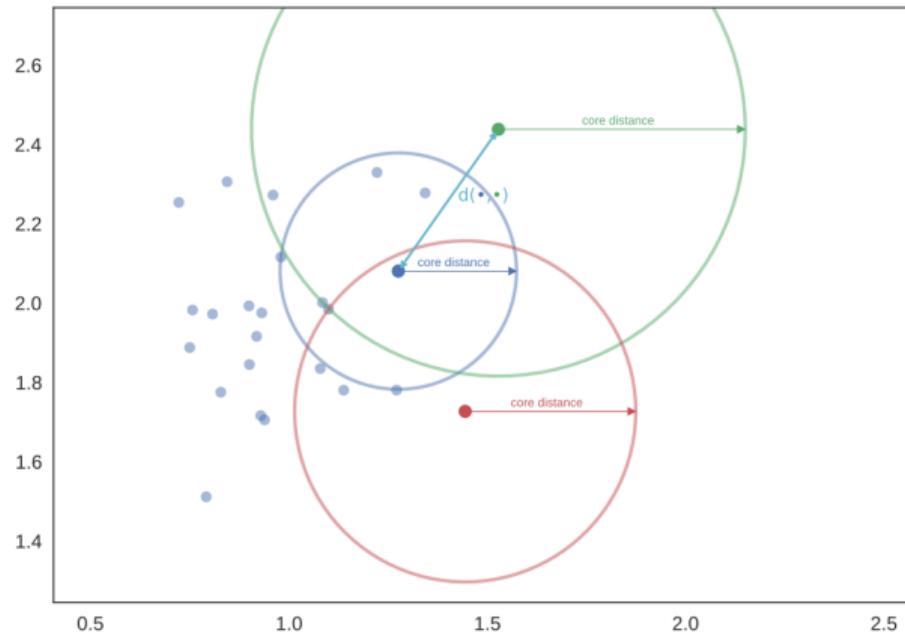
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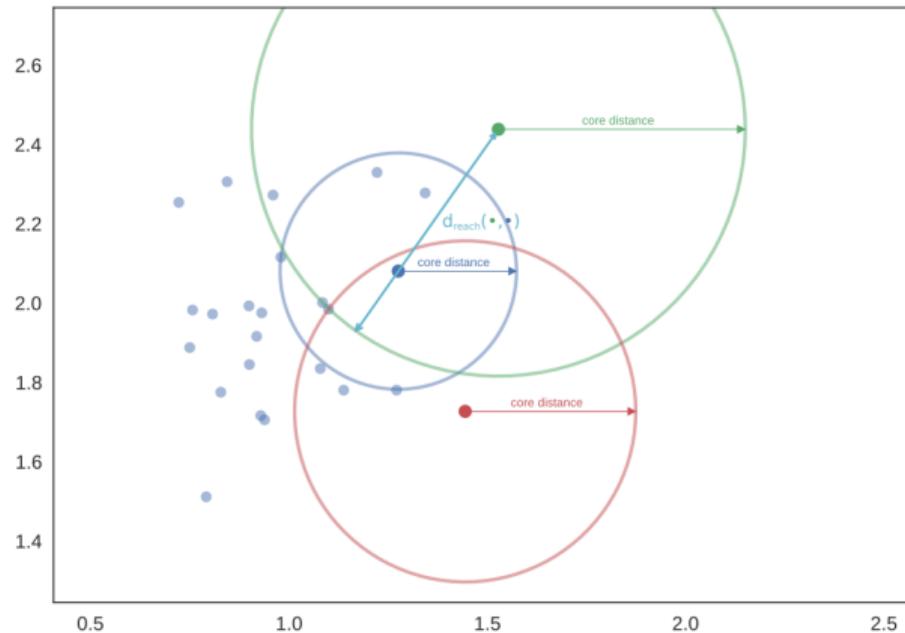
HDBSCAN



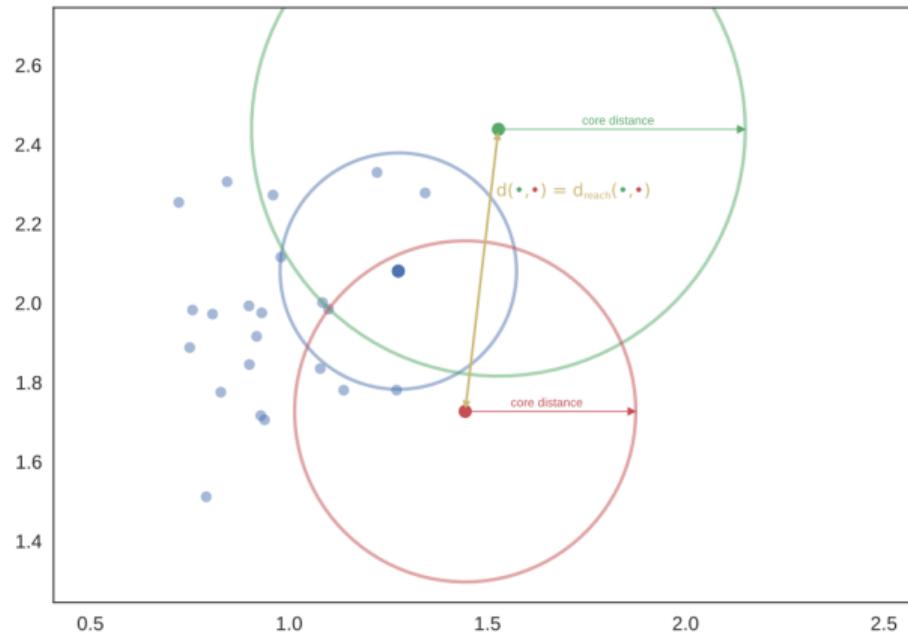
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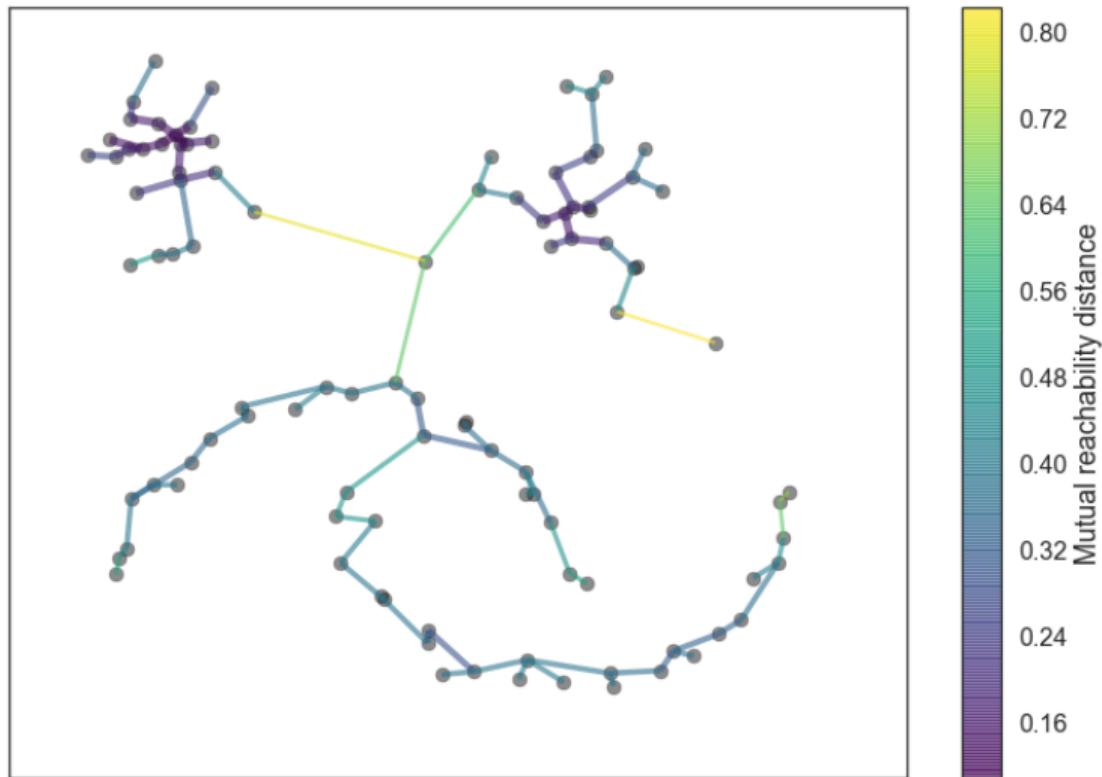
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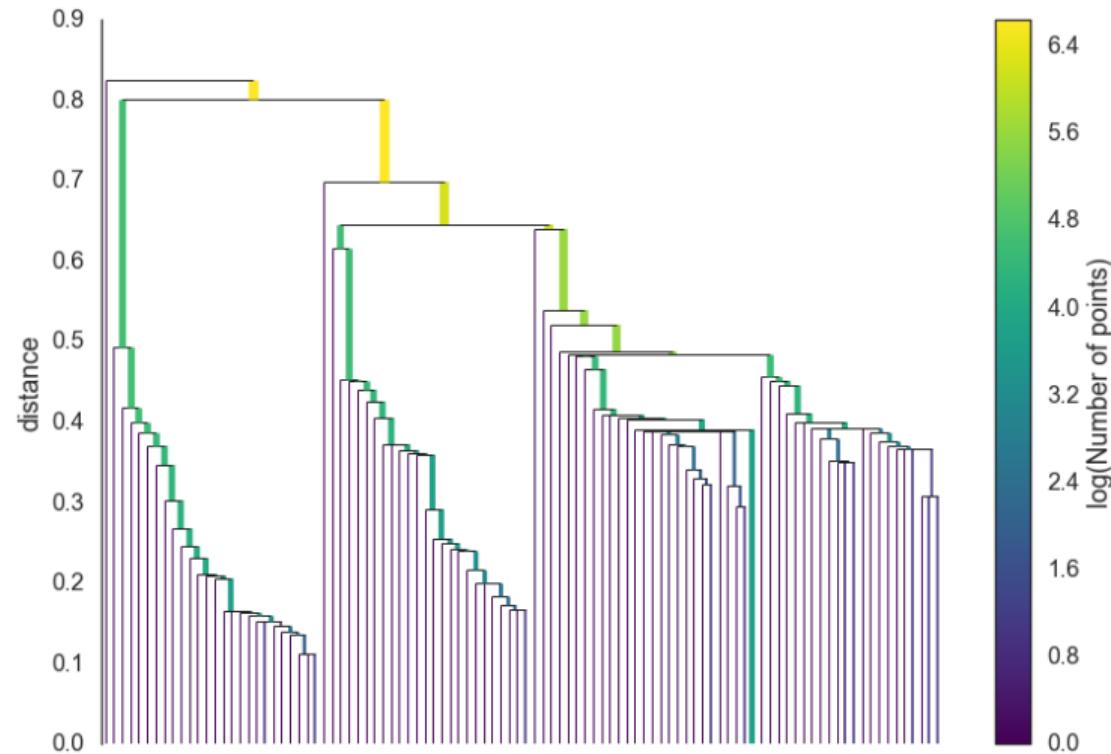
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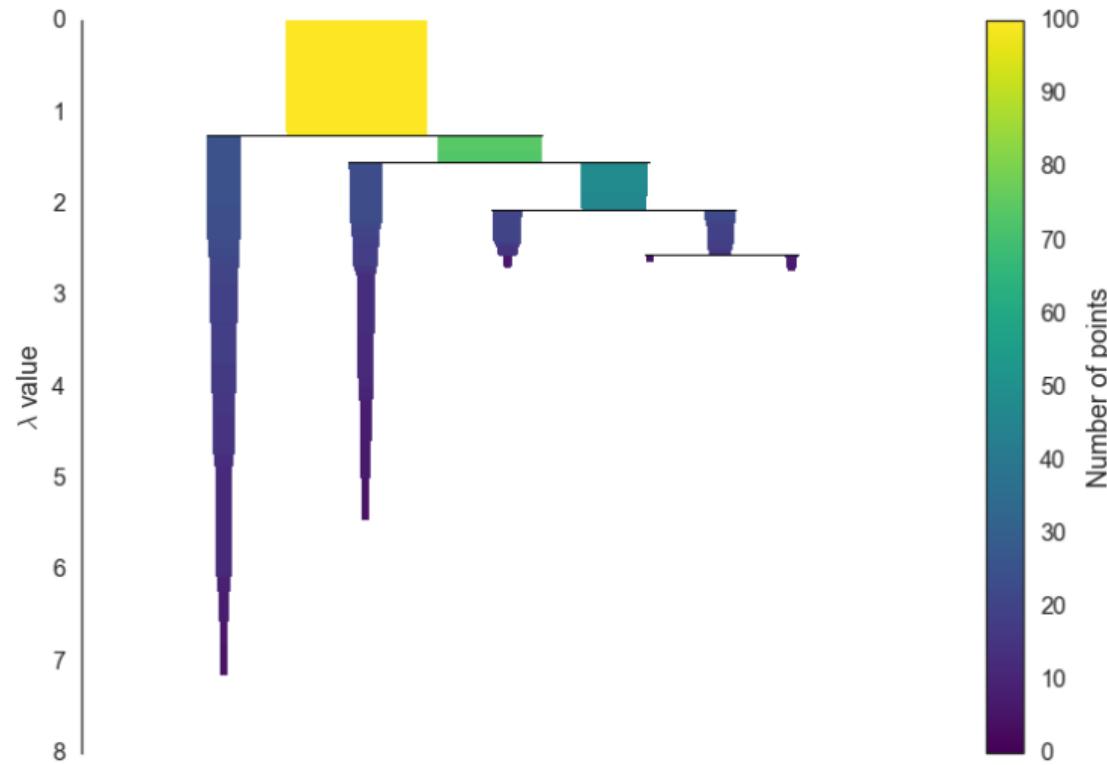
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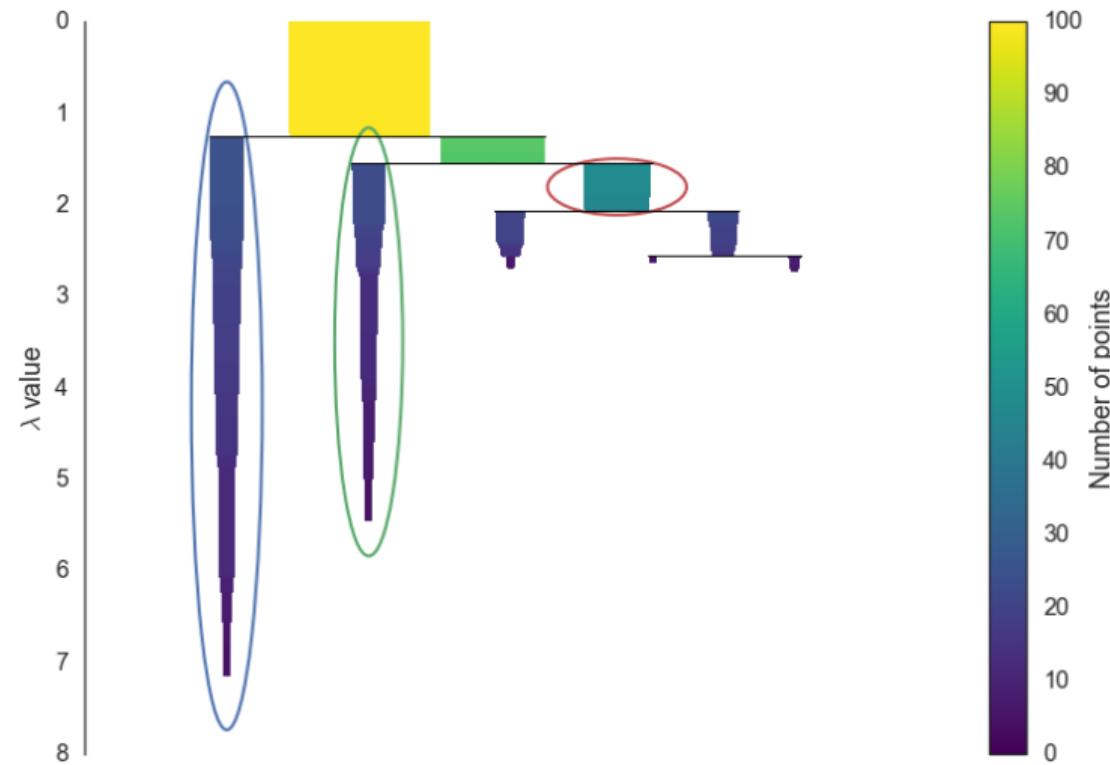
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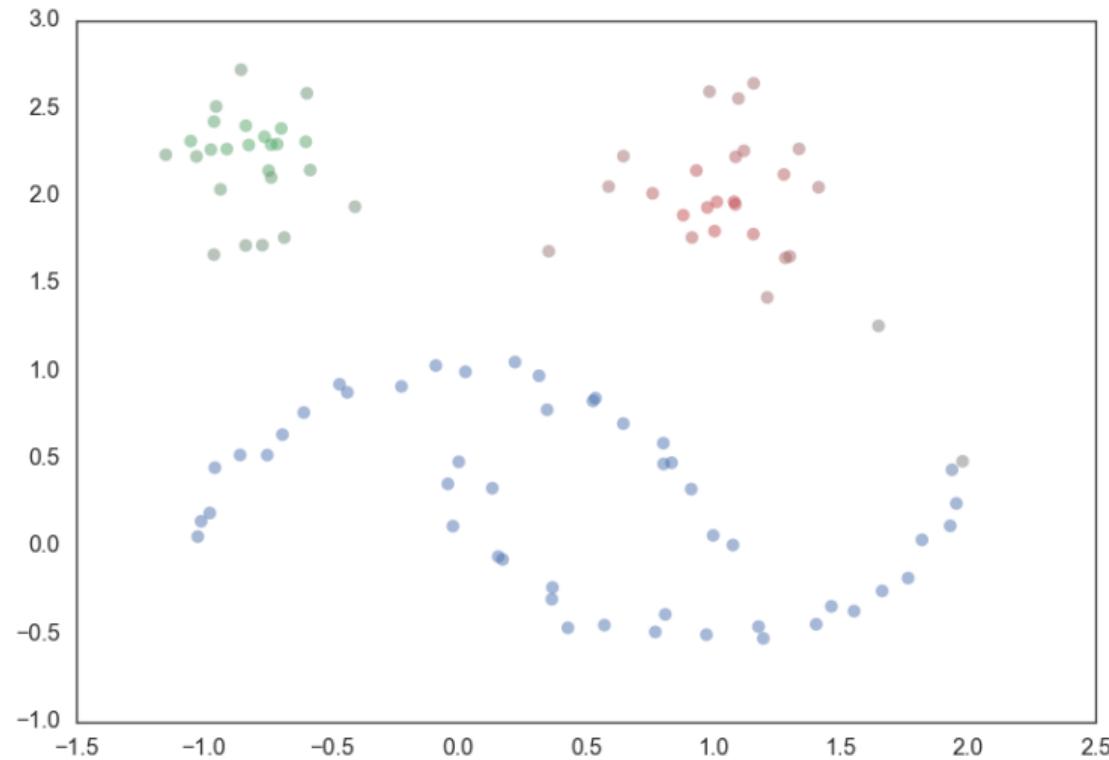
HDBSCAN



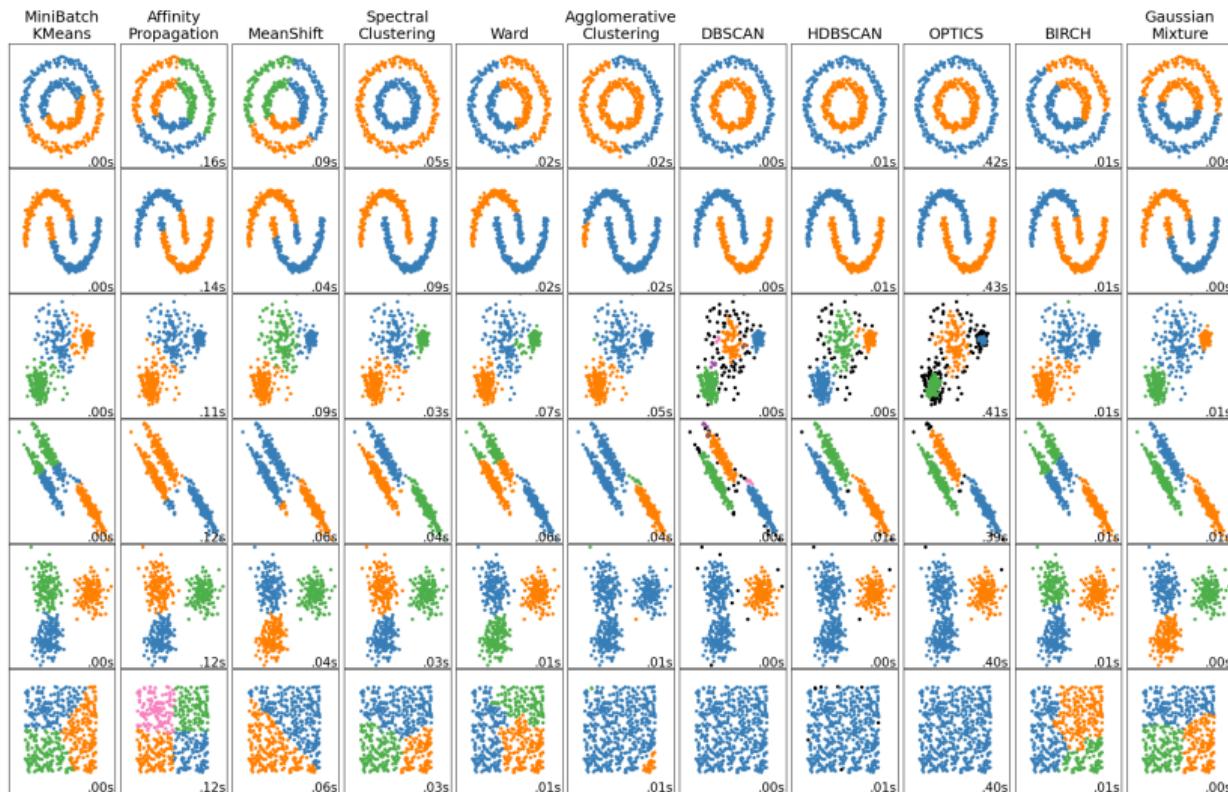
HDBSCAN



HDBSCAN



A lot of options !



Usefull ressources

- scikit-learn docs !
- deepia
- StatQuest

Thanks for you attention !

Let's practice !

References i

- Du, Trina Y (2019). “**Dimensionality reduction techniques for visualizing morphometric data: Comparing principal component analysis to nonlinear methods**”. In: *Evolutionary Biology* 46.1, pp. 106–121.
- Hinton, Geoffrey E and Sam Roweis (2002). “**Stochastic neighbor embedding**”. In: *Advances in neural information processing systems* 15.
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- Van der Maaten, Laurens and Geoffrey Hinton (2008). “**Visualizing data using t-SNE**”. In: *Journal of machine learning research* 9.11.