$Sprawozdanie-Piotr\ Tutak$ Scenariusz 2 – zagadnienie 1:

Użyte litery: c d f h l n q r s y B C D E I K N T Y Z

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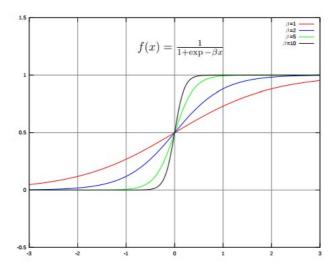
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Opis budowy:

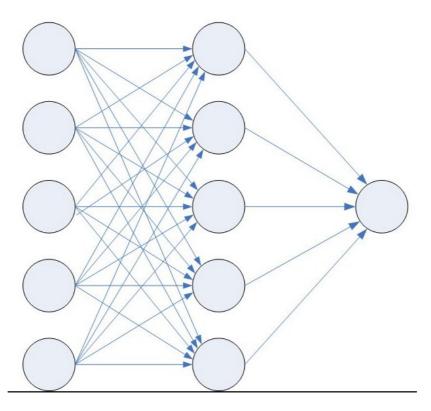
Sieć neuronowa składała się z 15 perceptronów z użytą funkcją aktywacji sigmoidalną ze współczynnikiem beta=1.0:

• Symetryczna sigmoida ($\lim_{x\to-\infty} \phi = -1$)

$$\phi(s) = \frac{1 - \exp(-\beta s)}{1 + \exp(-\beta s)}$$



Rysunek 1.4: Funkcja sigmoidalna z parametrami $\beta=1,\,\beta=3,\,\beta=10.$



Pierwsza warstwa perceptronów służyła jedynie do "wprzęgnięcia" wejścia, nie brała udziału w uczeniu, również ostatnia warstwa była jedynie wyjściem. Łącznie perceptronów w ukrytej warstwie było 15. Perceptronów wejściowych było 35.

Ostatni neuron był dwojakiego rodzaju, był to neuron z funkcją hard one, czyli:

$$f \cong x \mathfrak{D} \square \bigwedge_{i=0}^{\infty} 1 \operatorname{dla} x \geq 0$$
$$0 \operatorname{dla} x \square 0$$

Lub z funkcją identycznościową.

Wagi ostatniego neuronu były równe 1.0, współczynnik uczenia był równy 0.0. Pierwsze i ostatni neuron nie brały udziały w uczeniu sieci.

Algorytm uczenia odbywał się zgodnie ze wzorem:

$$w_1 += \eta * (d-y) * x_1$$

 $w_2 += \eta * (d-y) * x_2$

$$\theta$$
 += η * (*d-y*)

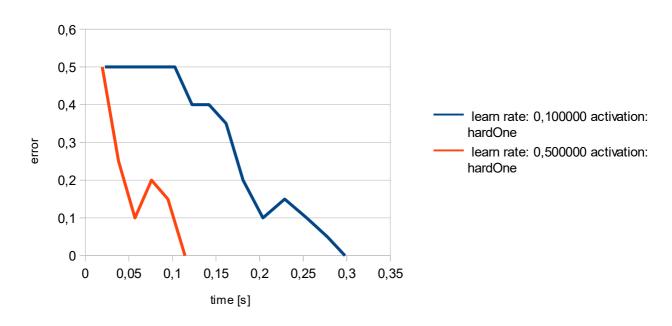
gdzie:

- $w_1, w_2... \text{wagi}$
- x_1, x_2 ... wartości wejściowe
- η niewielki współczynnik uczenia (n > 0)
- · *d* oczekiwana odpowiedź
- \cdot y odpowiedź neuronu
- θ próg wzbudzenia neuronu

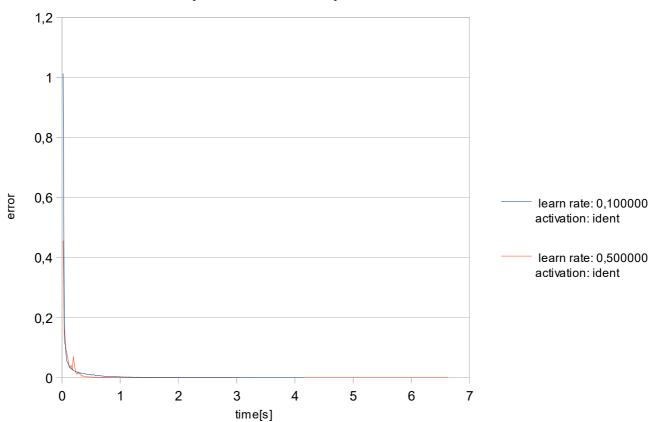
Testowane były w sumie 4 sieci neuronowe, po 2 dla współczynnika uczenia 0.1 i po 2 dla współczynnika uczenia 0.5 oraz po 2 dla funkcji końcowej hardOne, i po 2 dla funkcji identycznościowej. W przypadku funkcji identycznościowej uczenie dążyło by sieć zwracała albo wartość najbardziej zbliżoną do 1.0 albo do 0.0 w zależności od podawanej litery. Uczenie było przerywane przy wartości całkowitego błędu MSE dla wszystkich liter mniejszego od 0.0001

Wyniki:

Wykres wartości błędu MSE od czasu



Wykres zależności błędu MSE od czasu



Testowanie sieci:

Dane zaszumione w liczbie 5 pikseli

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Multilayer:
learnRate:0.10000
activFunc:hardOne
            14; time taken[s]:0.2980411653328474
iter number:
errors:
(letter, result, expected):
('h', 1.0, 0.0)
('y', 1.0, 0.0)
('C', 0.0, 1.0)
('W', 0.0, 1.0)
number of errors: 4
error value MSE: 0.2
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```
Multilayer:
learnRate:0.50000
activFunc:hardOne
iter number:
                6; time taken[s]:0.11453784536843159
errors:
(letter, result, expected):
('h', 1.0, 0.0)
('y', 1.0, 0.0)
('W', 0.0, 1.0)
number of errors: 3
error value MSE: 0.15
Multilayer:
learnRate:0.10000
activFunc:ident
iter number:
               201; time taken[s]:4.147680291568122
errors:
(letter, result, expected):
('a', 0.4003029132427893, 0.0)
('d', -0.0705466487190698, 0.0)
('h', 0.4249609164157855, 0.0)
('i', 0.9666831097365207, 0.0)
('1', 1.3219890469741231, 0.0)
('o', 0.2558906662628524, 0.0)
('p', -0.198042866868412, 0.0)
('w', 0.3341675070257659, 0.0)
('y', -0.05393175824373353, 0.0)
('z', 0.01715547055474631, 0.0)
('A', 1.2286040470108994, 1.0)
('C', 0.8191240746979747, 1.0)
('D', 1.1269092496421913, 1.0)
('F', 1.1820399676636804, 1.0)
('K', 0.8204157734561974, 1.0)
('O', 0.7876219049752287, 1.0)
('S', 1.1447620792745914, 1.0)
('W', 0.3743409644100484, 1.0)
('X', 1.1634058172152315, 1.0)
('Y', 1.333845963136409, 1.0)
number of errors: 20
error value MSE: 0.20048247147660062
Multilayer:
learnRate:0.50000
activFunc:ident
               336; time taken[s]:6.635513787529703
iter number:
errors:
(letter, result, expected):
('a', 0.7257317199848472, 0.0)
('d', -0.12398614084171711, 0.0)
```

('h', 0.6381558490452499, 0.0)

```
('i', 0.9421650016375748, 0.0)
```

('1', 0.8483597710343757, 0.0)

('o', -0.16071214628551567, 0.0)

('p', 0.27503213663414994, 0.0)

('w', 0.1512795117896355, 0.0)

('y', 0.5891148212548346, 0.0)

('z', 0.6114580244965981, 0.0)

('A', 1.038346055271147, 1.0)

('C', 0.8251904125100259, 1.0)

('D', 1.0046504620890355, 1.0)

('F', 1.1541203117080607, 1.0)

('K', 0.934210322829342, 1.0)

('O', 0.9392473891438692, 1.0)

('S', 1.0090556078334254, 1.0)

('W', 0.8251102425317566, 1.0)

('X', 0.9762899350559486, 1.0)

('Y', 0.9814794670483669, 1.0)

number of errors: 20

error value MSE: 0.17486905999303942

Analiza:

Jak widać sieć z funkcją aktywacji hardOne uczy się znacznie szybciej niż sieć z funkcją aktywacji sigmoidalną. Również zwiększenie współczynnika uczenia z 0.1 do 0.5 wpływa pozytywnie na szybkość uczenia sieci. Sieć z funkcją hardOne jest w stanie ostatecznie dobrze rozpoznać ponad 75% przypadków zaszumionych prawidłowo, natomiast sieć neuronowa z funkcją sigmoidalną nie rozpoznaje tych przypadków dokładnie a jedynie w sposób przybliżony. Ostatecznie jednak wartość błędu w obu przypadkach sieci i dla obu współczynników uczenia jest bardzo zbliżona i plasuje się na poziomie 0.15-0.20 jeśli chodzi o błąd MSE.

Sieć neuronowa z funkcją progową potrzebuje ok 0.15[s] by nauczyć się wszystkich przypadków i rozpoznawać je bezbłędnie. Sieć z funkcją ciągłą potrzebuje nawet do 7s by rozpoznawać przypadki z maksymalnym błędem równym 0.0001 (MSE), co jest znaczącą różnicą jeśli chodzi o zysk czasowy uczenia sieci – ok. 50krotny – natomiast procent rozpoznawania danych zaszumionych pozostaje na podobnym poziomie w obu przypadkach.

Wnioski:

- Jak widać najbardziej na czas uczenia i ilość potrzebnych przebiegów ma wybrana funkcja zbierająca wyniki i obliczająca wartość błędu:
 - w przypadku użycia funkcji granicznej (hardOne) sieć uczy się bardzo szybko i osiąga bardzo dobre wyniki w testach przy obu współczynnikach uczenia, zarówno 0.1 jak i 0.5
 - w przypadku użycia zwykłej sumy i funkcji identycznościowej sieć uczy się znacznie wolniej
- Sieć z funkcją końcową hardOne bardzo dobrze radzi sobie z klasyfikacją liter zaszumionych, natomiast dla sieci z funkcją identycznościową jest to trudniejsze zadanie, choć całkowita wartość błędu MSE jest ostatecznie bardzo zbliżona w przypadku obu sieci
- Zwiększenie współczynnika uczenia wpłynęło pozytywnie na oba rodzaje sieci pod względem testów na danych zaszumionych. Natomiast dla sieci z funkcją końcową identycznościową znacznie wydłużyło czas uczenia, dla sieci z funkcją hardOne – skróciło.

Użyta sieć:

Multilayer:

```
Layer(inputNumber:1, perceptronNumber:35, activFunc:hardOne, activFuncDeriv:zero, learnRate:0.00000)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights:[ 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000], bias:-0.50000, learnRate: 0.00000, activFunc: hardOne, activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.000001,bias:-0.50000,learnRate:0.00000,activFunc;hardOne,activFuncDeriv;zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne.activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: [1.00000], bias:-0.50000, learnRate: 0.00000, activFunc: hardOne, activFuncDeriv: zero)
  Perceptron(weights: [1.00000], bias:-0.50000, learnRate: 0.00000, activFunc: hardOne, activFuncDeriv: zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights:[ 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.000001,bias:-0.50000,learnRate:0.00000,activFunc;hardOne,activFuncDeriv;zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne.activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000], bias: -0.50000, learnRate: 0.00000, activFunc: hardOne, activFuncDeriv: zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
  Perceptron(weights: 1.00000],bias:-0.50000,learnRate:0.00000,activFunc:hardOne,activFuncDeriv:zero)
```

Layer(inputNumber:35, perceptronNumber:15, activFunc:signSigm(1.000), activFuncDeriv:signSigmDeriv(1.000), learnRate:0.10000 or 0.50000)

```
Perceptron(weights: 0.26928, 0.47171, -0.05028, 0.53446, 0.35564, 0.43071, -0.08592, -0.04487, 0.30404, -
0.03695, 0.74482, 0.51806, 0.32947, 0.27136, 0.34840, 0.61350, 0.89527, 0.68548, 0.68858, 0.80617, 0.50709,
0.63335, 0.01967, 0.52462, 0.58060, 0.46207, 0.78445, 0.53450, 0.54260, 0.87067, 0.59758, 0.45320, 0.78246,
0.45270, 0.69962],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv;signSigmDeriv(1.000))
                  Perceptron(weights: 0.47296, 0.40760, 0.41446, 0.66916, 0.88234, 0.17341, 0.50630, 0.14931, 0.60761,
0.40678, 0.06988, 0.39908, 0.52846, 0.53784, 0.15097, 0.10613, 0.37145, 0.63362, 0.09567, 0.16386, 0.23138,
0.27838, 0.05637],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
                  Perceptron(weights: 0.66682, 0.56927, 0.20252, 0.44448, 0.17188, 0.38047, 0.02411, 0.67469, 0.16549, 0.11777,
0.71727, 0.52862, 0.83467, 0.02065, 0.45466, 0.67310, 0.21865, 0.58927, 0.45410, 0.24048, 0.80033, 0.87806,
0.27702, 0.15158, 0.20151, 0.57086, 0.53620, 0.12908, 0.47518, 0.53320, 0.29060, 0.25854, 0.17780, 0.54619,
0.39209],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
                  Perceptron(weights: 0.10542, 0.07674, 0.06210, 0.46111, 0.46845, 0.36920, -0.08161, 0.11412, 0.84573, 0.31813,
0.02558, 0.52174, 0.17791, 0.59835, 0.76412, 0.00779, 0.54646, -0.02385, 0.37480, 0.54650, 0.54510, 0.44242, -0.02385, 0.37480, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.54650, 0.546500, 0.546500, 0.546500, 0.546500, 0.546500, 0.546500, 0.54600, 0.54600, 0.54600, 0.54600, 0.54600, 0.54600, 0.54600, 0.54600, 0.
0.01535, 0.62962, 0.61960, 0.58061, 0.51062, 0.39925, 0.32894, 0.10734, 0.12116, 0.11953, 0.72100, 0.61240, 0.01535, 0.02662, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.01960, 0.019600, 0.019600, 0.019600, 0.019600, 0.019600, 0.019600, 0.019600, 0.019600, 0.019600, 0.019600, 0.0196000
0.01731],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
                  Perceptron(weights: [0.55929, 0.19702, 0.69074, 0.70197, 0.34683, 0.46725, -0.06530, 0.33487, 0.00729, 0.22335,
0.05247, 0.36323, 0.54757, 0.32954, 0.25776, 0.46357, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.05247, 0.36323, 0.54757, 0.32954, 0.25776, 0.46357, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56381, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56881, 0.60283, 0.56874, -0.01359, 0.20992, 0.56626, 0.56881, 0.60283, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01359, 0.56874, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.01594, -0.015
0.24210, 0.33736, 0.48661, 0.69776, 0.27684, 0.66737, 0.10313, 0.17909, 0.02002, 0.34999, 0.41943, 0.70063,
0.11012],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
```

```
Perceptron(weights: 0.41971, 0.88702, 0.40966, 0.19770, 0.32976, 0.84578, 0.43859, 0.33020, 0.61625, 0.76607,
0.58785, 0.62340, 0.40442, 0.80887, 0.10292, 0.54376, 0.15530, 0.53487, 0.16066, 0.50325, 0.27430, 0.41400,
0.69553, 0.42108, 0.45592, 0.36584, -0.09547, 0.40517, 0.54755, 0.79923, 0.39672, 0.49726, 0.66151, 0.48122,
0.77263],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: [0.43871, 0.39380, 0.44571, 0.32012, 0.44937, 0.42731, 0.29211, 0.78879, 0.53685, 0.33691,
0.71153, 0.82298, 0.03724, 0.14652, 0.65097, 0.07829, 0.37188, 0.69802, 0.18192, 0.44675, 0.44993, 0.25178,
0.40501, 0.87293, -0.09003, 0.65962, 0.50981, 0.45167, 0.37036, 0.29617, -0.09205, -0.06841, 0.02751, 0.32266,
0.69456],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: 0.58740, 0.46967, 0.76585, 0.30557, 0.61193, 0.24260, 0.53565, 0.13956, 0.35912, 0.15549,
0.80632, 0.31711, 0.53110, 0.60966, 0.69272, 0.65411, 0.11553, 0.57990, 0.89998, 0.24193, 0.11648, 0.04221,
0.11433, 0.67785, 0.33605, 0.45848, 0.85537, 0.82075, 0.13886, 0.73275, -0.06366, 0.69217, 0.56413, 0.73300,
0.73863],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: [0.69036, 0.72290, 0.80859, 0.14907, 0.06003, 0.54275, 0.66674, 0.34913, 0.71693, 0.24548,
0.43617, 0.56011, -0.07397, 0.37389, 0.51001, 0.49779, 0.34339, 0.58519, 0.65757, 0.31347, 0.02250, 0.33408,
0.75345, 0.04484, 0.21513, 0.37272, 0.23030, 0.60043, 0.86723, -0.09276, -0.01826, 0.06949, 0.46738, 0.87370,
0.44459],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: 0.33890, 0.39709, 0.21708, 0.80742, 0.37789, 0.53115, 0.40360, 0.22832, 0.58172, 0.69949,
0.19768, 0.14247, 0.11534, 0.87104, 0.39576, 0.49242, 0.08769, 0.34599, 0.59007, -0.00253, 0.12450, 0.52743,
0.54953, 0.82678, 0.54162, 0.58454, 0.08552, 0.19365, 0.18150, 0.29599, 0.61460, 0.40497, 0.31029, 0.06644,
0.51998],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: 0.39178,-0.03502, 0.31493, 0.70809, 0.72055, 0.20872, 0.84911, 0.48142, 0.23622, 0.75280,
0.27212, -0.06354, 0.41919, 0.69369, 0.46894, 0.49077, 0.30816, 0.43258, 0.14590, 0.53129, 0.00903, 0.49146,
0.00444, -0.00425, 0.37452, 0.18276, 0.10754, 0.37232, 0.50623, 0.48598, 0.54841, 0.22722, 0.25636, 0.47142,
0.42938],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: 0.48094, -0.00479, 0.51667, 0.27046, 0.40603, 0.02767, 0.05975, 0.68226, 0.57310, 0.80570,
0.29536, 0.26770, 0.82653, 0.20734, 0.81729, 0.89375, 0.44354, 0.72123, 0.67369, 0.25213, 0.41401, 0.78174,
0.51586, -0.00217, 0.57164, 0.34430, 0.38046, 0.67067, 0.84532, 0.36054, 0.59864, 0.84984, 0.34213, 0.82002,
0.41749],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: 0.67687, 0.35784, 0.53619, 0.49974, 0.09618, 0.23936, 0.11645, 0.53015, 0.52998, 0.37464,-
0.06536, 0.06022, 0.58508, 0.57802, 0.15645, 0.47753, 0.11059, 0.20298, 0.86913, 0.33099, 0.40552, 0.30734,
0.61961, 0.05526, 0.43911, 0.67211, 0.43692, 0.61044, 0.50294, 0.31203, 0.33174, -0.09629, 0.46809, 0.67428,
0.52284],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: [-0.00816, 0.80433, 0.55585, 0.16349, 0.42838, 0.32982, 0.08756, 0.25956, 0.01074, 0.64941,
0.15871, 0.56169, 0.84784, 0.83748, 0.16358, 0.55715, 0.24708, 0.45867, 0.00318, 0.40684, 0.25625, 0.74984,
0.41258, 0.47078, 0.37182, 0.59524, 0.16693, 0.39714, 0.36841, 0.52461, 0.41698, 0.02624, 0.38357, 0.31631,
0.62249],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
     Perceptron(weights: [0.57968, 0.39193, 0.51424, 0.54423, 0.56927, 0.27404, 0.67974, 0.41023, 0.35466, 0.07853,
0.39482, 0.22319, 0.36074, 0.61903, 0.11176, 0.60789, -0.00130, 0.25307, 0.63136, 0.57944, 0.46828, 0.56321,
0.54962, 0.42840, 0.78501, 0.07578, 0.11028, 0.49377, -0.07297, 0.82753, 0.53444, 0.64362, 0.28032, 0.49553,
0.32910],bias:-0.05000,learnRate:0.10000,activFunc:signSigm(1.000),activFuncDeriv:signSigmDeriv(1.000))
```

Layer(inputNumber:15, perceptronNumber:1, activFunc: ident or hardOne, activFuncDeriv:one, learnRate:0.00000)
Perceptron(weights:[1.00000, 1.00000

Listing kodu:

```
# -*- coding: utf-8 -*-
Created on Sun Oct 22 11:20:52 2017
@author: PiotrTutak
from perceptron import *
from operator import itemgetter
import random
import time
import sys
import copy
#funkcja wypisująca zawartosc listy z zadaną precyzją
def listWithPrec(listA,prec):
  ret="["
  formatStr="{0: "+str(int(prec+3))+"."+str(int(prec))+"f}"
  for x in listA:
     ret+=formatStr.format(x)
     ret+=","
  ret=ret[:-1]+']'
  return ret
#funkcje liczace wartosci błędów
def MSE(results, expected):
  sum=0.0
  for i in range(len(results)):
     sum+=(results[i]-expected[i])**2
  return sum/len(results)
def MAPE(results, expected):
  sum=0.0
  for i in range(len(results)):
     sum+=abs((expected[i]-results[i])/expected[i])
  return 100*sum/len(results)
#przekierowanie wyjscia do pliku
STDOUT=sys.stdout
f=open('results.txt','w');
sys.stdout=f
literyLow=dict()
literyHigh=dict()
with open('litery.txt','r') as f:
  for 1 in f:
     x=l.strip().split('=')
     if x[0].islower():
       literyLow[x[0]]=[float(a) for a in x[1]]
     else:
       literyHigh[x[0]]=[float(a) for a in x[1]]
#utworzenie danych uczacych i testujacych
litery20=sorted(random.sample(list(literyLow.items()),10),key=itemgetter(0))
litery20.extend(sorted(random.sample(list(literyHigh.items()),10),key=itemgetter(0)))
litery20Expected=[[1.0] if x >9 else [0.0] for x in range(20)]
litery20ExpectedTest=[0.0 \text{ if } x \le 9 \text{ else } 1.0 \text{ for } x \text{ in range}(20)]
litery20Stirred=copy.deepcopy(litery20)
#liczba blednych pikseli w literze
```

```
NUMBER OF STIRR=5
for x in litery20Stirred:
  change=random.sample(set(range(35)),NUMBER OF STIRR)
  for c in change:
    if x[1][c]==0.0:
       x[1][c]=1.0
    else:
       x[1][c]=0.0
print('użyte litery:')
print(*list(x[0] for x in litery20),sep=' ')
print('\n')
for x in litery20:
  for j in range(5):
    for i in range(7):
       if x[1][j*7+i]:
         print(str(int(x[1][j*7+i]))+' ',end=")
         print(' ',end=")
    print(")
  print('\n')
listPerc=[]
RES_NUMBER=4
#przyjeta liczba perceptronow w warstwie
HIDDEN LAYER PERCEP NUMB=15
learnRate=0.5
multilayerOrig=Multilayer(
     [35,HIDDEN LAYER PERCEP NUMB,1],
     [hardOne,SignSigm()(1.0),hardOne],
     [zero,SignSigm().derivative(1.0),one],
     [[1.0],None,[1.0 for x in range(HIDDEN_LAYER_PERCEP_NUMB)]],
     [0.0,0.1,0.0],
     [-0.5, -0.05, 0.0]
#uczenie poszczegolnych warstw
while(len(listPerc)<RES NUMBER):
  multilayer=copy.deepcopy(multilayerOrig)
  print(multilayer)
  if len(listPerc)==1:
    multilayer[1]['learnRate']=0.5
  elif len(listPerc)==2:
    multilayer[2]['activFunc']=ident
  elif len(listPerc)==3:
    multilayer[2]['activFunc']=ident
    multilayer[1]['learnRate']=0.5
  i=0
  run=True
  start=time.clock()
  print('start learning:')
  print('iteration; time; error; learn rate: %f;'% (multilayer[1]['learnRate']))
  while(run):
    samples=list(litery20)
    while(run and samples):
       inp=random.sample(samples,1).pop(0)
       samples.remove(inp)
```

```
multilayer.learn(inp[1],litery20Expected[litery20.index(inp)])
    results=[]
     for inp in litery20:
       results.extend(multilayer.process(inp[1]))
     error=MSE(results,litery20ExpectedTest)
    if error<0.0001:
       run=False
    i+=1
    print("{0:9};{1: 8.5f}".format(i,time.clock()-start),error,sep=';')
  listPerc.append((multilayer,i,error,time.clock()-start))
  print("iter number: {0:8}".format(i),"; time taken[s]: {0:8}".format(time.clock()-start))
  print(")
print('\n\nTestowanie sieci:')
print('Dane zaszumione w liczbie %d pikseli' % NUMBER OF STIRR)
for x in litery20Stirred:
  for j in range(5):
     for i in range(7):
       if x[1][j*7+i]:
          print(str(int(x[1][j*7+i]))+'',end='')
       else:
          print(' ',end=")
     print(")
  print('\n')
#testowanie warstw na danych zaszumionych
for m in listPerc:
  res=[]
  errorCompute=[]
  print(repr(m[0]),end=")
  print("iter number: {0:8}".format(m[1]),"; time taken[s]: {0:8}".format(m[3]))
  print('errors:\n(letter, result, expected):')
  for s in litery20Stirred:
    res.append(m[0].process(s[1]))
     errorCompute.extend(m[0].process(s[1]))
  res=[(x[0],*y,*z) for x,y,z in zip(litery20,res,litery20Expected) if z[0]!=y[0]
  print(*res,sep='\n')
  print('number of errors:',len(res))
  print('error value MSE:',MSE(errorCompute,litery20ExpectedTest))
  print('\n')
f.close()
sys.stdout=STDOUT
```