In semantics, **extension** refers to the set of all real-world entities that a word or phrase can refer to. It's the collection of all things that fit a given description.

Extension vs. Intension

Extension is best understood in contrast to **intension**. This is a fundamental distinction in formal semantics and the philosophy of language.

- Extension (or Denotation): The set of all actual things in the world that a term applies to. For example, the extension of the word "dog" is every single dog that has ever existed, exists now, or will ever exist. The extension of the phrase "the current President of the United States" is the one person who holds that office at this moment.
- Intension (or Connotation): The set of properties or qualities that define a term. It is the concept or meaning of the word itself, separate from any specific entities. For example, the intension of "dog" is the conceptual meaning: a four-legged, domesticated canine. The intension of the phrase "the current President of the United States" is the concept of "the person who holds the office of the presidency in the U.S. at the present time."

The key relationship is that a word's **intension determines its extension**. The conceptual meaning of "dog" is what allows us to identify all individual dogs in the world.

Why this distinction matters:

- Words with No Extension: A word can have a clear intension but no extension. For example, the phrase "the present King of France" has a clear conceptual meaning (an intension), but because there is no king of France, its extension is the empty set (or null set).
- Different Intensions, Same Extension: Two different words or phrases can have different intensions but the same extension. For example, the phrases "the morning star" and "the evening star" have different conceptual meanings, but they both refer to the same object: the planet Venus. Therefore, their extension is the same.