SCSV3213

FUNDAMENTAL OF IMAGE PROCESSING

IMAGE ENHANCEMENT IN SPATIAL DOMAIN

Lecture 3 (week4-6)
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Acknowledgements

Most of the slide are taken and modified from other resources including books and slides from lectures from others universities. It is rearranged to suit the syllabus of the course.

SYNOPSIS

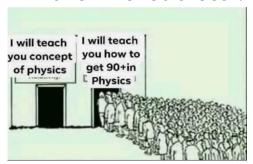
In this lecture, image enhancement operations in spatial domain will cover the followings

- 1. Point Processing
 - Arithmetic Processing
 - Histogram Processing
- 2. Neighborhood Operation
 - Fundamental of spatial filtering
 - Smoothing Spatial Filter
 - Sharpening Spatial Filters



An image worth thousands words !!! – Do you experience this??

WHICH ONE DO YOU CHOOSE!



Point Processing

- Remember this equation at the introduction lecture H(f(x,y)) = f(x,y)/2
- What does it tells ??
- The resulted operation is

•	me	rest	nte	ս Նի	refation is					١.
	6	8	2	0		3	4	1	0	
	12	200	20	10		6	100	10	5	ŀ

This is an example of point processing operation

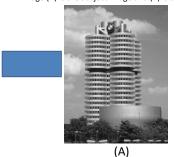
1. POINT PROCESSING

Point Processing

- Definition: Point processing is the operation that consider the pixel's value alone independent of the position of the pixel.
 - Example: g = t(f) % where t is the transformation operation
- Later we will see the different between point processing and neighborhood processing.
- For now we will use this definition for point processing.

Point operations

• Example: Can you guess what operation is applied to the image. Image (A) is the subject image and (B) is the resulted image





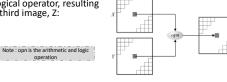
Point Processing

- The followings are the point processing operations covered in this lecture
 - Arithmetic and Logic operations
 - Addition and Subtraction
 - Multiplication and Division
 - AND , OR, XOR and NOT
 - Histogram operations
 - Histogram Stretching
 - Histogram Sliding
 - Histogram Shrinking
 - Histogram Equalization

1.1 ARITHMETIC AND LOGIC OPERATION

Arithmetic and logic operations

 Combine two images, pixelby-pixel, using an arithmetic or logical operator, resulting in a third image, Z:



X opn Y = Z

- · Or simply do operation with constant value to the image.
- H(f(x,y)) = f(x,y) opn A % A is constant

Arithmetic Operation: Addition

• H(f(x,y)) = f(x,y) + A

▶I = imread('cameraman.tif');
 ▶12 = I + 50;
 >subplot(1,2,1); imshow(I);
 >subplot(1,2,2);imshow(I2);

% read the image % 50 is a constant value %plot the images

•try see the max and min size of I and I2. You can find them using

- •function max(I(:)) and min(I(:)) or
- Just look at the workspace at the Matlab environment
- The value is capped to the max value for grey scale value ie 255.



Arithmetic Operation : Addition

Using imadd() function.

> I = imread('cameraman.tif');

> 12 = imadd(1,75);

> figure

> subplot(1,2,1), imshow(I), title('Original Image');

> subplot(1,2,2), imshow(i), title('Brighter Image');

•try see the max and min size of I

SIMILAR RESULT?





Arithmetic Operation : Addition

Handling overflow

Truncated

Normalized

$$g = \frac{L_{max}}{f_{max} - f_{min}} (f - f_{min})$$

> x = uint8([200 100 100; 0 10 50; 50 250 120])
> y = uint8([100 220 230; 45 95 120; 205 100 0])

> W = uint16(X) + uint16(Y)

> fmax = max(W(:))
> fmin = min(W(:))

> Za = uint8(255.0*double((W-fmin))/double((fmax-fmin)))

> Zb = imadd(X,Y)

Normalize the matric



Combining/ blend two images

Download the images at e-learning. Follow the script in the script1.txt #example4







Arithmetic Operation: Subtraction

- Used to used to detect differences between two images, decrease its overall brightness, or obtain its negative.
- Example 1 (subtractive image offset):





Z = X - 75

Arithmetic Operation : Subtraction

• Example (negative of an image):





Arithmetic Operation: Subtraction

- H(f(x,y)) = f(x,y) A.
- I = imread('cameraman.tif');
- > 12 = imsubtract(1,50);
- ➤ subplot(1,2,1), imshow(I), title('Original Image');
- > subplot(1,2,2), imshow(I2), title('Darker Image');



Use operator '-'

- Does the result the same?
- How do they (imsubtract & '-') cater the problem of negative value?

Arithmetic Operation: Subtraction

- What will happen to resulted image when two images are substracted. A = B - C?
- Let make a simple test.
- · Algorithm:
 - Open image A;
 - . Modify image A (ex. by making white stripe on the image) and save as
 - Subtract B from A and save to C. C = A B;
 - Plot all images
- · Write the Matlab code and see the result.

Arithmetic Operation: Subtraction

Subtracting two images

- A = imread('cameraman.tif');
- ➤ B = A;
- > B(130:160,:) = 255; B(:,130:160)=255;
- C = imsubtract(B,A);subplot(2,2,1);imshow(A);
- subplot(2,2,2);imshow(B);
- subplot(2,2,3:4);imshow(C);



Arithmetic Operation: Subtraction

Subtracting two images

- A = imread('cameraman.tif'); ➤ B = A; > B(130:160,:) = 255; B(:,130:160)=255; C = imsubtract(B,A); subplot(2,2,1);imshow(A); subplot(2,2,2);imshow(B); subplot(2,2,3:4);imshow(C);
- C= imsubtract(A,B);
- C=imabsdiff(A,B);
- > C=imcomplement(A); Explain the resulted image

Change this line to

Subtraction in MATLAB

- · Three functions:
 - imsubtract
 - -imabsdiff
 - imcomplement
- Example :

```
X = uint8([200 100 100; 0 10 50; 50 250 120])
Y = uint8([100 220 230; 45 95 120; 205 100 0])
Za = imsubtract(X,Y)
Zb = imsubtract(Y,X)
Zc = imabsdiff(Y,X)
```

Multiplication and division in MATLAB

- Functions:
 - immultiply
 - Imdivide

Example:









Combining arithmetic operations

- imlincomb function
- Example:

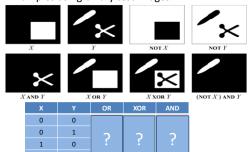
```
X = uint8([200 100 100; 0 10 50; 50 250 120])
Y = uint8([100 220 230; 45 95 120; 205 100 0])
Z = uint8([200 160 130; 145 195 120; 105 240 150])
Sa = imdivide(imadd(X,imadd(Y,Z)),3)
a = uint16(X) + uint16(Y)
b = a + uint16(Z)
Sb = uint8(b/3)
Sc = imlincomb(1/3,X,1/3,Y,1/3,Z,'uint8')
```

Logic operations

- Performed in a bit-wise fashion on the binary contents of each pixel value.
 - AND, XOR and OR require two or more arguments.
 - NOT operator only requires only one argument.
- The convention: 1 (true) for white pixels; 0 (false) for black pixels.

Logic operations

• Examples using binary test images



Logic operations on monochrome images

• Example 1 (AND)







· Explain the Images

Logic operations on monochrome images

• Example 2 (OR)







· Explain the Images

Logic operations on monochrome images

• Example 3 (XOR)







· Explain the Images

Logic operations on monochrome images

• Example 4 (NOT)





Image 2

Image 1

· Explain the Images

TUTORIAL ON ARITHMETIC AND LOGIC OPERATION

TUTORIAL 1: Addition

- Brighten an image using imadd()
- I = imread('tire.tif'); > 12 = im > figure

- subplot(1,2,1), imshow(I), title('Original Image');
 subplot(1,2,2), imshow(I2), title('Brighter Image');
- Blend 2 images
- > Ia = imread('rice.png');
- > Ib = imread('cameraman.tif');
 > Ic = imadd(la, lb);
- figure; subplot(2,2,1); imshow(la), title('Image 1');
 subplot(2,2,2),imshow(lb), title('Image 2');
- subplot(2,2,3:4),imshow(Ic), title('Blended Image');
- close all; % close all figures
- clear all; % clear all workspace variable

TUTORIAL 2: Subtraction

- Load two images and display them
- I = imread('cameraman.tif');
- J = imread('cameraman2.tif'); figure(1); subplot(1,2,1), imshow(I), title('Original Image');
- subplot(1,2,2), imshow(J), title('Altered Image');
- Subtract both image and display result
- diffim = imsubtract(I,J);
- > figure(2) > subplot(2,2,1), imshow(diffim), title('Subtracted Image');
- Zoom in the using zoom tool at the right area of the image. You should find a small region of pixel that is faintly white. Now use absolute diff function.
- diffim2 = imabsdiff(I,J);
- > subplot(2,2,2), imshow(diffim2), title('Abs Diff Image');
- Zoom in the using zoom tool at the right area of the image like before.
- Explain the different between the two functions.
- Can you make the faintly white region clearer?
- Write simple code to make the region white
- Close all figures and clear all variables.

TUTORIAL 3: Multiply

Comparing between normal brightening and dynamic brightening using multiply op

>I = imread('moon.tif'); >12 = imadd(I, 50);
>13 = immultiply(I, 1.2);

> subplot(1,3,1), imshow(i), title('Original Image'); > subplot(1,3,2), imshow(i2), title('Normal Brightening'); > subplot(1,3,3), imshow(i3), title('Dynamic Scaling');

· Blend two images using multiply op.

>I = im2double(imread('earth1.tif')); >J = im2double(imread('earth2.tif'));

K = immultiply(I,J);

> figure

> subplot(1,3,1), imshow(I), title('Planet Image'); > subplot(1,3,2), imshow(J), title('Gradient');

>subplot(1,3,3), imshow(K,[]), title('3D Planet');

TUTORIAL 4: Multiply and Division

Use division operation to dynamically darken the image

➤I = imread('moon.tif');
➤I2 = imdivide(I,2);

Figure

➤ subplot(1,3,1), imshow(I), title('Original Image');

>subplot(1,3,2), imshow(I2), title('Darker Image w/ Division');

Get the same result using multiply

≥13 = immultiply(1,0.5);

>subplot(1,3,3), imshow(I3), title('Darker Image w/ Multiplication');

TUTORIAL 5: Logic operation

· Use bitxor op to fiind the different of two images

>I = imread('cameraman.tif'); >12 = imread('cameraman2.tif');

>I_xor = bitxor(I,I2);

> figure; subplot(1,3,1), imshow(I), title('Image 1');
> subplot(1,3,2), imshow(I2), title('Image 2');

>subplot(1,3,3), imshow(I_xor,[]), title('XOR Image')

Make lindsay eyes dark

➤I = imread('lindsay.tif');

>I_adj = imdivide(I,1.5); >subplot(1,2,1); imshow(I);

>subplot(1,2,2); imshow(I adj);

bw = im2uint8(roipoly(I)); % Generate a mask by creating a region of interest polygor

>% Use logic operators to show the darker image only within the region of

➣% interest while displaying the original image elsewhere.

>bw_cmp = bitcmp(bw); >roi = bitor(I_adj,bw_cmp); %mask complement %roi image

%non_roi image >not_roi = bitor(I,bw);

>new_img = bitand(roi,not_roi); %generate new image

>imshow(new_img) %display new image

Test your understanding

- The code below add 4 moles for lindsay image..
- Write a simple code using arithmetic and logic operations to detect the position of the image by comparing both images.

>1 = imread('lindsay.tif'); >12=i; >12(166:167,176:177)=0; >12(166:167,145:146)=0; >12(56:57,176:177)=0; >12(13:124,115:116)=0; >figure; subplot(1,2,1);imshow(1); >subplot(1,2,2);imshow(12);

1.2. HISTOGRAM OPERATION

Histogram

- The histogram of a monochrome image is a graphical representation of the frequency of occurrence of each gray level in the image.
- The data structure that stores the frequency values is a 1D array of numerical values, h, whose individual elements store the number (or percentage) of image pixels that correspond to each possible gray level.

What is a histogram?

$$h(k) = n_k = \operatorname{card}\{(x,y)|f(x,y) = k\}$$

where:

k = 0, 1, ..., L – 1, where L is the number of gray levels of the digitized image; and $\operatorname{card}\{\cdots\}$ denotes the cardinality of a set, i.e. the number of elements in that set (n_k) . A normalized histogram can be mathematically defined as:

$$p(r_k) = \frac{n_k}{n}$$

where:

n = total number of pixels in the image; and $p(r_k)$ = probability (percentage) of the k-th gray level (r_k) .

What is a histogram?

$$h(k)=n_k=\mathrm{card}\{(x,y)|f(x,y)=k\}$$

where: $k=0,1,...,L-1, \text{ where } L \text{ is the number of gray levels of the digitized image; and card} \{\cdots\} \text{ denotes the cardinality of a set, i.e. the number of elements in that set } (n_k).$ A normalized histogram can be mathematically defined as:

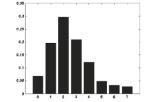
$$p(r_k) = \frac{n_k}{n}$$

n = total number of pixels in the image; and $p(r_k)$ = probability (percentage) of the k-th gray level (r_k) .

Histogram example

• Histogram for a hypothetical image containing 128×128 pixels and 8 gray levels.

Gray level (r_k)	n_k	$p(r_k)$
0	1120	0.068
1	3214	0.196
2	4850	0.296
3	3425	0.209
4	1995	0.122
5	784	0.048
6	541	0.033
7	455	0.028
Total	16384	1.000



Calculate the histogram of 8 grey level image of this image portion

3	3	4	4	4	4
4	4	3	3	3	6
4	4	5	5	3	1
4	4	5	6	6	1
6	6	5	5	5	6
6	6	5	5	5	5

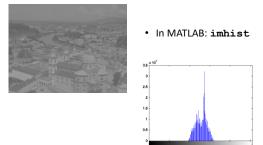
Grey Level (n_k)	n_k	$P(r_k)$
0		
1		
2		
3		
4		
5		
6		
7		
Total		

Calculate the histogram of 8 grey level image

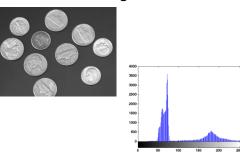
3	3	4	4	4	4
4	4	3	3	3	6
4	4	5	5	3	1
4	4	5	6	6	1
6	6	5	5	5	6
6	6	5	5	5	5

•		
Grey Level (n_k)	n_k	P(r_k)
0	0	0.00
1	2	0.05
2	0	0.00
3	6	0.17
4	10	0.28
5	10	0.28
6	8	0.22
7	0	0.00
Total	36	1.00

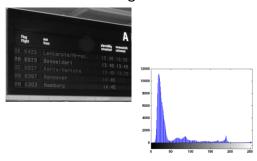
Examples of images and their histograms



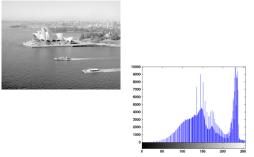
Examples of images and their histograms



Examples of images and their histograms



Examples of images and their histograms



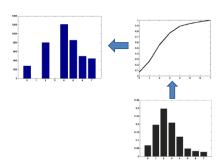
Interpreting image histograms

- Histograms have become a popular tool for conveying image statistics and helping determine certain problems in an image.
- A histogram carries significant qualitative and quantitative information about the corresponding image (e.g., minimum, average, and maximum gray level values, dominance of bright or dark pixels, etc.).
- A histogram is not enough to draw qualitative conclusions about the overall quality of the image, presence or absence of noise, etc.

Interpreting image histograms

- Although a histogram provides the frequency distribution of gray levels in an image, it tells us nothing about the spatial distribution of the pixels whose gray levels are represented in the histogram.
- Histograms can be used whenever a statistical representation of the gray level distribution in an image is desired.
- Histograms can also be used to enhance or modify the characteristics of an image, particularly its contrast.

Histogram equalization



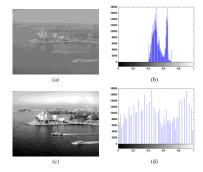
Histogram equalization

• In MATLAB: histeq

```
I = imread('sydney_low_contrast.png');
I = im2double(I);
J = histeq(I);
figure, subplot(2,2,1), imshow(I), ...
subplot(2,2,2), imshow(J), ...
subplot(2,2,2), imshow(I), ...
subplot(2,2,3), imshist(I), ylim('auto'),...
subplot(2,2,4), imshist(J), ylim('auto')
```

Histogram equalization

• Example:



Global vs. local histogram equalization

 In MATLAB: histeq and adapthisteq

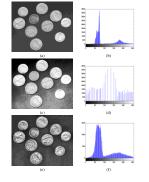
```
I = imread('coins.png');
figure, subplot(1,2,1), imshow(I), ...
subplot(1,2,2), imhist(I), ylim('auto')

J = histeq(I);
figure, subplot(1,2,1), imshow(J), ...
subplot(1,2,2), imhist(J), ylim('auto')

K = adapthisteq(I);
figure, subplot(1,2,1), imshow(K), ...
subplot(1,2,2), imhist(K), ylim('auto')
```

Global vs. local histogram equalization

• Example :



Direct histogram specification

• Example

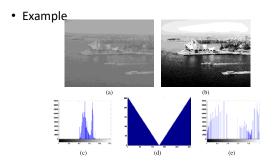


Direct histogram specification

• In MATLAB: histeq

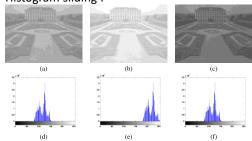
• Example:

Direct histogram specification



Other histogram modification techniques

· Histogram sliding:



Histogram sliding

- In MATLAB: imadd and imsubtract
- Example:

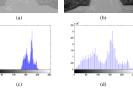
Other histogram modification techniques

· Histogram stretching:







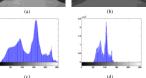


Other histogram modification techniques

· Histogram shrinking:







Histogram stretching and shrinking

• In MATLAB: imadjust

% Histogram stretching
I = imread('schonbrunn_gray_low_contrast.png');
figure, imhist(I), ylim('auto'), title ('Original histogram');
12 = imadjust(I);
figure, imhist(I2), ylim('auto'), title ('After histogram stretching');
figure, subplot(1,2,1), imshow(I), subplot(1,2,2), imshow(I2)

% Histogram shrinking
I = imread('schonbrunn_gray.png');
figure, imhist(I), ylim('auto'), title ('Original histogram');
Id = im2double(I);
Jd = im2double(I);
J = uint8(255.*3d);
figure, imhist(J), ylim('auto'), title ('After histogram shrinking');
figure, subplot(1,2,1), imshow(I), subplot(1,2,2), imshow(J)

TUTORIAL ON HISTOGRAM

TUTORIAL 6: Displaying Histogram

Displaying an image and its histogram using 256 bins

```
> I = imread('circuit.tif');
> figure, subplot(2,2,1), imshow(I), title('Image')
> subplot(2,2,2), imhist(I,256), axis tight, title('Histogram')
```

· Using different bins

```
> subplot(2,2,3), imhist(1,64), axis tight, ...
> title('Histogram with 64 bins')
> subplot(2,2,4), imhist(1,32), axis tight, ...
> title('Histogram with 32 bins')
```

Get the value of the hist to C and normalize the value

```
>c = imhist(I,32);
>c_norm = c / numel(I);
```

TUTORIAL 6: continue

Displaying using bar chart

```
> figure, subplot(1,2,1), bar_1 = bar(c);
> set(gca, 'XLim', [0 32], 'YLim', [0 max(c)]);
> set(gca, 'XTick', [0:8:32], 'YTick', ...
> [linspace(0,700.8) max(c)]);
> set(bar_1, 'FaceColor', 'r'), title('Bar Chart')
> subplot(1,2,2), bar_2 = bar(c_norm);
> set(gca, 'XTick', [0:8:32], 'YTick', ...
> [linspace(0,0.09,10) max(c_norm)])
> xlim([0 32]), ylim([0 max(c_norm)])
> title('Normalized Bar Chart')
> set(bar_2, 'FaceColor', 'g')
```

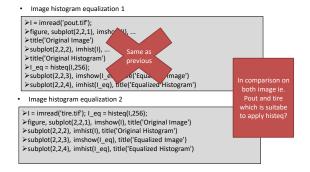
TUTORIAL 7: Hist Equalization

Image histogram equalization

```
> I = imread('pout.tif');
> figure, subplot(2,2,1), imshow(I), ...
> title('Original Image')
> subplot(2,2,2), imshist(I), ...
> title('Original Histogram')
> I_eq = histeq(I,256);
> subplot(2,2,3), imshow(I_eq), title('Equalized Image')
> subplot(2,2,4), imshist(I_eq), title('Equalized Histogram')
```

Explain the effect ..

TUTORIAL 7: continue



TUTORIAL 8: Hist modification

· Addition / sliding in histogram

TUTORIAL 9: Hist modification

Histogram sliding

```
%continue ffrom previous exmple
> const = 0.5;
> | 3 = | 1 + const;
> bad_values = find(|3 > 1);
> | 3(|bad_values) = 1;
> subplot(|3,2.5), imshow(|3), title('Original Image + 0.5')
> subplot(|3,2.6), imhist(|3), axis tight, ...
> title('Original Hist + 0.5')
```

TUTORIAL 10: Hist modification

· Histogram streching

```
➤img_limits = stretchlim(I);
▶I_stretch = imadjust(I,img_limits,[]);
> figure; subplot(3,2,1), imshow(I), title('Original Image')
> subplot(3,2,2), imhist(I), axis tight, ...
≻title('Original Histogram')
>subplot(3,2,3), imshow(I_stretch), ...
➤title('Stretched Image')
>subplot(3,2,4), imhist(I_stretch), axis tight, ...
➤ title('Stretched Histogram')
▶% Perform histogram stretching with _imadjust_ using default parameters and
>% confirm that the results are identical to the ones obtained before.
➤I_stretch2 = imadjust(I);
>subplot(3,2,5), imshow(I_stretch2), ...
➤title('Stretched Image')
➤ subplot(3,2,6), imhist(I_stretch2), axis tight, ...
> title('Stretched Histogram')
> I_stretch_diff = imabsdiff(I_stretch, I_stretch2);
> figure, imshow(I_stretch_diff,[])
 >min(I_stretch_diff(:))
> max(I_stretch_diff(:))
```

TUTORIAL 11: Hist modification

```
Histogram shrinking

I = imread('salzburg.npg');

I_shrink = imadjust(l,stretchlim(l),[0.25 0.75]);

Figure; subplot(2,2,1), imshow(l), title('Original Image')

Subplot(2,2,2), imshist(l), axis tight, ...

Hitle('Original Histogram')

Subplot(2,2,3), imshow(l_shrink), ...

Hitle('Shrunk Image')

Subplot(2,2,4), imhist(l_shrink), axis tight, ...

Hitle('Shrunk Histogram')

Whitle('Shrunk Histogram')

Whitle('Strunk Histogram')

Whitle('Shrunk His
```

TUTORIAL 12: Hist modification

Histogram shrinking with gamma value

Histogram shrinking with gamma value

| L_shrink = imadjust(I,stretchlim(I),[0.25 0.75],2);
| X = reshape(I,1,prod(size(I)));
| Y = reshape(I_shrink,1,prod(size(I_shrink)));
| Figure |
| Subplot(2,2,1), imshow(I), title('Original Image') |
| Subplot(2,2,2), imhist(I), axis tight, ... |
| Hitle('Original Histogram') |
| Subplot(2,2,3), imshow(I_shrink), title('Adjusted Image') |
| Subplot(2,2,4), imhist(I_shrink), axis tight, ... |
| Hitle('Adjusted Histogram') |
| Figure, plot(X,Y,'.'), xlim([0 255]), ylim([0 255])

End Part 1: **Spatial Domain Enhancemnet** SCSV 3213