A quaternion-indicative solution for null points illustrating negative low-energy states for the electron

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This letter proposes a mathematical hypothesis for null points in an electrical circuital arrangement under the influence of magnetic field induction. The formalism is used a means to describe uniquely coupled fields that manifest a planar waves perpendicular to the angle of propagation. The quaternion method for computing the longitudinal wave is supported by the differential method. The solution indicates the circuital arrangement satisfies Dirac's contention of negative-energy electron states where charges are posited at their lowest energy at minimal velocity.

I. THE CIRCUITAL MODEL

Consider the circuital configuration shown in Fig.1 of the case of two solenoids: The first consists of a sinusoidal winding at a given angle between successive turns along its length; the second consists of a single strand of wire affixed in such a manner as to have regular divisions cross along the length. The first coil, the primary, has leads on each end while the second coil, the secondary, has both leads toward one end while at its extremity, loops back.

The approximation consists of a primary coil tightly wound with wire of a radius much smaller than its length such that the distance between turns is nearly zero and that the angle, Connections to each end of the primary coil extend outward so they can be connected to external equipment and components. The secondary coil is wound with a wide spacing between turns: The first traversal along the length coincides with the center line of the structure; the second traversal loops back along the length crossing the same center line such that there are a series of crossed wires, as shown in Fig.1. Connections to the same end of the secondary coil extend outward from the coil where they can be connected to external equipment and components.

A series of experiments are conducted to illustrate the contention of electromagnetic phenomena at the interface of the secondary coil as sinusoidal currents are applied to the primary, following the mathematical analysis. The experiment strives to answer the following questions: Due to Faraday, as the emission of energy from a primary-secondary sinusoidal coil is well-known, what is the case when the secondary has such a winding? When a continuous electromagnetic signal is applied to the primary, what is the character of the electromagnetic wave induced in the secondary? What kind of special character, if any, would the secondary exhibit patterns that have not been accounted for in Faraday's research but that which might be still covered by Maxwell? Does the wave exhibit this character because of the influence upon electrons moving in contradictory motion at the crossing of the wire in the secondary? Can the mathematical framework of this special character be described by ordinary vector analysis or it is necessary to call upon other analytical tools from the period? Can the analysis yield the contention that there are observable null points in

this circuital configuration?

II. THE MATHEMATICAL MODEL

In consideration of the circuital arrangement described in the previous section, the applied electromagnetic wave at the primary, via a signal generator in the range of 2 - 9MHz, is imagined to consist as a plane wave of the general form of the three-dimensional wave equation

$$\frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} + \frac{\partial^2 f}{\partial z^2} - \frac{1}{c^2} \frac{\partial^2 f}{\partial t^2} = 0.$$
 (1)

The wave equation can be derived from Maxwell's equations in free space and in the absence of charges and currents, beginning with Faraday's equation. The spatial frequency of the plane wave is given by

$$E(x,z) = \exp\left\{i\frac{2\pi}{\lambda}\left(x\sin\theta + z\cos\theta\right)\right\}$$
$$= \exp\left\{i2\pi\left(\frac{x}{\lambda}\right)\right\},$$
 (2)

where,

$$\Lambda \approx \frac{\lambda}{\sin \theta}.\tag{3}$$

As the wave induced in the secondary is similar in character to the one in the primary, there is a minimum of superpositioning where,

$$a\cos(k_1z - \omega_1t) \approx a\cos(k_2z - \omega_2t)$$
. (4)

Given the rather ordinary treatment, what can be said about the result of these waves interacting? Let's examine the arrangement without the "scaffolding" Ampère introduced into the process. Given Tait [1] (§453-456) the equation of coaxial circular currents [2, 3] is

ii'dsds' $\frac{1}{r^2(\sin\theta\sin\theta'\cos\omega+k\cos\theta\cos\theta')}$,

Inline math may be typeset using the \$ delimiters. Bold math symbols may be achieved using the bm package and the \bm{#1} command it supplies. For instance, a

bold α can be typeset as ∞ giving α . Fraktur and Blackboard (or open face or double struck) characters should be typeset using the $\mathrm{mathfrak}\{\#1\}$ and $\mathrm{mathbb}\{\#1\}$ commands respectively. Both are supplied by the amssymb package. For example, $\mathrm{mathbb}\{R\}$ gives \mathbb{R} and $\mathrm{mathfrak}\{G\}$ gives \mathfrak{G}

In LATEX there are many different ways to display equations, and a few preferred ways are noted below. Displayed math will center by default. Use the class option fleqn to flush equations left.

$$\left\{ab12345678abc123456abcdef\alpha\beta\gamma\delta1234556\alpha\beta\frac{1\sum_{b}^{a}}{A^{2}}\right\}.$$

When the \label{#1} command is used [cf. input for Eq. (1)], the equation can be referred to in text without knowing the equation number that TEX will assign to it. Just use \ref{#1}, where #1 is the same name that used in the \label{#1} command.

Unnumbered single-line equations can be typeset using the $\[\]$ format:

$$g^+g^+ \to g^+g^+g^+g^+\dots$$
, $q^+q^+ \to q^+g^+g^+\dots$

A. Multiline equations

Multiline equations are obtained by using the equarray environment. Use the \nonumber command at the end of each line to avoid assigning a number:

$$\mathcal{M} = ig_Z^2 (4E_1 E_2)^{1/2} (l_i^2)^{-1} \delta_{\sigma_1, -\sigma_2} (g_{\sigma_2}^e)^2 \chi_{-\sigma_2} (p_2) \times [\epsilon_j l_i \epsilon_i]_{\sigma_1} \chi_{\sigma_1} (p_1), \tag{6}$$

$$\sum |M_g^{\text{viol}}|^2 = g_S^{2n-4}(Q^2) N^{n-2}(N^2 - 1)$$

$$\times \left(\sum_{i < j}\right) \sum_{\text{perm}} \frac{1}{S_{12}} \frac{1}{S_{12}} \sum_{\tau} c_{\tau}^f . \quad (7)$$

Note: Do not use \label{#1} on a line of a multiline equation if \nonumber is also used on that line. Incorrect cross-referencing will result. Notice the use \text{#1} for using a Roman font within a math environment.

To set a multiline equation without *any* equation numbers, use the \begin{eqnarray*}, \end{eqnarray*}

format:

$$\begin{split} \sum |M_g^{\rm viol}|^2 &= g_S^{2n-4}(Q^2) \ N^{n-2}(N^2-1) \\ &\times \left(\sum_{i < j}\right) \left(\sum_{\rm perm} \frac{1}{S_{12}S_{23}S_{n1}}\right) \frac{1}{S_{12}} \ . \end{split}$$

To obtain numbers not normally produced by the automatic numbering, use the $\text{tag}\{\text{#1}\}$ command, where #1 is the desired equation number. For example, to get an equation number of (2.6'),

 $g^+g^+ \to g^+g^+g^+g^+\dots$, $q^+q^+ \to q^+g^+g^+\dots$. (2.6') a. A few notes on tags \tag{#1} requires the amsmath package. Place the \tag{#1} command before the \label{#1}, if any. The numbering produced by \tag{#1} does not affect the automatic numbering in REVTEX; therefore, the number must be known ahead of time, and it must be manually adjusted if other equations are added. \tag{#1} works with both single-line and multiline equations. \tag{#1} should only be used in exceptional cases—do not use it to number many equations in your paper. Please note that this feature of the amsmath package is not compatible with the hyperref (6.77u) package.

Enclosing display math within \begin{subequations} and \end{subequations} will produce a set of equations that are labeled with letters, as shown in Eqs. (8b) and (8a) below. You may include any number of single-line and multiline equations, although it is probably not a good idea to follow one display math directly after another.

$$\mathcal{M} = ig_Z^2 (4E_1 E_2)^{1/2} (l_i^2)^{-1} (g_{\sigma_2}^e)^2 \chi_{-\sigma_2}(p_2)$$

$$\times [\epsilon_i]_{\sigma_1} \chi_{\sigma_1}(p_1).$$
(8a)

$$\left\{abc123456abcdef\alpha\beta\gamma\delta1234556\alpha\beta\frac{1\sum_{b}^{a}}{A^{2}}\right\},\qquad(8b)$$

Giving a \label{#1} command directly after the \begin{subequations}, allows you to reference all the equations in the subequations environment. For example, the equations in the preceding subequations environment were Eqs. (8).

1. Wide equations

The equation that follows is set in a wide format, i.e., it spans the full page. The wide format is reserved for long equations that cannot easily be set in a single column:

$$\mathcal{R}^{(d)} = g_{\sigma_2}^e \left(\frac{[\Gamma^Z(3,21)]_{\sigma_1}}{Q_{12}^2 - M_W^2} + \frac{[\Gamma^Z(13,2)]_{\sigma_1}}{Q_{13}^2 - M_W^2} \right) + x_W Q_e \left(\frac{[\Gamma^{\gamma}(3,21)]_{\sigma_1}}{Q_{12}^2 - M_W^2} + \frac{[\Gamma^{\gamma}(13,2)]_{\sigma_1}}{Q_{13}^2 - M_W^2} \right) . \tag{9}$$

This is typed to show how the output appears in wide

format. (Incidentally, since there is no blank line between

the equation environment above and the start of this paragraph, this paragraph is not indented.)

III. CROSS-REFERENCING

REVTEX will automatically number such things as sections, footnotes, equations, figure captions, and table captions. In order to reference them in text, use the \label{#1} and \ref{#1} commands. To reference a particular page, use the \pageref{#1} command.

The \label{#1} should appear within the section heading, within the footnote text, within the equation, or within the table or figure caption. The \ref{#1} command is used in text at the point where the reference is to be displayed. Some examples: Section I on page 1, Table I, and Fig. 1.

IV. FLOATS: FIGURES, TABLES, VIDEOS, ETC.

Figures and tables are usually allowed to "float", which means that their placement is determined by LATEX, while the document is being typeset.

Use the figure environment for a figure, the table environment for a table. In each case, use the \caption command within to give the text of the figure or table caption along with the \label command to provide a key for referring to this figure or table. The typical content of a figure is an image of some kind; that of a table is an alignment.

Insert an image using either the graphics or graphix packages, which define the \includegraphics{#1} command. (The two packages differ in respect of the optional arguments used to specify the orientation, scaling, and translation of the image.) To create an alignment, use the tabular environment.

The best place to locate the figure or table environment is immediately following its first reference in text; this sample document illustrates this practice for Fig. 1,

TABLE I. A table that fits into a single column of a two-column layout. Note that REVTEX 4 adjusts the intercolumn spacing so that the table fills the entire width of the column. Table captions are numbered automatically. This table illustrates left-, center-, decimal- and right-aligned columns, along with the use of the ruledtabular environment which sets the Scotch (double) rules above and below the alignment, per APS style.

Left ^a	$Centered^b$	Decimal	Right
1	2	3.001	4
10	20	30	40
100	200	300.0	400

^a Note a.

which shows a figure that is small enough to fit in a single column.

In exceptional cases, you will need to move the float earlier in the document, as was done with Table II: LATEX's float placement algorithms need to know about a full-page-width float earlier.

Fig. 2 has content that is too wide for a single column, so the figure* environment has been used.

The content of a table is typically a tabular environment, giving rows of type in aligned columns. Column entries separated by &'s, and each row ends with \\. The required argument for the tabular environment specifies how data are aligned in the columns. For instance, entries may be centered, left-justified, right-justified, aligned on a decimal point. Extra column-spacing may be be specified as well, although REVTFX 4 sets this spacing so that the columns fill the width of the table. Horizontal rules are typeset using the \hline command. The doubled (or Scotch) rules that appear at the top and bottom of a table can be achieved enclosing the tabular environment within a ruledtabular environment. Rows whose columns span multiple columns can be typeset using the $\mbox{\mbox{multicolumn}{#1}{#2}{#3}\ \mbox{command (for example, see}$ the first row of Table II).

Tables I, II, III, and IV show various effects. A table that fits in a single column employs the table environment. Table II is a wide table, set with the table* environment. Long tables may need to break across pages. The most straightforward way to accomplish this is to specify the [H] float placement on the table or table* environment. However, the LATEX 2_{ε} package longtable allows headers and footers to be specified for each page of the table. A simple example of the use of longtable can be found in the file summary.tex that is included with the REVTEX 4 distribution.

There are two methods for setting footnotes within a table (these footnotes will be displayed directly below the table rather than at the bottom of the page or in the bibliography). The easiest and preferred method is just to use the \footnote{#1} command. This will automatically enumerate the footnotes with lowercase roman letters. However, it is sometimes necessary to have multiple entries in the table share the same footnote. In this case, there is no choice but to manually create the footnotes using \footnotemark[#1] and \footnotetext[#1]{#2}. #1 is a numeric value. Each time the same value for #1 is used, the same mark is produced in the table. The \footnotetext[#1]{#2} commands are placed after the tabular environment. Examine the LaTeX source and output for Tables I and IV for examples.

Video 1 illustrates several features new with REVTEX4.2, starting with the video environment, which is in the same category with figure and table. The

 ${
m FIG.}$ 1. A figure caption. The figure captions are automatically numbered.

^b Note b.

FIG. 2. Use the figure* environment to get a wide figure that spans the page in twocolumn formatting.

TABLE II. This is a wide table that spans the full page width in a two-column layout. It is formatted using the table* environment. It also demonstates the use of \multicolumn in rows with entries that span more than one column.

	D_{z}^{2}	$1 \\ 4h$	D	$\frac{5}{4h}$
Ion	1st alternative	2nd alternative	lst alternative	2nd alternative
K	(2e) + (2f)	(4i)	(2c) + (2d)	(4f)
Mn	$(2g)^{\mathrm{a}}$	(a) + (b) + (c) + (d)	(4e)	(2a) + (2b)
Cl	(a) + (b) + (c) + (d)	$(2g)^{\mathrm{a}}$	$(4e)^{a}$	
$_{\mathrm{He}}$	$(8r)^{\mathrm{a}}$	$(4j)^{\mathrm{a}}$	$(4g)^{\mathrm{a}}$	
Ag		$(4k)^{\mathrm{a}}$		$(4h)^{a}$

^a The z parameter of these positions is $z \sim \frac{1}{4}$.

Video 1. Students explain their initial idea about Newton's third law to a teaching assistant. Clip (a): same force. Clip (b): move backwards.

\setfloatlink command causes the title of the video to be a hyperlink to the indicated URL; it may be used with any environment that takes the \caption command. The \href command has the same significance as it does in the context of the hyperref package: the second argument is a piece of text to be typeset in your document; the first is its hyperlink, a URL.

Physical Review style requires that the initial citation of figures or tables be in numerical order in text, so don't cite Fig. 2 until Fig. 1 has been cited.

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We wish to acknowledge the support of the author community in using REVTEX, offering suggestions and encouragement, testing new versions,

TABLE III. Numbers in columns Three–Five are aligned with the "d" column specifier (requires the dcolumn package). Non-numeric entries (those entries without a ".") in a "d" column are aligned on the decimal point. Use the "D" specifier for more complex layouts.

One	Two	Three	Four	Five
one	two	$_{ m three}$	four	five
$_{\mathrm{He}}$	2	2.77234	45672.	0.69
C^{a}	$C_{\rm p}$	12537.64	37.66345	86.37

^a Some tables require footnotes.

Appendix A: Appendixes

To start the appendixes, use the \appendix command. This signals that all following section commands refer to appendixes instead of regular sections. Therefore, the \appendix command should be used only once—to setup the section commands to act as appendixes. Thereafter normal section commands are used. The heading for a section can be left empty. For example,

\appendix \section{}

will produce an appendix heading that says "APPENDIX A" and

\appendix \section{Background}

will produce an appendix heading that says "APPENDIX

TABLE IV. A table with numerous columns that still fits into a single column. Here, several entries share the same footnote. Inspect the IATEX input for this table to see exactly how it is done.

	r_c (Å)	r_0 (Å)	κr_0		r_c (Å)	r_0 (Å)	κr_0
Cu	0.800	14.10	2.550	Sna	0.680	1.870	3.700
Ag	0.990	15.90	2.710	$\mathrm{Pb^{b}}$	0.450	1.930	3.760
Au	1.150	15.90	2.710	Ca^{c}	0.750	2.170	3.560
Mg	0.490	17.60	3.200	$\mathrm{Sr^d}$	0.900	2.370	3.720
Zn	0.300	15.20	2.970	Li^{b}	0.380	1.730	2.830
Cd	0.530	17.10	3.160	Na^{e}	0.760	2.110	3.120
$_{\mathrm{Hg}}$	0.550	17.80	3.220	K^{e}	1.120	2.620	3.480
Al	0.230	15.80	3.240	Rb^{c}	1.330	2.800	3.590
Ga	0.310	16.70	3.330	Cs^d	1.420	3.030	3.740
In	0.460	18.40	3.500	$\mathrm{Ba^e}$	0.960	2.460	3.780
Tl	0.480	18.90	3.550				

 $^{^{\}rm a}$ Here's the first, from Ref. ? .

^b Some tables need more than one footnote.

 $^{^{\}rm b}$ Here's the second.

^c Here's the third.

^d Here's the fourth.

^e And etc.

A: BACKGROUND" (note that the colon is set automatically).

If there is only one appendix, then the letter "A" should not appear. This is suppressed by using the star version of the appendix command (\appendix* in the place of \appendix).

Appendix B: A little more on appendixes

Observe that this appendix was started by using

\section{A little more on appendixes}

Note the equation number in an appendix:

$$E = mc^2. (B1)$$

1. A subsection in an appendix

You can use a subsection or subsubsection in an appendix. Note the numbering: we are now in Appendix B 1.

Note the equation numbers in this appendix, produced with the subequations environment:

$$E = mc,$$
 (B2a)

$$E = mc^2, (B2b)$$

$$E \gtrsim mc^3$$
. (B2c)

They turn out to be Eqs. (B2a), (B2b), and (B2c).