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Article

## **Title**

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Abstract: To be completed.

**Keywords:** Gauge equation, spectral sequence, KV-cohomology, hessian manifold, statistical manifold.

1. Introduction

1.1. Notations and writing conventions

All manifolds are assumed to be smooth. Thorough this document, the next writing conventions are applied: M is a smooth manifold. For a vector bundle  $E \xrightarrow{\pi} M$ , the notation  $\Gamma(U;E)$  with  $U \subset M$  an open subset of the manifold M stands for the  $C^{\infty}(M)$ -module of smooth sections over U. The functor  $U \mapsto \Gamma(U;E)$  defines a sheaf denoted by  $\Gamma_E$ . Finally,  $\Gamma(E)$  is a shorthand notation for  $\Gamma(M;E)$ . Lowercase letters are used for sections, uppercase ones for tangent vectors.

## 2. The gauge equation

Let  $E \xrightarrow{\pi} M$  be a vector bundle. An affine connection  $\nabla$  is a  $\mathbb{R}$ -linear mapping:

$$\nabla \colon \Gamma(E) \to \Gamma(T^*M \otimes E) \tag{1}$$

such that for any  $f \in C^{\infty}(M)$ , any  $s \in \Gamma(E)$  and any tangent vector X,  $\nabla_X f s = X(f) s + f \nabla_X s$ . Let  $E^{\star} \xrightarrow{\pi^{\star}} M$  be the bundle obtained by dualizing E fiberwise. A section  $\theta \in \Gamma(E^* \otimes E)$ , that is a (1,1)-tensor, defines two bundle morphisms:

$$E \xrightarrow{\theta} E \qquad E^{\star} \xrightarrow{\theta^{t}} E^{\star}$$
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(2)

where  $\theta_{R}^{t}$  is such that for any  $p \in M$ ,  $X \in T_{p}M$ ,  $\xi \in T_{p}^{\star}M$ :

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$$\left(\theta_p^t \xi\right)(X) = \xi\left(\theta_p X\right)$$
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$$(3)$$

**Definition 2:** Int. Let  $20\overline{M}_{1by}$  behar couple of affine connections. A (1,1)-tensor  $\theta$  is said to be a solution to the gauge equation.

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- 3. KV cohomologyms and conditions
- 4. A spectral sequence ommons Attri-
- 5. Application 46 statistical intanifolds

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References

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