

Day 1: Big-O; Search

→ Binary Search

find "19" [2, 3, 5, 7, 11, 13, 17, 19]
mid
7 < 13
discard

[11, 13, 17, 19]
mid
13 < 19
discard

[17, 19]
mid
17 < 19

[19]
✓
found 19

pseudocode

1. calculate midpoint
 $\rightarrow \text{len(array)}$
 $\text{mid} = \frac{n}{2}$ if n is even
 $= \left\lfloor \frac{n}{2} \right\rfloor$ if n is odd
2. if $\text{array}[\text{mid}] == \text{target}$:
 terminate with "success"
3. if $\text{array}[\text{mid}] < \text{target}$:
 $\text{array} \leftarrow \text{array}[\text{mid}+1:]$
4. if $\text{array}[\text{mid}] > \text{target}$:
 $\text{array} \leftarrow \text{array}[:\text{mid}]$
5. repeat 1 to 4 if
 $\text{len(array)} > 0$

Binary Search Patterns:

I Rotated Sorted arrays:

e.g. $[4, 5, 6, 7, 8, 1, 2]$
left mid right

target = 1

$arr[left] \leq arr[mid]$

but target not in the range!

Takeaway:

Even when rotated, we know 3 things about a sorted array: leftmost, middle, rightmost elements

And hence we can find a target or pivot by comparisons

$[8, 1, 2]$
left mid right

$arr[mid] < arr[right]$

target within this range.

$[1, 2]$
mid right
left

$arr[mid] = target$

index (5)

↖ pivot[^] wouldn't be known beforehand

1. determine whether it's left- or right-rotated

2. if $array[mid] \geq array[left]$:

3. if $array[left] \leq target < array[mid]$
right $\leftarrow mid - 1$

4. else:
left $\leftarrow mid + 1$

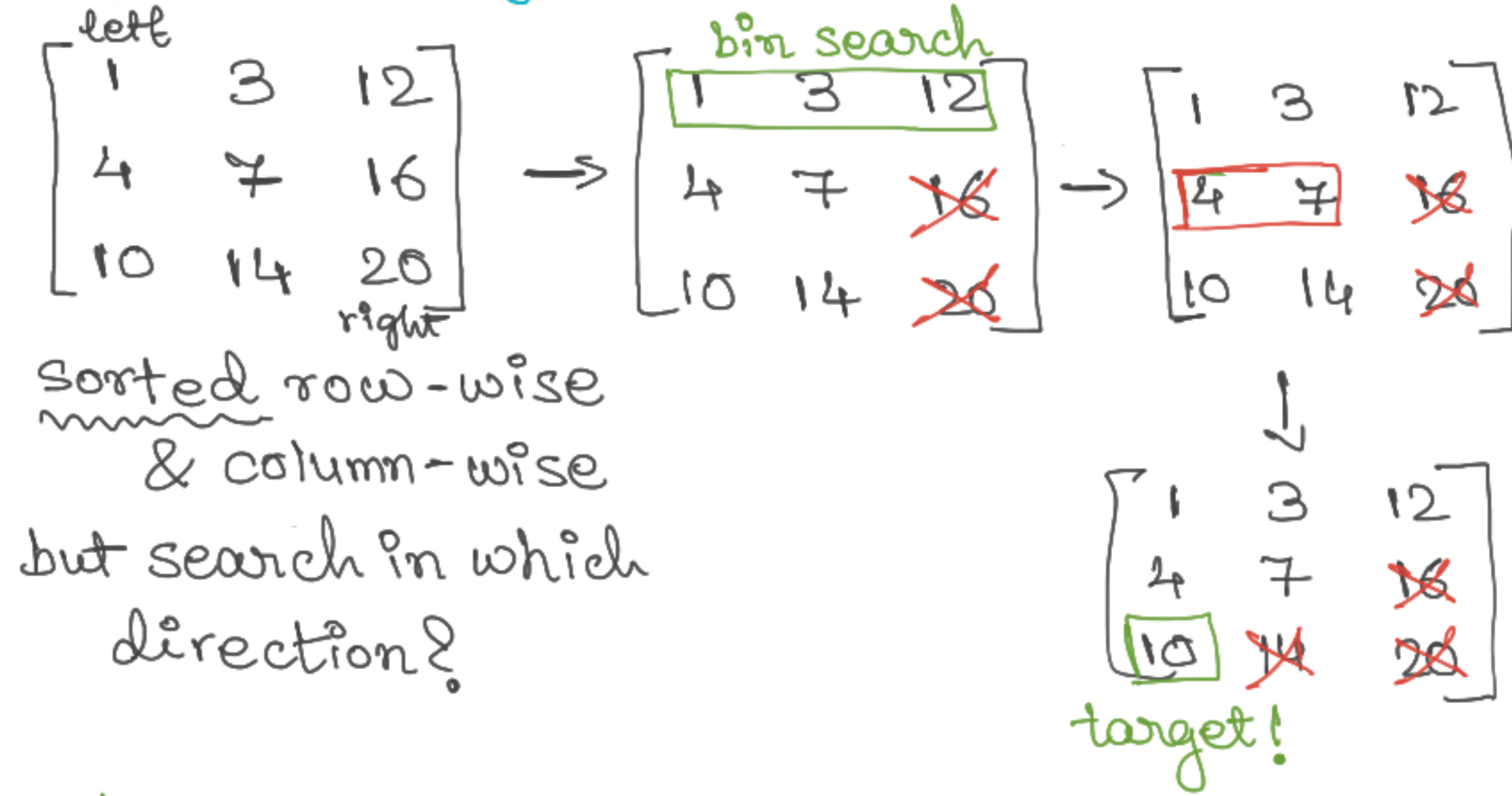
5. else:

6. if $array[mid] < target \leq array[right]$
left $\leftarrow mid + 1$

7. else:
right $\leftarrow mid - 1$

if $array[mid] == target$:
return target / mid

2) Matrices: $\text{target} = 10$



1. $\text{rows} = [0, 1, 2], \text{cols} = [0, 1, 2]$

2. for row in rows:

→ perform bin search for row with cols element
delete cols element
where $\text{mat}[\text{row}][\text{col}] > \text{target}$.

if $\text{mat}[\text{row}][0] \leq \text{target} \leq \text{mat}[\text{row}][\text{col}]$

Takeaway:

Treat each row as a 1D array and perform bin search

Can prune some columns & rows on the go

3) Data Streams:

Task: Given a data stream input of non-negative integers a_1, a_2, \dots, a_n , summarize the numbers in a sorted manner.

[1, 3, 7, 2, 6, ...]

↑
[] we do not know
↓ what's next

1. 1 → [1] (count of elements received / len: 1)

2. 3 → [1, 3] (len: 2)

3. 7 → [1, 3, 7]

4. 2 → [1, 2, 3, 7]

5. 6 → [1, 2, 3, 6, 7]

} use binary search to find out where to insert a new element

Q. what's the right data structure for storing such a data stream?

4) Counting:

Task: You are given an integer array `nums` and you have to return a new counts array. The counts array has the property where `counts[i]` is the number of smaller elements to the right of `nums[i]`.

Input: `nums = [5,2,6,1]` -->
Output: `[2,1,1,0]`

$[5, 2, 6, 1] \xrightarrow{\text{sort}} [1, 2, 5, 6]$
 ↑
 how many element are smaller than this element?
 find index (with what?)

count = index

order / input: $[1, 6, 2, 5]$ ← backwards of the original input
 use binary search to find correct index
 count how many elements to the left

streams:

a. $[] + 1$

→ $[1]$

0

b. $[1] + 6$

→ $[1, 6]$

1

c. $[1, 6] + 2$

→ $[1, 2, 6]$

1

d. $[1, 2, 6] + 5$

→ $[1, 2, 5, 6]$

2

Sorting:

1 Duplicates

[Remove Duplicates In-place]

Task: Given an integer array nums sorted in non-decreasing order, remove the duplicates in-place such that each unique element appears only once. The relative order of the elements should be kept the same.

Input: [1, 1, 2, 3, 4, 4, 5]

Expected

Output: [1, 2, 3, 4, 5, ,] can have any value

logic:

i = 0

```
for j in range(1, len(nums)):
    if nums[j] != nums[i]:
        i += 1
        nums[i] = nums[j]
```

Takeaways:

- a. for in-place ^{array} operations, consider using more than one pointer.
- b. compare and swap

iter #1	{	i = 0, j = 1	nums = [1, 1, 2, 3, 4, 4, 5]
		i = 0, j = 1	nums = [1, 1, 2, 3, 4, 4, 5]
iter #2	{	i = 0, j = 2	nums = [1, 1, 2, 3, 4, 4, 5]
		i = 1, j = 2	nums = [1, 2, 2, 3, 4, 4, 5]
iter #3	{	i = 1, j = 3	nums = [1, 2, 2, 3, 4, 4, 5]
		i = 2, j = 3	nums = [1, 2, 3, 3, 4, 4, 5]
iter #4	{	i = 2, j = 4	nums = [1, 2, 3, 3, 4, 4, 5]
		i = 3, j = 4	nums = [1, 2, 3, 4, 4, 4, 5]
iter #	{	i = 3, j = 5	nums = [1, 2, 3, 4, 4, 4, 5]
		i = 3, j = 5	nums = [1, 2, 3, 4, 4, 4, 5]
iter #	{	i = 3, j = 6	nums = [1, 2, 3, 4, 4, 4, 5]
		i = 4, j = 6	nums = [1, 2, 3, 4, 5, 4, 5]

② Anagrams:

s = a n a g r a m
t = n a g a r a m

different approaches:

1. use dictionary to keep char occurrence counts
2. sort both strings and compare
3. remove a char from s when a char from t matches

s_sorted = "aaagmnr"

t_sorted = "aaagmnr"

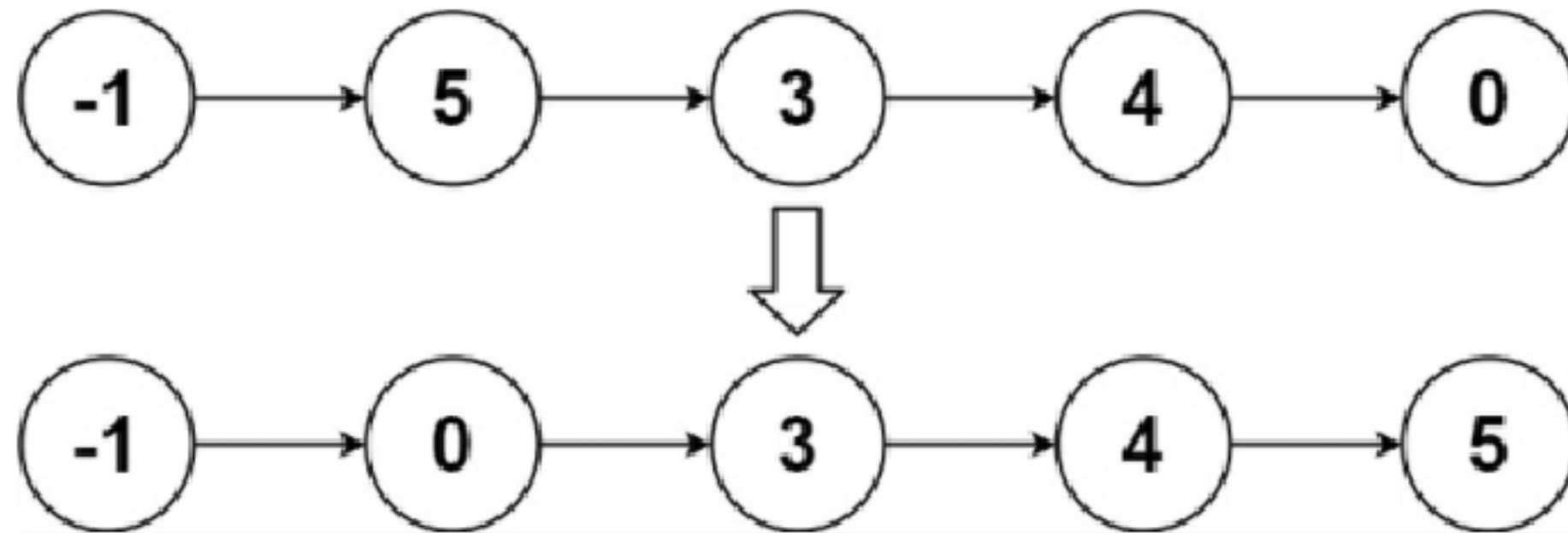
Task: Given two strings s and t, return true if t is an anagram of s, and false otherwise.

Input: s = "anagram", t = "nagaram" -->
Output: true

③ Linked Lists

- Some of the "random access" assumptions for sorting an array wouldn't work here.

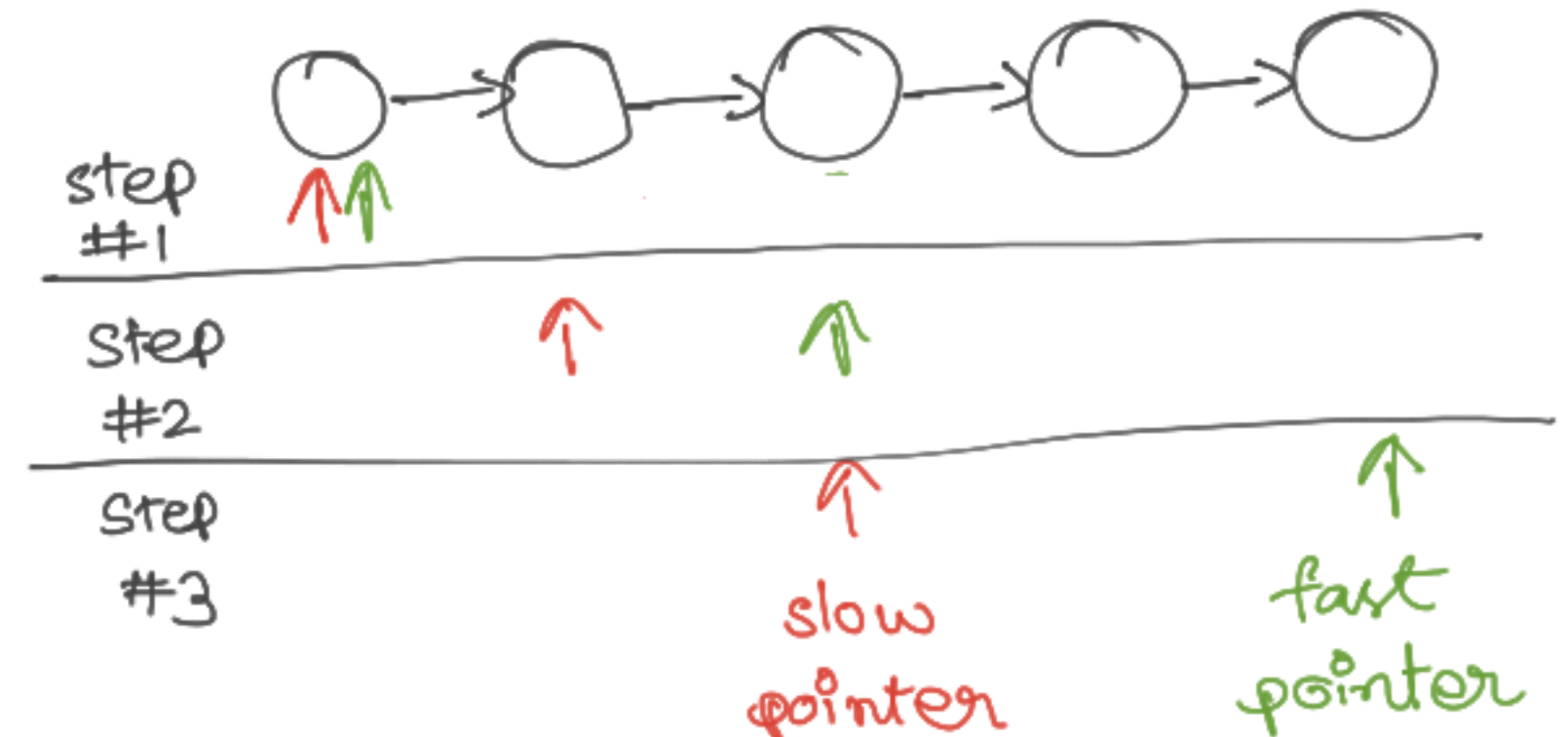
Task: Can you sort the linked list in $O(n \log n)$ time and $O(1)$ memory (i.e. constant space)?



Input: head = [-1, 5, 3, 4, 0]

Output: [-1, 0, 3, 4, 5]

How do we find the middle element?



④ In place Sorting:

We cannot return a new array; although, you can use temporary variables.

which sorting algorithms are in-place?

Also remember: Stable algorithms

[20 30 10 10] $\xrightarrow{\text{Sort}}$

Addresses: 0x01 0x02 0x03 0x04

from 0x03	from 0x04	from 0x01	from 0x02
[10	10	20	30]
0x05	0x06	0x07	0x08

Day 3 : Recursion

① Iterations \longrightarrow Recursions

4 parts

```
foo_iterative(params){  
  1. header      2.  
  while(condition){  
    3. loop_body  
  }  
  return tail 4.  
}
```

\longrightarrow "init" function

```
foo_recursive(params){  
  1. header  
  return foo_recursion(params, header_vars)  
}
```

```
foo_recursion(params, header_vars){  
  if(!condition){ 2.  $\longrightarrow$  terminating condn  
    return tail 4.  
  }
```

```
  loop_body 3.  
  return foo_recursion(params, modified_header_vars)  
}
```

\hookrightarrow last call would return tail too

④ Ordering:

$s1 = \text{"car"}$
 $s2 = \text{"race"}$ } permutation?

more about memoization

$s1_dict = \{c: 1, a: 1, r: 1\}$

$s2_dict = \{r: 1, a: 1, c: 1, e: 1\}$ } is subset ✓

⑤ Divide & Conquer

See Merge Sort

② Subproblems:

Fibonacci Numbers:

0, 1, 2, 3, 5, 8, 13, ...

$$\text{Fib}(0) = 0$$

$$\text{Fib}(1) = 1$$

$$\text{Fib}(n) = \text{Fib}(n-1) + \text{Fib}(n-2)$$

if $n > 1$

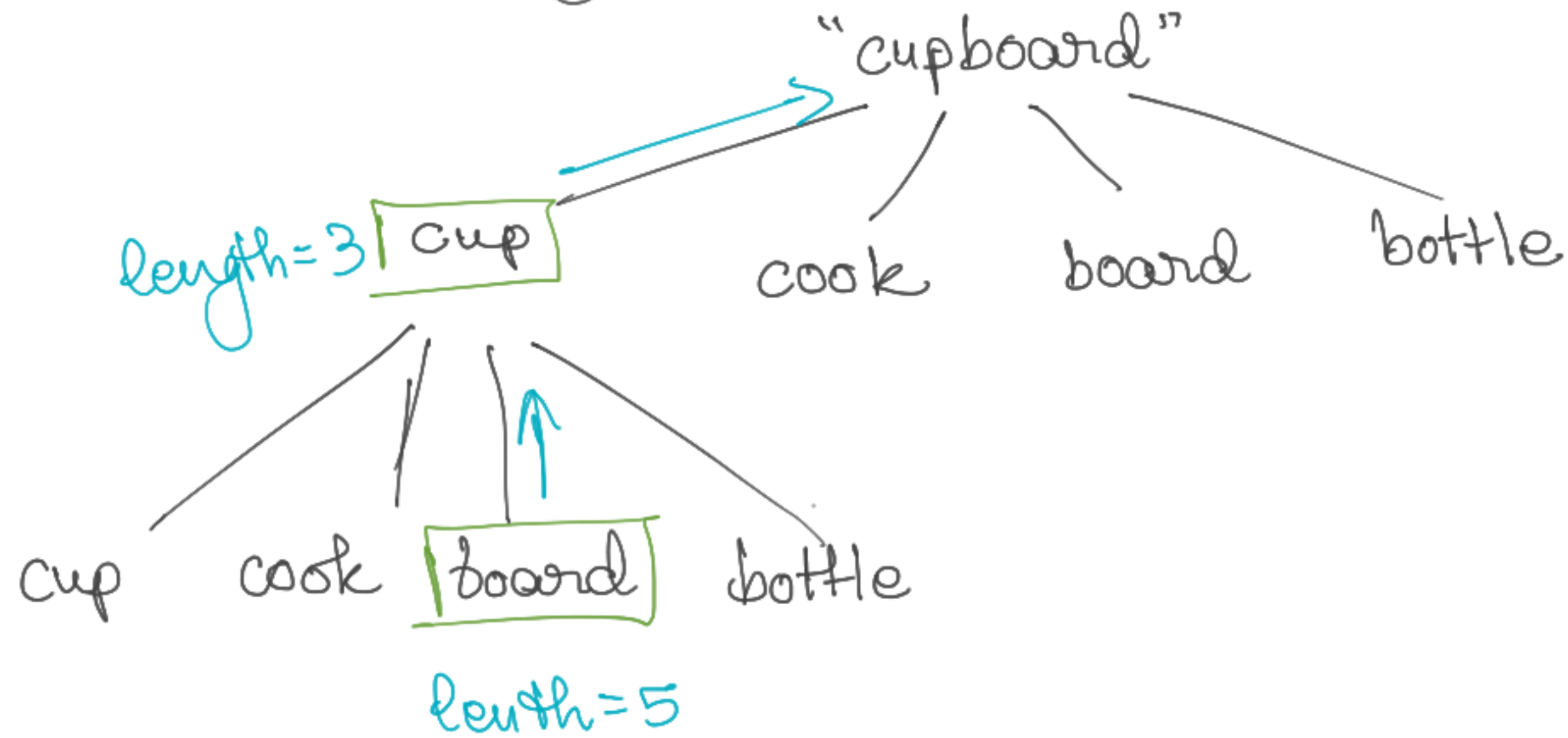
```
def fib(self, n: int) -> int:
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return self.fib(n-1) + self.fib(n-2)
```

but... we are calculating
this every time!

Memoization introduces space complexity.

③ Backtracking

dict = {cup, cook,
board, bottle}

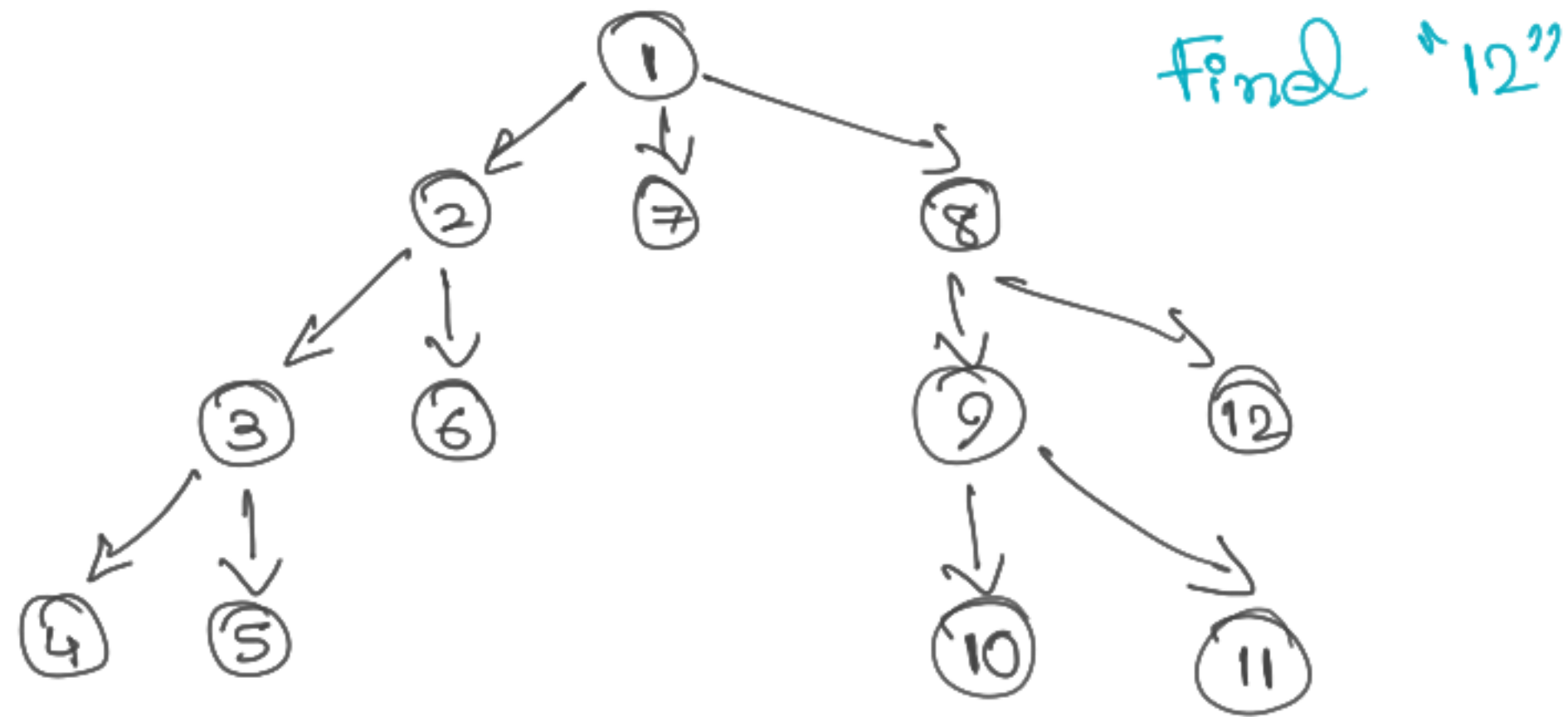


memo = {

0	: True
1	: False
2	: False
3	: True
4	: False
5	: False
6	: False
7	: False

}

⑥ Depth First Search : Recursion + Backtracking



⑤ Sliding Window:

"c b a e b a b a c d"

b b a

b b a

"b b a"

Sliding window should be of length 3

Check whether is anagram with counter dictionary

⑥ Comparison:

Longest Common Subsequence

	a	b	e
a	✓		
b		✓	
c			
d			
e			✓

→

	a	b	e
a	1	1	1
b	1	2	2
c	1	2	2
d	1	2	2
e	1	2	3

if $c1 == c2$:

$$tbl[i+1][j+1] = tbl[i][j] + 1$$

else:

$$tbl[i+1][j+1] =$$

$$\max(tbl[i+1][j], tbl[i][j+1])$$

Day 5: Hash Tables

① Numbers

Task -

You are given an integer array `nums` with the following properties:

* `nums.length == 2 * n`.

* `nums` contains `n + 1` unique elements.

* Exactly one element of `nums` is repeated `n` times.

Return the element that is repeated `n` times.

Input: `nums = [2,1,2,5,3,2]`

Output: 2

conclude \rightarrow If number x is getting repeated, it will be getting repeated $x-1$ times.

e.g. `[2, 1, 2, 5, 3, 2]`

hash table = `{ 2 : 1 }`

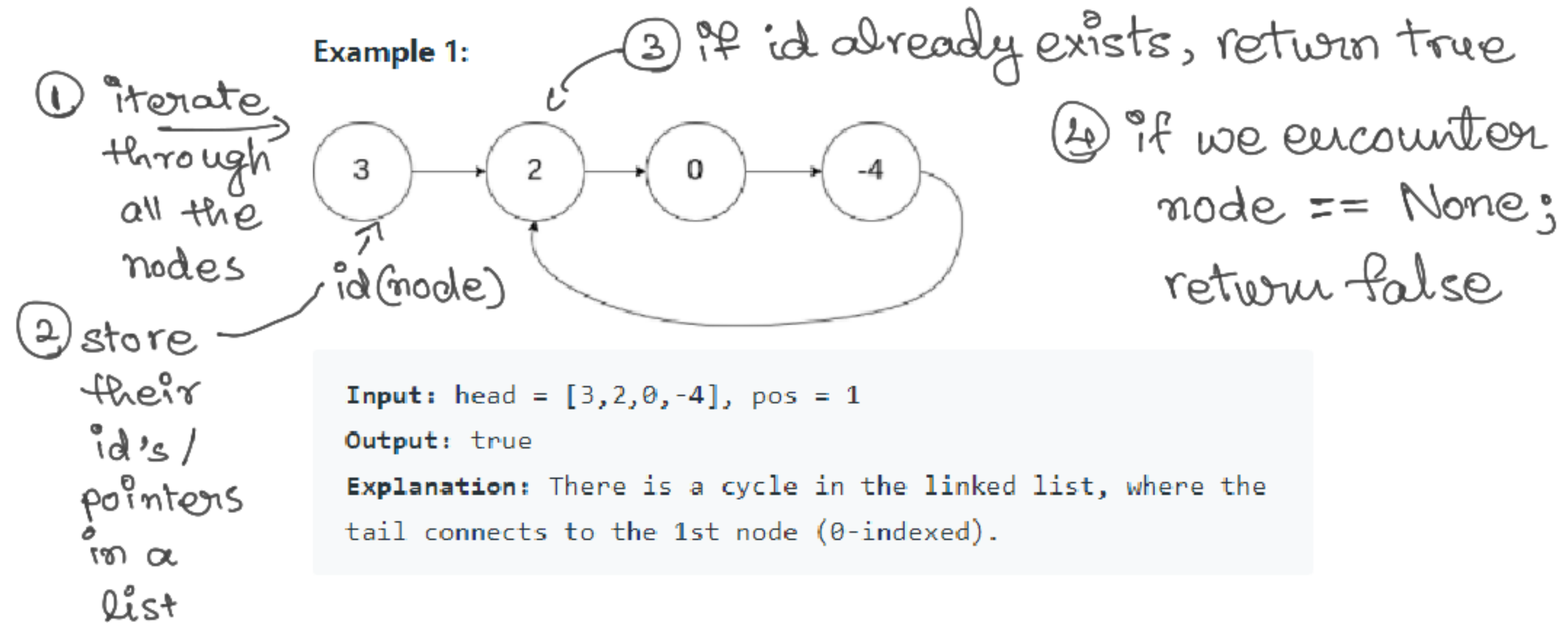
`{ 2 : 1, 1 : 1 }`

`{ 2 : 2, 1 : 1 }`
!!!

② Linked lists:

Task:

Given head, the head of a linked list, determine if the linked list has a cycle in it.



③ Arrays :

Task:

Given two integer arrays nums1 and nums2, return an array of their intersection. Each element in the result must be unique and you may return the result in any order.

Input: nums1 = [1,2,2,1], nums2 = [2,2]

Output: [2]

num1 = [1, 2, 2, 1]

num2 = [2, 2]

a. dictionary = {1: 1} $\xrightarrow{\text{next}}$ {1: 1, 2: 1} $\xrightarrow{\text{next}}$ {1: 1, 2: 2} $\xrightarrow{\text{next}}$ {1: 2, 2: 2}
from num1

b. remove from = {1: 2, 2: 2} $\xrightarrow{\text{next}}$ {1: 2, 2: 1} $\xrightarrow{\text{next}}$ {1: 2, 2: 0}
dictionary
with num2