

# HW5: Representation Learning with Autoencoder



# Notes

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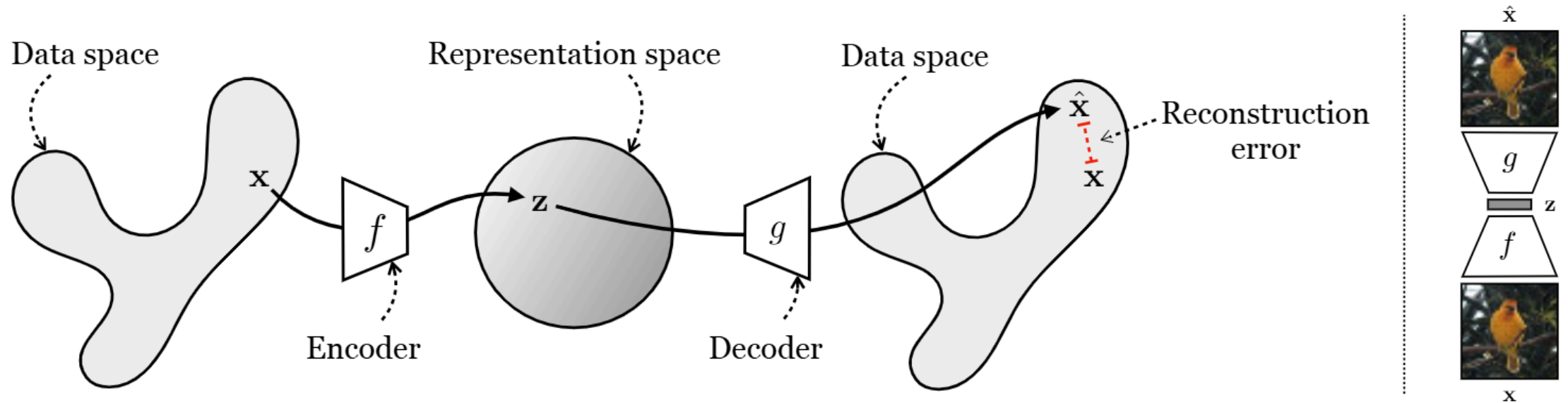
- Please make sure you read slide decks 17
- Please make sure you read chapter 30 of the textbook

# Outline

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- Recap of Autoencoder
- Recap of Convolution
- Homework description (programming part)
- Homework description (written part)

# Autoencoder

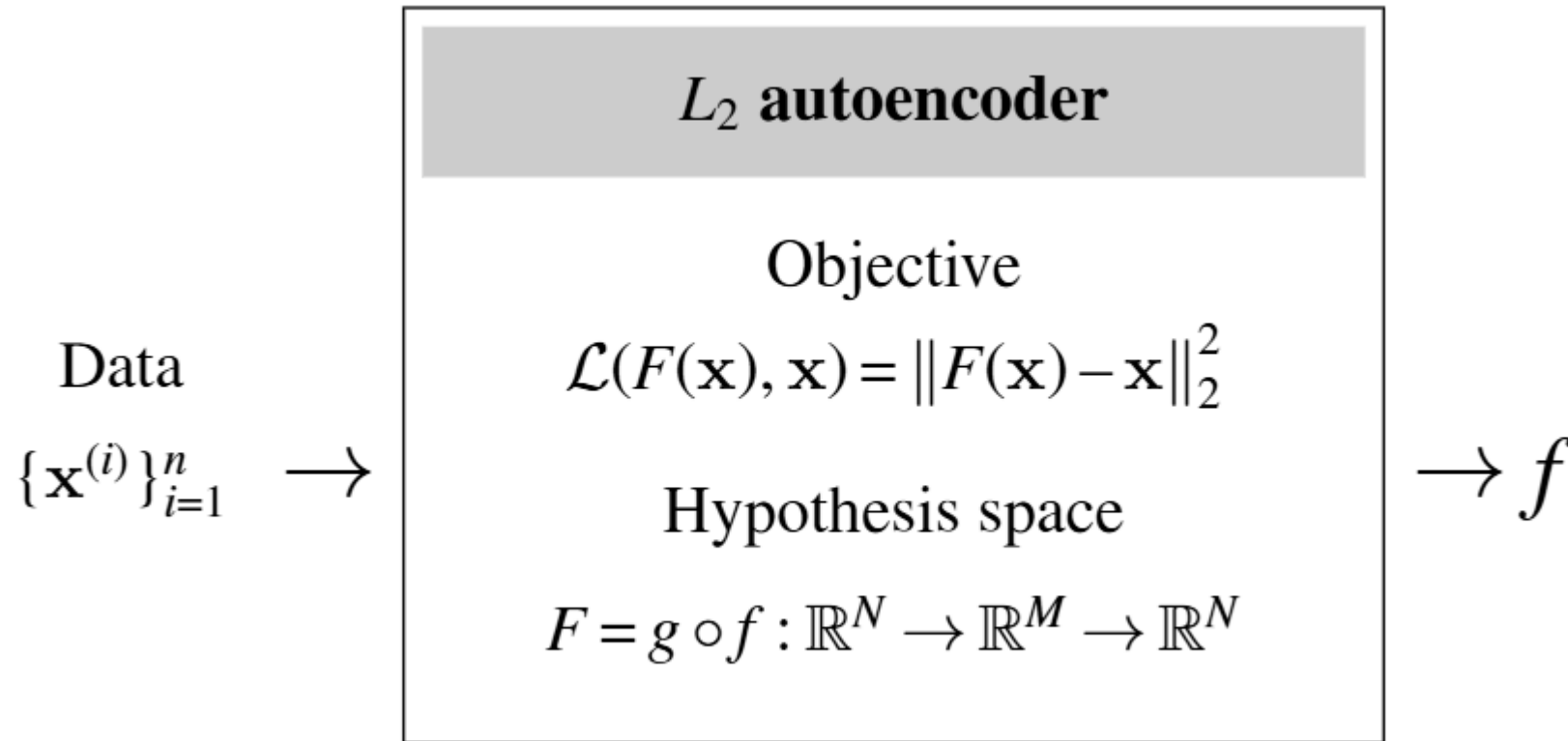


**Objective function:** 
$$f^*, g^* = \arg \min_{f, g} \mathbb{E}_{\mathbf{x}} \|g(f(\mathbf{x})) - \mathbf{x}\|_2^2$$

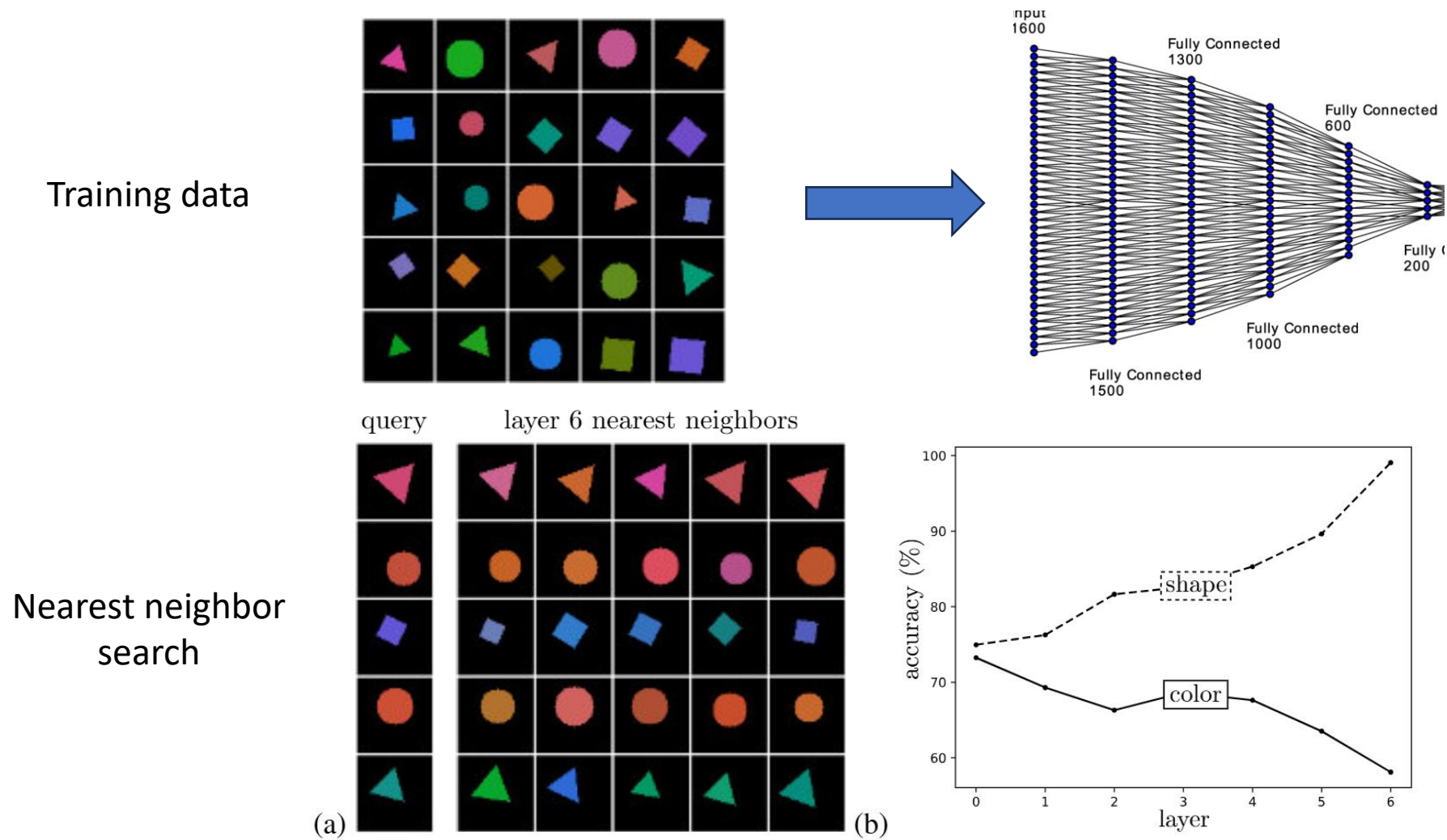
**Design principle:**  $\mathbf{z}$  with lower dimensionality

# Autoencoder

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# Example



# Convolution

Inner product  
Element-wise multiplication and sum

0	0	0	0	1
0	0	0	1	1
0	0	1	1	1
0	1	1	1	1
1	1	1	1	1

0	0	1
0	1	1
1	1	1

“Filter” weights  
(3-by-3)

	1			

Feature map (nodes) at layer  $t$

Feature map at layer  $t+1$

# Convolution

Inner product

0	0	0	0	1
0	0	0	1	1
0	0	1	1	1
0	1	1	1	1
1	1	1	1	1

0	0	1
0	1	1
1	1	1

“Filter” weights  
(3-by-3)

			6	

Feature map (nodes) at layer  $t$

Feature map at layer  $t+1$



# Convolution

Inner product

0	0	0	0	1
0	0	0	1	1
0	0	1	1	1
0	1	1	1	1
1	1	1	1	1

Feature map (nodes) at layer  $t$

0	0	1
0	1	1
1	1	1

“Filter” weights  
(3-by-3)

Zero-padding:  
Set the missing  
values to be 0

				1

Feature map at layer  $t+1$

# Outline

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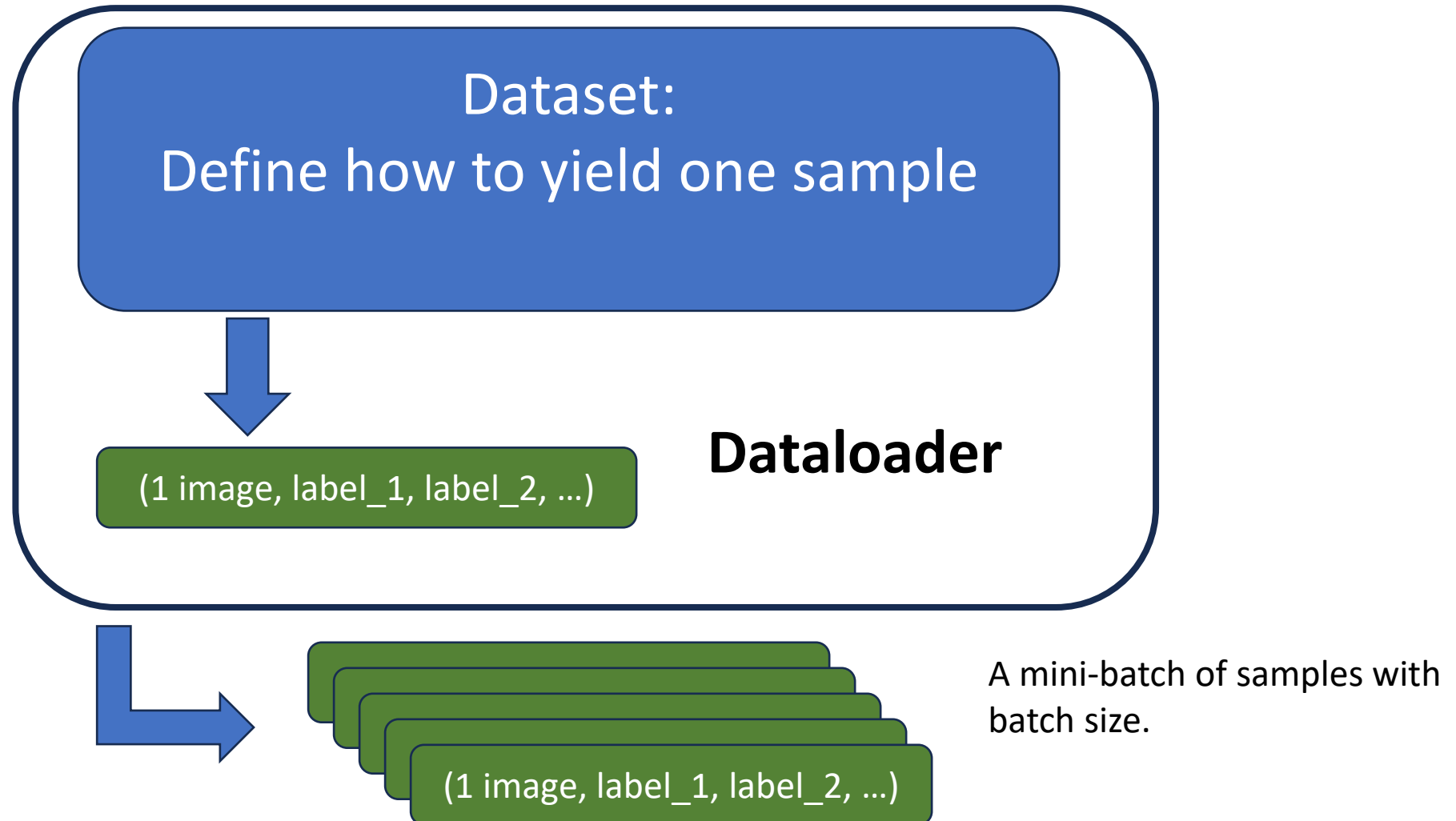
# Q1: Generate the Training Dataset

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- In Q1, you are to implement the following steps
  - Generate the training data with **THREE SHAPES** and **EIGHT COLORS**
  - You will be given the following
    - $s$ : scale for the shape
    - $cx$  and  $cy$ : the center of the shape
  - Shapes:
    - Circle: Draw a circle centered at  $(cx, cy)$  with a diameter of  $s$ . Use `d.ellipse()`.
    - Square: Draw a square centered at  $(cx, cy)$ , with side length  $s$ , and rotated by a random angle. Use `d.polygon()`.
    - Triangle: Draw an equilateral triangle centered at  $(cx, cy)$ , scaled by  $s$ , and rotated by a random angle. Use `d.polygon()`.

# Dataset and Dataloader

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# Q2 Create the AutoEncoder and Train It

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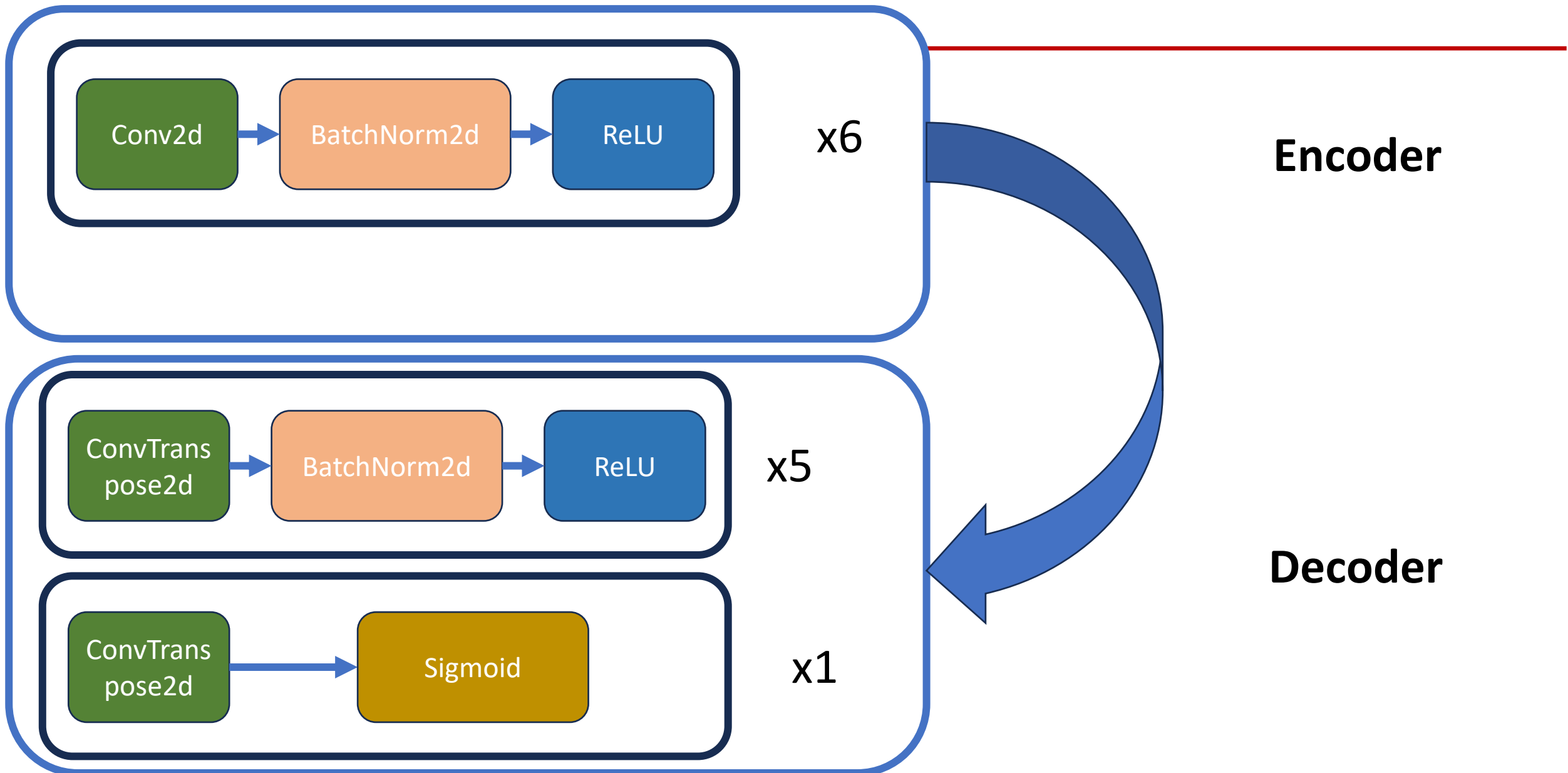
**ColorShapeDataset** is responsible for loading each image (given an index) and preparing the labels

- In `__getitem__`, you need to load one path from `all_paths` using `idx`
- Load the image with `PIL.Image`, apply the transform
- Parse shape & color labels from the filename using `parse_labels`.

**build\_data\_loader** is responsible for creating an instance of the Dataset and wrapping it inside the `DataLoader` to yield data batch by batch:

- Instantiate a `ColorShapeDataset` with `build_transform()`.
- Wrap it in a `DataLoader` with the given `batch_size`, `shuffle`, and `num_workers`.

# Q2 AutoEncoder



# Q3 K Nearest Neighbor

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Distance matrix 'dist'

Num\_ref\_embeddings

Num\_query\_  
embeddings

0.1	0.01	0.052	0.12	0.04	0.5	0.3	0.03	0.06

For each query embedding,

- You will calculate the distance between this query embedding and all the reference embedding
- Thus, 'dist' has shape num\_query\_embeddings x num\_ref\_embeddings
- For K= 3, you will select the closest 3 reference embeddings to plot.
- For the distance, please use **cosine distance**, that is, pre-normalize each vector to have its L2 norm equal to 1, and compute the L2 distance

# Q4 Achieve the best shape accuracy

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- You **must NOT** use any images from the **test set** (data\_folder\_test) for training.
- You should **NOT** do any **supervised** training using **labels** from the training data

## Potential directions

- Modify the autoencoder architecture
  - Larger model?
  - Better architecture?
- Change the training setup
  - Better loss?
  - Adjusting hyper-parameters?
- Change the training set or adding data augmentations:
  - More data?
  - Data augmentation?