

HW2



Preparation - 1

- Please make sure you have read the Lectures 6 & 7 slide decks, especially about convolutions.
- Please read Textbook chapters 15, at least those covered by lectures.
- The notations in this slide deck may be a bit different from the lecture slides!
The goal is to make implementation easier.

Preparation - 2

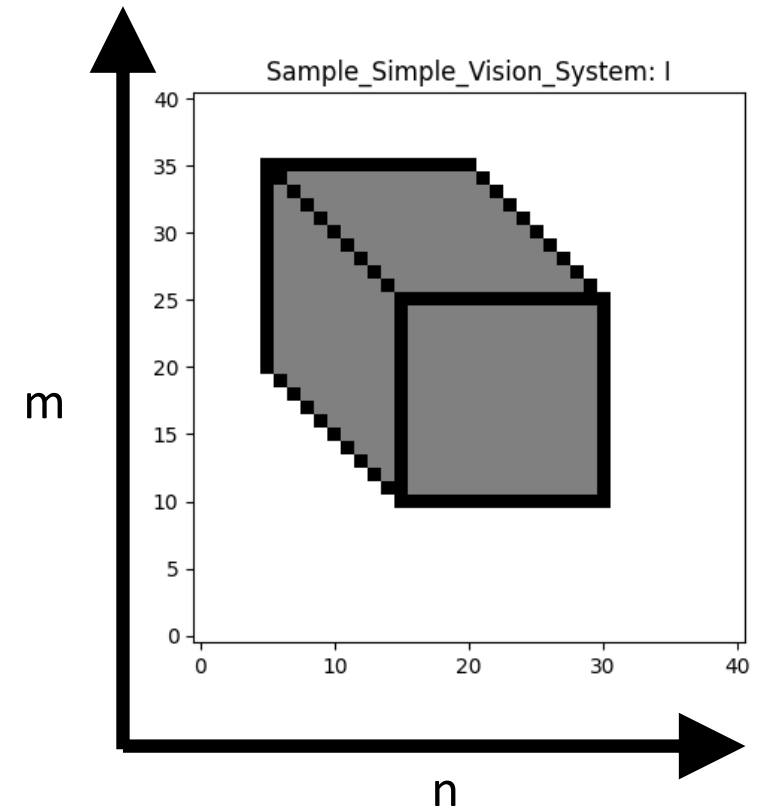
- Please make sure you have read the Lectures 9 & 10 slide decks, especially about the Gaussian pyramid and the Laplacian pyramid.
- Please read the Textbook chapter 23 about the Gaussian pyramid and the Laplacian pyramid.
- The Gaussian pyramid down-samples an image sequentially.
- The Laplacian pyramid records “information loss” during down-sampling.
- By combining them, we can reconstruct the image of the original size.

Caution

- Please do not import packages (like scikit learn) that are not listed in the provided code.
- In this homework, you are NOT allowed to use NumPy's or other Python libraries' built-in **convolution, filter functions, down-sampling, up-sampling, Gaussian pyramid, and Laplacian pyramid functions**. If you use them, you will get 0 points for the entire assignment.

Convention

- In this homework, given a map (or a matrix), say I
 - $I[n, m]$ means the i -th horizontal index (left-right) and j -th vertical index (bottom-up)
 - $n \geq 0, m \geq 0$



Color images

- Please note that a color image I means that the image I is a 3D tensor. The 3rd dimension corresponds to R, G, and B.



- In this homework, you will **process each channel separately**. You can extract each by $I[:, :, c]$, where c is between 0 and 2.

Question 1: Convolution

- There are many variants, but in this homework, please follow the formula below.
 - Given an image I , we will first do zero padding (think about why)



Question 1: Convolution

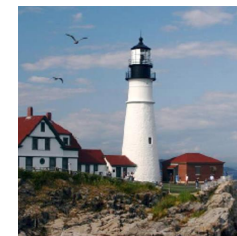
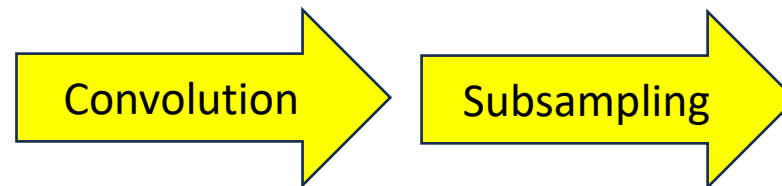
- Then, we perform
- $$I_{out}[n, m, c] = \sum_{k=0}^{K-1} \sum_{l=0}^{L-1} I_{pad}[n + k, m + l, c] h[K - 1 - k, L - 1 - l]$$
- K and L are the 2D kernel h's shape
- The range of n and m are $[0, N-1]$ and $[0, M-1]$, respectively, where N and M are the input image I's shape (not I_pad)
- That is, I_{out} will have the same shape as the input image I

Question 1: Convolution

- In your implementation, if you can implement $\sum_{k=0}^{K-1} \sum_{l=0}^{L-1} [\textit{something}]$ without using a for loop, it will save a lot of computation time in Python

Question 2: Down-sampling

- There are many variants, but please follow the formula below.
 - Given an image I , we will first convolve it with a 2D binomial filter to obtain $I_{\text{convolved}}$
 - I and $I_{\text{convolved}}$ have the same size
 - We will then sub-sample the convolved image $I_{\text{convolved}}$ by a factor of two
 - If $I_{\text{convolved}}$ is 128×128 , the subsampled image I_{down} is 64×64 by keeping pixels at “even” Python indices. That is, $I_{\text{down}}[n, m, :] = I_{\text{convolved}}[2n, 2m, :]$



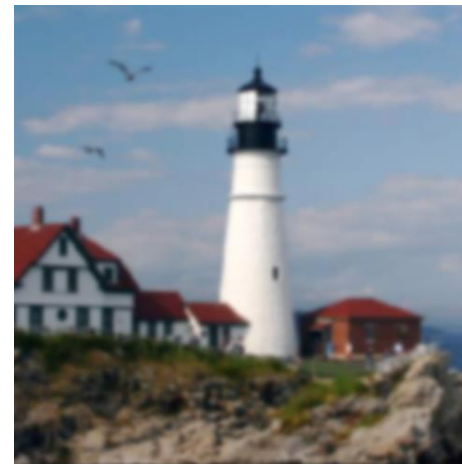
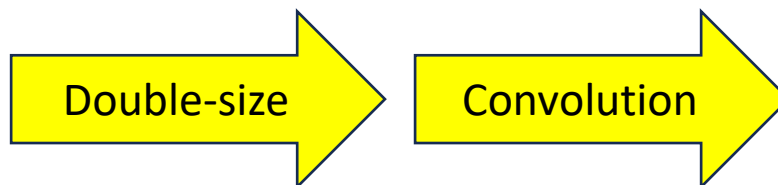
Question 3: Gaussian pyramid

- Create a sequence of sub-sampled images



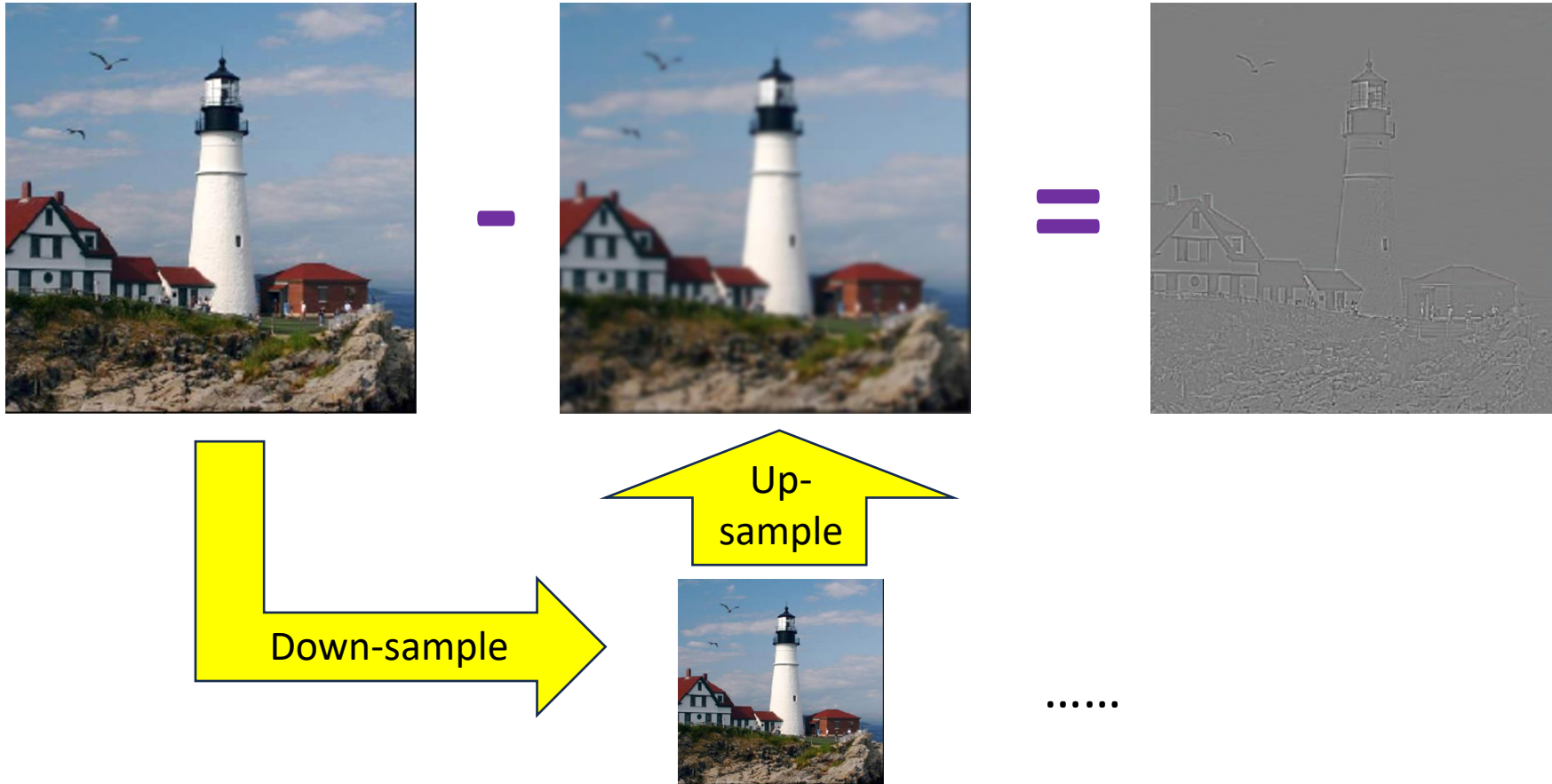
Question 4: Up-sampling

- There are many variants, but please follow the formula below.
 - Given an image I , we will first double its size in each dimension to obtain I_{up}
 - If I is 64×64 , I_{up} is 128 .
 - $I_{up}[n, m, :] = 4 * I[n/2, m/2, :]$ when n and m are “even” Python indices
 - Please make sure you multiply the pixel values by 4
 - $I_{up}[n, m, :] = 0$ when n and m are “odd” Python indices
 - We will then convolve I_{up} with a 2D binomial filter to obtain $I_{convolved}$
 - I_{up} and $I_{convolved}$ have the same size



Question 5: Laplacian pyramid

- Create a sequence of residual images



Question 6: Image reconstruction

