

Name:..... ID:.....

1. A company wants to purchase large, medium, and small delivery trucks. The company wants to purchase about 10 large, 5 medium, and 15 small trucks. Each large truck costs \$30,000 and has a 10-ton capacity. Each medium truck costs \$20,000 and has a 6-ton capacity. Each small truck costs \$12,000 and has a 4-ton capacity. The company wants to have about 200 tons of capacity and spend about \$600,000.

1.1 Formulate a goal programming model of this problem.

Objective function: (Not MiniMax Q)

Subject to:

1.2 Formulate a goal programming model of this problem. (9 points)

Objective function: (Using MiniMax Q)

Subject to:

2. **Multiple Objectives Linear Programming.** A university hospital dietary staff is required to satisfy the minimum nutritional needs of the patients while minimizing total food costs. Each food can consist of a combination of five ingredients as presented in the table below. For nutritional needs, each food must contain at least 38 units of vitamin C and 44 units of vitamin D. Not more than 50 units of all ingredients may be used in a food. The three objective functions are

f_1 = Minimize cost

f_2 = Maximize food taste

f_3 = Maximize food nutrition

The problem is to decide the best combination of ingredients (X_i) to optimize the three objectives.

| | Ingredient 1 (X_1) | Ingredient 2 (X_2) | Ingredient 3 (X_3) | Ingredient 4 (X_4) | Ingredient 5 (X_5) | Required |
|----------------|---------------------------|------------------------|---------------------------|---------------------------|---------------------------|------------------|
| Vitamin C | 4 | 1 | 2 | 1 | 2 | At least 38 |
| Vitamin D | 2 | 2 | 3 | 0.5 | 1 | At least 44 |
| Ingredients | 1 | 1 | 1 | 1 | 1 | Not more than 50 |
| Cost/unit | 0.3 | 0.15 | 0.2 | 1 | 0.1 | |
| Taste/unit | 1 | 2 | 1 | 10 | 1 | |
| Nutrition/unit | 15 | 2 | 1 | 1 | 2 | |

| Problem | Decision Variables | | | | | Objective functions | | |
|----------------|--------------------|-------|-------|-------|-------|---------------------|-------|-------|
| | X_1 | X_2 | X_3 | X_4 | X_5 | f_1 | f_2 | f_3 |
| Minimize f_1 | 0 | 0 | 12.5 | 0 | 6.5 | \$3.15 | 19 | 25.5 |
| Maximize f_2 | 0 | 0 | 7.6 | 42.4 | 0 | \$43.92 | 431.6 | 50 |
| Maximize f_3 | 50 | 0 | 0 | 0 | 0 | \$15.00 | 50 | 750 |

Write MOLP model