

# Net electric force and point charge

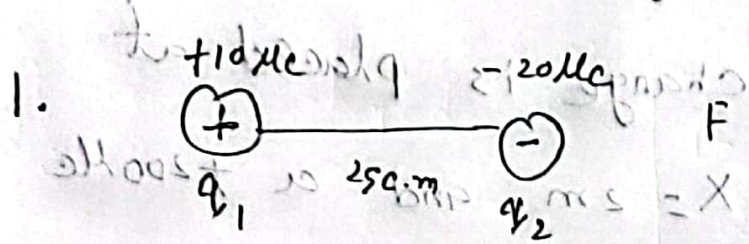
$$F = k \frac{q_1 q_2}{r^2}$$

$$k = 9 \times 10^9 \text{ N/m}^2 \text{C}^2$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2$$

$$k = \frac{1}{4\pi\epsilon_0}$$

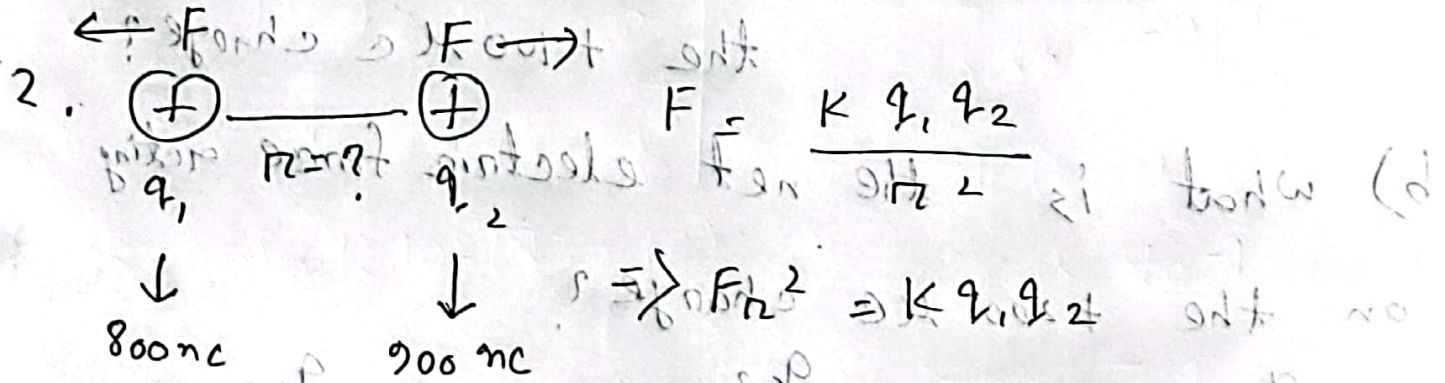
$$r \uparrow F \downarrow$$



$$F = \frac{9 \times 10^9 \times (10 \times 10^{-6}) \times (20 \times 10^{-6})}{(25 \times 10^{-2})^2} = 28.8 \text{ N}$$

# Force act on  $q_1$  due to  $q_2$   $F_{12}$

#  $q_2$  does not interact with  $q_1$ ,  $F_{21} = 0$

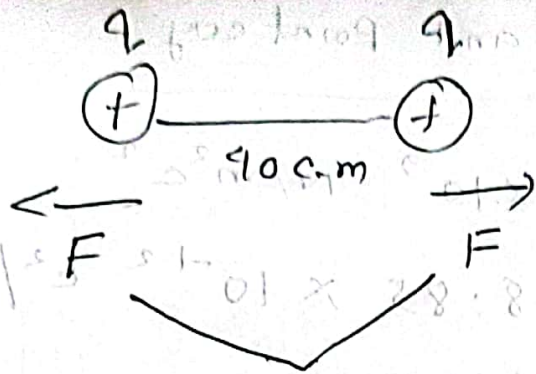


magnitude = 15 N

$$r = \sqrt{\frac{k q_1 q_2}{F_{\text{rep}}}} = \sqrt{\frac{9 \times 10^9 \times (800 \times 10^{-9}) \times (900 \times 10^{-9})}{15}} = 0.02078 \text{ m}$$



3.



$$F = \frac{K \cdot q^2}{r^2}$$

$$q^2 = \frac{F r^2}{K}$$

$$q = \sqrt{\frac{F r^2}{K}}$$

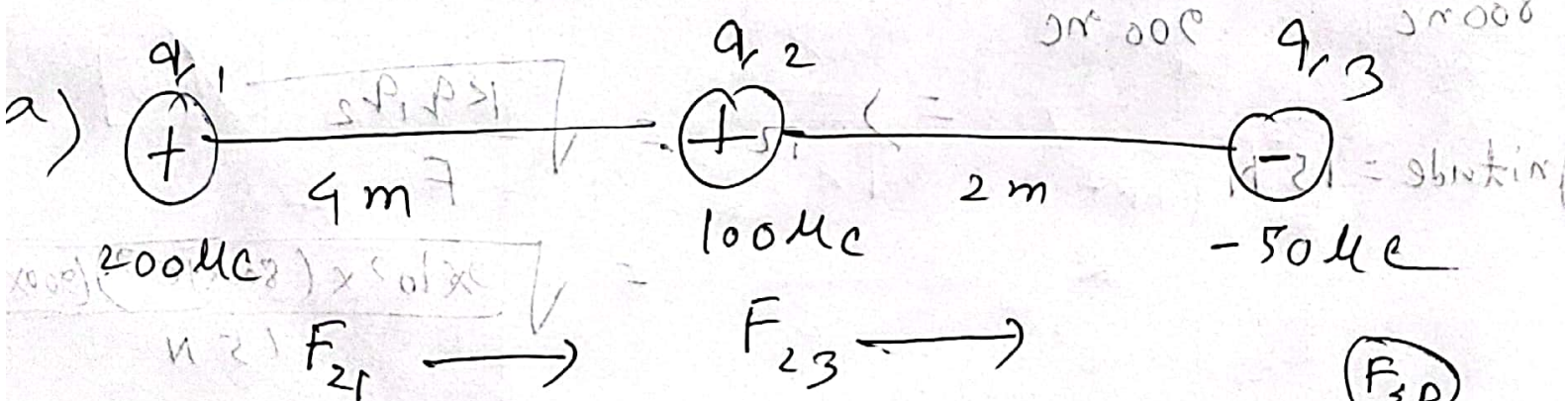
$$= \sqrt{\frac{500 \times (0.90)^2}{9 \times 10^9}}$$

$$q = 9.428 \times 10^{-5}$$

(\*) two identical point charges

~~##~~ +100  $\mu\text{C}$  charge is placed at the origin. A -50  $\mu\text{C}$  charge is placed at  $x = 2\text{ m}$  and a +200  $\mu\text{C}$  is placed at  $x = -4\text{ m}$ .

a) what is the net electric force acting on the +100  $\mu\text{C}$  charge?



(F<sub>32</sub>)

source move to point 288 J

$$F_{\text{net}} = F_{21} + F_{23} \quad \left| \quad F_{21} = \frac{9 \times 10^9 (200 \times 10^{-6}) \times (100 \times 10^{-6})}{4^2} \right.$$

$$= 11.25 \text{ N}$$

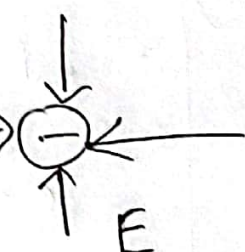
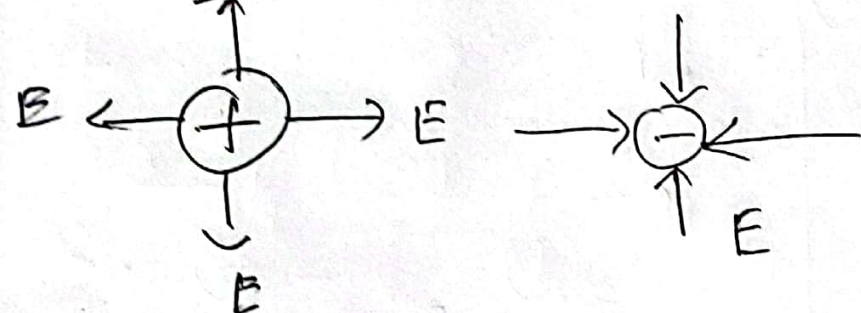
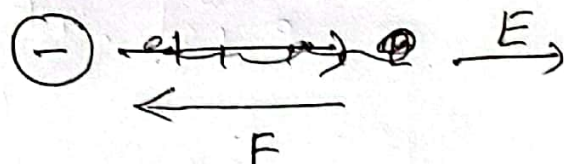
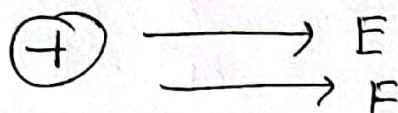
$$F_{23} = \frac{k q_2 q_3}{r^2} = \frac{9 \times 10^9 \times (100 \times 10^{-6}) \times (50 \times 10^{-6})}{2^2}$$

$$= 11.25 \text{ N}$$

$$F_{\text{net}} = 22.5 \text{ N}$$

### Electric field

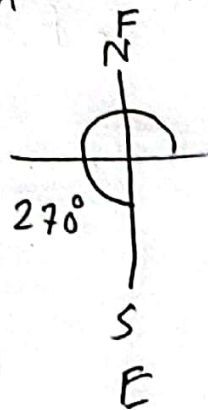
$$\boxed{1} E = \frac{F}{q}, \quad \boxed{2} E = \frac{kq}{r^2}$$



# Given, Force directed north - 20 Mc, so, will be on south.

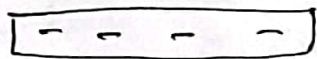
$$E = \frac{F}{q} = \frac{100}{20 \times 10^{-6}}$$

$$= 5 \times 10^6 \text{ NC}^{-1}$$

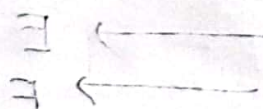
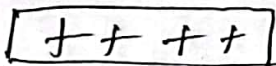




# A positive charge of  $+50 \mu\text{C}$  is placed in an electric field of  $50,000 \text{ N/C}$  directed upward. What mass should the charge have to remain suspended in the air?



$F \uparrow \oplus \uparrow E$



$$\sum F_y = F_E - W = 0$$

$$F_E = W$$

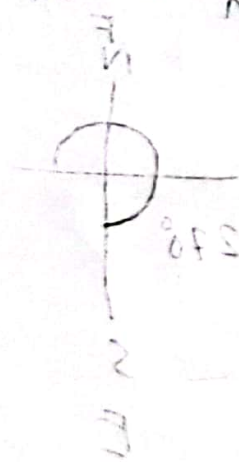
$$\Rightarrow Eq = mg$$

|                  |      |
|------------------|------|
| $E$ (int. field) | $F$  |
| $q$              |      |
| $F = qE$         | $Eq$ |

$$m = \frac{Eq}{g}$$

$$= \frac{50,000 (50 \times 10^{-6})}{9.8}$$

Answer = 0.255 kg



Answer = 0.255 kg

$$\frac{100}{50 \times 10^{-6}} = \frac{F}{q}$$

$$2 \times 10^6 \text{ N/C}$$

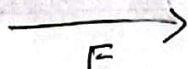
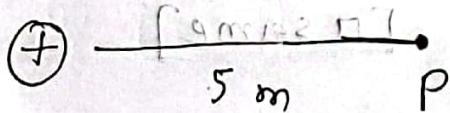
# A  $+90 \mu\text{C}$  point charge is placed at the origin.

Find magnitude and direction of the elec. field

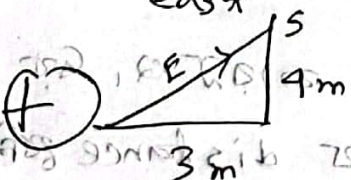
created by point charge. A) point P (5m, 0)

B) point S (3m, 4m)

Q



east



$$E = \frac{kQ}{r^2}$$

$$= \frac{9 \times 10^9 \times (90 \times 10^{-6})}{(5)^2}$$

$$E = 19,400 \text{ N/C}$$

$$E = \frac{kQ}{r^2}$$

$$= \frac{9 \times 10^9 \times (90 \times 10^{-6})}{(5)^2}$$

$$c^2 = a^2 + b^2$$

$$c^2 = 3^2 + 4^2$$

$$c = \sqrt{25} = 5$$

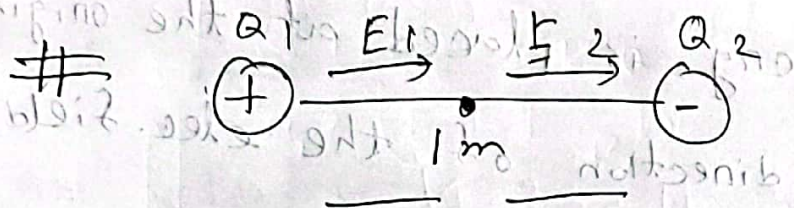
$$\tan \theta = \frac{4}{3}$$

$$\theta = \tan^{-1} \left( \frac{4}{3} \right)$$

$$\theta = 53.1^\circ$$



\* Elec. field between  
midway of 2 charges  
and 30 cm away.



(0.5m)  $r_1$   $r_2$

$$E_{net} = E_1 + E_2$$

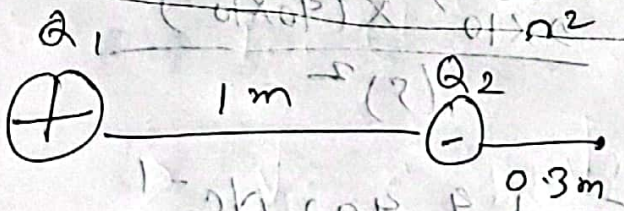
$$= \frac{kQ_1}{r_1^2} + \frac{kQ_2}{r_2^2}$$

$$E_{net} = \frac{9 \times 10^9}{(0.5)^2} [200 \times 10^{-6} + 300 \times 10^{-6}]$$

$$= 1.8 \times 10^7 \text{ N/C}$$

[r same]

$$E = \frac{k}{r^2} [Q + Q_2]$$



$E_1$  [E. at distance of  $Q_1$  is 1.3m]

$E_2$

$$E_{net} = E_1 - E_2$$

[E2 is at distance of  $Q_2$  is 0.3m]

$$E = \frac{kQ_1}{r^2} - \frac{kQ_2}{r_2^2}$$

$$= \frac{9 \times 10^9 \times (200 \times 10^{-6})}{(1.3)^2} - \frac{9 \times 10^9 \times (300 \times 10^{-6})}{(0.3)^2}$$

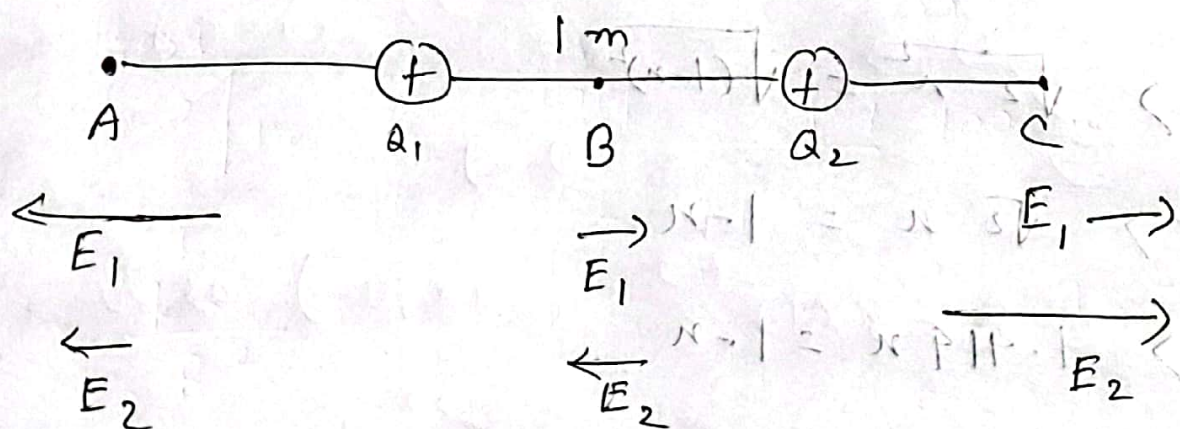
$$1.82 = 0$$

$$= 1.065 \times 10^8 - 3 \times 10^7$$

$$= -2.89 \times 10^7 \text{ N/C}$$



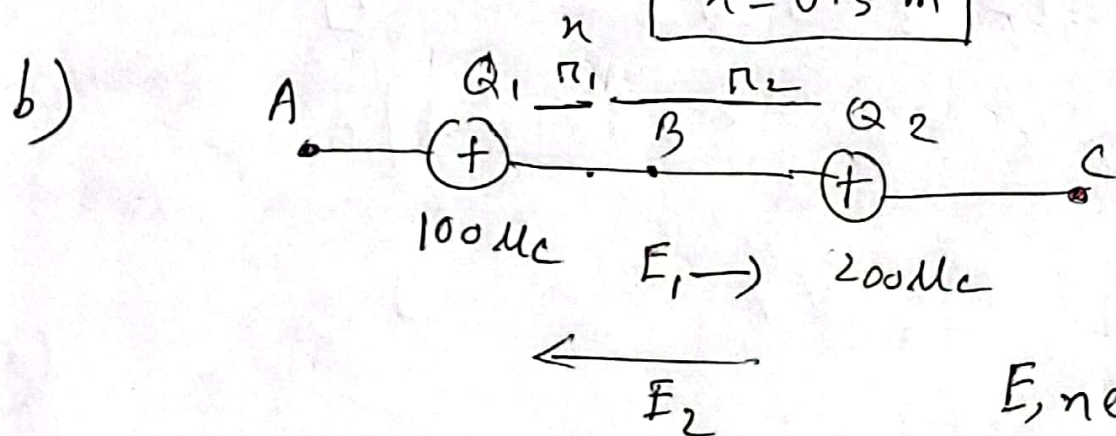
- # Two identical point cng with a magnitude of  $+100 \mu\text{C}$  are separated by  $1 \text{ m}$  distance. a) At what point will the net electric field be equal to zero.
- b) If the cng on  $Q_2$  doubles to  $+200 \mu\text{C}$ , where along the  $x$  axis relative to the 1st cng will the net electric field be equal to zero?



a)

$$E_{\text{net}} = 0$$

$$x = 0.5 \text{ m}$$



$$E_{\text{net}} = E_1 - E_2 = 0$$

$$E_1 = E_2$$

$$r_1 = x$$

$$r_2 = (1 - x)$$



...  $Q_1 = Q_2$  ...  
 $Q_1 n^2 = Q_2 (1-n)^2$  ...  
 $Q_1 n^2 = Q_2 (1-n)^2$  ...  
 $Q_1 n^2 = Q_2 (1-n)^2$  ...

$$\Rightarrow \frac{200}{100} n^2 = \frac{100}{100} (1-n)^2$$

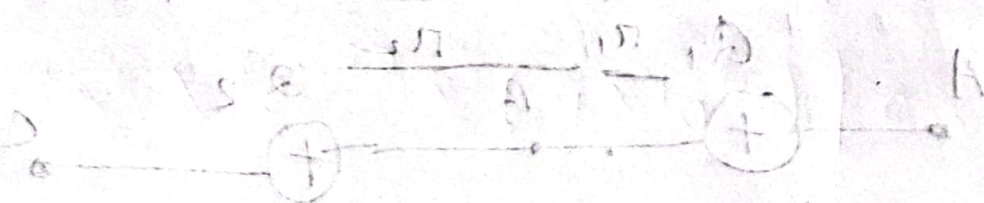
$$\Rightarrow \sqrt{2} n = 1-n$$

$$\Rightarrow \sqrt{2} n = 1-n$$

$$\Rightarrow 1.414 n = 1-n$$

$$\Rightarrow n = \frac{1}{2.414} = 0.414$$

$$n = 0.414$$



...  
 ...  
 ...

$$E_{net} = E_1 - E_2 = 0$$

$$E_1 = E_2$$

$$(1-n) =$$



## Electric field

Due to Ring of charge, Linear charge Density.

$$1. E_x = \frac{kQx}{R^3} \quad 2. R = \sqrt{a^2 + x^2} \quad 3. \lambda = \frac{Q}{L} = \frac{Q}{2\pi a}; \lambda = \frac{dq}{ds}$$
$$\Rightarrow Q = 2\pi a \lambda$$

$$4. E_{\text{net}} = \frac{k(2\pi a)\lambda x}{R^3}$$

# A ring shaped conductor with radius 5 cm has a total charge of +50 nC a) what is the electric field at a point 12 cm east from its center? b) Linear charge density of the ring?

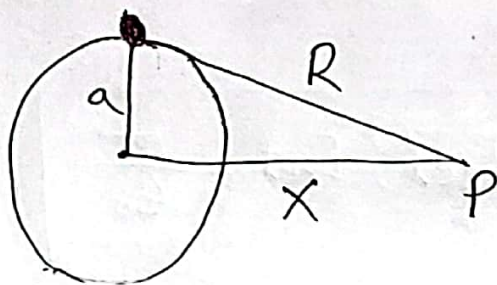
(a)

$$\rightarrow a = 0.05 \text{ m}, Q = +50 \text{ nC}, x = 0.12 \text{ m}$$

$$\therefore R = \sqrt{(0.05)^2 + (0.12)^2} = 0.13 \text{ m}$$

$$E_x = \frac{9 \times 10^9 \times (0.12) \times (50 \times 10^{-9})}{(0.13)^3}$$

$$E_x = 24,579 \text{ N C}^{-1}$$



$$\lambda = \frac{Q}{2\pi a}$$

$$= \frac{50 \times 10^{-9}}{2\pi \times (0.05)}$$

$$= 1.59 \times 10^{-7} \text{ C/m}$$



Charge per unit area  $\sigma = \frac{Q}{A}$

Due to charged disk, infinite sheet of chg,  $E_x = \frac{\sigma}{2\epsilon_0} \left[ 1 - \frac{x}{\sqrt{x^2 + R^2}} \right]$

# A disk of radius 3m contains a total chg of +480nC

a) what is the charge per unit area? b) what is the electric field 25 cm away from the center of the disk?

a)  $\sigma = \frac{Q}{A} = \frac{Q}{\pi R^2}$

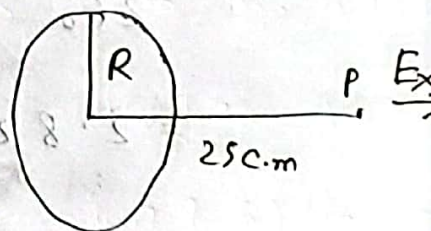
$$= \frac{480 \times 10^{-9}}{\pi (3\text{m})^2}$$

$\Rightarrow \sigma = 1.697 \times 10^{-8} \text{ C.m}^{-2}$

$R = 3\text{m}$

$Q = +480\text{nC}$

$x = 0.25\text{m}$



b)  $E_x = \frac{\sigma}{2\epsilon_0} \left[ 1 - \frac{x}{\sqrt{x^2 + R^2}} \right]$

$$= \frac{1.697 \times 10^{-8}}{2 \times (8.85 \times 10^{-12})} \left[ 1 - \frac{0.25}{\sqrt{(0.25)^2 + 9}} \right]$$

$$= 959.1 (0.91695)$$

# R infinite  $\Rightarrow E_x = 879.5 \text{ N.C}^{-1}$

$\lim_{R \rightarrow \infty} \frac{x}{\sqrt{x^2 + R^2}} = \frac{x}{\sqrt{x^2 + \infty^2}} = \frac{x}{\infty} = 0$

$\therefore E_x = \frac{\sigma}{2\epsilon_0} [1 - 0] = \frac{\sigma}{2\epsilon_0}$

Between 2 infinite plates

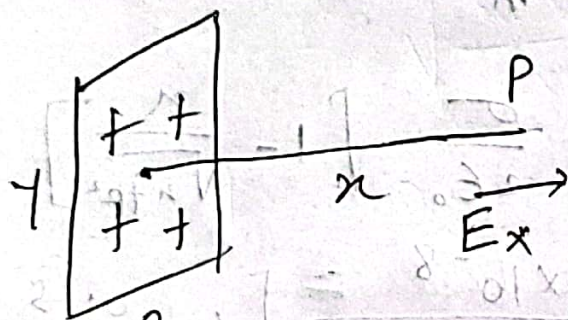


# What is the elec. field produced by an infinite sheet of chg. that has a chg. per unit area of  $+5 \mu\text{C}$  at a distance of  
 a) 500 m and b) 5 m away from the center of the plate

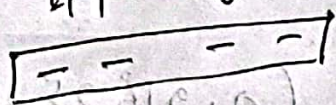
$$a) E_x = \frac{\sigma}{2\epsilon_0} = \frac{5 \times 10^{-6}}{2 \times (8.85 \times 10^{-12})}$$

$$= 2.82 \times 10^5 \text{ N/C}$$

[Plate  $\infty$  &  $\infty$   
 distance  $\infty$  &  $\infty$   
 always infinite  
 distance  $\infty$ ]

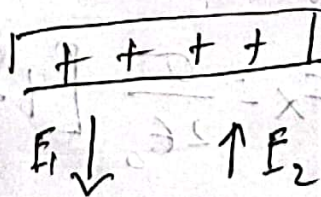


# outside,  $E_{\text{net}} = E_1 - E_2 = 0$



between  $E_{\text{net}} = E_1 + E_2$

$$= \frac{\sigma}{2\epsilon_0} + \frac{\sigma}{2\epsilon_0} = \frac{\sigma}{\epsilon_0}$$



$E_{\text{net}} = E_1 + E_2 = 0$   $= \frac{\sigma}{\epsilon_0}$

$\therefore$  Between 2 infinite sheet,  $E_{\text{net}} = \frac{\sigma}{\epsilon_0}$