

Assignment 02

submitted for
EN3551 - Digital Signal Processing
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Progress on GitHub [↗](#)

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Question 03 The relevant images and quality levels are `cameraman.mat`, `Monarch.mat`, `Parrot.mat`, and 80%, 30% and 15%. We compress and decompress each image and compare with the original image at each of the quality levels given.

Note that we skip the process of coding and decoding, as we are only interested in the effects of compression on the visual quality of the image.

Results obtained for each image are as follows:

1. `cameraman.mat`



Figure 1: `cameraman.mat` at various compression levels

Quality Level	80%	30%	15%
Percentage of Zeros	74.9786%	89.386%	93.3502%
PSNR (dB)	35.7235	29.6951	27.4598

Comments on visual quality:

- 80% compression
 - virtually indistinguishable from the original

- slight reduction in contrast levels, e.g., the coat is grayer than in the original
- 30% compression
 - slight blockiness is visible, especially towards the upper right
 - some ringing is visible at the edges; there is a slight halo around the cameraman and camera
 - the grass on the ground appears blurry
- 15% compression
 - significant blockiness is visible
 - ringing effects are visible—there is a blurry halo around the cameraman and camera
 - the grass on the ground is significantly more blurry
 - there is a clear reduction in contrast levels

2. Monarch.mat



Figure 2: Monarch.mat at various compression levels

Quality Level	80%	30%	15%
Percentage of Zeros	71.8948%	85.7666%	90.2161%
PSNR (dB)	35.7556	30.0778	27.725

Comments on visual quality:

- 80% compression
 - virtually indistinguishable from the original
 - slight reduction in contrast levels, e.g., the black lines in the wings seem a lighter shade of gray and the brighter, white regions seem more dull
- 30% compression
 - blockiness is visible
 - further reduction in contrast levels
- 15% compression
 - significant blockiness is visible
 - the outlines around the white regions on the wings are no longer sharp and have blurred out

3. Parrot.mat

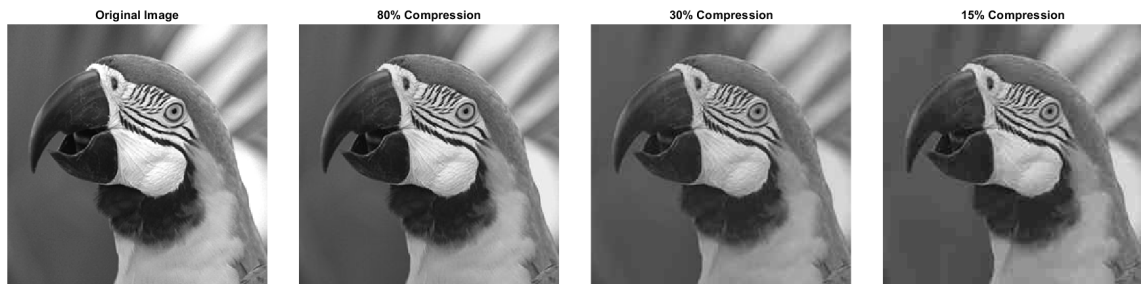


Figure 3: Parrot.mat at various compression levels

Quality Level	80%	30%	15%
Percentage of Zeros	80.5573%	91.2155%	94.1544%
PSNR (dB)	38.2348	32.9118	30.4194

Comments on visual quality:

- 80% compression
 - virtually indistinguishable from the original
 - slight reduction in contrast levels, e.g., the black lines in the wings seem a lighter shade of gray and the brighter, white regions seem more dull
- 30% compression
 - blockiness is visible
 - further reduction in contrast levels
- 15% compression
 - significant blockiness is visible
 - the outlines around the white regions on the wings are no longer sharp and have blurred out

4. Image of Choice - pisa.jpg

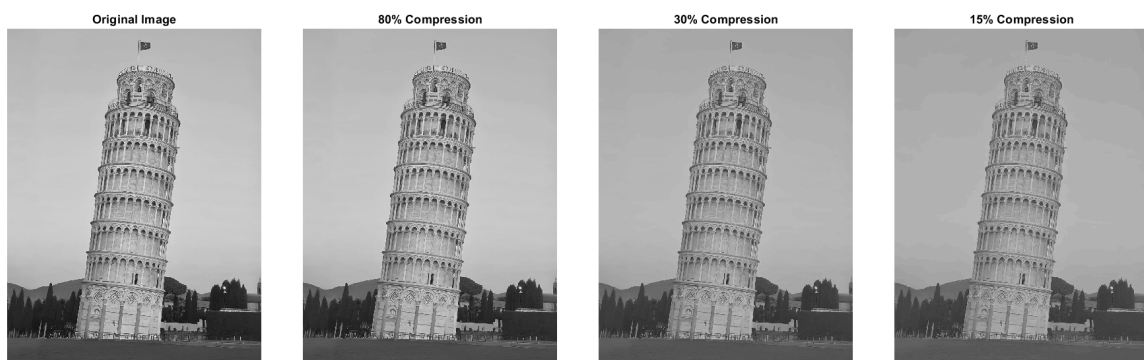


Figure 4: pisa.jpg at various compression levels

Quality Level	80%	30%	15%
Percentage of Zeros	87.8315%	93.783%	95.6683%
PSNR (dB)	42.1905	34.3926	31.6468

Comments on visual quality:

- 80% compression
 - virtually indistinguishable from the original
 - slight reduction in contrast levels, e.g., the black lines in the wings seem a lighter shade of gray and the brighter, white regions seem more dull
- 30% compression
 - blockiness is visible
 - further reduction in contrast levels
- 15% compression
 - significant blockiness is visible
 - the outlines around the white regions on the wings are no longer sharp and have blurred out

A Code Snippets

A.1 Harmonic Detection

```
clear;
clc;
close all;

% 3.1.1 - Load the relevant signal
load('signal658.mat');

% Define useful constants
fs = 128; % Sampling frequency (given)
Ns = [128 256 512 1024 1792]; % Sizes of subsets to be formed (given)

% For plotting
figure(1);
tiledlayout(3, 2, "TileSpacing", "compact", "Padding", "compact");

% Try to detect harmonics from the DFTs of increasingly bigger subsets of
% the signal

for i = 1:5
    N_i = Ns(i); % Number of samples in the ith subset
    f_i = [0:(N_i-1)] * fs / N_i; % Frequency axis corresponding to the ith subset

    % 3.1.2 - Form the ith subset s_i
    s_i = xn_test(1:N_i);

    % 3.1.3 - Obtain the DFT S_i of the ith subset, and then its magnitude
    S_i = fft(s_i);
    S_i_mag = abs(S_i);
```

```

% We will plot the first four figures in a 2x2 configuration, with the
% last one in a row of its own
if i <= 4
    nexttile(i);
else
    nexttile(i, [1, 2]);
end

% 3.1.3 - Plot the magnitudes of the DFT of the ith signal
stem(f_i, S_i_mag, "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "auto");

title("DFT-Magnitude of  $S_{-} + i + \$$ ", "Interpreter", "latex");
xlabel("Frequency (Hz)", "Interpreter", "latex");
xlim([0 f_i(N_i)]);
grid on;
grid minor;
end

% Try to detect harmonics by averaging

L = 14; % Number of subsets
K = 128; % Number of samples in a subset

% 3.1.4 - Find the average DFT from L = 14 consecutive subsets of K = 128
% samples each, and then obtain its magnitude
X_avg = dft_average(xn_test, L, K);
X_avg_mag = abs(X_avg);

f = [0:(K-1)] * fs / K; % Define the frequency axis

% Plot the magnitude of the average DFT
figure(2);

stem(f, X_avg_mag, "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "auto");

title("Magnitude of Averaged DFTs", "Interpreter", "latex");
xlabel("Frequency (Hz)", "Interpreter", "latex");
xlim([0 f(K)]);
grid on;
grid minor;

% 3.1.5 - What is the smallest value of L such that the peaks remain
% visible?

figure(3);
tiledlayout(3, 2);

% We will try smaller values L_s for L, starting from 1 less than the last
% used value
for L_s = [13 10 8 7 6 5]
    % Obtain the average DFT for the chosen pair L_s, K
    X_avg_ = dft_average(xn_test, L_s, K);
    X_avg_mag_ = abs(X_avg_);
end

```

```

nexttile;

% Plot
stem(f, X_avg_mag_, "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "auto");

title("Average DFT Magnitude, $L=$ + L_s + "$, $K=$ + K + "$, "Interpreter", "
      latex");
xlabel("Frequency (Hz)", "Interpreter", "latex");
xlim([0 f(K)]);
grid on;
grid minor;
end

```

Listing 1: Main Code

```

function [result] = dft_average(x, L, K)
% DFT_AVERAGE Average DFT of L consecutive subsets of K samples each from x
% x = time-domain signal
% L = number of subsets
% K = number of samples from each subset
%
% Computes the DFT of L consecutive K-point signal formed by partitioning
% x, and returns the average; i.e., sum of the DFTs divided by L

% We compute the DFTs of K-point signals; they will have K samples
% themselves; construct a dummy K-dimensional array to store the result
result = complex(zeros(1, K));

for j = 0:(L-1)
    x_j = x(j*K+1:(j+1)*K); % jth subset
    X_j = fft(x_j); % DFT of the jth subset

    % Keep accumulating the DFT over subsets
    result = result + X_j;
end

% Average the DFT
result = result / L;

end

```

Listing 2: DFT averaging

A.2 Interpolation

```

clear;
clc;
close all;

% 3.2.1 - Load the signal
load handel;

% We will only be looking at the first 20,000 samples of the signal

```

```

N = 20000;
x_1 = y(1:N);

% Visualize the original signal
figure;

stem(x_1(1:50), "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "auto");

title("Original Signal", "Interpreter", "latex");
grid on;
grid minor;

% Empty array to store interpolations for later comparison
interpolations = {};

for i = 2:4
    % 3.2.2 - Form the signal x_i as described
    x_i = y(1:i:N);

    % 3.2.3 -
    % Obtain an interpolated version of x_i from the zero-padded DFT of x_i
    % with K = i - 1
    x_i_interpolated = interpolate(zero_padded_dft(x_i, i-1), i-1);

    % Compute the norm of the difference between the original signal and
    % the interpolated version
    disp("Norm of difference: " + difference_norm(x_i_interpolated, x_1));

    % Plot the signals for comparison
    plot_interpolation_v_actual(x_i_interpolated, x_1);

    % Save the current interpolated version for later comparison
    interpolations{end+1} = x_i_interpolated;
end

% Plot all interpolated signals together, and on top of each other with the
% original signal for comparison
figure;

% Plot the original signal
subplot(5, 1, 1);

stem(x_1(1:50), "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "auto");

title("Original Signal", "Interpreter", "latex");
grid on;
grid minor;

% Plot each interpolated signal in succession
for i = 1:3
    subplot(5, 1, i + 1);

    interpolation_i = interpolations{i};

```

```

        stem(interpolation_i(1:50), "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "
            auto");

        title("$x_" + (i+1) + "$ Interpolated", "Interpreter", "latex");
        grid on;
        grid minor;
    end

% Plot all interpolations and the original signal on top of each other
subplot(5, 1, 5);

stem(x_1(1:50), "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "auto");
hold on;

for j = 1:3
    interpolation_j = interpolations{j};
    stem(interpolation_j(1:50), "Marker", "o", "MarkerSize", 2+j);
    hold on;
end

title("Comparison", "Interpreter", "latex");
legend("Original Signal", "$x_2$ Interpolated", "$x_3$ Interpolated", "$x_4$
    Interpolated", "Interpreter", "latex");
grid on;
grid minor;

% Helper Functions

function [] = plot_interpolation_v_actual(interpolation, actual)
    figure;

    % Plot the interpolated signal
    subplot(2, 1, 1);

    stem(interpolation(1:50), "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "
        auto");

    title("Interpolated Signal", "Interpreter", "latex");
    grid on;
    grid minor;

    % Plot the interpolated signal on top of the actual signal for
    % comparison
    subplot(2, 1, 2);

    stem(interpolation(1:50), "Marker", "o", "MarkerSize", 3, "MarkerFaceColor", "
        auto");
    hold on;
    stem(actual(1:50), "Marker", "o", "MarkerSize", 5);

    title("Interpolated Signal vs. Actual Signal", "Interpreter", "latex");
    legend("Interpolated Signal", "Actual Signal");
    grid on;
    grid minor;
end

```



```

end

function [result] = difference_norm(x1, x2)
    % Find the length of the shorter signal
    N = min(length(x1), length(x2));

    % Truncate both signals to the same length
    x1_trunc = x1(1:N);
    x2_trunc = x2(1:N);

    % Compute the norm of the difference between the truncated signals
    result = norm(x1_trunc - x2_trunc);
end

```

Listing 3: Main Code

```

function [result] = zero_padded_dft(x, K)
% ZERO_PADDED_DFT Obtain an (K+1)N-point DFT of x with zeros inserted in
% the middle
%
% x = time-domain signal, of length N
% K = sets the length of the resulting DFT
%
% Compute the DFT of x, split it in the middle, insert zeros between the
% two halves, and return the result. Splitting and other manipulations are
% done depending on the parity of N.

% Start by obtaining the DFT of x
X = fft(x);
N = length(X);

if mod(N, 2) % If X has an odd number of samples
    n = (N+1)/2; % Index of the point to split from

    % Insert KN zeros as described
    result = [
        X(1:n);
        complex(zeros(K*N, 1));
        X((n+1):N)
    ];
else % If X has an even number of samples
    n = N/2; % Index of the point to split from

    % Insert KN - 1 zeros as described
    result = [
        X(1:n);
        X(n+1)/2;
        complex(zeros((K*N)-1, 1));
        X(n+1)/2;
        X((n+2):N)
    ];
end

end

```

Listing 4: Zero-padding DFT

```
function [result] = interpolate(X, K)
%INTERPOLATE

N = length(X)/(K+1);

x = (K+1) * ifft(X);

result = x(1:((K+1)*(N-1)+1));

end
```

Listing 5: Interpolation