

Interpolation and Approximation Splines



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Spline Representation

Spline is a flexible strip used to produce a smooth curve through a designed set of points.

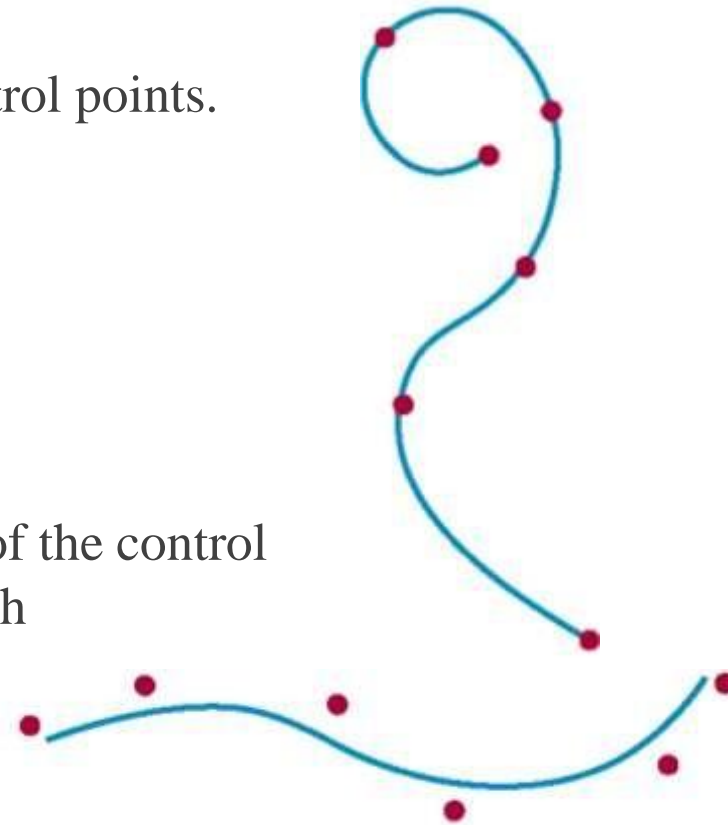
Spline mathematically describe with a piecewise cubic polynomial function whose first and second derivative are continuous across the various curve section.

A spline curve is specified using a set of coordinate position called **control points**, which indicates the general shape of the curve.

There are two ways to fit a curve to these points:

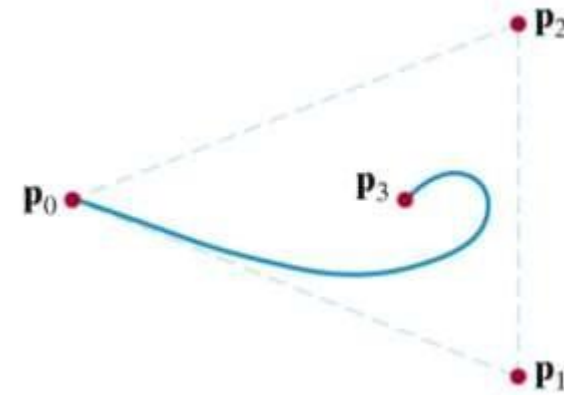
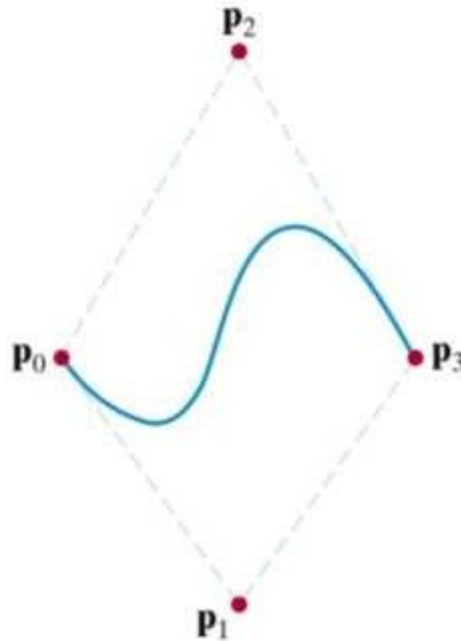
Interpolation - the curve passes through all of the control points.

Approximation - the curve does not pass through all of the control points, that are fitted to the general control-point path



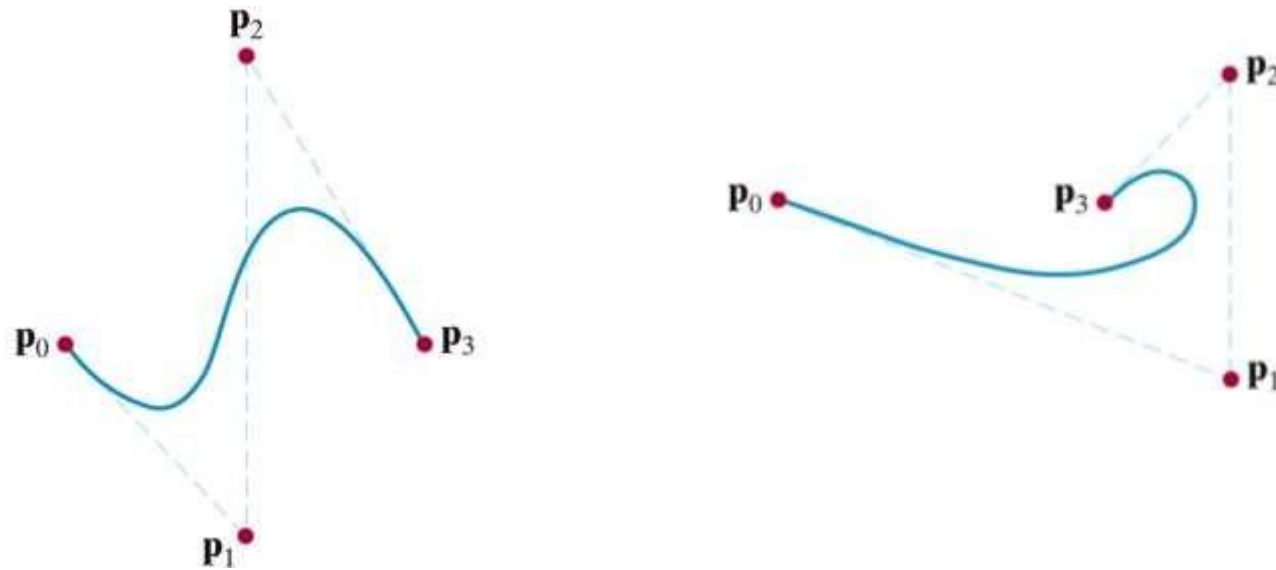
The spline curve is defined, modified and manipulated with operation on the control points.

The boundary formed by the set of control points is known as a **convex hull**



A polyline connecting the control points is known as a **control graph**.

Usually displayed to help designers keep track of their splines.



Other names for the series of straight-line sections connecting the control points in the order specified are **control polygon** and **characteristic polygon**.