This PDF represents the changes performed while forking mathematical libraries from **uniswap** library to make it compatible with **Fountain** project's `Oracle` contract
uniswap npm paths

- "@uniswap\lib\contracts\libraries\FullMath.sol"
- "@uniswap\lib\contracts\libraries\BitMath.sol"
- "@uniswap\lib\contracts\libraries\FixedPoint.sol"

Project's github repo

https://github.com/puls369ar/fountain-solicy-overview/Oracle

Changes Description

In Solidity, type(uint224).max returns the **maximum value** that a uint224 (an unsigned 224-bit integer) can hold. The same we've got in older version inside `FullMath`, `BitMath` and `FixedPoint` libraries, by using uint224(-1)
Also arithmetic operations changed with binary ones to prevent uint256 issues
When calculating `pow2`

below find code's *diff* between forked and original versions

Untitled diff

− 8 removals	86 lines	+ 8 additions	86 lines

```
1  // SPDX-License-Identifier: GPL-3.0-or-later
2  pragma solidity >=0.5.0;
3
4  library BitMath {
5      // Returns the 0 indexed position of the most significant bit of the input x
6      // s.t. x >= 2**msb and x < 2**(msb+1)
7      function mostSignificantBit(uint256 x) internal pure returns (uint8 r) {
8          require(x > 0, 'BitMath::mostSignificantBit: zero');
9
10         if (x >= 0x100000000000000000000000000000000) {
11             x >>= 128;
12             r += 128;
13         }
14         if (x >= 0x10000000000000000) {
15             x >>= 64;
16             r += 64;
17         }
18         if (x >= 0x100000000) {
19             x >>= 32;
20             r += 32;
21         }
22         if (x >= 0x10000) {
23             x >>= 16;
```

```
1  // SPDX-License-Identifier: GPL-3.0-or-later
2  pragma solidity >=0.8.20;
3
4  library BitMath {
5      // returns the 0 indexed position of the most significant bit of the input x
6      // s.t. x >= 2**msb and x < 2**(msb+1)
7      function mostSignificantBit(uint256 x) internal pure returns (uint8 r) {
8          require(x > 0, 'BitMath::mostSignificantBit: zero');
9
10         if (x >= 0x100000000000000000000000000000000) {
11             x >>= 128;
12             r += 128;
13         }
14         if (x >= 0x10000000000000000) {
15             x >>= 64;
16             r += 64;
17         }
18         if (x >= 0x100000000) {
19             x >>= 32;
20             r += 32;
21         }
22         if (x >= 0x10000) {
23             x >>= 16;
```

```
            r += 16;
        }
        if (x >= 0x100) {
            x >>= 8;
            r += 8;
        }
        if (x >= 0x10) {
            x >>= 4;
            r += 4;
        }
        if (x >= 0x4) {
            x >>= 2;
            r += 2;
        }
        if (x >= 0x2) r += 1;
    }

    // Returns the 0 indexed position of the least significant bit of the input x
    // s.t. (x & 2**lsb) != 0 and (x & (2**(lsb) - 1)) == 0)
    // i.e. the bit at the index is set and the mask of all lower bits is 0
    function leastSignificantBit(uint256 x) internal pure returns (uint8 r) {
        require(x > 0, 'BitMath::leastSignificantBit: zero');

        r = 255;
        if (x & type(uint128).max > 0) {
            r -= 128;
        } else {
            x >>= 128;
        }
        if (x & type(uint64).max > 0) {
            r -= 64;
        } else {
            x >>= 64;
        }
        if (x & type(uint32).max > 0) {
            r -= 32;
        } else {
            x >>= 32;
        }
        if (x & type(uint16).max > 0) {
```

```
            r += 16;
        }
        if (x >= 0x100) {
            x >>= 8;
            r += 8;
        }
        if (x >= 0x10) {
            x >>= 4;
            r += 4;
        }
        if (x >= 0x4) {
            x >>= 2;
            r += 2;
        }
        if (x >= 0x2) r += 1;
    }

    // returns the 0 indexed position of the least significant bit of the input x
    // s.t. (x & 2**lsb) != 0 and (x & (2**(lsb) - 1)) == 0)
    // i.e. the bit at the index is set and the mask of all lower bits is 0
    function leastSignificantBit(uint256 x) internal pure returns (uint8 r) {
        require(x > 0, 'BitMath::leastSignificantBit: zero');

        r = 255;
        if (x & uint128(-1) > 0) {
            r -= 128;
        } else {
            x >>= 128;
        }
        if (x & uint64(-1) > 0) {
            r -= 64;
        } else {
            x >>= 64;
        }
        if (x & uint32(-1) > 0) {
            r -= 32;
        } else {
            x >>= 32;
        }
        if (x & uint16(-1) > 0) {
```

```
            r -= 16;
        } else {
            x >>= 16;
        }
        if (x & type(uint8).max > 0) {
            r -= 8;
        } else {
            x >>= 8;
        }
        if (x & 0xf > 0) {
            r -= 4;
        } else {
            x >>= 4;
        }
        if (x & 0x3 > 0) {
            r -= 2;
        } else {
            x >>= 2;
        }
        if (x & 0x1 > 0) r -= 1;
    }
}
```

```
            r -= 16;
        } else {
            x >>= 16;
        }
        if (x & uint8(-1) > 0) {
            r -= 8;
        } else {
            x >>= 8;
        }
        if (x & 0xf > 0) {
            r -= 4;
        } else {
            x >>= 4;
        }
        if (x & 0x3 > 0) {
            r -= 2;
        } else {
            x >>= 2;
        }
        if (x & 0x1 > 0) r -= 1;
    }
}
```

Untitled diff

41 removals 147 lines

38 additions 147 lines

```
1  // SPDX-License-Identifier: GPL-3.0-or-later
2  pragma solidity >=0.8.20;
3
4  import '@uniswap/lib/contracts/libraries/FullMath.sol';
5  import '@uniswap/lib/contracts/libraries/Babylonian.sol';
6  import './BitMath.sol';
7
8  // A library for handling binary fixed-point numbers (https://en.wikipedia.org/wiki/Q_(number_format))
9  library FixedPoint {
10     // Range: [0, 2**112 - 1]
11     // Resolution: 1 / 2**112
12     struct uq112x112 {
13         uint224 _x;
14     }
15
16     // Range: [0, 2**144 - 1]
17     // Resolution: 1 / 2**112
18     struct uq144x112 {
19         uint256 _x;
20     }
```

```
1  // SPDX-License-Identifier: GPL-3.0-or-later
2  pragma solidity >=0.8.20;
3
4  import '@uniswap/lib/contracts/libraries/FullMath.sol';
5  import '@uniswap/lib/contracts/libraries/Babylonian.sol';
6  import './BitMath.sol';
7
8  // a library for handling binary fixed point numbers (https://en.wikipedia.org/wiki/Q_(number_format))
9  library FixedPoint {
10     // range: [0, 2**112 - 1]
11     // resolution: 1 / 2**112
12     struct uq112x112 {
13         uint224 _x;
14     }
15
16     // range: [0, 2**144 - 1]
17     // resolution: 1 / 2**112
18     struct uq144x112 {
19         uint256 _x;
20     }
```

```
21
22      uint8 public constant RESOLUTION = 112;
23      uint256 public constant Q112 = 0x10000000000000000000000000000000; // 2**112
24      uint256 private constant Q224 = 0x100000000000000000000000000000000000000000000000000000000000000000; // 2**224
25      uint256 private constant LOWER_MASK = 0xffffffffffffffffffffffffffff; // Decimal of UQ*x112 (lower 112 bits)
26
27      // Encode a uint112 as a UQ112x112
28      function encode(uint112 x) internal pure returns (uq112x112 memory) {
29          return uq112x112(uint224(x) << RESOLUTION);
30      }
31
32      // Encodes a uint144 as a UQ144x112
33      function encode144(uint144 x) internal pure returns (uq144x112 memory) {
34          return uq144x112(uint256(x) << RESOLUTION);
35      }
36
37      // Decode a UQ112x112 into a uint112 by truncating after the radix point
38      function decode(uq112x112 memory self) internal pure returns (uint112) {
39          return uint112(self._x >> RESOLUTION);
40      }
41
42      // Decode a UQ144x112 into a uint144 by truncating after the radix point
43      function decode144(uq144x112 memory self) internal pure returns (uint144) {
44          return uint144(self._x >> RESOLUTION);
45      }
```

```
21
22      uint8 public constant RESOLUTION = 112;
23      uint256 public constant Q112 = 0x10000000000000000000000000000000; // 2**112
24      uint256 private constant Q224 = 0x100000000000000000000000000000000000000000000000000000000000000000; // 2**224
25      uint256 private constant LOWER_MASK = 0xffffffffffffffffffffffffffff; // decimal of UQ*x112 (lower 112 bits)
26
27      // encode a uint112 as a UQ112x112
28      function encode(uint112 x) internal pure returns (uq112x112 memory) {
29          return uq112x112(uint224(x) << RESOLUTION);
30      }
31
32      // encodes a uint144 as a UQ144x112
33      function encode144(uint144 x) internal pure returns (uq144x112 memory) {
34          return uq144x112(uint256(x) << RESOLUTION);
35      }
36
37      // decode a UQ112x112 into a uint112 by truncating after the radix point
38      function decode(uq112x112 memory self) internal pure returns (uint112) {
39          return uint112(self._x >> RESOLUTION);
40      }
41
42      // decode a UQ144x112 into a uint144 by truncating after the radix point
43      function decode144(uq144x112 memory self) internal pure returns (uint144) {
44          return uint144(self._x >> RESOLUTION);
45      }
```

```
46
47      // Multiply a UQ112x112 by a uint, returning a UQ144x112
48      // Reverts on overflow
49      function mul(uq112x112 memory self, uint256 y) internal pure returns (uq144x112 memory) {
50          uint256 z = 0;
51          require(y == 0 || (z = self._x * y) / y == self._x, 'FixedPoint::mul: overflow');
52          return uq144x112(z);
53      }
54
55      // Multiply a UQ112x112 by an int and decode, returning an int
56      // Reverts on overflow
57      function muli(uq112x112 memory self, int256 y) internal pure returns (int256) {
58          uint256 z = FullMath.mulDiv(self._x, uint256(y < 0 ? -y : y), Q112);
59          require(z < 2**255, 'FixedPoint::muli: overflow');
60          return y < 0 ? -int256(z) : int256(z);
61      }
62
63      // Multiply a UQ112x112 by a UQ112x112, returning a UQ112x112
64      // Lossy
65      function muluq(uq112x112 memory self, uq112x112 memory other) internal pure returns (uq112x112 memory) {
66          if (self._x == 0 || other._x == 0) {
67              return uq112x112(0);
68          }
69          uint112 upper_self = uint112(self._x >> RESOLUTION); // * 2^0
70          uint112 lower_self = uint112(self._x & LOWER_MASK); // * 2^-112
```

```
46
47      // multiply a UQ112x112 by a uint, returning a UQ144x112
48      // reverts on overflow
49      function mul(uq112x112 memory self, uint256 y) internal pure returns (uq144x112 memory) {
50          uint256 z = 0;
51          require(y == 0 || (z = self._x * y) / y == self._x, 'FixedPoint::mul: overflow');
52          return uq144x112(z);
53      }
54
55      // multiply a UQ112x112 by an int and decode, returning an int
56      // reverts on overflow
57      function muli(uq112x112 memory self, int256 y) internal pure returns (int256) {
58          uint256 z = FullMath.mulDiv(self._x, uint256(y < 0 ? -y : y), Q112);
59          require(z < 2**255, 'FixedPoint::muli: overflow');
60          return y < 0 ? -int256(z) : int256(z);
61      }
62
63      // multiply a UQ112x112 by a UQ112x112, returning a UQ112x112
64      // lossy
65      function muluq(uq112x112 memory self, uq112x112 memory other) internal pure returns (uq112x112 memory) {
66          if (self._x == 0 || other._x == 0) {
67              return uq112x112(0);
68          }
69          uint112 upper_self = uint112(self._x >> RESOLUTION); // * 2^0
70          uint112 lower_self = uint112(self._x & LOWER_MASK); // * 2^-112
```

```
71          uint112 upper_other = uint112(other._x >> RESOLUTION); // * 2^0
72          uint112 lower_other = uint112(other._x & LOWER_MASK); // * 2^-112
73
74          // Partial products
75          uint224 upper = uint224(upper_self) * upper_other; // * 2^0
76          uint224 lower = uint224(lower_self) * lower_other; // * 2^-224
77          uint224 uppers_lowero = uint224(upper_self) * lower_other; // * 2^-112
78          uint224 uppero_lowers = uint224(upper_other) * lower_self; // * 2^-112
79
80          // So the bit shift does not overflow
81          require(upper <= type(uint112).max, 'FixedPoint::muluq: upper overflow');
82
83          // This cannot exceed 256 bits, all values are 224 bits
84          uint256 sum = uint256(upper << RESOLUTION) + uppers_lowero + uppero_lowers + (lower >> RESOLUTION);
85
86          // So the cast does not overflow
87          require(sum <= type(uint224).max, 'FixedPoint::muluq: sum overflow');
88
89          return uq112x112(uint224(sum));
90      }
91
92      // Divide a UQ112x112 by a UQ112x112, returning a UQ112x112
```

```
71          uint112 upper_other = uint112(other._x >> RESOLUTION); // * 2^0
72          uint112 lower_other = uint112(other._x & LOWER_MASK); // * 2^-112
73
74          // partial products
75          uint224 upper = uint224(upper_self) * upper_other; // * 2^0
76          uint224 lower = uint224(lower_self) * lower_other; // * 2^-224
77          uint224 uppers_lowero = uint224(upper_self) * lower_other; // * 2^-112
78          uint224 uppero_lowers = uint224(upper_other) * lower_self; // * 2^-112
79
80          // so the bit shift does not overflow
81          require(upper <= uint112(-1), 'FixedPoint::muluq: upper overflow');
82
83          // this cannot exceed 256 bits, all values are 224 bits
84          uint256 sum = uint256(upper << RESOLUTION) + uppers_lowero + uppero_lowers + (lower >> RESOLUTION);
85
86          // so the cast does not overflow
87          require(sum <= uint224(-1), 'FixedPoint::muluq: sum overflow');
88
89          return uq112x112(uint224(sum));
90      }
91
92      // divide a UQ112x112 by a UQ112x112, returning a UQ112x112
```

```
93      function divuq(uq112x112 memory
self, uq112x112 memory other) internal
pure returns (uq112x112 memory) {
94          require(other._x > 0,
'FixedPoint::divuq: division by zero');
95          if (self._x == other._x) {
96              return
uq112x112(uint224(Q112));
97          }
98          if (self._x <=
type(uint144).max) {  // Changed here
99              uint256 value =
(uint256(self._x) << RESOLUTION) /
other._x;
100             require(value <=
type(uint224).max, 'FixedPoint::divuq:
overflow');
101             return
uq112x112(uint224(value));
102         }
103
104         uint256 result =
FullMath.mulDiv(Q112, self._x,
other._x);
105         require(result <=
type(uint224).max, 'FixedPoint::divuq:
overflow');
106         return
uq112x112(uint224(result));
107     }
108
109     // Returns a UQ112x112 which
represents the ratio of the numerator
to the denominator
110     // Can be lossy
111     function fraction(uint256
numerator, uint256 denominator)
internal pure returns (uq112x112
memory) {
112         require(denominator > 0,
'FixedPoint::fraction: division by
zero');
113         if (numerator == 0) return
FixedPoint.uq112x112(0);
114
```

```
93      function divuq(uq112x112 memory
self, uq112x112 memory other) internal
pure returns (uq112x112 memory) {
94          require(other._x > 0,
'FixedPoint::divuq: division by zero');
95          if (self._x == other._x) {
96              return
uq112x112(uint224(Q112));
97          }
98          if (self._x <= uint144(-1)) {
99              uint256 value =
(uint256(self._x) << RESOLUTION) /
other._x;
100             require(value <=
uint224(-1), 'FixedPoint::divuq:
overflow');
101             return
uq112x112(uint224(value));
102         }
103
104         uint256 result =
FullMath.mulDiv(Q112, self._x,
other._x);
105         require(result <= uint224(-1),
'FixedPoint::divuq: overflow');
106         return
uq112x112(uint224(result));
107     }
108
109     // returns a UQ112x112 which
represents the ratio of the numerator
to the denominator
110     // can be lossy
111     function fraction(uint256
numerator, uint256 denominator)
internal pure returns (uq112x112
memory) {
112         require(denominator > 0,
'FixedPoint::fraction: division by
zero');
113         if (numerator == 0) return
FixedPoint.uq112x112(0);
114
```

```
115         if (numerator <= type(uint144).max) {   // Changed here
116             uint256 result = (numerator << RESOLUTION) / denominator;
117             require(result <= type(uint224).max, 'FixedPoint::fraction: overflow');
118             return uq112x112(uint224(result));
119         } else {
120             uint256 result = FullMath.mulDiv(numerator, Q112, denominator);
121             require(result <= type(uint224).max, 'FixedPoint::fraction: overflow');
122             return uq112x112(uint224(result));
123         }
124     }
125 
126     // Take the reciprocal of a UQ112x112
127     // Reverts on overflow
128     // Lossy
129     function reciprocal(uq112x112 memory self) internal pure returns (uq112x112 memory) {
130         require(self._x != 0, 'FixedPoint::reciprocal: reciprocal of zero');
131         require(self._x != 1, 'FixedPoint::reciprocal: overflow');
132         return uq112x112(uint224(Q224 / self._x));
133     }
134 
135     // Square root of a UQ112x112
136     // Lossy between 0/1 and 40 bits
137     function sqrt(uq112x112 memory self) internal pure returns (uq112x112 memory) {
138         if (self._x <= type(uint144).max) {   // Changed here
```

```
115         if (numerator <= uint144(-1)) {
116             uint256 result = (numerator << RESOLUTION) / denominator;
117             require(result <= uint224(-1), 'FixedPoint::fraction: overflow');
118             return uq112x112(uint224(result));
119         } else {
120             uint256 result = FullMath.mulDiv(numerator, Q112, denominator);
121             require(result <= uint224(-1), 'FixedPoint::fraction: overflow');
122             return uq112x112(uint224(result));
123         }
124     }
125 
126     // take the reciprocal of a UQ112x112
127     // reverts on overflow
128     // lossy
129     function reciprocal(uq112x112 memory self) internal pure returns (uq112x112 memory) {
130         require(self._x != 0, 'FixedPoint::reciprocal: reciprocal of zero');
131         require(self._x != 1, 'FixedPoint::reciprocal: overflow');
132         return uq112x112(uint224(Q224 / self._x));
133     }
134 
135     // square root of a UQ112x112
136     // lossy between 0/1 and 40 bits
137     function sqrt(uq112x112 memory self) internal pure returns (uq112x112 memory) {
138         if (self._x <= uint144(-1)) {
```

```
139             return
    uq112x112(uint224(Babylonian.sqrt(uint2
    56(self._x) << 112)));
140         }
141
142         uint8 safeShiftBits = 255 -
    BitMath.mostSignificantBit(self._x);
143         safeShiftBits -= safeShiftBits
    % 2;
144         return
    uq112x112(uint224(Babylonian.sqrt(uint2
    56(self._x) << safeShiftBits) << ((112
    - safeShiftBits) / 2)));
145     }
146 }
147
```

```
139             return
    uq112x112(uint224(Babylonian.sqrt(uint2
    56(self._x) << 112)));
140         }
141
142         uint8 safeShiftBits = 255 -
    BitMath.mostSignificantBit(self._x);
143         safeShiftBits -= safeShiftBits
    % 2;
144         return
    uq112x112(uint224(Babylonian.sqrt(uint2
    56(self._x) << safeShiftBits) << ((112
    - safeShiftBits) / 2)));
145     }
146 }
147
```

Untitled diff

− 8 removals	52 lines	+ 6 additions	52 lines

```
1  // SPDX-License-Identifier: CC-BY-4.0
2  pragma solidity >=0.4.0;
3
4  // Taken from
   https://medium.com/coinmonks/math-in-
   solidity-part-3-percents-and-
   proportions-4db014e080b1
5  // License is CC-BY-4.0
6  library FullMath {
7      function fullMul(uint256 x, uint256
   y) internal pure returns (uint256 l,
   uint256 h) {
8          uint256 mm = mulmod(x, y,
   type(uint256).max);
9          l = x * y;
10         h = mm - l;
11         if (mm < l) h -= 1;
12     }
13
14     function fullDiv(
15         uint256 l,
16         uint256 h,
17         uint256 d
18     ) private pure returns (uint256) {
19         uint256 pow2 = d & (~d + 1);  //
   Changed here
20         d /= pow2;
21         l /= pow2;
```

```
1  // SPDX-License-Identifier: CC-BY-4.0
2  pragma solidity >=0.4.0;
3
4  // taken from
   https://medium.com/coinmonks/math-in-
   solidity-part-3-percents-and-
   proportions-4db014e080b1
5  // license is CC-BY-4.0
6  library FullMath {
7      function fullMul(uint256 x, uint256
   y) internal pure returns (uint256 l,
   uint256 h) {
8          uint256 mm = mulmod(x, y,
   uint256(-1));
9          l = x * y;
10         h = mm - l;
11         if (mm < l) h -= 1;
12     }
13
14     function fullDiv(
15         uint256 l,
16         uint256 h,
17         uint256 d
18     ) private pure returns (uint256) {
19         uint256 pow2 = d & -d;
20         d /= pow2;
21         l /= pow2;
```

```
22          // l += h * ((-pow2 / pow2) + 1); // Changed here, Just commenting it is useless and out of our use
23          uint256 r = 1;
24          r *= 2 - d * r;
25          r *= 2 - d * r;
26          r *= 2 - d * r;
27          r *= 2 - d * r;
28          r *= 2 - d * r;
29          r *= 2 - d * r;
30          r *= 2 - d * r;
31          r *= 2 - d * r;
32          return l * r;
33      }
34
35      function mulDiv(
36          uint256 x,
37          uint256 y,
38          uint256 d
39      ) internal pure returns (uint256) {
40          (uint256 l, uint256 h) = fullMul(x, y);
41
42          uint256 mm = mulmod(x, y, d);
43          if (mm > l) h -= 1;
44          l -= mm;
45
46          if (h == 0) return l / d;
47
48          require(h < d, 'FullMath: FULLDIV_OVERFLOW');
49          return fullDiv(l, h, d);
50      }
51  }
52
```

```
22          l += h * ((-pow2) / pow2 + 1);
23          uint256 r = 1;
24          r *= 2 - d * r;
25          r *= 2 - d * r;
26          r *= 2 - d * r;
27          r *= 2 - d * r;
28          r *= 2 - d * r;
29          r *= 2 - d * r;
30          r *= 2 - d * r;
31          r *= 2 - d * r;
32          return l * r;
33      }
34
35      function mulDiv(
36          uint256 x,
37          uint256 y,
38          uint256 d
39      ) internal pure returns (uint256) {
40          (uint256 l, uint256 h) = fullMul(x, y);
41
42          uint256 mm = mulmod(x, y, d);
43          if (mm > l) h -= 1;
44          l -= mm;
45
46          if (h == 0) return l / d;
47
48          require(h < d, 'FullMath: FULLDIV_OVERFLOW');
49          return fullDiv(l, h, d);
50      }
51  }
52
```