

Data Science & Artificial Intelligence

Machine Learning

Bayesian Learning
Discussion Notes

DPP- 01



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#Q. Assume $P(A)=0.2$, $P(B)=0.6$, $P(A \cup B)=0.5$, Then $P[A|B]=$

A 0.2

B 0.3

C 0.6

D 0.5

Conditional Probability formula

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

Inclusion exclusion principle $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$$\Rightarrow 0.2 + 0.6 - P(A \cap B)$$

$$P(A \cap B) = 0.3$$

$$P(A|B) = 0.3 / 0.6 = 0.5$$

[MCQ]



#Q. Match List-I with List-II

multiplication
Conditional

	List-I		List-II
A.	Bayer' Theorem	I.	$P(\bar{E}) = 1 - P(E)$
B.	Conditional Probability	II.	$P(E_1 \cup E_2) = P(E_1) + P(E_2)$
C.	Theorem of complementary	III.	$P(E_2/E_1) = \frac{P(E_1 \cap E_2)}{P(E_1)}$
D.	Theorem of addition	IV.	$P(H_i/E) = \frac{P(H_i \cap E)}{P(E)}$

Choose the correct answer from the options given below:

A

A-I, B-IV, C-III, D-II

B

A-III, B-IV, C-II, D-I

C

A-III, B-IV, C-I, D-II

D

A-IV, B-III, C-I, D-II

[NAT]



$$\frac{\frac{6}{10} \times \frac{8}{10}}{\left(\frac{6}{10} \cdot \frac{8}{10} + \frac{4}{10} \cdot \frac{9}{10}\right)} = \frac{4}{7}$$

#Q. A bike manufacturing factory has two plants P and Q. Plant P manufactures 60 percent of bikes and plant Q manufacture 40 percent. 80 percent of the bikes at plant P and 90 percent of the bikes at plant Q are rated of standard quality. A bike is chosen at random and is found to be of standard quality. What is the probability that it has come from plant P?

Bayes theorem

$$P(E|A) = \frac{P(E) \times P(A|E)}{\sum_{i=1}^n P(E) \times P(A|E_i)} \quad \rightarrow i, = 1 \dots 2n$$

$$P(E_1|A) = \frac{P(E_1) \times P(A|E_1)}{\sum_{i=1}^n P(E_i) \times P(A|E_i)}$$

$$P(E_1) = \frac{60}{100} = 0.6$$

$$P(E_2) = \frac{40}{100} = 0.4$$

$$P(A|E_1) = \frac{80}{100} = 0.8$$

$$P(A|E_2) = 0.9$$

$$P(E_1|A) = \frac{P(E_1) \cdot P(A|E_1)}{P(E_1) \cdot P(A|E_1) + P(E_2) \cdot P(A|E_2)}$$

#Q. The chance of a defective screw in three boxes A, B, C are $\frac{1}{5}$, $\frac{1}{6}$ and $\frac{1}{7}$ respectively. A box is selected at random and a screw drawn from it at random is found to be defective. Find the probability that it came from box A.

A

$$\frac{42}{107}$$

$$\frac{1}{3} \times \frac{1}{5}$$

B

$$\frac{28}{107}$$

C

$$\frac{45}{107}$$

$$\frac{1}{3} \times \frac{1}{5} + \frac{1}{3} \times \frac{1}{6} + \frac{1}{3} \times \frac{1}{7}$$

D

$$\frac{66}{107}$$

$$= \frac{42}{107}$$

$$\begin{aligned}
 P(E_1) &= P(E_2) = P(E_3) \\
 &= \frac{1}{3} \\
 P(A|E_1) &= \frac{1}{5} \\
 P(A|E_2) &= \frac{1}{6} \\
 P(A|E_3) &= \frac{1}{7}
 \end{aligned}$$

#Q. Which of the following best describes Bayesian Learning?

A It is a type of machine learning that relies on probabilistic inference.

B It is a type of supervised learning that uses decision trees. *not-rectic*

C It is a type of unsupervised learning that uses clustering.

D It is a type of reinforcement learning that uses reward systems.

#Q. In Bayesian learning, the term $P(H|D)$ represents:



A

The prior probability of the hypothesis.

B

The likelihood of the hypothesis given the data.

C

The posterior probability of the hypothesis given the data.

$P(H|D)$

D

The marginal likelihood of the hypothesis.

update - belief about -
hypothesis after observing
the data.



THANK - YOU