Data Science and Artificial Intelligence

# Machine Learning

**Support Vector Machine** 

Lecture No. 6



# **Recap of Previous Lecture**





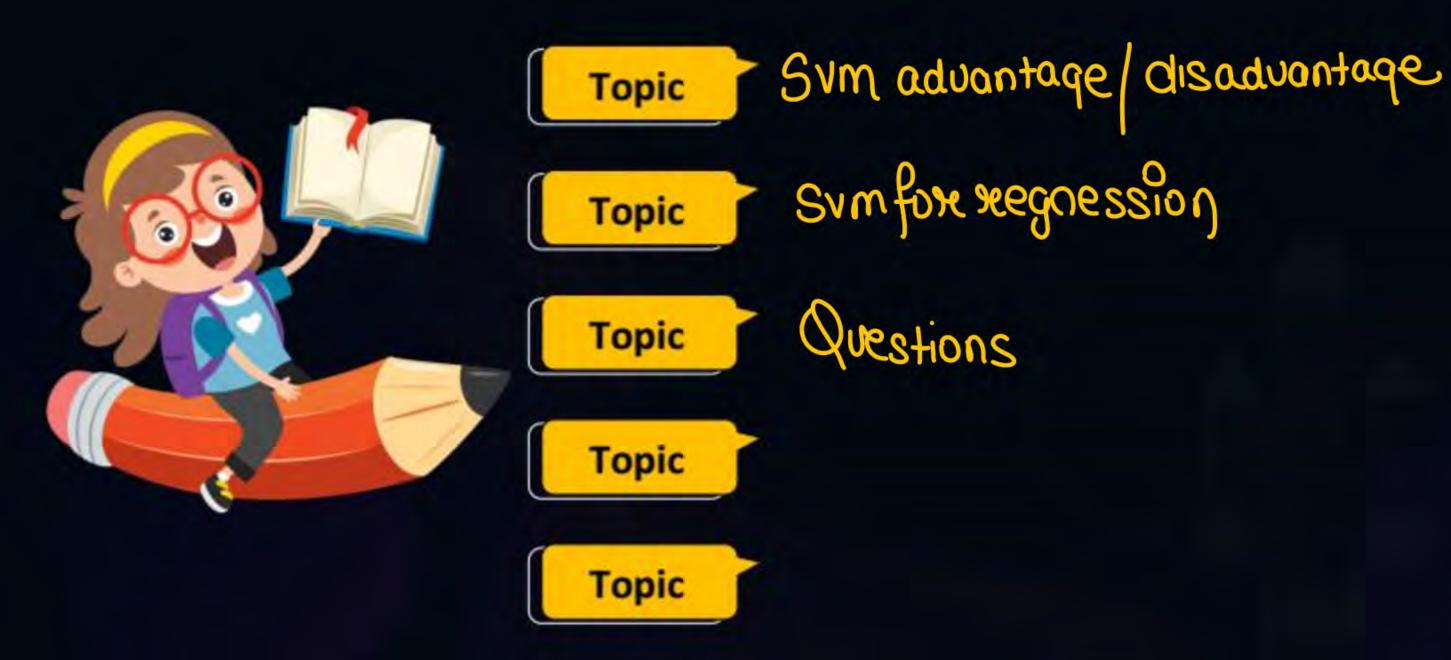


# **Topics to be Covered**













### **Basics of Machine Learning**







i=0 for sv's and other points



### **Basics of Machine Learning**





### **Soft Margin SVMs**

Ei = distance of point from morginal plane

KKT ) 
$$\frac{\partial L}{\partial \omega} = 0 \neq 10 = \sum \lambda i y i x i$$
2)  $\frac{\partial L}{\partial b} = 0 \neq \sum \lambda i y i = 0$ 
3)  $\frac{\partial L}{\partial b} = 0 \neq \lambda \lambda i + \lambda i = 0$ 
4)  $\lambda i \in 0$ 
5)  $\lambda i \left(1 - y : (\omega x i + b) - \delta i\right) = 0$ 

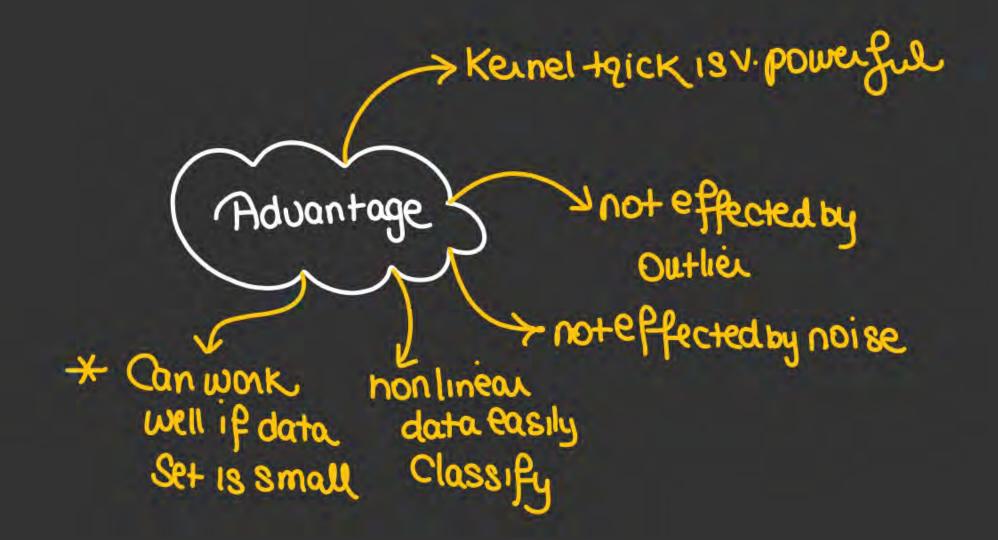


### **Basics of Machine Learning**





## **Soft Margin SVMs**







#### **Advantages of SVM**

- Handling high-dimensional data: SVMs are effective in handling high-dimensional data, which is common in many applications such as image and text classification.
- Handling small datasets: SVMs can perform well with small datasets, as they only require a small number of support vectors to define the boundary.
- Modeling non-linear decision boundaries: SVMs can model non-linear decision boundaries by using the kernel trick, which maps the data into a higher-dimensional space where the data becomes linearly separable.
- Robustness to noise: SVMs are robust to noise in the data, as the decision boundary is determined by the support vectors, which are the closest data points to the boundary.



# → Reduce dimensions >> Use subset of data

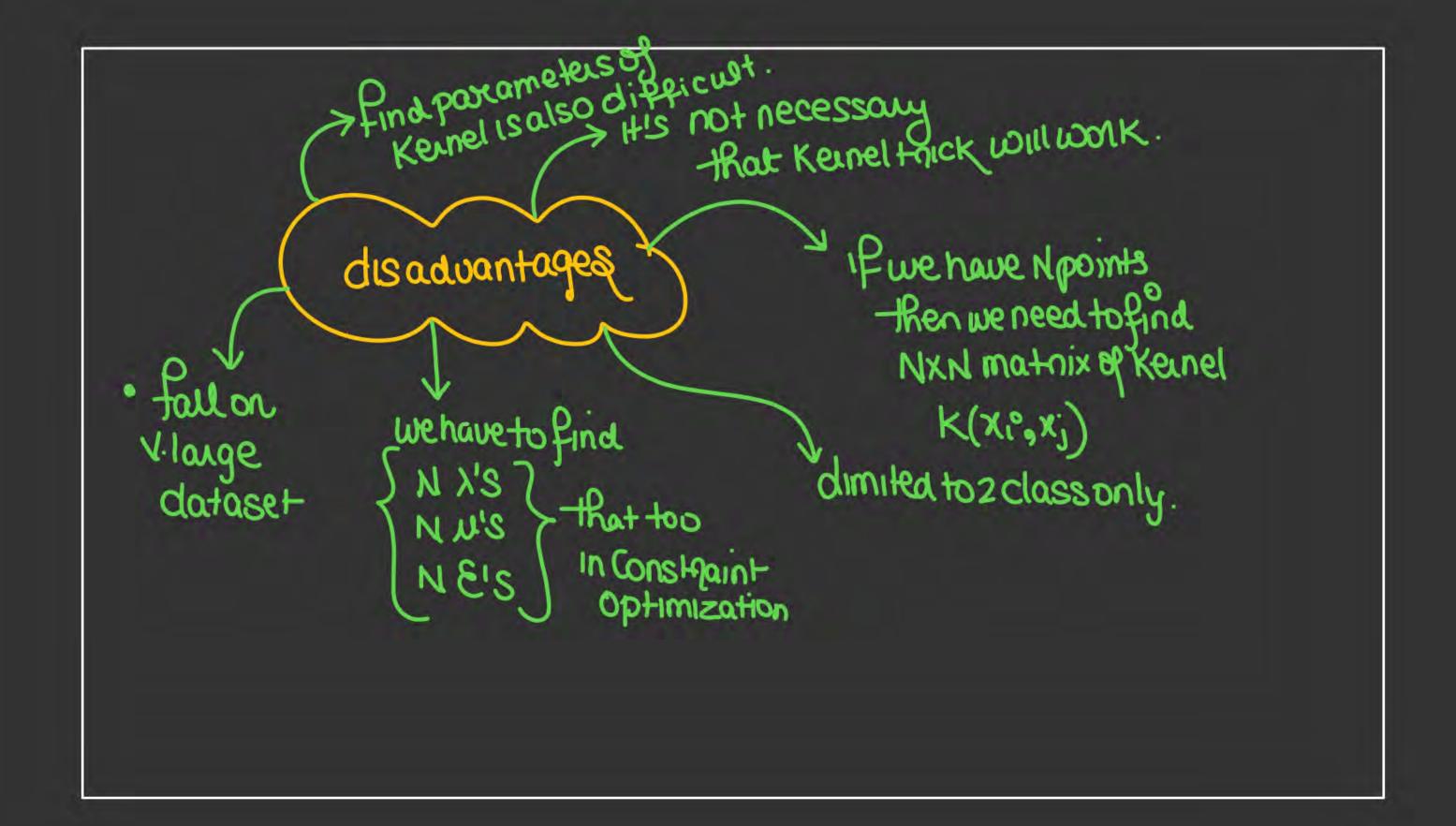


#### Advantages of SVM

Symaruse sy's

> In lasso also>> Some pl=0 801+uses few dimension.

- Sparse solution: SVMs have sparse solutions, which means that they only use a subset of the training data to make predictions. This makes the algorithm more efficient and less prone to overfitting.
- Regularization: SVMs can be regularized, which means that the algorithm can be modified to avoid overfitting.







#### Disadvantages of SVM

## -> Paxameters of Kernel of, C'

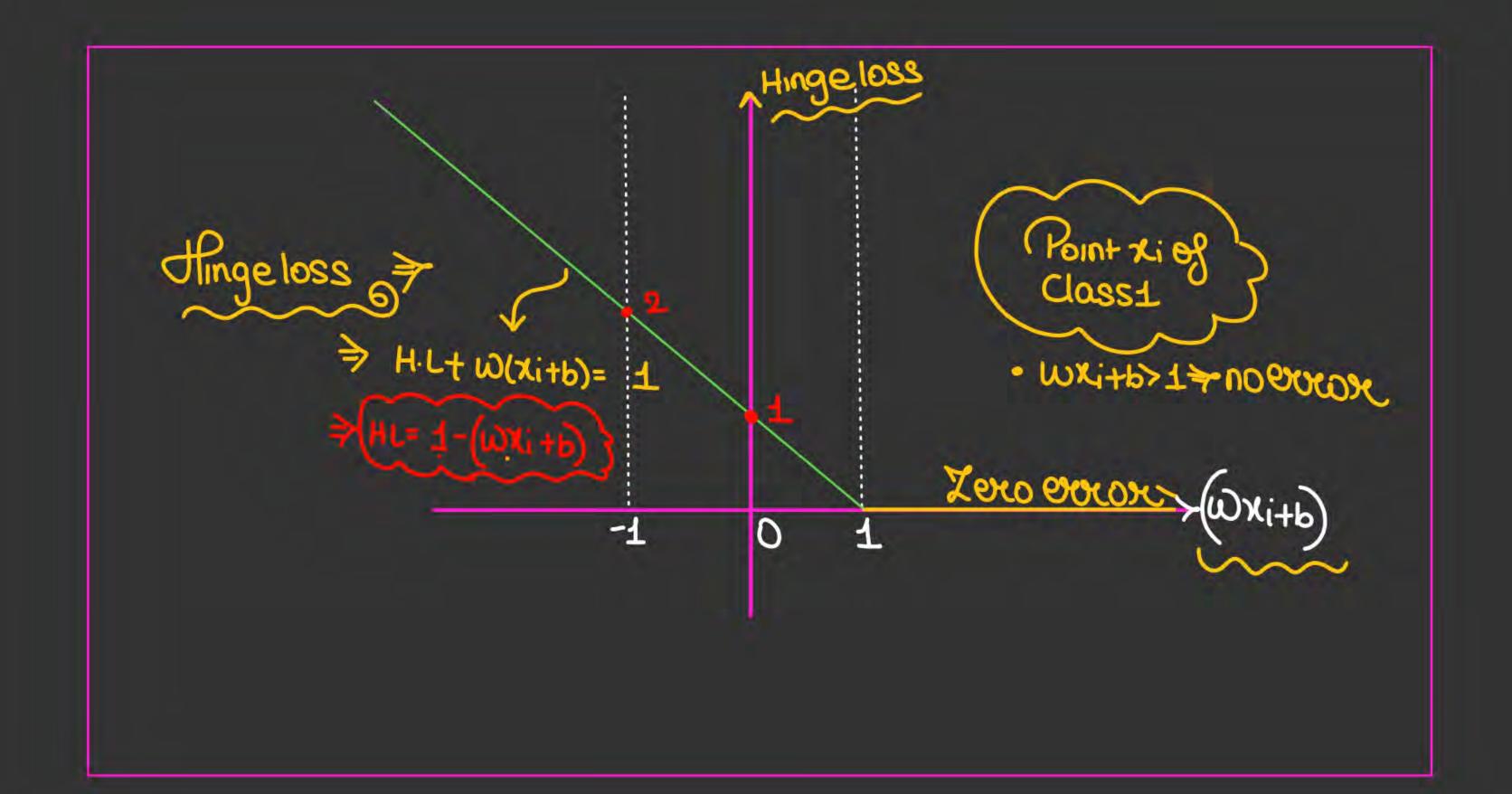
- Computationally expensive: SVMs can be computationally expensive for large datasets, as the algorithm requires solving a quadratic optimization problem.
- Choice of kernel: The choice of kernel can greatly affect the performance of an SVM, and it can be difficult to determine the best kernel for a given dataset.
- Sensitivity to the choice of parameters: SVMs can be sensitive to the choice of parameters, such as the regularization parameter, and it can be difficult to determine the optimal parameter values for a given dataset.
- Memory-intensive: SVMs can be memory-intensive, as the algorithm requires storing the kernel matrix, which can be large for large datasets.
- Limited to two-class problems: SVMs are primarily used for two-class problems, although multi-class problems can be solved by using one-versus-one or one-versus-all strategies.

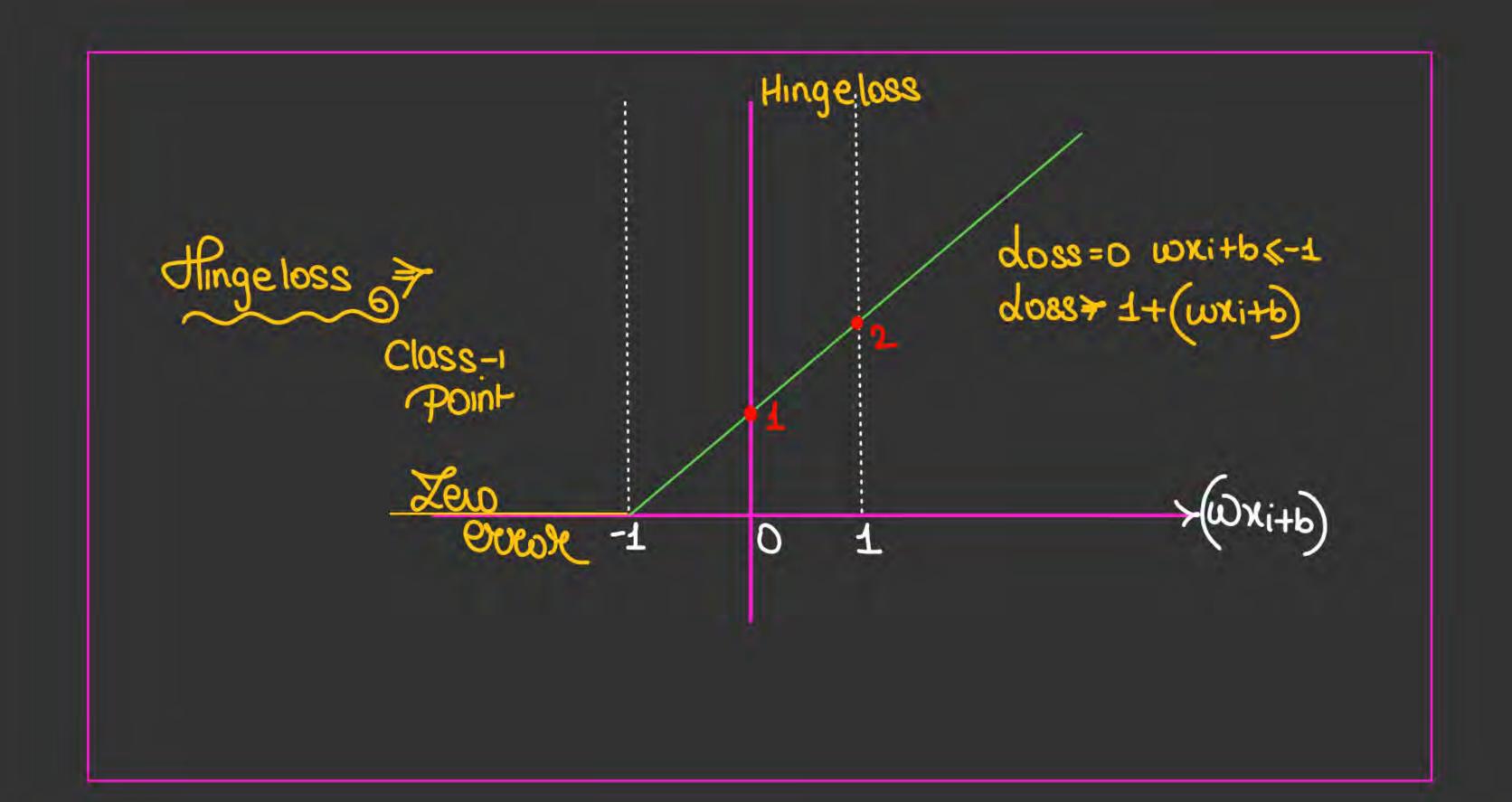




#### Disadvantages of SVM

- Not suitable for large datasets with many features: SVMs can be very slow and can consume a lot of memory when the dataset has many features.
- Not suitable for datasets with missing values: SVMs requires complete datasets, with no missing values, it can not handle missing values.





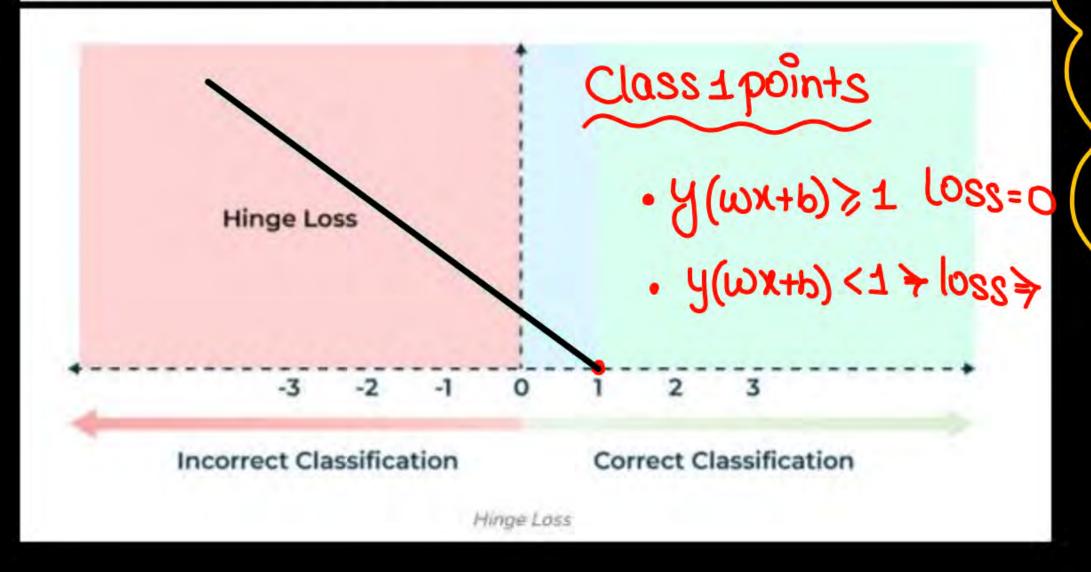




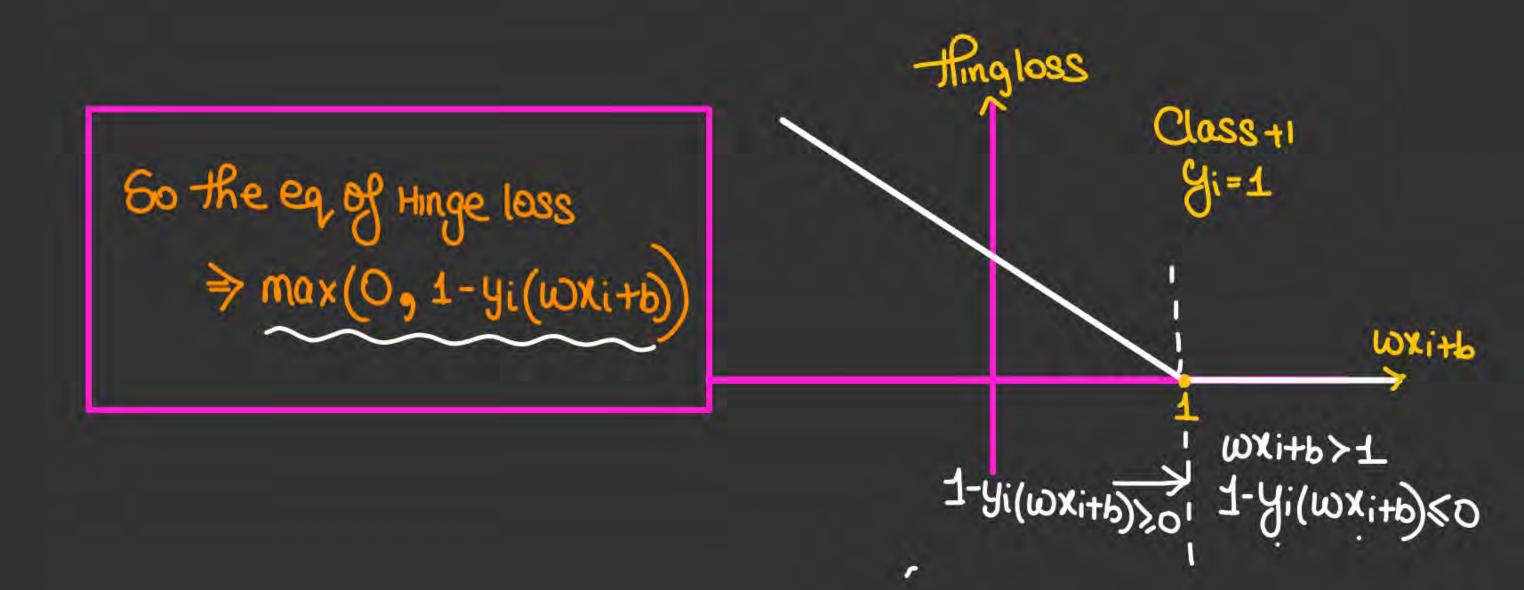
#### **Hinge Loss in SVMs**

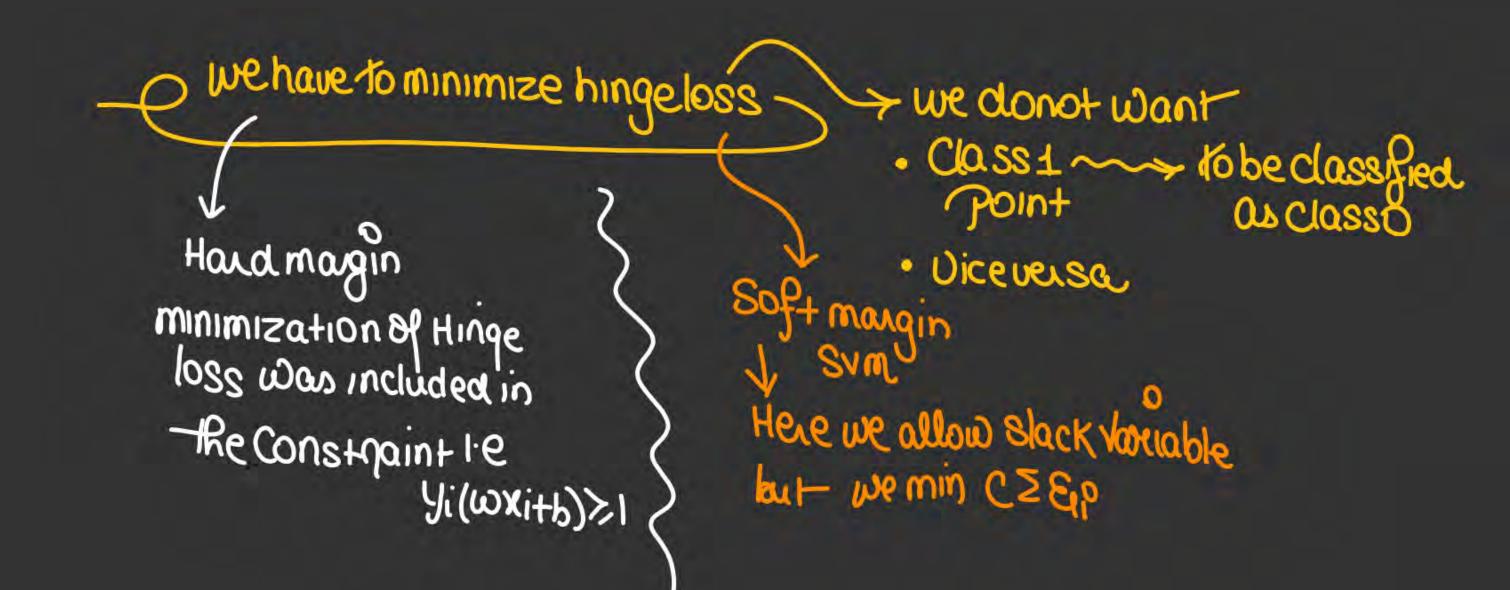
Mathematically, Hinge loss for a data point can be represented as :

$$L(y,f(x)) = max(0,1 - y * f(x))$$



```
Combine or
general eq
  d= 1-yi(wxi+b)
Class=1 yi=1
   d=1-(wxi+b)
 Class-1 yi=-1
    d=1+(wxi+b)
```









#### **Hinge Loss in SVMs**

- If we look at the mathematical formulation the hinge loss is effectively present in the constraints of a hard margin. This ensures that the decision boundary (the hyperplane) is positioned in such a way that it maximizes the margin without allowing any data points to be within or on the wrong side of the margin.

  Mesoftmagn symbol. Here the hinge loss component, is part of the objective
- Here the hinge loss component, is part of the objective function itself through slack variable.





The soft margin SVM is more preferred than the hard-margin svm when:

1. The data is linearly separable

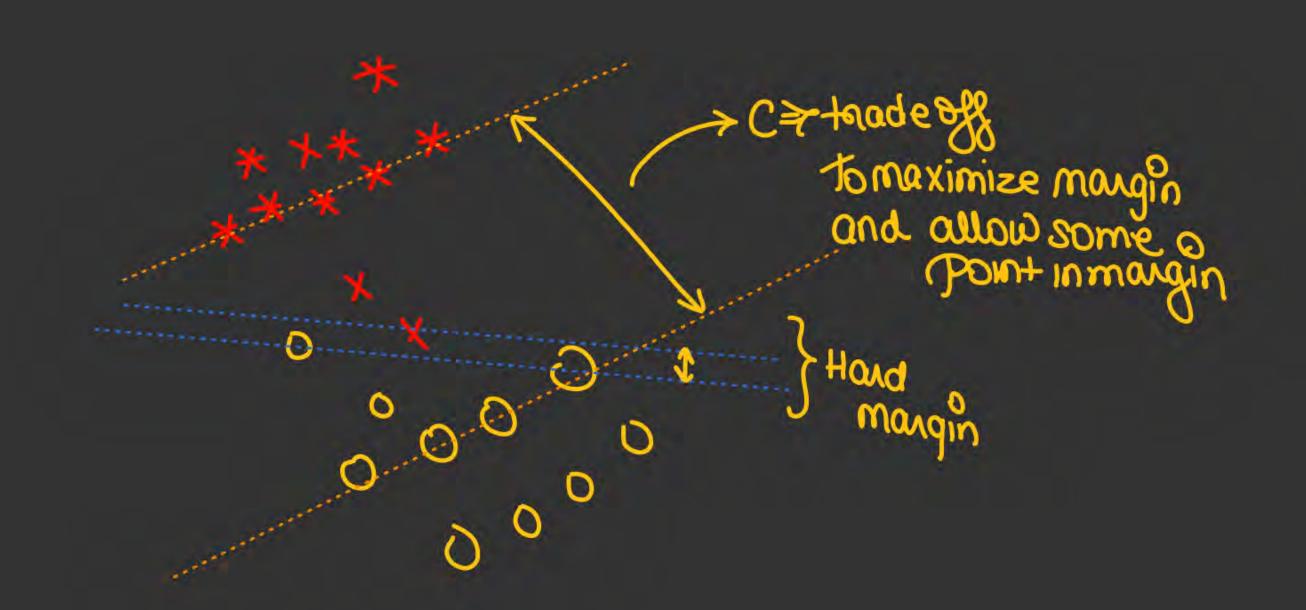
The data is noisy and contains overlapping point





In the linearly non-separable case, what effect does the C parameter have on the SVM mode.

- a. it determines how many data points lie within the margin
- it is a count of the number of data points which do not lie on their respective side of the hyperplane
- it allows us to trade-off the number of misclassified points in the training data and the size of the margin
- d. it counts the support vectors







SVM is a supervised Machine Learning can be used for Options :	
O Regression	O Classification
both a or b	O None of These



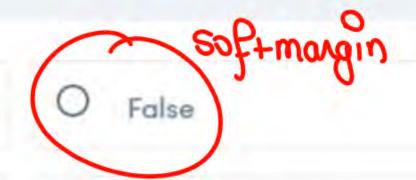


Closest Point to the hyperplane are support vectors



O (True) Hard margin

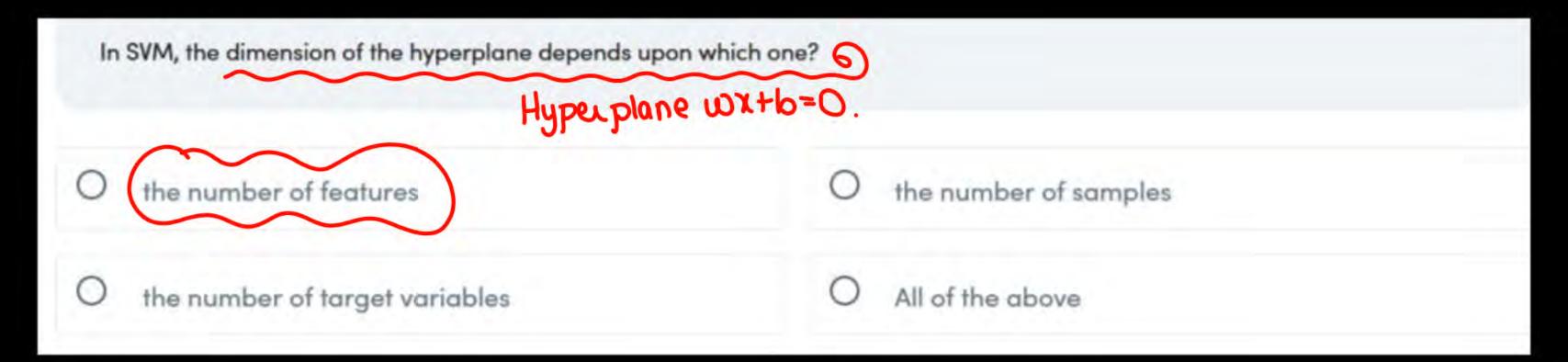
O Unpredictable



O None of these













Choose the correct option regarding classification using SVM for two classes Constraint

Statement i) While designing an SVM for two classes, the equation  $y_i(a^tx_i+b) \ge 1$  is used to choose the separating plane using the training vectors.

Statement ii : During inference, for an unknown vector  $x_j$ , if  $y_j(a^tx_j+b) \ge 0$ , then the vector can be assigned class 1.

Statement iii : During inference, for an unknown vector  $x_j$  , if  $(a^tx_j+b)>0$  , then the vector can be assigned class 1.

- a. Only Statement i is true
- Both Statements i and iii are true
  - c. Both Statements i and ii are true
  - d. Both Statements ii and iii are true





#### **QUESTION 7:**

Suppose we have the below set of points with their respective classes as shown in the table. Answer the following question based on the table.

X.	Y	Class Label
1	0	+1
-1	0	-1
2	1	+1
-1	-1	-1
2	0	+1

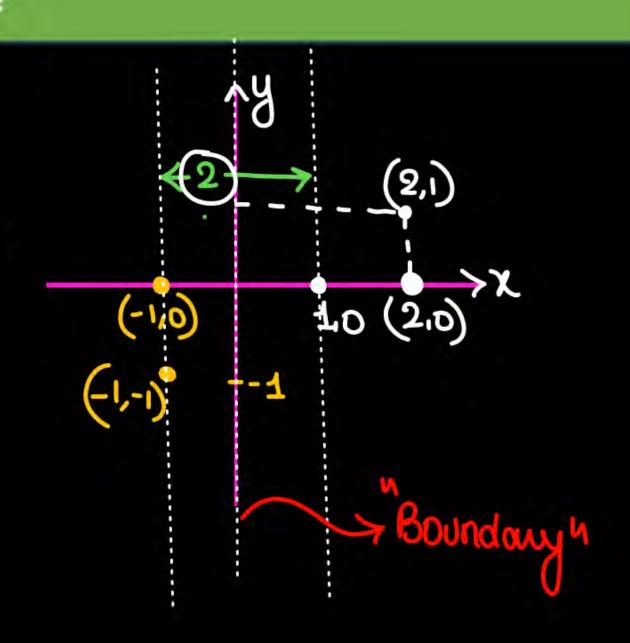
To find margin Simply

find the euclediandistance

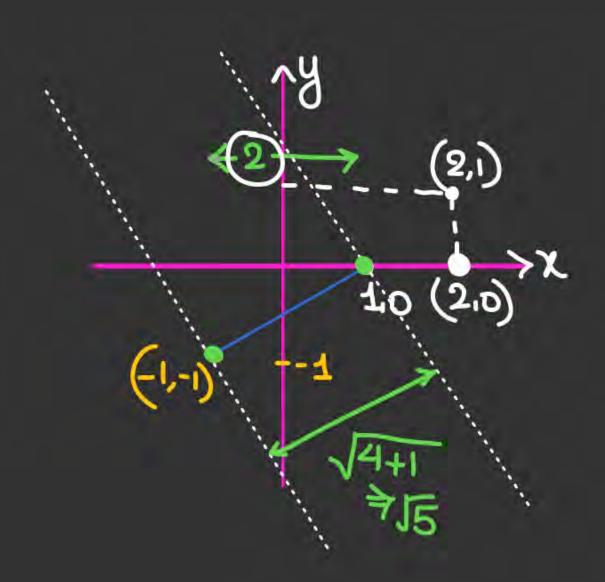
bliw sv's

What will happen to maximum margin if we remove the point (-1,0) from the training set?

- a. Maximum margin will decrease
- Maximum margin will increase
- c. Maximum margin will remain same
- d. Can not decide











Suppose we have the below set of points with their respective classes as shown in the table. Answer the following question based on the table.

X	Y	Class Label
1	0	+1
-1	0	-1
2	1	+1
-1	-1	-1
2	0	+1

What can be a possible decision boundary of the SVM for the given points?

a. 
$$y = 0$$

$$x=0$$

$$c. x = y$$

d. 
$$x + y = 1$$





Suppose we have the below set of points with their respective classes as shown in the table. Answer the following question based on the table.

х	Y	Class Label
1	0	+1
-1	0	-1
2	1	+1
-1	-1	-1
2	0	+1

Find the decision boundary of the SVM trained on these points and choose which of the following statements are true based on the decision boundary.

The point (-1,-2) is classified as -1

The point (1,-2) is classified as -1

The point (-1,-2) is classified as +1

The point (1,-2) is classified as +1





Which one of the following is a valid representation of hinge loss (of margin = 1) for a two-class problem?

Wewill see 6

y = class label (+1 or -1).

p = predicted (not normalized to denote any probability) value for a class.?

- L(y, p) = max(0, 1-yp)
- b. L(y, p) = min(0, 1-yp)
- c. L(y, p) = max(0, 1 + yp)
- d. None of the above



- #Q. Consider the problem of finding an optimal hyperplane for non-seperable patterns, we introduce a new set of variables,  $\{\xi_i\}_{i=1}^N$  into the definition of the 2 points separating hyperplane as  $d_i(w^{\dagger}x_i+b) > 1 \xi_i$ . Choose the correct statements from the options given below.
- The slack variable  $\xi_i$  can take both positive and negative values.
- For  $0 < \xi_i \le 1$  the data point falls inside the region of separation, but on the correct side of the decision surface.
- For  $\xi_i > 1$  the data point falls on the wrong side of the separating hyperplane.
- For support vectors  $\xi_i$  will be always zero.



#Q. For the nonseparable case, we minimize the cost function defined as

$$L = \frac{1}{2}\omega^T \omega + C \sum_{i=1}^{N} \xi_i$$

(True/False) The optimal value of C is obtained by minimizing the cost function with respect to C.

false

Ly (we find c by Cross Valudation)

- A True
- B False



- #Q. In continuation with question 2, consider the following statements:
  - (a) The parameter C can be chosen using cross validation approach.
  - (b) When C is assigned a small value, the training samples are considered to be noisy, and less emphasis should therefore be placed on it.
  - (c) The optimization problem for linearly separable patterns can be considered as a special case of optimization problem for nonseparable patterns, by setting  $\xi_1 = 0$  for points all i.
  - When C is assigned a large value, the implication is that the designer of the SVM has high confidence in the quality of the training samples. Which of the above statements are correct?
- A Only a and c

B Only b and d

C Only a, b and c

D

a, b, c and d



- #Q. If we are using a kernel function k to evaluate the inner products in a feature space with feature map 4, the associated Gram matrix G has entries  $G_{1j} = k(x_i, x_j) = \phi(x_1)^T \phi(x_j)$ . Then the kernel matrix G is
- A Positive definite.
- B Negative definite.
- C Positive semi-definite.
- D Negative semi-definite.



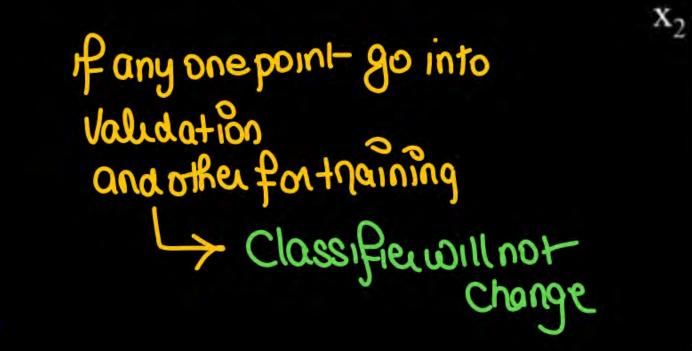
- #Q. In the linearly non-separable case, what effect does the C parameter have on the SVM model?
- A it determines the count of support vectors
- it is a count of the number of data points which do not lie on their respective side of the hyperplane
- c it determines how many data points lie within the margin
- it allows us to trade-off the number of misclassified points in the training data and the size of the margin

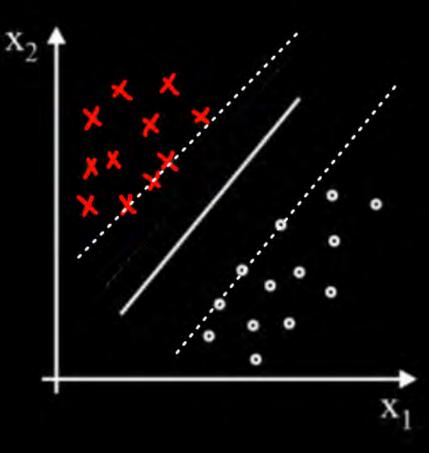


#Q. What is the leave-one-out cross-validation error estimate for maximum margin separation in the following figure?



- B 2
- C
- D 6









### **SVM** for regression

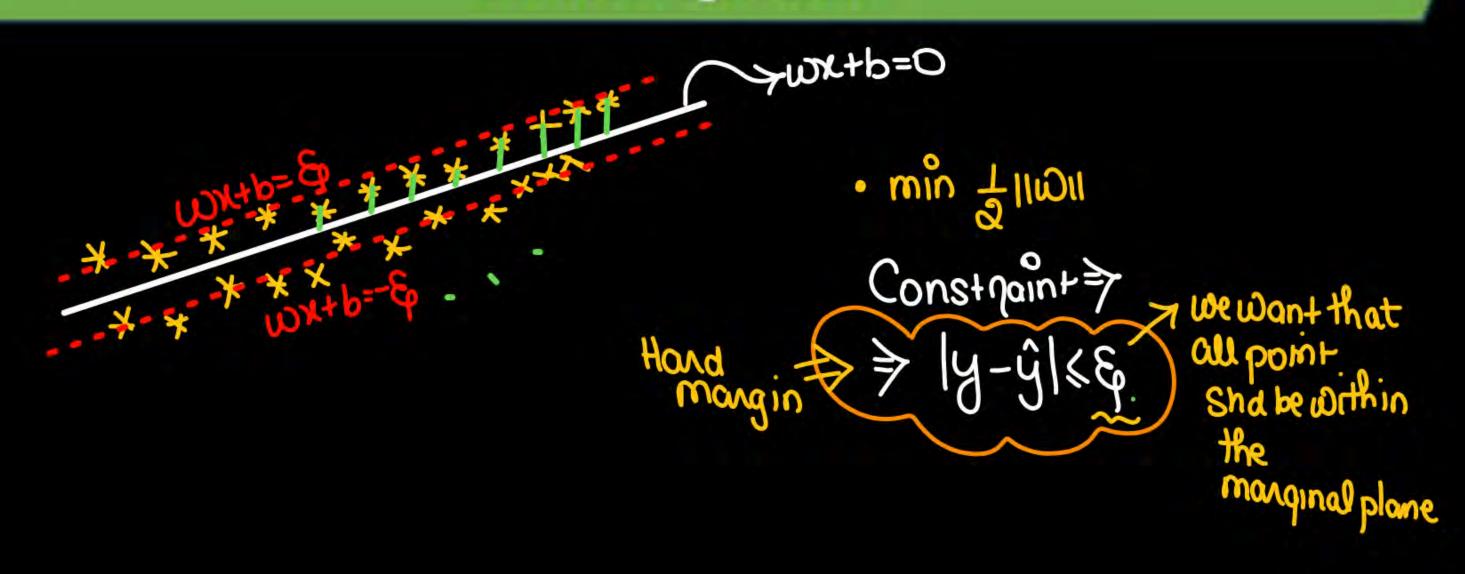
· generally we use sum for classification but we can use Surregnessor also.

.





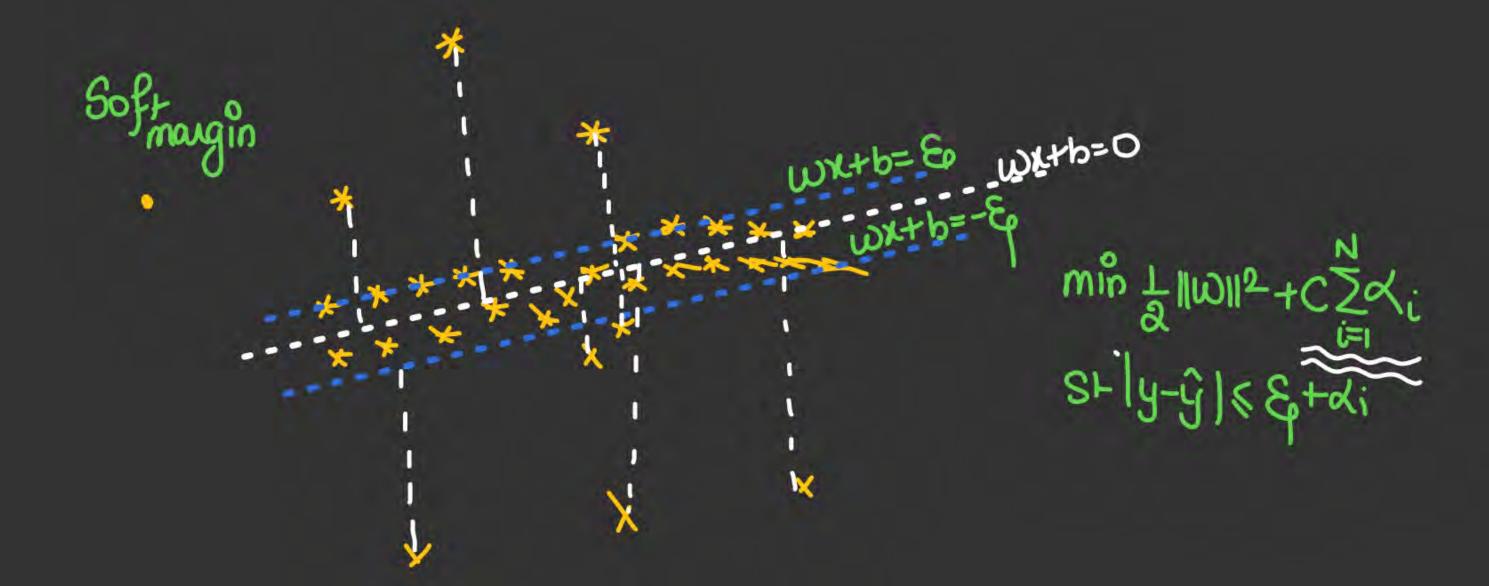
### **SVM** for regression







### **SVM** for regression





# THANK - YOU