

GATE

DATA SCIENCE + CS & IT

**Engineering
Mathematics**

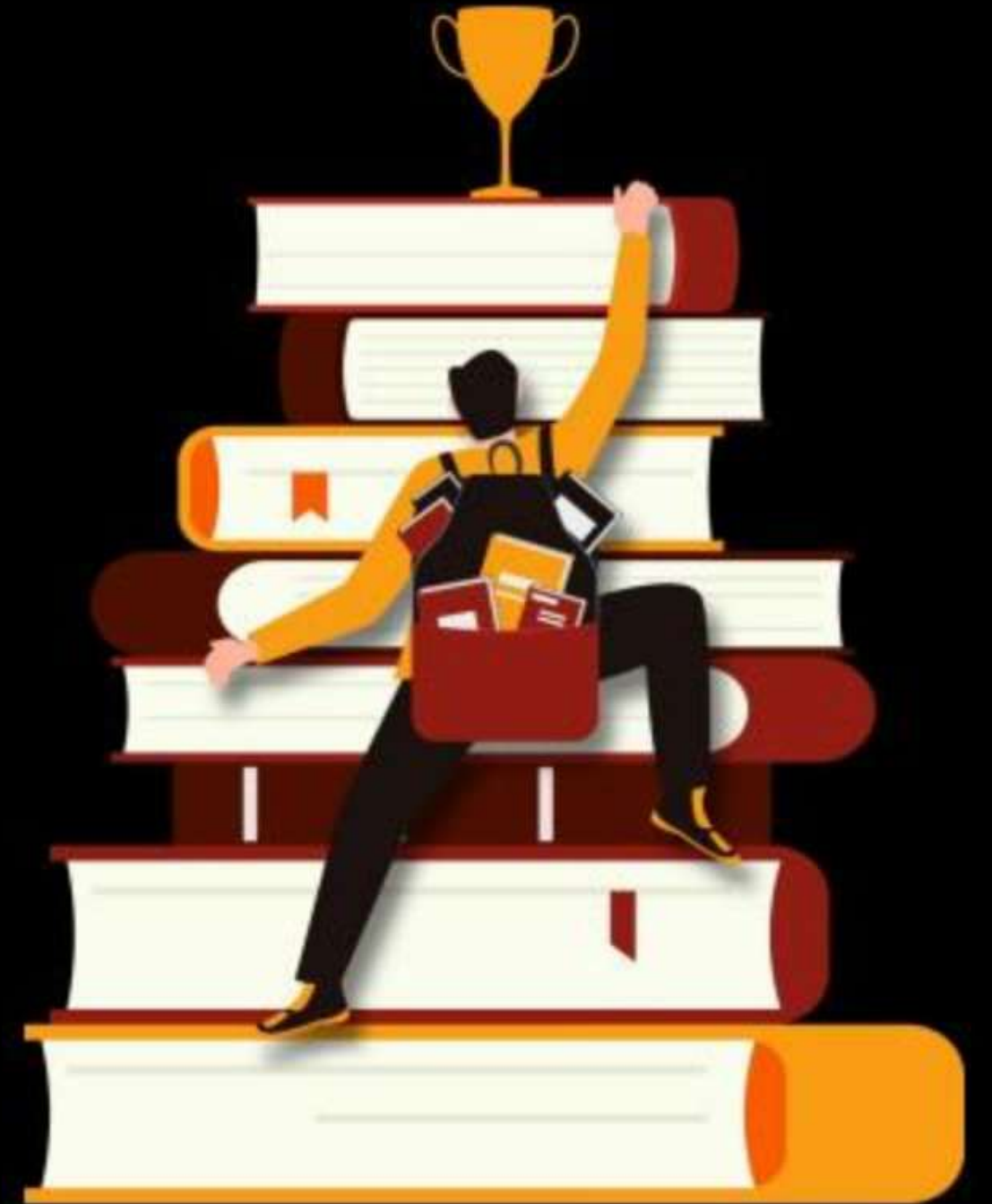
DOUBT SESSION

By – Dr. Puneet Sharma Sir



Topics *to be covered*

DOUBT SESSION



① $y = a + bn + cn^2$ $n = \text{no. of points}$

$$\begin{aligned} \sum y &= na + b\sum n + c\sum n^2 \\ \sum ny &= a\sum n + b\sum n^2 + c\sum n^3 \\ \sum n^2 y &= a\sum n^2 + b\sum n^3 + c\sum n^4 \end{aligned}$$

② $P(4^{\text{th}} H \text{ in } 9^{\text{th}} \text{ toss}) = P(\text{exactly 3H in } 1^{\text{st}} 8 \text{ toss}) + P(H \text{ in } 9^{\text{th}})$

$$= \left(\frac{{}^8C_3}{2^8} \right) \times \frac{1}{2} \times 1$$

③ $\dim(V_1 + V_2) = \dim(V_1) + \dim(V_2) - \dim(V_1 \cap V_2)$

$$\textcircled{4} \quad y = [x] = \begin{cases} -1 & -1 \leq x < 0 \\ 0 & 0 \leq x < 1 \\ 1 & 1 \leq x < 2 \\ 2 & 2 \leq x < 3 \end{cases}$$

$$0 \leq 3+x < 1$$

$$-3 \leq x < -2$$

$$1 \leq 3+x < 2$$

$$-2 \leq x < -1$$

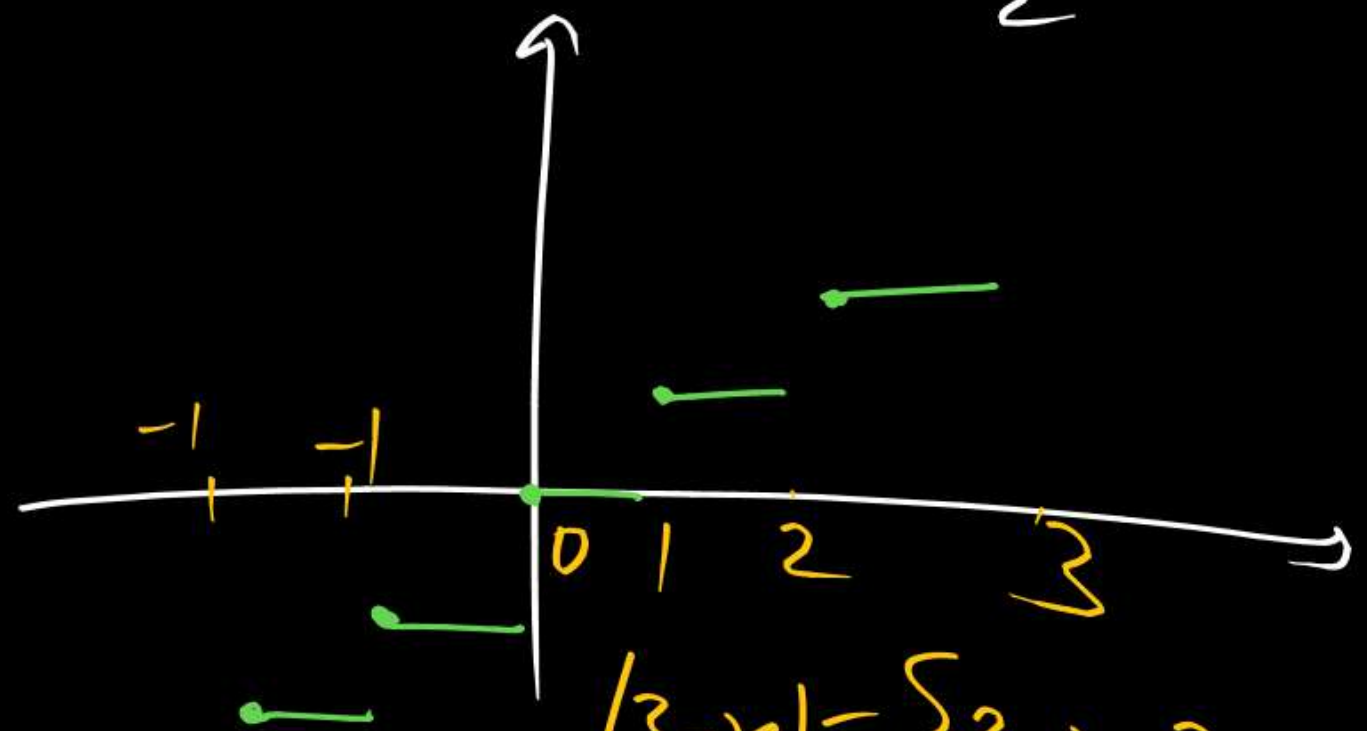
$$2 \leq 3+x < 3$$

$$-1 \leq x < 0$$

$$-1 \leq 3+x < 0$$

$$-4 \leq x < -3$$

$$y = |3-x| + [3+x]$$



$$|3-x| = \begin{cases} 3-x & 3-x \geq 0 \\ -(3-x) & 3-x < 0 \end{cases}$$

$$y = \begin{cases} 3-x, & x \leq 3 \\ x-3, & x > 3 \end{cases}$$

$$\textcircled{x-3} \quad x > 3$$

$$y = \begin{cases} (3-x) + 0, & -3 \leq x < -2 \\ (3-x) + 1, & -2 \leq x < -1 \\ (3-x) + 2, & -1 \leq x < 0 \\ (3-x) + 3, & 0 \leq x < 1 \end{cases}$$

$$-2 \leq x < -1$$

$$-1 \leq x < 0$$

$$0 \leq x < 1$$

Calculus:-

Limit

Cont.

TS/M.S

LMVTH/RTH

Max-min (one Variable)

" " (two Variable)

Partial Diff (Euler Th)

Definite Int. (Property)

D. Int.

CS/IT

DA

✓

?

✓

✓

✓

✓

✓

✓

×

✓

✓

✓

✓

✓

?

✓

?

✓

⑧ E Vectors of AA^T and $A^T A$ are same or different,

let $A_{2 \times 3}$ & $A^T_{3 \times 2}$ $\begin{cases} (AA^T)_{2 \times 2} \\ (A^T A)_{3 \times 3} \end{cases}$

Non Zero E Values are generally same
but E Vectors not necessarily same

P&C and Prob

CS/IT

DA

(Aptitude)

P&C

Ind Events

ME Events

Conditional Prob

Addition Th.

Baye's Th.

fundamental Q

✓

✓

✓

✓

or

✓

✓

✓

✓

✓

✓

✓

✓

✓

✓

| <u>Stats</u> | <u>CS/V</u> | <u>DA (100%)</u> |
|---------------------------|--------------|------------------|
| Prob Dist. (G. & B.) | ✓ | ✓ |
| Binomial or Poisson | ✓ or ✓ | ✓ |
| C.R.V (G. & B.) | ✓ | ✓ |
| U-Dist. | ✓ | ✓ |
| E-Dist. | ? | ? |
| N-Dist. | ✓ | ✓ |
| joint pmf / p.d.f | X | ✓ |

| | CS/IT | DA |
|------------|-------|----|
| Z test | x | ? |
| t-test | x | ✓ |
| Ch-Sq-test | x | ✓✓ |
| C.L-TH | ? | ? |

| <u>L. Algebra</u> | CS/IT | DA |
|-------------------------------|-------|----|
| ① Prop of Det & Inverse | ✓ | ✓ |
| ② Types of Matrices | ✓ | ✓ |
| ③ Rank (Property Based) | ✓ | ✓ |
| ④ Echelon form | ? | ? |
| ⑤ Non Homog System | ? | ? |
| ⑥ Homog System (Nullity) | ✓ | ✓ |
| ⑦ E Values & C.H.T.H | ✓ | ✓ |
| ⑧ E Vectors & Diagonalisation | ? | ? |
| ⑨ L-U Factorisation | ? | ? |

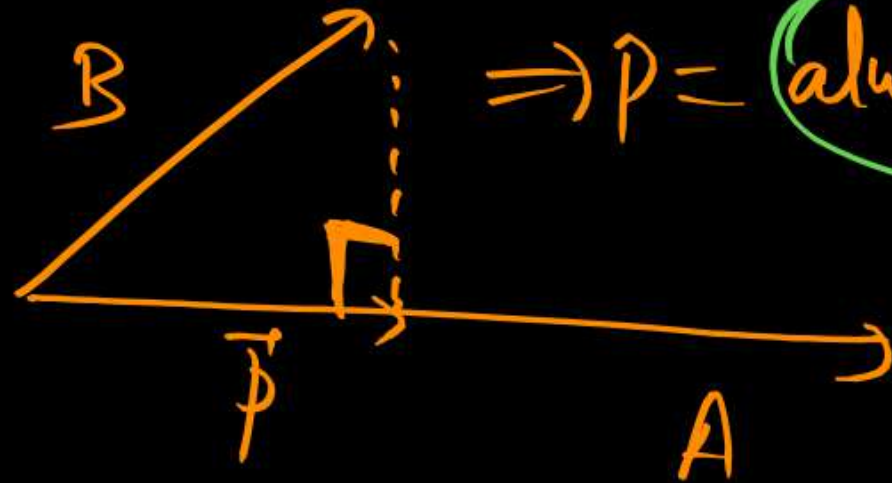
| <u>Linear-2</u> | CS/IT | DA |
|-----------------|-------|-----------------------|
| SUD | X | ? (lengthy question) |
| Q. Form | X | ✓ |
| Progression Mat | X | ✓ |
| Partition Mat | X | ? |
| V. Space | ? | ✓ (Not sure to solve) |

Let P be a projection matrix. Which of the following properties does not necessarily hold?

- (a) P is idempotent. (T)
- (b) The eigen values of P are either 0 or 1. (T)
- (c) P is always diagonalizable. (T)
- (d) P is always symmetric.

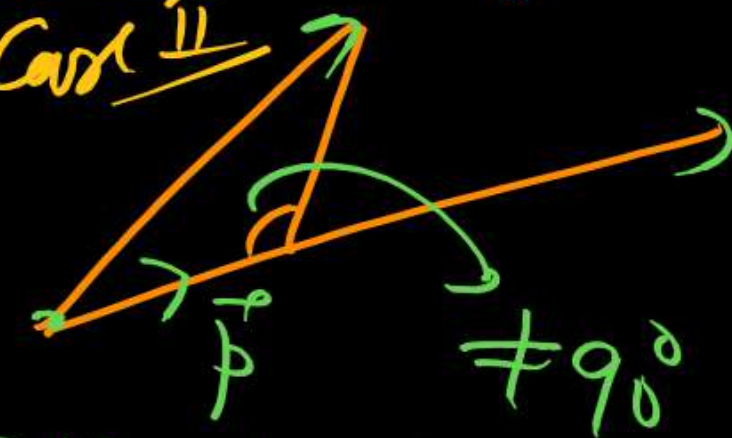
Projection Mat will be Symm only for orthogonal projections.

Case I



$\Rightarrow P = \text{always Symm.}$

Case II



It is not orthogonal projection
 $P = \text{Not Necessarily Symm.}$

Telegram



@DRPUNEETSIRPW



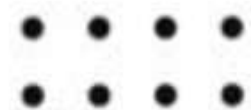
Summary



Doubt Session

The word 'Thank' is written in a large, bold, yellow script font. A yellow arrow starts from the top of the 'T', extends horizontally to the right, and then curves downwards to point at the end of the word 'Thank'.

Thank
THANK



Keep Hustling!