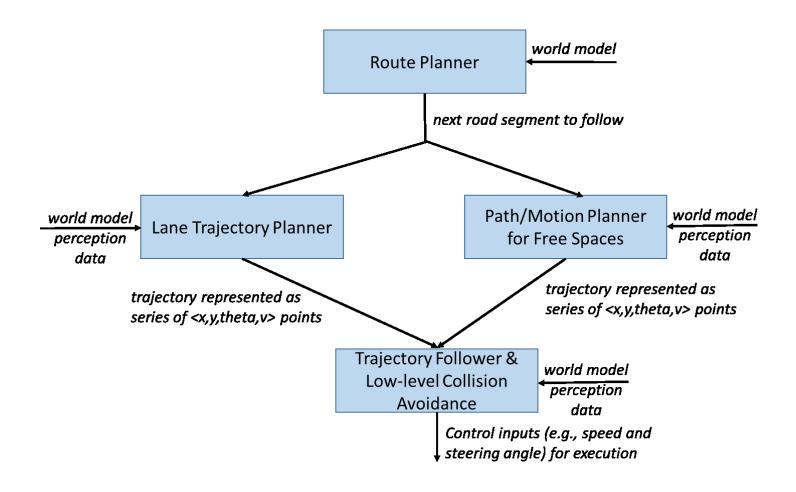
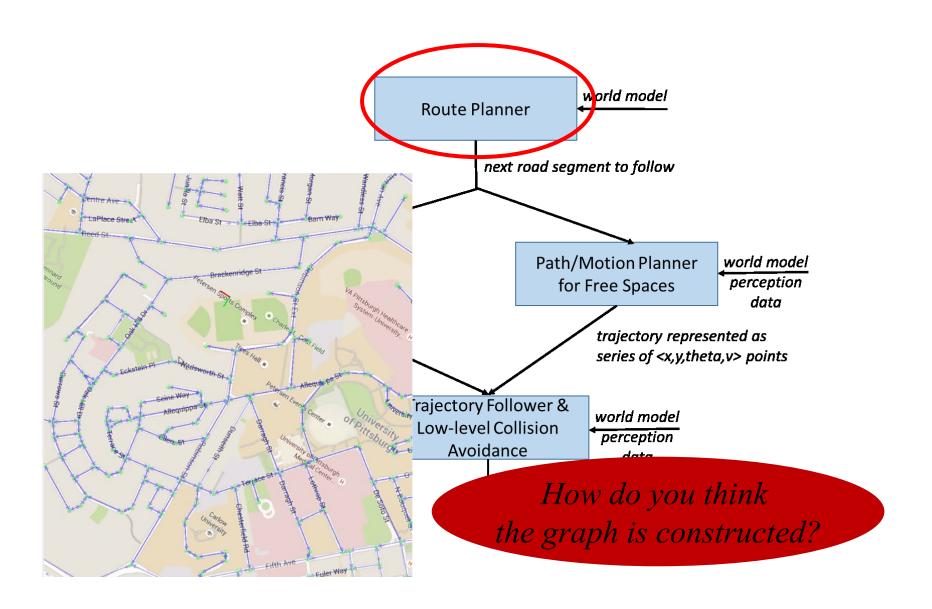
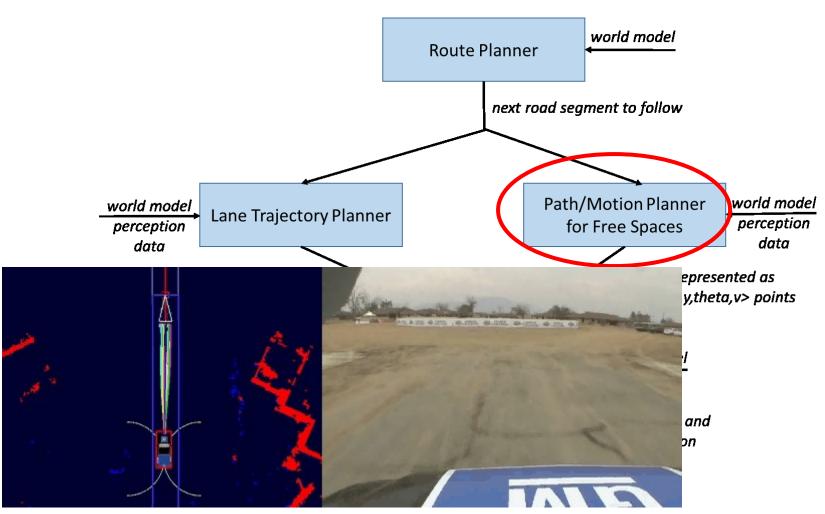
16-782 Planning & Decision-making in Robotics

Case Study: Planning for Autonomous Driving

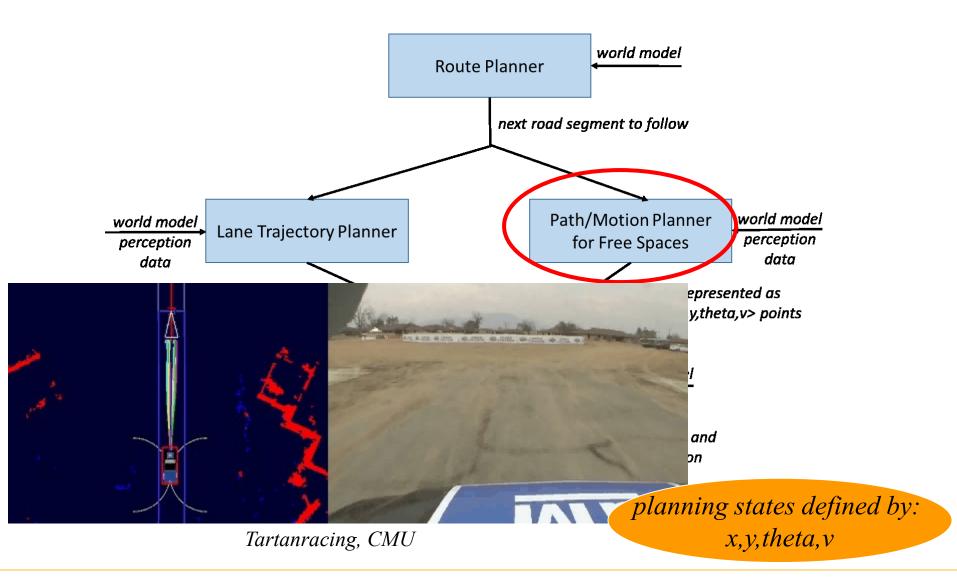
Maxim Likhachev
Robotics Institute
Carnegie Mellon University





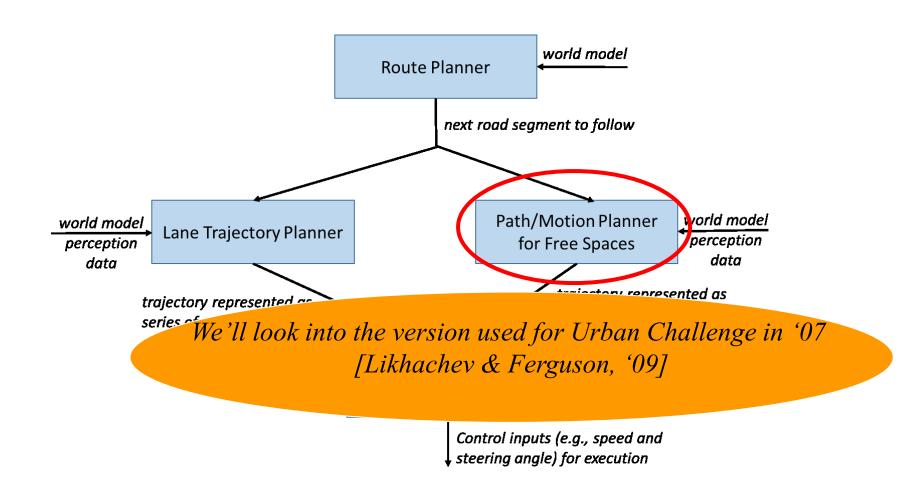


Tartanracing, CMU



Typical Planning Architecture for Autonomous Vehicle н н world mode Lane Trajectory Planner perception for Free Spaces perception data data trajectory represented as trajectory represented as series of <x,y,theta,v> points series of <x,y,theta,v> points Trajectory Follower & world model Low-level Collision perception **Avoidance** data Control inputs (e.g., speed and steering angle) for execution

Typical Planning Architecture for Autonomous Vehicle н world mode Lane Trajectory Planner perception perception planning states defined by: data discretization along a lane (=x) and perpendicular to it (=y), lane ID, v, time perception **Avoidance** data Control inputs (e.g., speed and steering angle) for execution



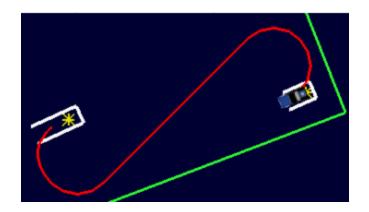
Motivation

• Planning long complex maneuvers for the Urban Challenge vehicle from CMU (Tartanracing team)



- Planner suitable for
 - autonomous parking in very large (200m by 200m) cluttered parking lots
 - navigating in off-road conditions
 - navigating cluttered intersections/driveways

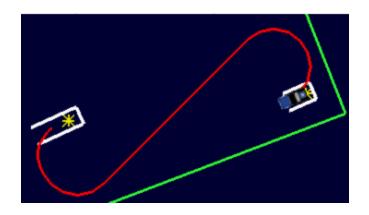
• Generate a path that can be tracked well (at up to 5m/sec):



– path is a 4-dimensional trajectory:

$$(x, y, \theta, v)$$
orientation speed

• Generate a path that can be tracked well (at up to 5m/sec):



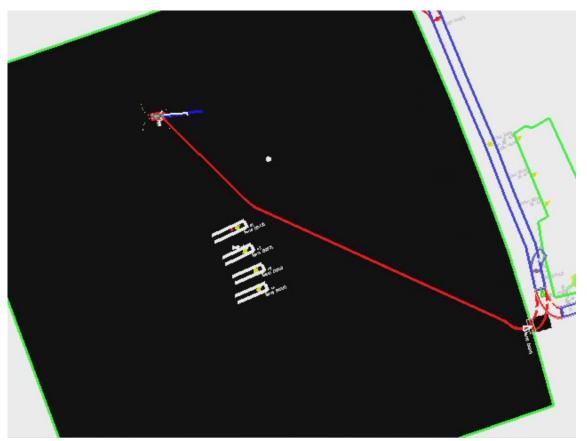
– path is a 4-dimensional trajectory:

$$(x, y, \theta, v)$$
orientation speed

Orientation of the wheels is not included.

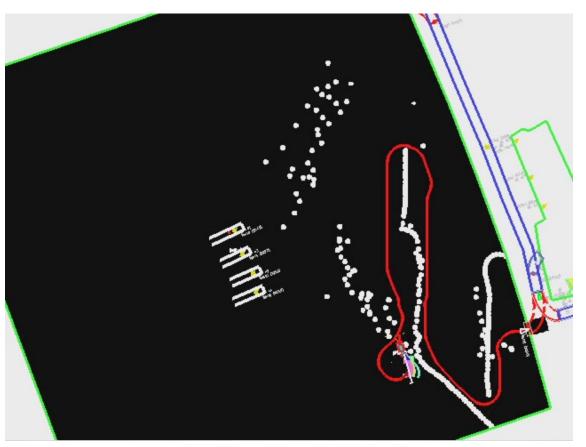
When will that be a problem?

• Fast (2D-like) planning in trivial environments:



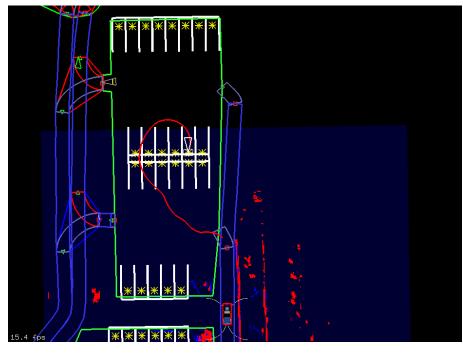
200 by 200m parking lot

• But can also handle large non-trivial environments:

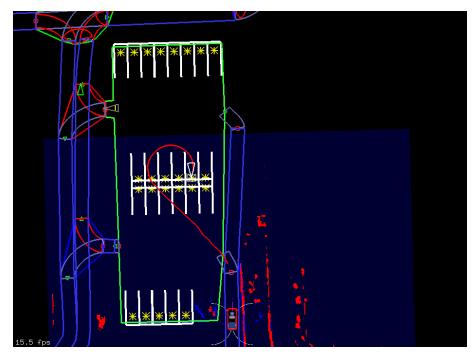


200 by 200m parking lot

• Anytime property: finds the best path it can within X secs and then improves the path while following it



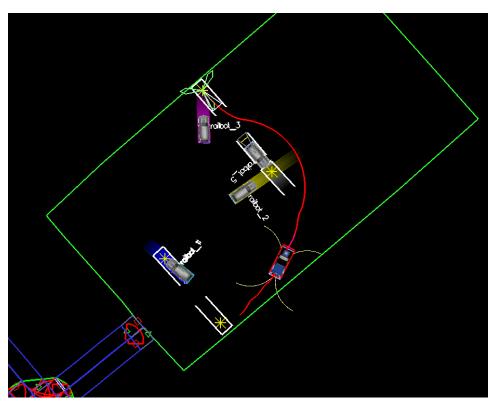
initial path



converged (to optimal) path

Fast replanning, especially since we need to avoid other

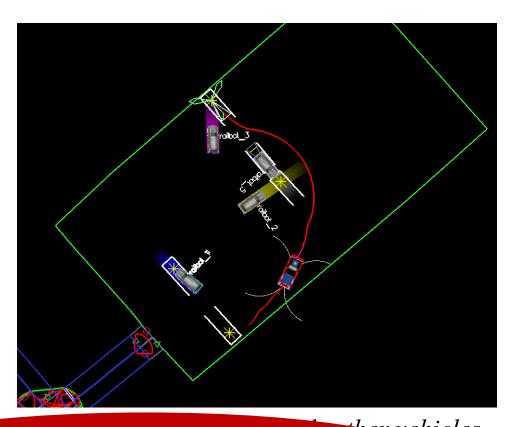
vehicles



planning a path that avoids other vehicles

Fast replanning, especially since we need to avoid other

vehicles



Time is not part of the state-space.

When will that be a problem?

Our Approach

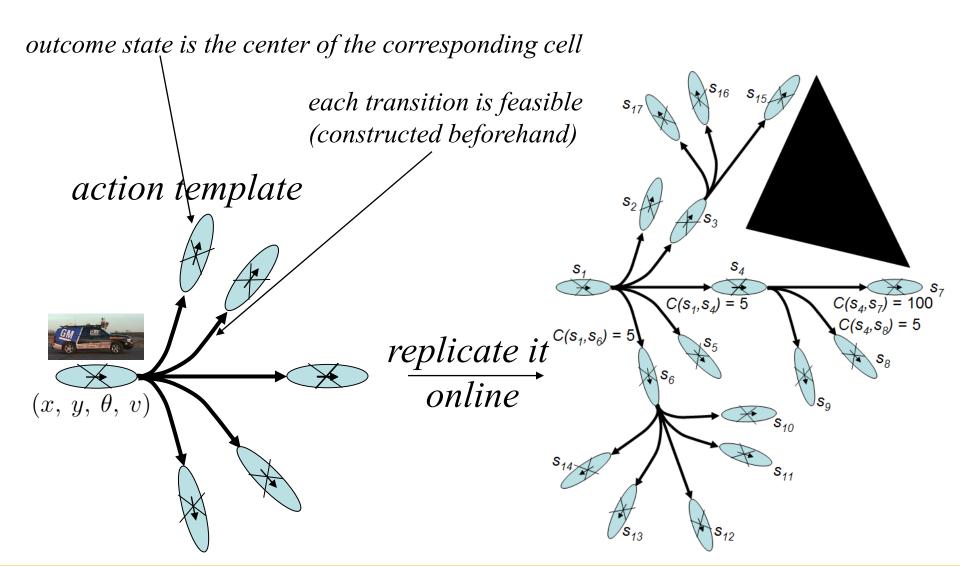
- Build a graph
 - multi-resolution version of a lattice graph

- Search the graph for a least-cost path
 - Anytime D* [Likhachev et al. '05]

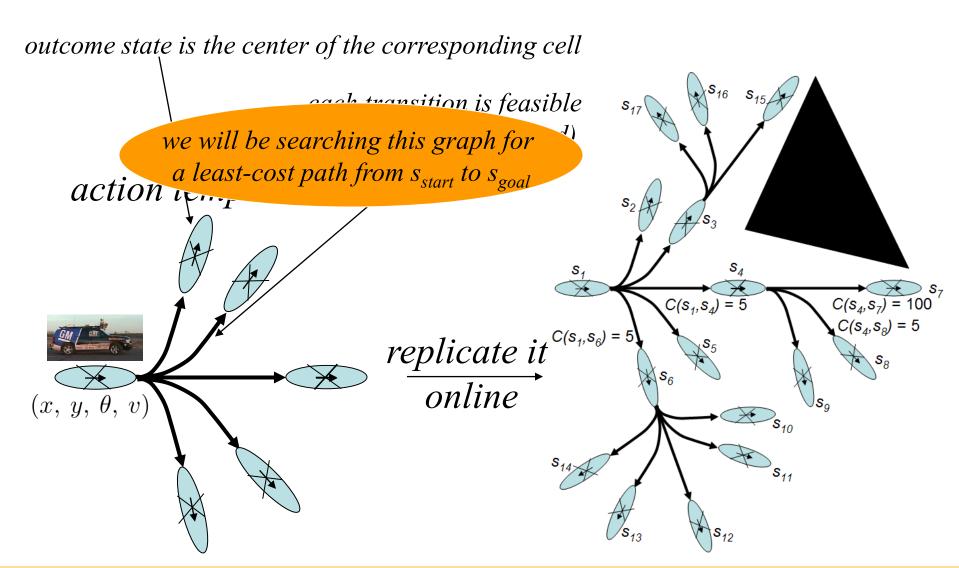
• Lattice-based graph [Pivtoraiko & Kelly, '05]:

outcome state is the center of the corresponding cell each transition is feasible (constructed beforehand) action template

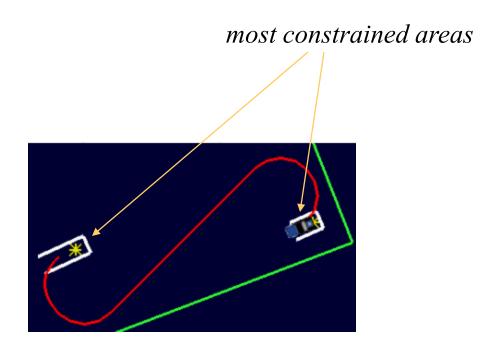
• Lattice-based graph [Pivtoraiko & Kelly, '05]:



• Lattice-based graph [Pivtoraiko & Kelly, '05]:



- Multi-resolution lattice:
 - high density in the most constrained areas (e.g., around start/goal)
 - low density in areas with higher freedom for motions



- The construction of multi-resolution lattice:
 - the action space of a low-resolution lattice is a strict subset of the action space of the high-resolution lattice

reduces the branching factor for the low-res. lattice

- The construction of multi-resolution lattice:
 - the action space of a low-resolution lattice is a strict subset of the action space of the high-resolution lattice

reduces the branching factor for the low-res. lattice

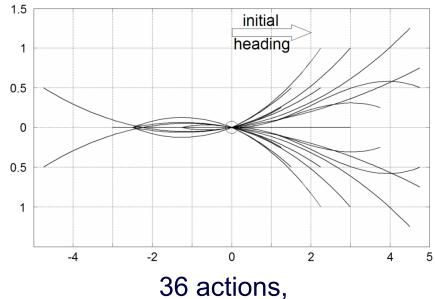
 the state-space of a low-resolution lattice is discretized to be a subset of the possible discretized values of the state variables in the high-resolution lattice

reduces the size of the state-space for the low-res. lattice

both allow for seamless transitions

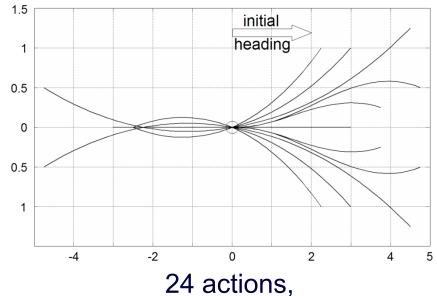
• Multi-resolution lattice used for Urban Challenge:





32 discrete values of heading 0.25m discretization for x,y

low-resolution lattice



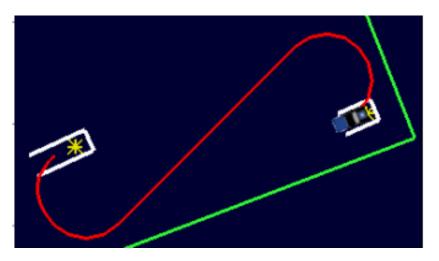
16 discrete values of heading 0.25m discretization for x,y

can be multiple levels

can also be non-uniform in x,y & v

- Properties of multi-resolution lattice:
 - utilization of low-resolution lattice: every path that uses only the action space of the low-resolution lattice is guaranteed to be a valid path in the multi-resolution lattice
 - validity of paths: every path in the multi-resolution lattice is guaranteed to be a valid path in a lattice that uses only the action space of the high-resolution lattice

• Benefit of the multi-resolution lattice:

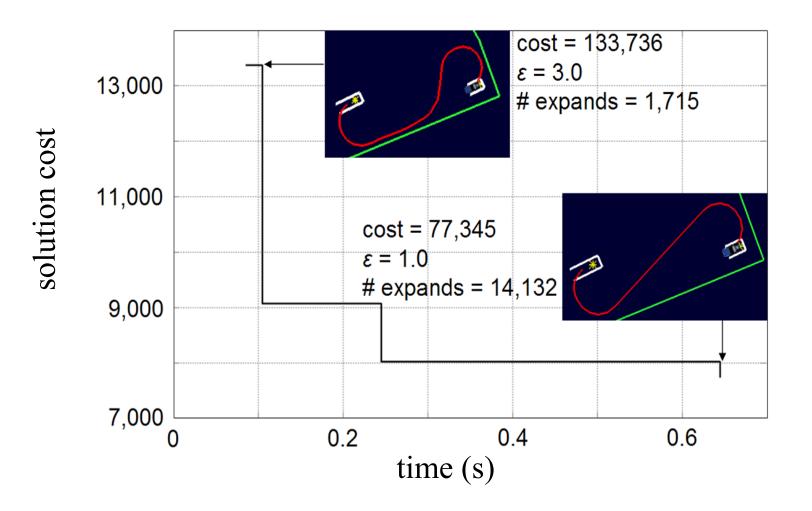


Lattice	States Expanded	Planning Time (s)
High-resolution	2,933	0.19
Multi-resolution	1,228	0.06

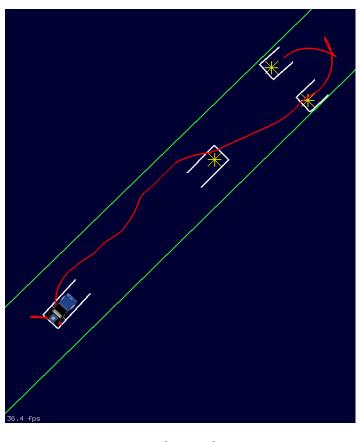
- Anytime D* [Likhachev et al. '05]:
 - anytime incremental version of A*
 - anytime: computes the best path it can within provided time and improves it while the robot starts execution.
 - incremental: it reuses its previous planning efforts and as a result, re-computes a solution much faster

Anytime D* [Likhachev et a computes a path reusing all of the previous search efforts desired bound on was set ε to large value; guarantees that until goal is reached $cost(path) \le \varepsilon cost(optimal\ path)$ ComputePathwithReuse(); publish ε -suboptimal path for execution; update the map based on new sensory information; update current state of the agent; if significant changes were observed increase ε or replan from scratch; else decrease ε : makes it improve the solution

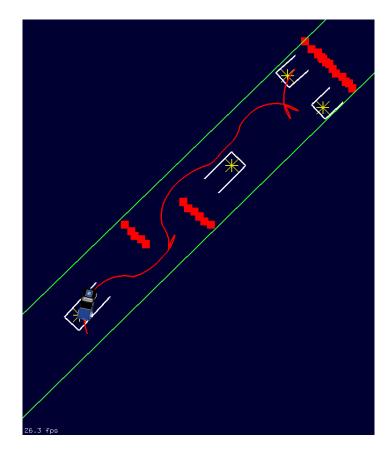
• Anytime behavior of Anytime D*:



• Incremental behavior of Anytime D*:



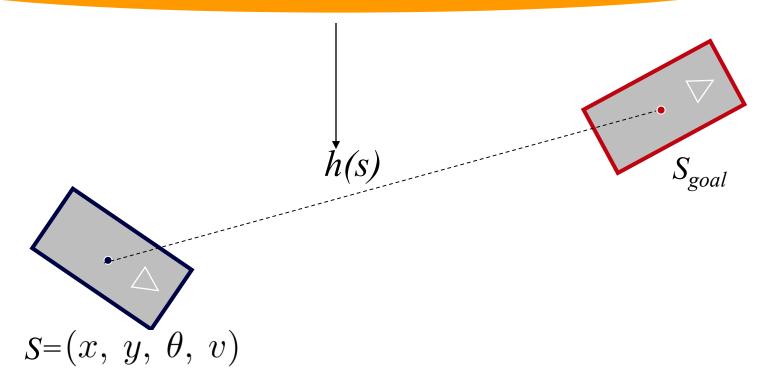
initial path



a path after re-planning

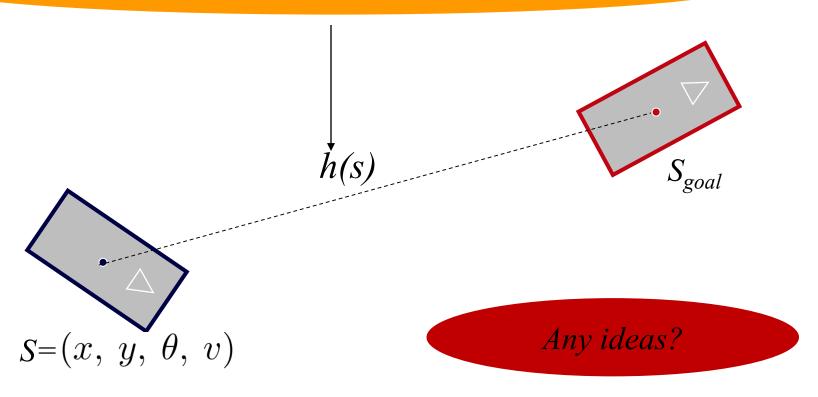
• Performance of Anytime D* depends strongly on heuristics h(s): estimates of cost-to-goal

should be consistent and admissible (never overestimate cost-to-goal)



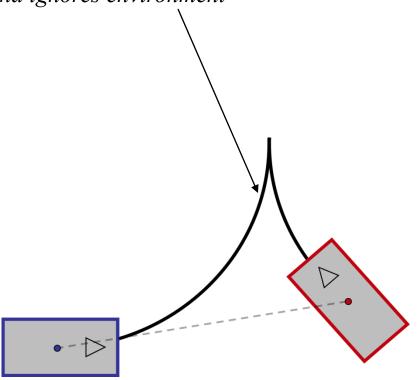
• Performance of Anytime D* depends strongly on heuristics h(s): estimates of cost-to-goal

should be consistent and admissible (never overestimate cost-to-goal)

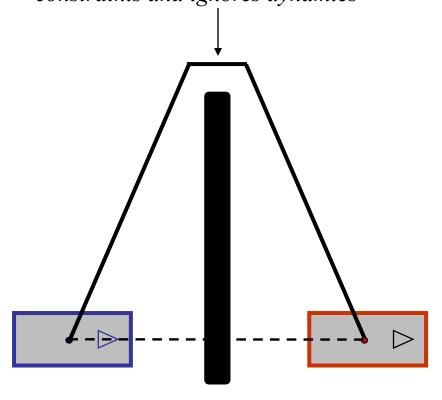


- In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$, where
 - $-h_{mech}(s)$ mechanism-constrained heuristic
 - $-h_{env}(s)$ environment-constrained heuristic

 $h_{mech}(s)$ – considers only dynamics constraints and ignores environment



 $h_{env}(s)$ – considers only environment constraints and ignores dynamics



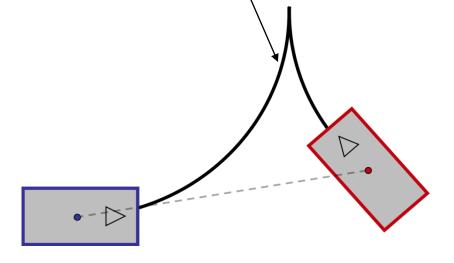
- In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$, where
 - $-h_{mech}(s)$ mechanism-constrained heuristic
 - $-h_{env}(s)$ environment-constrained heuristic

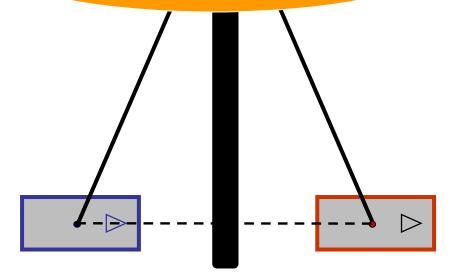
 $h_{mech}(s)$ – considers only dynamics constraints and ignores environment

 $h_{env}(s)$ – considers only environment constraints and ignores dynamics

pre-computed as a table lookup for high-res. lattice

computed online by running a 2D A* with late termination





- In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$, where
 - $-h_{mech}(s)$ mechanism-constrained heuristic
 - $-h_{env}(s)$ environment-constrained heuristic

 $h_{mech}(s)$ – considers only dynamics constraints and ignores environment

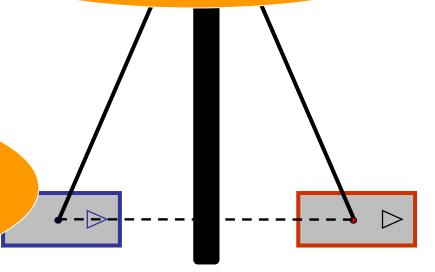
 $h_{env}(s)$ – considers only environment constraints and ignores dynamics

pre-computed as a table lookup for high-res. lattice

computed online by running a 2D A* with late termination

Any other options?

Closed-form analytical solutions (Dubins paths [Dubins, '57], Reeds-Shepp paths [Reeds & Shepp, '90])



Any challenges using it?

• In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$

• h(s) needs to be admissible and consistent

for efficiency, valid paths, suboptimality bounds, optimality in the limit

- In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$
- h(s) needs to be admissible and consistent
- if $h_{mech}(s)$ and $h_{env}(s)$ are admissible and consistent, then h(s) is admissible and consistent [Pearl, 84]

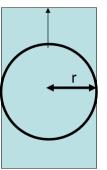
• $h_{mech}(s)$ – cost of a path in high-res. lattice with no obstacles and no boundaries

 $h_{mech}(s)$ – admissible and consistent

• In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$

- h(s) needs to be admissible and consistent
- if $h_{mech}(s)$ and $h_{env}(s)$ are admissible and consistent, then h(s) is admissible and consistent [Pearl, 84]

• $h_{env}(s)$ – cost of a 2D path of the inner circle of the vehicle into the center of the goal location

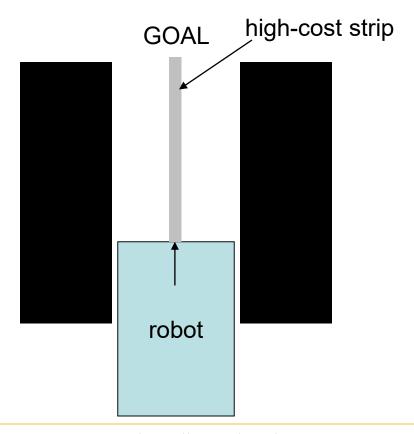


 $h_{env}(s) - NOT$ admissible

• In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$

$$h_{env}(s) - NOT$$
 admissible

• $h_{env}(s)$ – cost of a 2D path of the inner circle of the vehicle into the center of the goal location

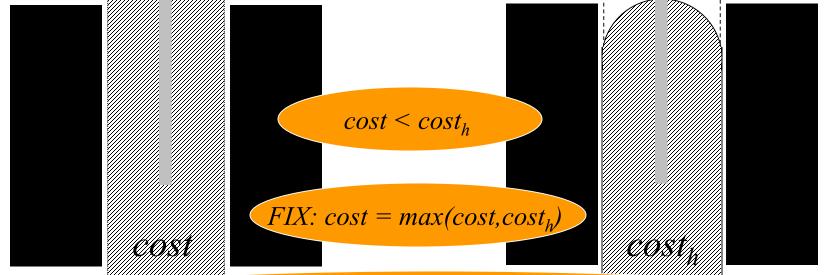


• In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$

$$h_{env}(s) - NOT admissible$$

• $h_{env}(s)$ – cost of a 2D path of the inner circle of the vehicle into the center of the goal location

 $according to h_{env}(s)$: cost = average over this box (convolution) cost = average over the trace of inner circle



equivalent to slightly higher cost for obstacles close to the middle of the vehicle

• In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$

- $h_{mech}(s)$ admissible and consistent
- $h_{env}(s)$ admissible and consistent
- h(s) admissible and consistent

• In our planner: $h(s) = max(h_{mech}(s), h_{env}(s))$

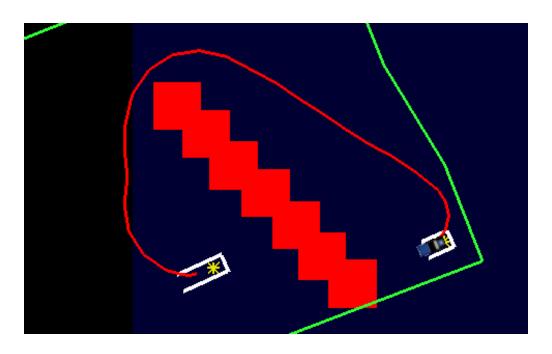
• $h_{mech}(s)$ – admissible and consistent

• $h_{env}(s)$ – admissible and consistent

• h(s) – admissible and consistent

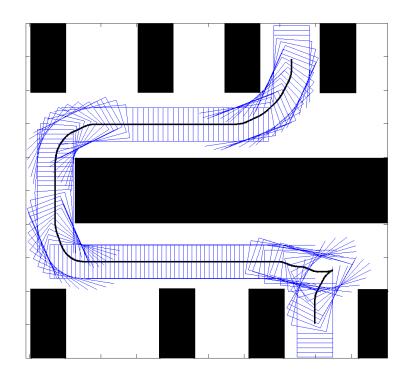
Theorem. The cost of a path returned by Anytime D^* is no more than ε times the cost of a least-cost path from the vehicle configuration to the goal configuration using actions in the multi-resolution lattice, where ε is the current value by which Anytime D^* inflates heuristics.

• Benefit of the combined heuristics:

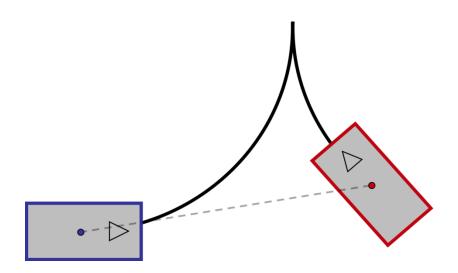


Heuristic	States Expanded	Planning Time (s)
Environment-constrained only	26,108	1.30
Mechanism-constrained only	124,794	3.49
Combined	2,019	0.06

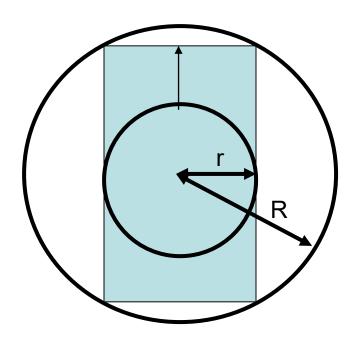
- Pre-compute as much as possible
 - convolution cells for each action for each initial heading



- Pre-compute as much as possible
 - mechanish-constrained heuristics



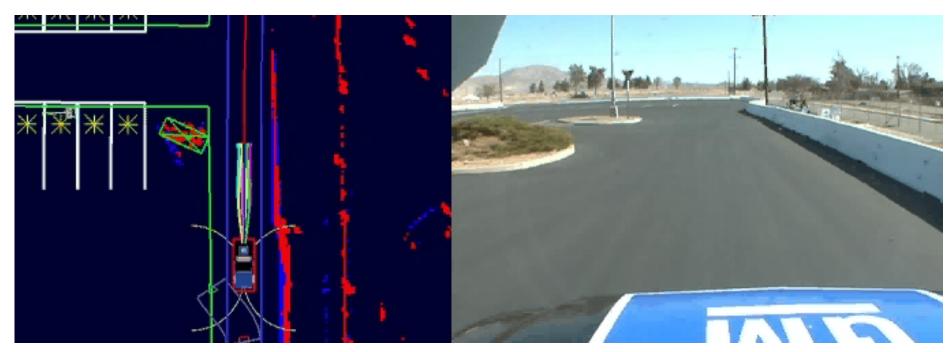
 avoid convolutions based on collision checking with inner and outer circles



- Efficient re-planning by maintaining low-resolution boolean map of states expanded
 - each map update may affect thousands of states
 - need to iterate over those states to see if they are effected
 - optimization: iterate and update edge costs only when map update is in the area that have states expanded

Results

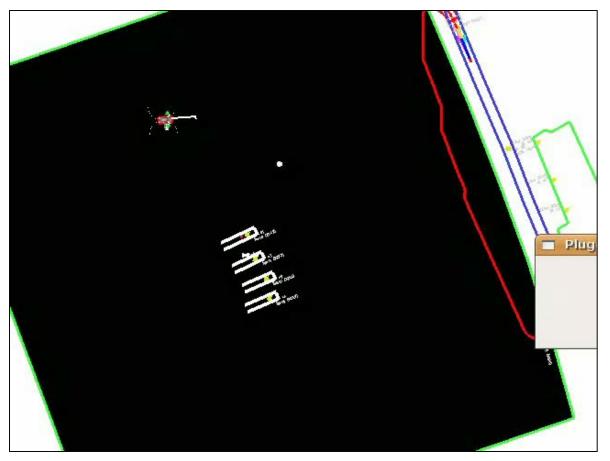
• Plan improvement



Tartanracing, CMU

Results

• Replanning in a large parking lot (200 by 200m)



Tartanracing, CMU

What You Should Know...

• Different types of planning for autonomous driving and how they interact

• What is multi-resolution lattice

• Different heuristic functions used in Motion Planning