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AIML (Birla Institute of Technology and Science, Pilani)



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Question 1

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You can write your answers in the provided space or write your answer on a piece of paper and scan and upload the handwritten answers using the QR Code available in the Scan and Upload Section of this exam.

Kindly ensure all answer sheets to be uploaded against the corresponding questions only. All sheets should not be uploaded against one question

(A) Consider a point in 2D space $\mathcal{P}=(4,2)$ abd a line represented by the equation f(x,y)=0. Using the method of Lagrange multipliers, derive the closest point on this line to the given point \mathcal{P} . You can assume that the closeness between two points is measured by square of euclidean distance. Derive the closest point to \mathcal{P} when

i)
$$f(x, y) = x - 2y + 3$$

ii)
$$f(x, y) = x + 2y + 5$$

Also derive the distance to ${\cal P}$ in both cases. (4 marks)

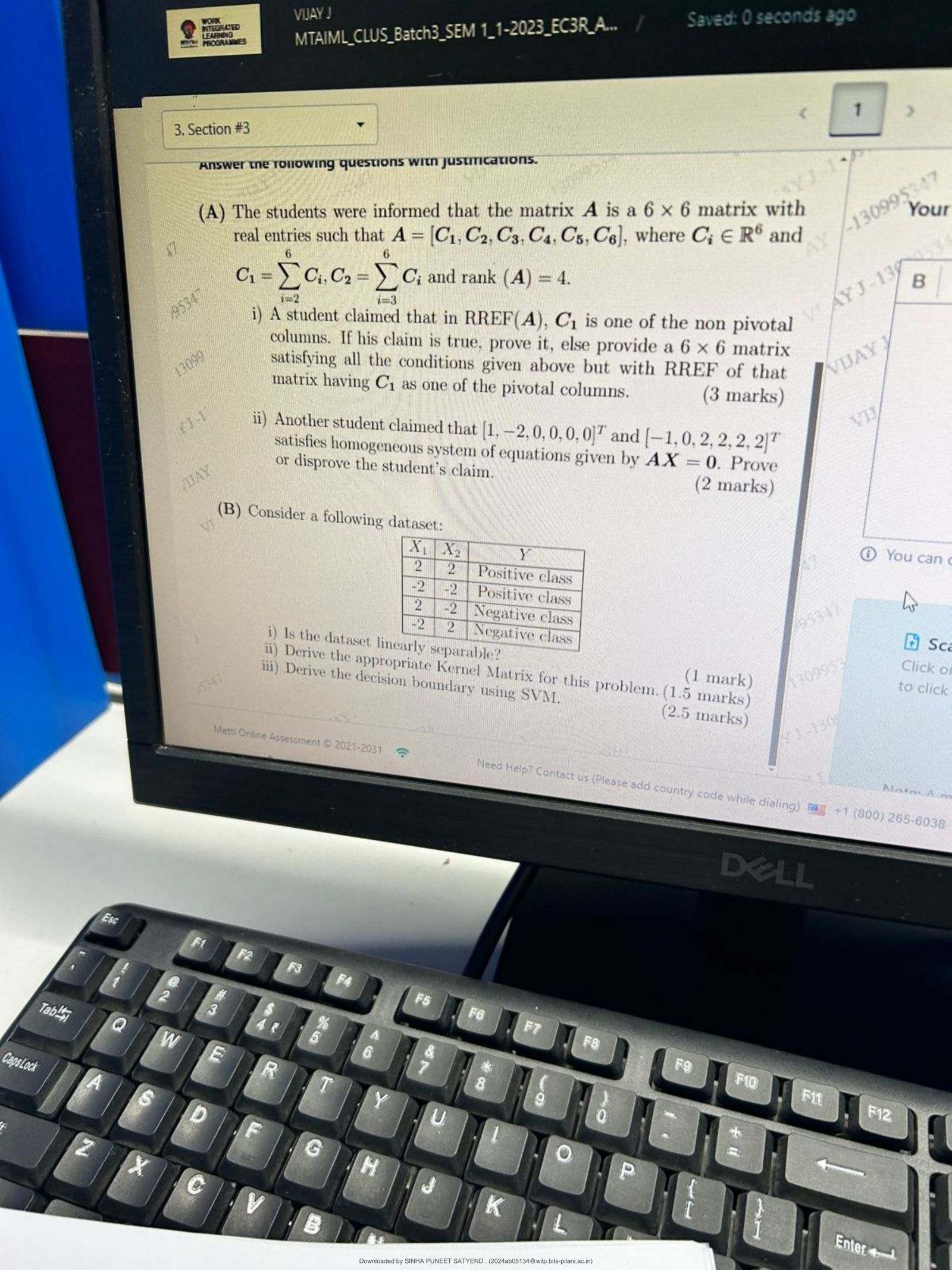
(B) Consider the following matrix C

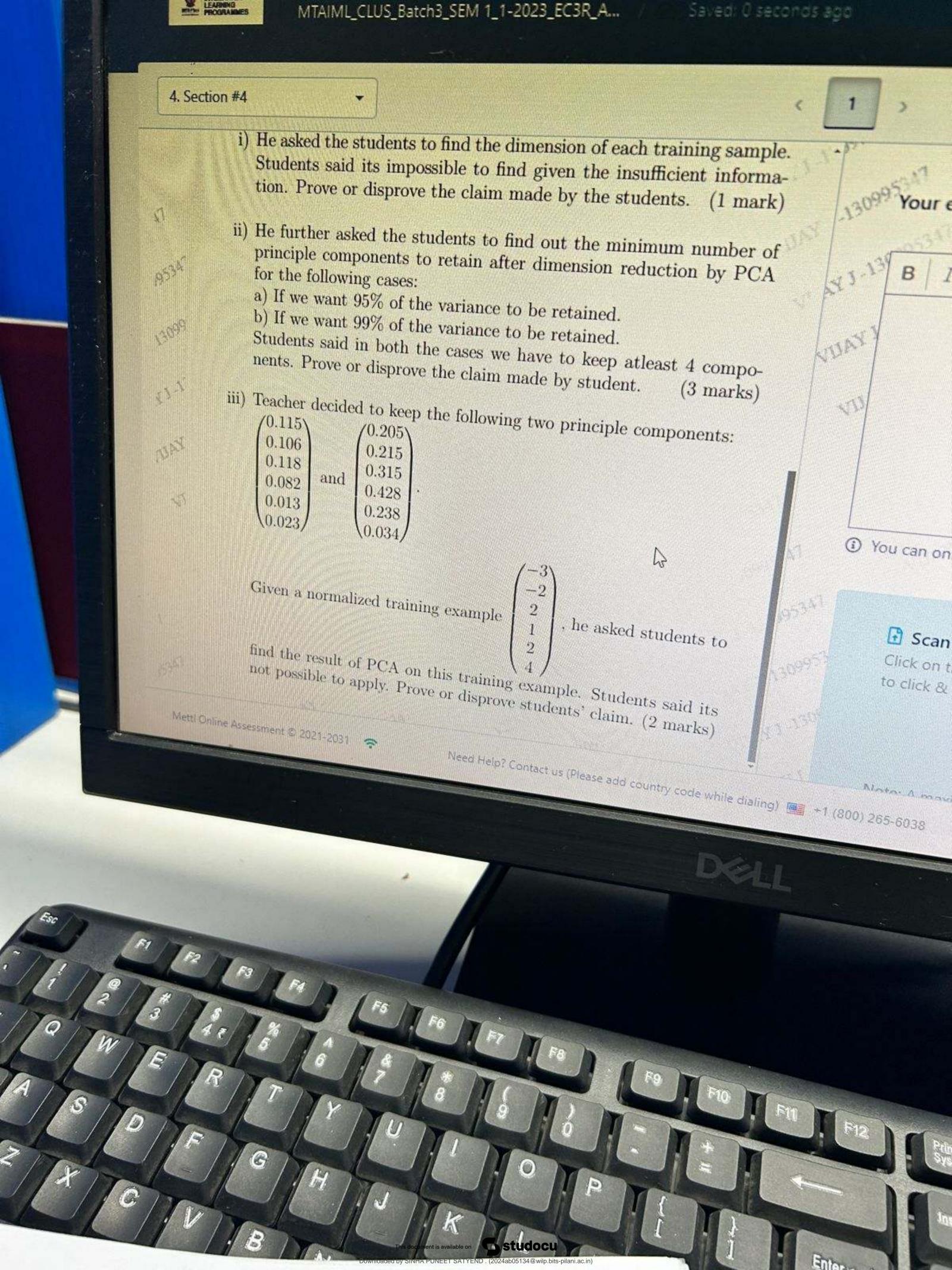
$$\mathbf{C} = \begin{bmatrix} 6 & -33 & 19 \\ 6 & -8 & \frac{4}{3} \\ 9 & -33 & 16 \end{bmatrix}$$

- i) Calculate the Trace of the matrix C_1 where $C_1 = C^6$
- ii) Calculate the determinant of the matrix C_2 where $C_2 = C^7$

(3 marks)

(C) A professor gave his students three linearly independent vectors in R n named \mathbf{a} , \mathbf{b} and \mathbf{c} . He asked the students to construct three vectors \mathbf{x} , \mathbf{y} and \mathbf{z} defined as $\mathbf{x} = \mathbf{b} - \mathbf{c}$, $\mathbf{y} = \mathbf{a} + \mathbf{c}$ and $\mathbf{z} = \mathbf{a} - \mathbf{b}$. He asked students to consider a set of vectors named $\mathcal{H} = \{\mathbf{x}, \mathbf{y}, \mathbf{z}\}$. Prove or disprove that the set \mathcal{H} is linearly independent. (3 marks)





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(A) Consider a point in 2D space \mathcal{P} = (4, 2) abd a line represented by the equation f(x, y) = 0. Using the method of Lagrange multipliers, derive the closest point on this line to the given point ${\mathcal P}$. You can assume that the closeness between two points is measured by square of euclidean distance. Derive the closest point to ${\mathcal P}$ when

i)
$$f(x, y) = x - 2y + 3$$

ii)
$$f(x, y) = x + 2y + 5$$

Also derive the distance to ${\cal P}$ in both cases. (4 marks)

(B) Consider the following matrix C

$$\mathbf{C} = \begin{bmatrix} 6 & -33 & 19 \\ 6 & -8 & \frac{4}{3} \\ 9 & -33 & 16 \end{bmatrix}$$

i) Calculate the Trace of the matrix C_1 where $C_1 = C^6$

ii) Calculate the determinant of the matrix C_2 where $C_2 = C^7$

(C) A professor gave his students three linearly independent vectors in R n named **a**, **b** and **c**. He asked the students to construct three vectors **x**, **y** and z defined as x = b - c, y = a + c and z = a - b. He asked students to consider a set of vectors named $\mathcal{H} = \{x,y,z\}$. Prove or disprove that

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