Quantinuum, Terrington House, 13-15 Hills Rd, Cambridge, CB2 1NL, UK

September 30, 2024

Quantinuum, 303 South Technology Ct., Broomfield, CO 80021, USA

To whom it may concern,

Please find attached a resume for the mathematician *James Dolan*, as well as two letters of recommendation written by John Baez and Todd Trimble.

I have been working/learning/collaborating with James since 2017. He is a big source of inspiration and ideas for the work I do at Quantinuum and it only seems reasonable that he is actually employed as a consultant or otherwise by Quantinuum. I'm sure others will also benefit from interacting with James, and that his experience in number theory, representation theory and algebraic geometry will play a role in the design of our quantum computers.

Simon Burton

# James Dolan

### Resume

Hauppauge, New York— james.dolan<br/>1@students.mq.edu.au — (631) 724-2127 — ncatlab.org/nlab/show/James+Dolan —

# **POSITIONS**

1982-1986 SUNY Buffalo mathematics PhD student / teaching assistant (studying under William Lawvere and Stephen Schanuel).

1993-1996 UC Riverside mathematics PhD student / teaching assistant (studying under John Baez).

1997 Video co/dec programmer for a startup in Riverside, California.

1998 Software engineer for Sanga inc. in Montreal.

2001 Macquarie University mathematics research associate (working with Ross Street).

1993-2010 Research collaboration with John Baez at UC Riverside.

2015-2017 Macquarie University mathematics PhD student (studying under Ross Street).

2018 Consultant on patents for data-encryption and user-authentication.

# SELECTED PUBLICATIONS

Baez, John C., and James Dolan. "Higher-dimensional Algebra and Topological Quantum Field Theory." Journal of Mathematical Physics 36.11 (1995): 6073-6105.

Baez, John C., and James Dolan. "Higher-Dimensional Algebra III. n-Categories and the Algebra of Opetopes." Advances in Mathematics 135.2 (1998): 145-206.

Baez, John C., and James Dolan. "Categorification." Higher Category Theory, eds. Ezra Getzler and Mikhail Kapranov, Contemp. Math. 230, American Mathematical Society, Providence, Rhode Island, (1998): 1-36.

Baez, John C., and James Dolan. "From Finite Sets to Feynman Diagrams" Mathematics Unlimited - 2001 and Beyond, vol. 1, eds. Björn Engquist and Wilfried Schmid, Springer, Berlin, (2001): 29-50.

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June 15, 2024

### To Whom It May Concern:

This is a letter of recommendation for James Dolan, who is applying for a job at Quantinuum. Some of my very best work was done with Dolan, and he's the only person I've worked with who I'd call a "genius", able to routinely come up with ideas that completely take me by surprise. He is nonconformist to a degree that drives me crazy, yet nobody else tells me as many exciting new things. Working with him often consists of explaining problems and ideas, waiting, seeing what he comes up with, getting him to explain it, repeatedly pressing him on points that he hasn't fully worked out, and finally wrestling it down into a clear presentation.

The best example is our 1995 paper "Higher-dimensional algebra and topological quantum field theory", where we stated the Tangle Hypothesis, which is a general description of higher-dimensional string diagrams in terms of n-categories, and the TQFT Hypothesis, a conjectured classification of n-dimensional extended topological quantum field theories. The latter was later modified and rebranded as the Cobordism Hypothesis by Jacob Lurie, who in 2009 gave a 111-page proof sketch in his paper "On the classification of topological quantum field theories". Much work has been done on this topic since then, and the ideas continue to inspire plenty of new research on topological quantum field theory. Various generalizations have become important in topological quantum computing and condensed matter physics.

James Dolan has also done pioneering work on *n*-categories, homotopy theory, the mathematical foundations of Feynman diagrams, and other topics. His work on algebraic geometry is still unpublished, and to get some of it out into the world, I've been putting videos of a series of conversations on my YouTube channel.

James has also begun talking with Simon Burton about Simon's work on quantum computing. This could lead to some revolutionary developments if adequately supported:. I believe Simon just needs to focus Dolan's attention on some good problems, and novel ideas will emerge. They have a good relationship, so this can be done, but a financial inducement would help.

Sincerely.

John Baez

This is a letter of recommendation for James ("Jim") Dolan for a possible position at Quantinuum, as proposed by Simon Burton.

I state without exaggeration that Jim has for decades been a legendary influence in the area of category theory, inspiring several generations of category theorists. I first learned of him in 1995, through an open letter he and John Baez sent on their groundbreaking approach to "weak n-categories", a notoriously tricky concept I was also working on at the time, via opetopic sets and conditions of horn filler type. These ideas, published by Baez and Dolan in Higher-Dimensional Algebra III, continue to be studied intensively. Later I met Baez and Dolan in 1997 at a workshop on higher-dimensional categories (published as number 230 in the AMS Contemporary Mathematics series; see their paper Categorification). I immediately became friendly with both, and Jim particularly. I quickly got the sense that although John was officially Jim's PhD advisor, in fact it was Jim who was John's true teacher in category theory, and that Jim was almost certainly the idea engine throughout their long collaboration, at least with regard to the category-theoretic input.

As samples of this historic collaboration, there is firstly Higher-dimensional algebra and topological quantum field theory (later referred to as "HDA I", the first of the HDA series), also groundbreaking in its programmatic sweep; for example this is where the "cobordism hypothesis" and also the "periodic table" of higher-dimensional categorical structures first appeared. Secondly I'll mention From finite sets to Feynman diagrams, a short but beautiful paper in which the basic combinatorics of quantum field theory is set out in terms of "stuff, structure, properties", a triad of concepts also due primarily to Dolan (which first appeared in the early 1990's on the old Usenet). Today these concepts are fundamental for working category theorists. Thirdly, two lesser known but very attractive articles, Dirichlet series and the Hasse-Weil zeta function and Zeta functions of Z-sets, which set forth with startling simplicity and clarity the combinatorial underpinnings of zeta functions generally, along lines similar to Joyal species and the "Montreal school" of combinatorics (as represented by Bergeron, Labelle, Leroux, et al.).

Many of Jim's ideas have been propagated not by him but by other mathematicians who fall into conversation with him and thereby fall under their spell. For example, Martin Brandenburg's thesis owes a large debt to Jim's 2-categorical "doctrinal" approach to algebraic geometry (an ongoing project which may be seen someday as Dolan's magnum opus). Another case is the Macquarie thesis of Daniel Steffen, interpreting free cartesian closed categories in terms of games with take-back strategies, directly tracing to conversations they had while Jim was briefly there in the early 2000's, and which was again described some years later at the n-Category Cafe (blog article dated October 20, 2006, describing Jim's guest lecture Holodeck strategies and the lambda-calculus). Finally, I'll mention the case of Dolan's response to Street's conjectural notion of "file" as an approach to semi-strictification of weak n-categories, circa 1995: despite the fact that Street is a world leader in the area, Jim quickly realized and convinced Street and others that the approach cannot work, thereby saving us all a lot of time; a description of Jim's thinking was written up many years

later by Bourke and Gurski, https://arxiv.org/pdf/1412.1320.

I have spent hundreds of hours in conversation with Dolan, who is extraordinarily generous with his time and his ideas. (An idea of what mathematical conversation with Dolan is like can be gleaned from a quick Google search of the recent recorded conversations he has been having with Baez.) What regularly amazes me is that, just working as he does with a few well-chosen examples and protracted thinking them through, he produces deep conjectures which invariably turn out to be correct. I cannot think of any counterexample.

I am going to have to stop somewhere and sum it up, otherwise I'll find myself going on about more programs he has helped inaugurate (e.g., "groupoidification" and homotopy cardinality, among others). Simply put, Jim Dolan is a genius. This is a sadly overused word, so I'll put it much more emphatically: it is my sincere opinion that he is literally one in a million. Although he is mostly regarded as a theory man, I can attest to his power to solve problems, in the spirit of Grothendieck (ask him a question in group theory, and he will insightfully answer). Provided that he is properly supported, investing in his talents would be well rewarded indeed.

Todd Trimble, PhD.
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Western Connecticut State University