



### An Example

- Do you want to play tennis?
- Suppose that you have the following rule in your brain to answer to this question?
- PlayTennis Rule in your brain :

```
if ( Outlook =Sunny \times Humidity = Normal )
```

- v ( Outlook = Overcast )
- ∨ ( *Outlook* = *Rain* ∧ *Wind* = *Weak* ) **then** Yes **else** No

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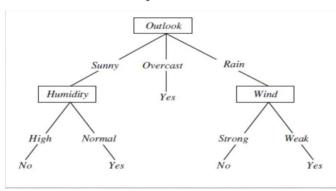
## An Example of Decision Tree

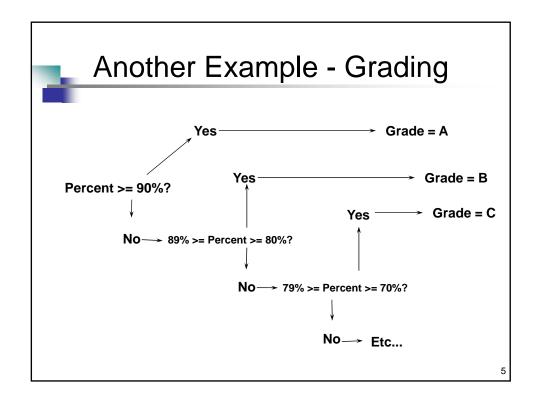
if ( Outlook =Sunny \( \times \) Humidity = Normal )

- v ( Outlook = Overcast )
- ∨ ( *Outlook* = *Rain* ∧ *Wind* = *Weak* ) **then** Yes

else No









#### Introduction

- Decision Trees
  - Powerful/popular for classification & prediction
  - Useful to explore data to gain insight into relationships of a large number of attribute variables to a target(classification) variable
- You may often use mental decision trees in practice
  - Remember PlayTennis example!



#### **Decision Tree Types**

• Binary decision trees – only two choices in each split.

rcent >= 90%?

Yes

Yes

Yes

Grade = B

Yes

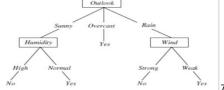
Fracet >= 80%?

No -- 78% >= Percent >= 70%?

No -- Etc...

 N-way or ternary decision trees – three or more choices in at least one of its splits

(3-way, 4-way, etc.)





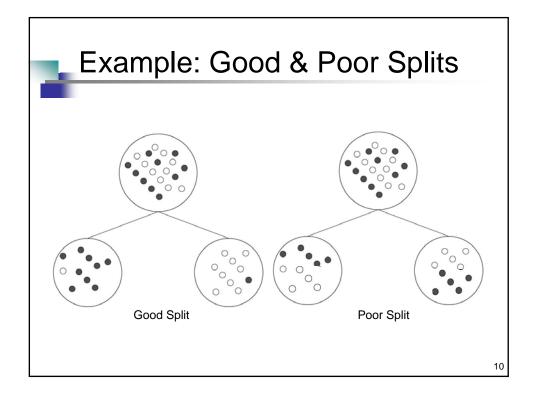
#### Decision Tree – More details

- A tree structure that can be used to split a large set of records into successively smaller sets of records by applying a sequence of simple decision rules
- A decision tree model consists of a set of split rules for dividing a large heterogeneous population into smaller, more homogeneous groups with respect to a particular target variable



## **Decision Tree Splits**

- The best split at root or child nodes is defined as one that does the best job of separating the data into groups each of which is homogeneous
  - Homogeneous means that each data has the same target value as the other
- Just split data according to the above "best split" rule!





## Split Criteria

- The measure used to evaluate how good a potential split is purity!
- If a data group contains several classes(several target values), then we say it is impure
- If a data group contains one class(one target value), then we say it is pure

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## Split Criteria

- The best split is one that increases purity of the sub-sets by the greatest amount
- A good split also creates nodes of similar size or at least does not create very small nodes

impure set of 10 data

highly pure set of 5 data

highly pure set of 5 data

# Impurity (or Diversity) Measures

- Impurity Measures for Choosing Best Split :
  - Information Gain based on Entropy
  - Gini (population diversity)
  - Information Gain Ratio (as a simple variation of Information Gain)
  - Chi-square Test based (on chi-square distribution in Statistics)

We will only explore Information Gain and Gini in this class!

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## Information Gain

#### ■ Entropy

To measure degree of impurity

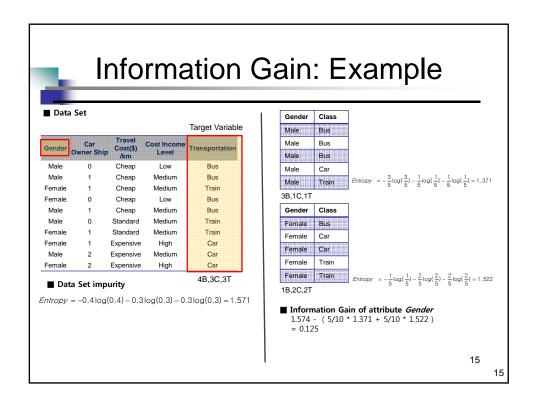
$$Entropy = \sum_{i} - p_{i} \log_{2} p_{i}$$

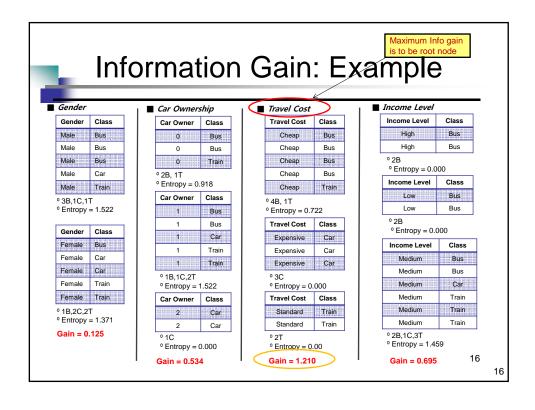
where  $p_j$  values of probability of class j

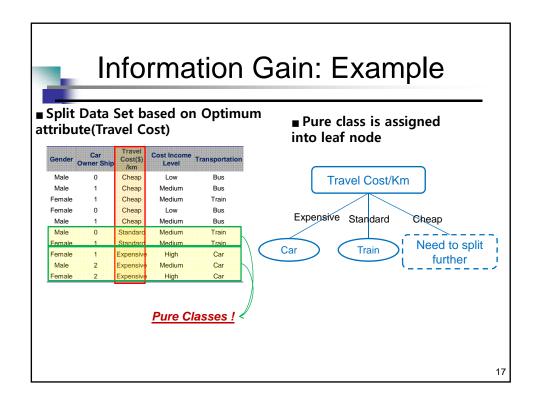
#### **■** Information gain

 $\bigcirc$  To compare the difference of impurity degrees between an original data set S and its split subsets  $S_V$ 

$$Gain(S, A) = Entropy(S) - \sum_{v \in Values(A)} \frac{|S_v|}{|S|} Entropy(S_v)$$







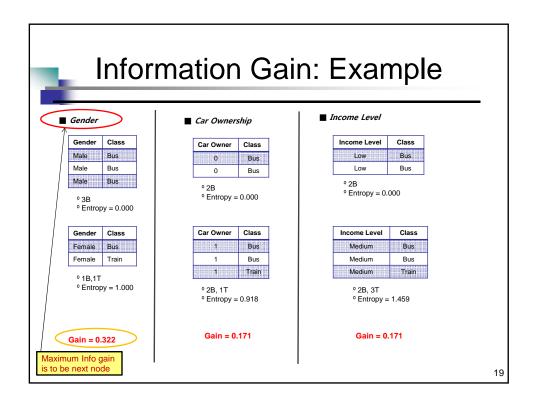
## Information Gain: Example

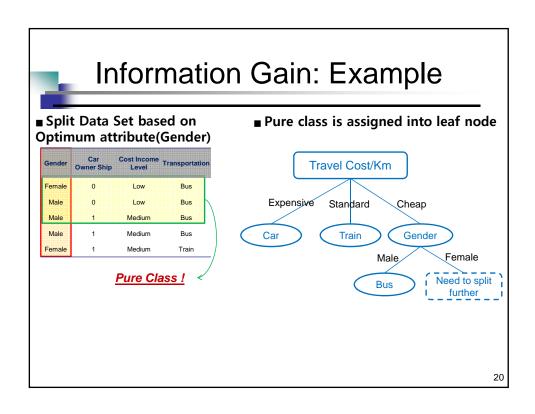
- Second iteration
  - Attribute Travel cost is not needed any more so it is removed
  - In the same way as the previous, we repeat the computations of Impurity and Information Gain for each of the three attributes

			Target Variable	
Gender	Car Owner Ship	Cost Income Level	Transportation	
Female	0	Low	Bus	
Male	0	Low	Bus	
Male	1	Medium	Bus	
Male	1	Medium	Bus	
Female	1	Medium	Train	

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Entropy = 
$$-\frac{1}{5}\log(\frac{1}{5}) - \frac{4}{5}\log(\frac{4}{5}) = 0.722$$

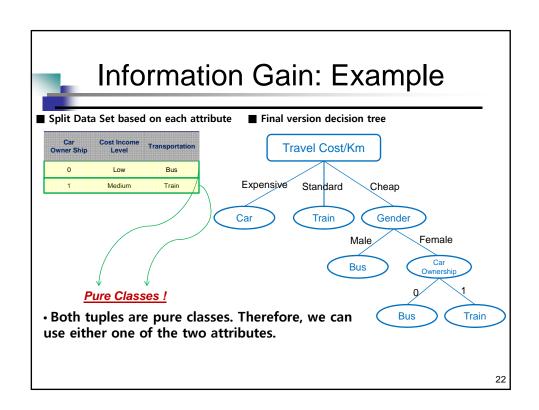






- **■** Third iteration
  - Attribute Gender cost is not needed any more so it is removed
  - In the same way as the previous, we repeat the computations of Impurity and Information Gain for each of the two attributes

Car Owner Ship	Cost Income Level	Transportation
0	Low	Bus
1	Medium	Train

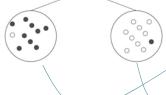


## Gini Purity (Population Diversity)

• The Gini measure of a node is the sum of the squares of the proportions of the classes:  $Gini = \sum_{i} p_{j}^{2}$ 



Root Node:  $0.5^2 + 0.5^2 = 0.5$  (evenly balanced: impure)



Each Leaf Node:  $0.1^2 + 0.9^2 = 0.82$  (close to pure)

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## Gini Purity (Population Diversity)

• Just replacing Entropy() with Gini() is enough to determine the best splitting attribute for a decision tree node

$$Gain(S, A) = \sum_{v \in Values(A)} \frac{|S_v|}{|S|} Gini(S_v) - Gini(S)$$

$$Entropy = \sum_{j} - p_{j} \log_{2} p_{j}$$



#### **Decision Tree Advantages**

- 1. Easy to understand
- 2. Mapped nicely to a set of business rules
- 3. Applied to a variety of real classification and prediction problems
- 4. Make no prior assumptions about the data
- Able to process both numerical and categorial attributes in data

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## Decision Tree Disadvantages

- Target(Classification) attribute must be categorial
- 2. Limited to one target attribute (one class)
- 3. Decision tree algorithms are sometimes unstable (similar to local search!)
- Trees created from numerical-attribute datasets can be very complex

