

# <<< Only Problem 1 and 2 will be graded >>>

## Problem 1 (sound)

Denoising time with FFT (DFT)

```
In [1]: # !pip install praat-parselmouth
```

```
In [2]: import numpy as np
import pandas as pd
from scipy import signal, fftpack
import cv2
from skimage.io import imread
import matplotlib.pyplot as plt
plt.style.use('seaborn-v0_8-whitegrid')
import IPython.display as ipd
import os

import librosa
import parselmouth
```

```
In [3]: sampling_rate = 32000
N=10001
Nf = 3 # Nf--> num freq
t = np.arange(N, dtype=float)
# pick rand period between 10-2010 and convert to freq

# random period
Ts = np.random.rand(Nf)*2000+10
fs=1/Ts

# fs in sampling rate = 32000
fs_real = fs*sampling_rate

# pick rand Amp and phase
amp = np.random.rand(Nf)*200+ 100
phi = np.random.rand(Nf)*2*np.pi

# create clean signal
h = np.zeros(N)
for i in range(len(fs)):
    h += amp[i]*np.sin(2*np.pi*fs[i]*t + phi[i])

# signal with noise
h_w_noise = h + np.random.randn(N)*3*h + np.random.randn(N)*700
```

```
In [4]: # TODO 1.1 : plot (1) clean signal and (2) noisy signal with label

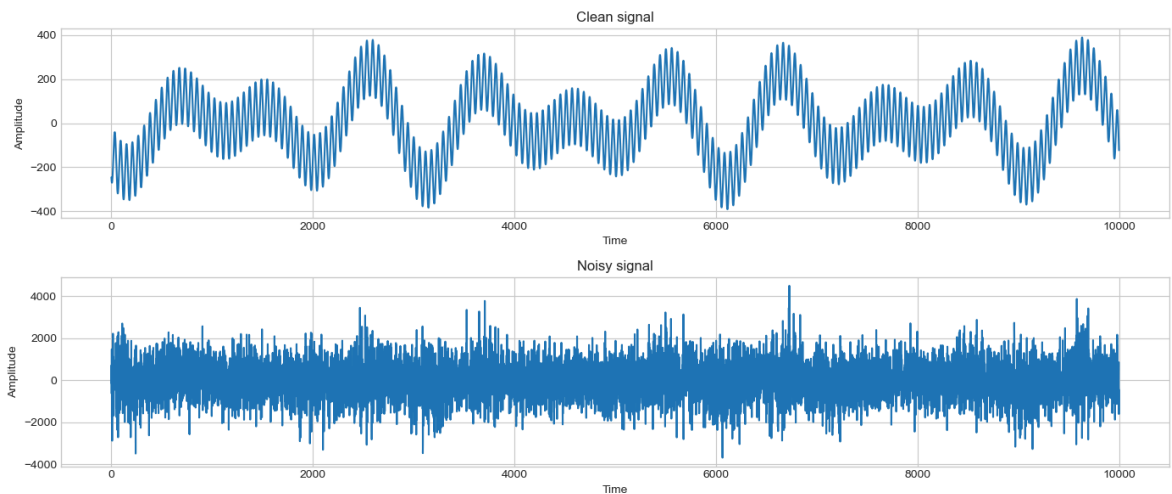
plt.figure(figsize=(14,6))

# Clean signal
plt.subplot(2, 1, 1)
```

```
plt.plot(t, h)
plt.title('Clean signal')
plt.xlabel('Time')
plt.ylabel('Amplitude')
plt.grid(True)

# Noisy signal
plt.subplot(2, 1, 2)
plt.plot(t, h_w_noise)
plt.title('Noisy signal')
plt.xlabel('Time')
plt.ylabel('Amplitude')
plt.grid(True)

plt.tight_layout()
plt.show()
```



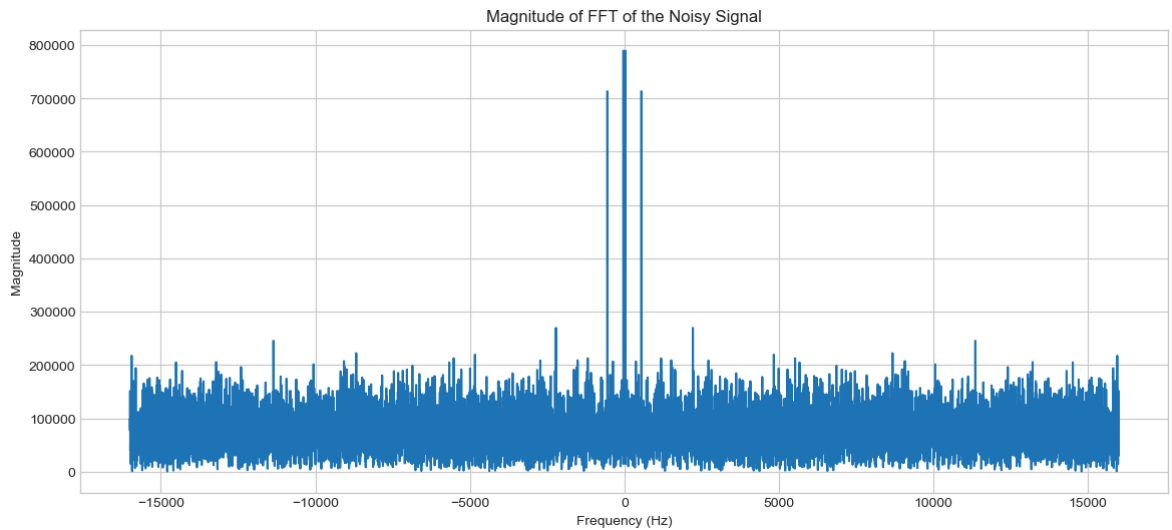
In [5]: *# TODO 1.2: plot magnitude of FFT of the noisy signal (freq sort form min*

```
# Compute the FFT of the noisy signal
H_w_noise_fft = np.fft.fft(h_w_noise)
magnitude = np.abs(H_w_noise_fft)

frequencies = np.fft.fftfreq(N, d=1/sampling_rate)
sorted_indices = np.argsort(frequencies)

sorted_frequencies = frequencies[sorted_indices]
sorted_magnitude = magnitude[sorted_indices]

# Plot
plt.figure(figsize=(14, 6))
plt.plot(sorted_frequencies, sorted_magnitude)
plt.title('Magnitude of FFT of the Noisy Signal')
plt.xlabel('Frequency (Hz)')
plt.ylabel('Magnitude')
plt.grid(True)
plt.show()
```



In [26]: *# TODO 1.3 : cleaning the noisy signal using magnitude of FFT*

```
# Wiener filtering
h_filtered = signal.wiener(h_w_noise)

# Plot
plt.figure(figsize=(14, 6))
plt.plot(t, h_filtered, color='orange')
plt.title('Filtered Signal')
plt.xlabel('Time')
plt.ylabel('Amplitude')
plt.grid(True)
plt.show()
```



In [7]: *# TODO 1.4 : plot clean signal, noise signal and filtered signal (from yo*

```
plt.figure(figsize=(18, 9))

# Clean signal
plt.subplot(3, 1, 1)
plt.plot(t, h)
plt.title('Clean signal')
plt.xlabel('Time')
plt.ylabel('Amplitude')
plt.grid(True)
```

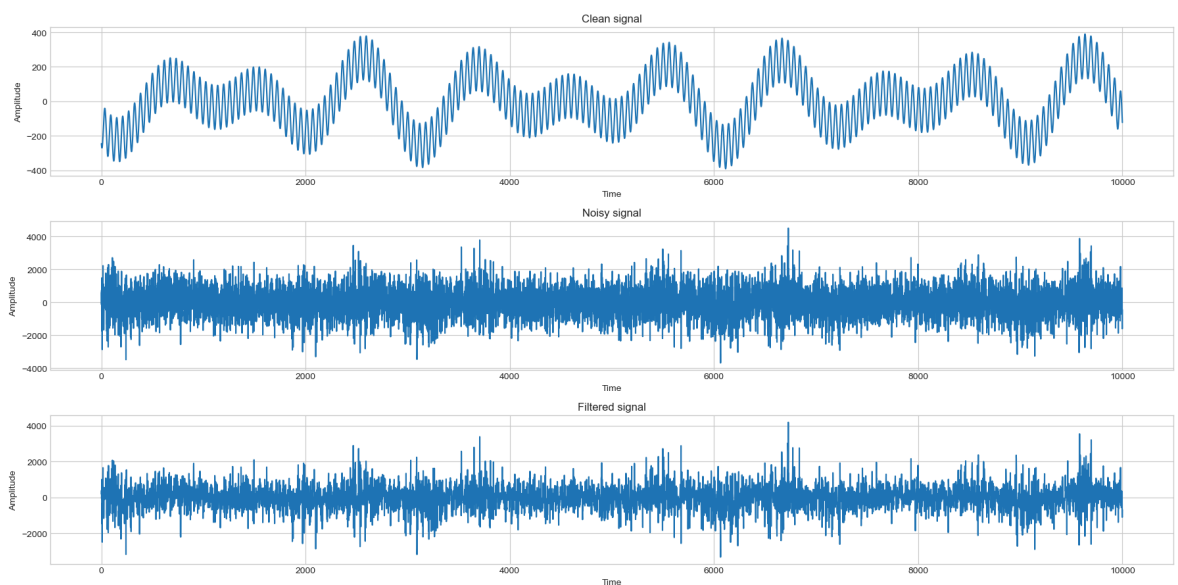
```

# Noisy signal
plt.subplot(3, 1, 2)
plt.plot(t, h_w_noise)
plt.title('Noisy signal')
plt.xlabel('Time')
plt.ylabel('Amplitude')
plt.grid(True)

# Filtered signal
plt.subplot(3, 1, 3)
plt.plot(t, h_filtered)
plt.title('Filtered signal')
plt.xlabel('Time')
plt.ylabel('Amplitude')
plt.grid(True)

plt.tight_layout()
plt.show()

```



In [8]: *# TODO 1.5 : export with IPython.display, listen to (1) original signal (*

```

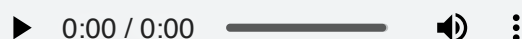
print("Clean Signal:")
ipd.display(ipd.Audio(data=h, rate=sampling_rate))

print("Noisy Signal:")
ipd.display(ipd.Audio(data=h_w_noise, rate=sampling_rate))

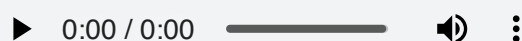
print("Filtered Signal:")
ipd.display(ipd.Audio(data=h_filtered, rate=sampling_rate))

```

Clean Signal:



Noisy Signal:



Filtered Signal:

In [22]: # TODO 1.6 : Write to explain and analyze the results

Answer:

โดยพื้นฐานทั้งสามเสียงจะมี ความถี่ค่อนข้างสูง(เสียงแหลม) สังเกตได้จากการฟังเสียง และการพิจารณา graph ใน TODO-1.4 โดยจะสังเกตได้ว่าตั้งแต่ clean signal จะมีความถี่(f)ค่อนข้างมาก/คาบ(T)สั้นๆ

ทำให้ noisy signal และ filtered signal มีพื้นฐานที่สร้างจาก clean signal ทำให้ ความถี่ค่อนข้างสูง(เสียงแหลม) ตามไปด้วย แต่ความรู้สึกเวลาฟังเสียงจะมีความซ่าๆกว่า clean signal โดย noisy signal จะมีความแสบแก้วหู(น่ารำคาญ) กว่า filtered signal ที่จะไม่มีความจางกว่า

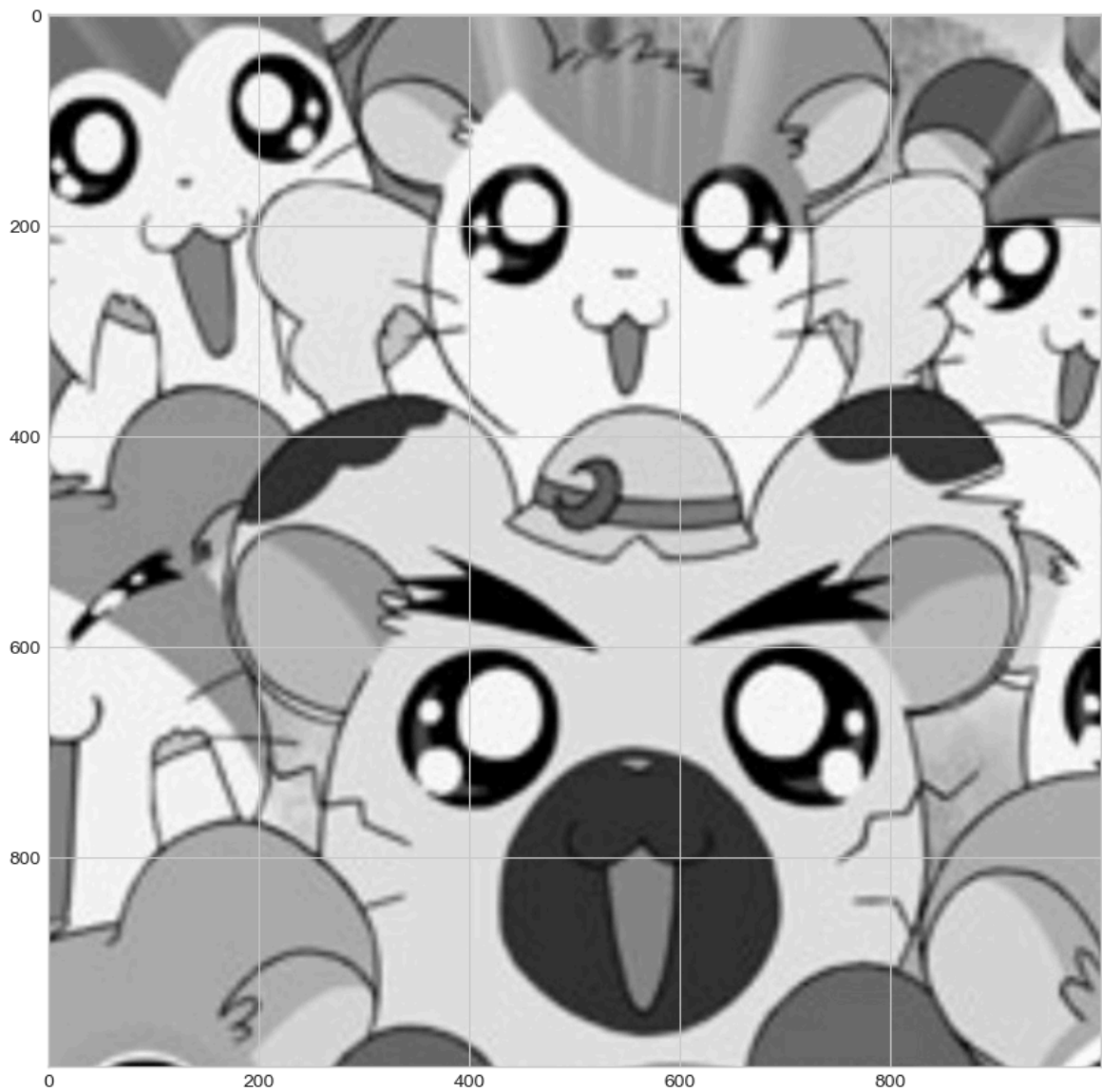
## Problem 2 (image FFT)

Download a 1000 x 1000 image ("hamtaro.png") below

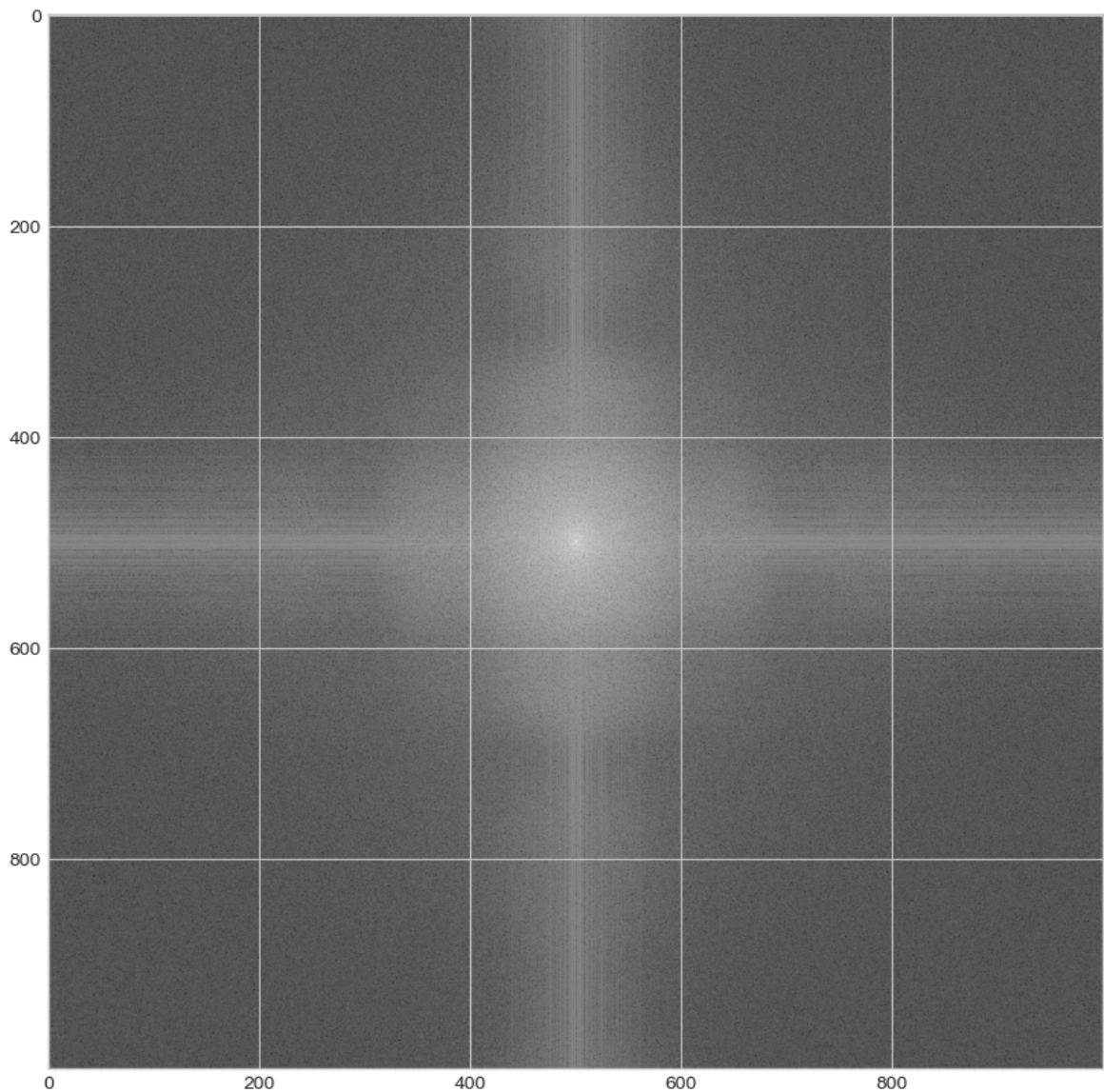


```
In [10]: screen_shot = cv2.imread('hamtaro.png',0)

plt.figure(figsize=(10,10))
plt.imshow(screen_shot, cmap='gray')
plt.show()
```



```
In [11]: # Apply FFT to the given image
F1 = fftpack.fft2((screen_shot).astype(float))
F2 = fftpack.fftshift(F1) # FFT center zeros freq
plt.figure(figsize=(10,10))
plt.imshow( (20*np.log10( 0.1 + np.abs(F2))).astype(int), cmap=plt.cm.gra
plt.show()
```



```
In [12]: # TODO 2.1 : Implement an ideal high-pass filter with a box size of 100x100

rows, cols = screen_shot.shape
# Create a mask
high_pass_mask = np.ones((rows, cols), dtype=np.float32)

# Create a central square of zeros (low-pass removal region)
n = 100 # 100x100 box
center_row, center_col = rows // 2, cols // 2
high_pass_mask[center_row - n//2:center_row + n//2, center_col - n//2:center_col + n//2] = 0

# Apply the filter
F2_filtered = F2 * high_pass_mask

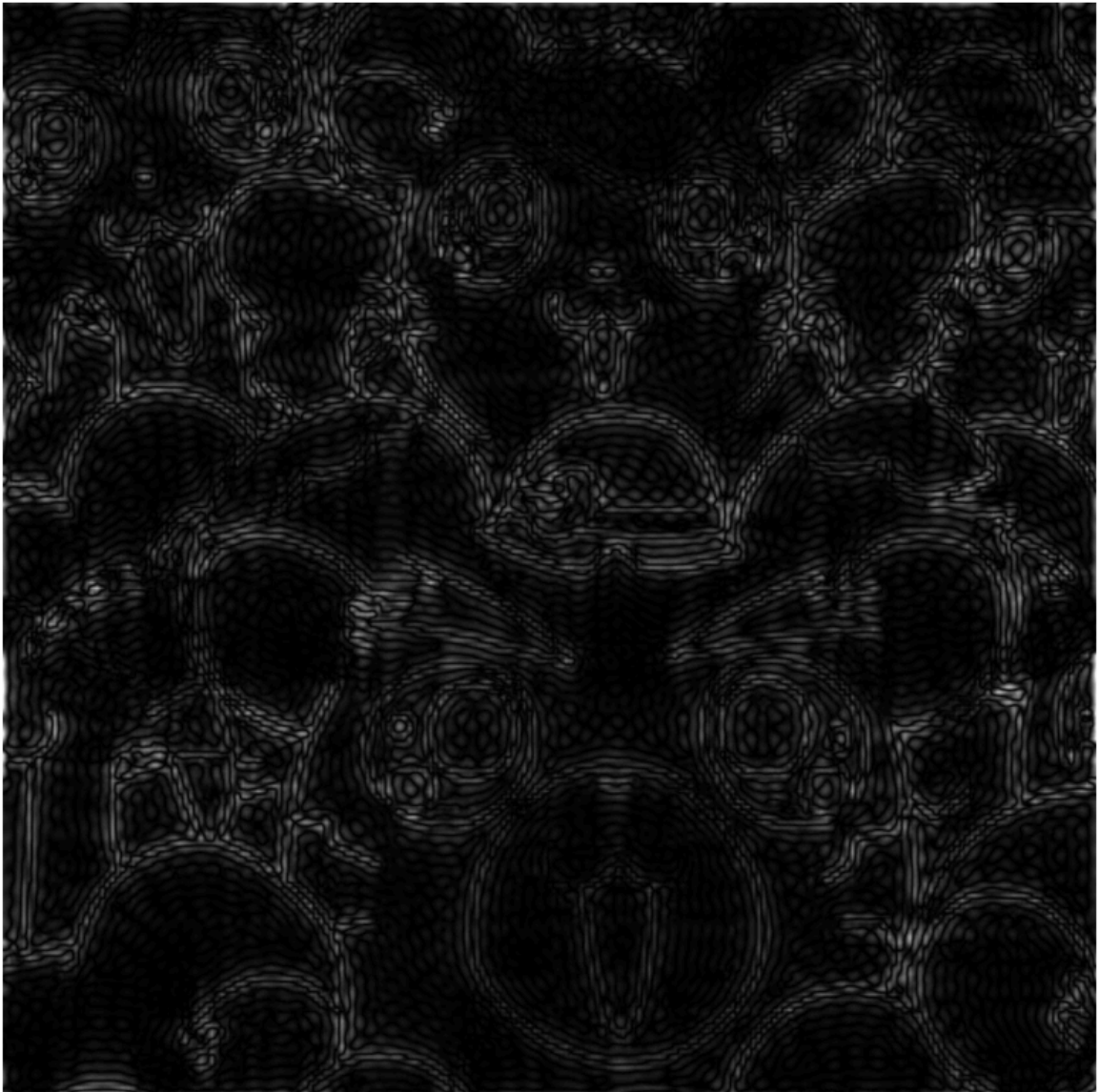
# Perform IFFT Shift and IFFT
F1_filtered = fftpack.ifftshift(F2_filtered)
image_filtered = fftpack.ifft2(F1_filtered)
image_filtered = np.abs(image_filtered)

# Plot
plt.figure(figsize=(10, 10))
plt.imshow(image_filtered, cmap='gray')
plt.title('High-Pass Filtered Image (100x100 Box)')
```



```
plt.axis('off')
plt.show()
```

High-Pass Filtered Image (100x100 Box)



```
In [13]: # TODO 2.2 : Implement an ideal low-pass filter with a box size of 100x100

rows, cols = screen_shot.shape
# Create a mask
low_pass_mask = np.zeros((rows, cols), dtype=np.float32)

# Create a central square of zeros (low-pass removal region)
n = 100 # 100x100 box
center_row, center_col = rows // 2, cols // 2
low_pass_mask[center_row - n//2:center_row + n//2, center_col - n//2:center_col + n//2] = 1

# Apply the filter
F2_filtered = F2 * low_pass_mask

# Perform IFFT Shift and IFFT
F1_filtered = fftpack.ifftshift(F2_filtered)
image_filtered = fftpack.ifft2(F1_filtered)
image_filtered = np.abs(image_filtered)

# Plot
plt.figure(figsize=(10, 10))
```



```
plt.imshow(image_filtered, cmap='gray')
plt.title('High-Pass Filtered Image (100x100 Box)')
plt.axis('off')
plt.show()
```

High-Pass Filtered Image (100x100 Box)



## Problem 3

A digital signal can be generated from sampling of an analog signal using a periodic impulse-train. Explain how you can reconstruct an analog signal from a digital signal and aliasing problem does not occur when  $f_s \leq 2f_{max}$  using frequency analysis.

where  $f_s$  is the sampling frequency and  $f_{max}$  is the maximum frequency of the analog signal

$$\text{HINT : } \mathcal{F} \left\{ \sum_{n=-\infty}^{\infty} \delta(t - nT_s) \right\} = \sum_{n=-\infty}^{\infty} \delta(\omega - n\omega_s) \text{ if } \omega_s = \frac{2\pi}{T_s} = 2\pi f_s$$

## Problem 4 : Aliasing

### Problem 4.1

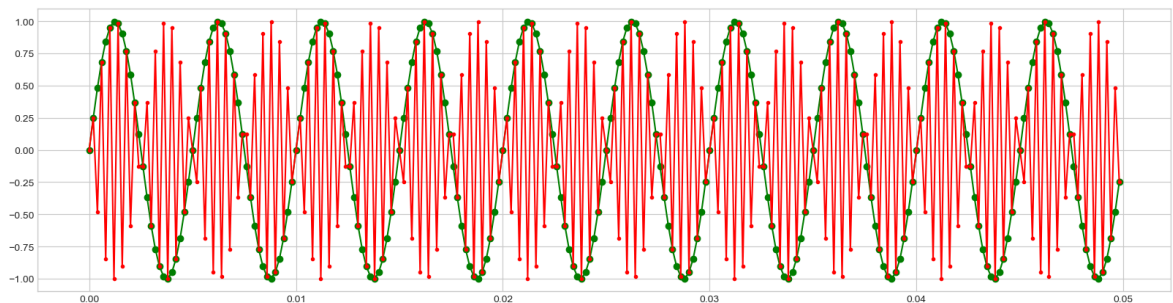
The following code generates two sine waves (x01\_ts01 and x02\_ts01) which are sampled in a range of  $t = 0, 0.05$  with sampling rate = 5000 Hz (f\_samp\_01). Study and write a report to analyze the results.

```
In [14]: t_st = 0
t_end = 0.05
f_01 = 200
f_02 = 2300

f_samp_01 = 5000

ts01 = np.linspace(t_st, t_end, int((t_end-t_st)*f_samp_01), endpoint=False)
x01_ts01 = np.sin(2*np.pi*f_01*ts01)
x02_ts01 = np.sin(2*np.pi*f_02*ts01)

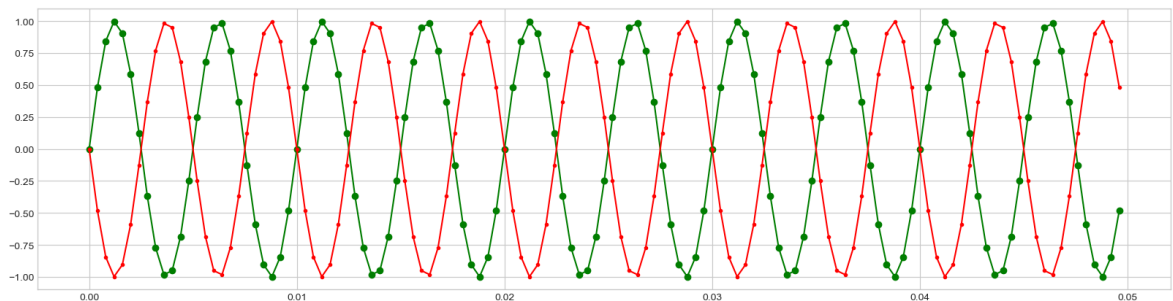
plt.figure(figsize=(20, 5))
plt.plot(ts01, x01_ts01, 'go-', ts01, x02_ts01, 'r.-')
plt.show()
```



The sampling rate is reduced to 2500 Hz (f\_samp\_02). Study and write a report to compare the results.

```
In [15]: f_samp_02 = 2500
ts02 = np.linspace(t_st, t_end, int((t_end-t_st)*f_samp_02), endpoint=False)
x01_ts02 = np.sin(2*np.pi*f_01*ts02)
x02_ts02 = np.sin(2*np.pi*f_02*ts02)

plt.figure(figsize=(20, 5))
plt.plot(ts02, x01_ts02, 'go-', ts02, x02_ts02, 'r.-')
plt.show()
```



Ans.

## Problem 4.2

The following code generate audio signals at different frequencies. Play the sound and write a report the analyse the results.

```
In [16]: t_st = 0
         t_end = 5
         f_01 = 50
         f_02 = 22050 - f_01
         f_03 = 22050 + f_01
         f_samp_02 = 22050

         ts02 = np.linspace(t_st, t_end , int((t_end-t_st)*f_samp_02), endpoint=False)

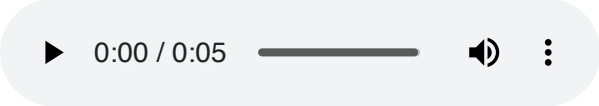
         # CREATE SIGNAL WITH DIFFERENT FREQ

         x01_ts02 = np.sin(2*np.pi*f_01*ts02)
         x02_ts02 = np.sin(2*np.pi*f_02*ts02)
         x03_ts02 = np.sin(2*np.pi*f_03*ts02)
```

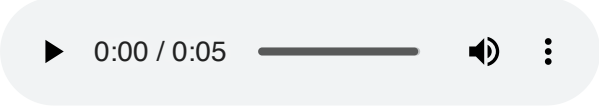
```
In [17]: x02_ts02
```

```
Out[17]: array([ 0.          , -0.0142471 , -0.02849132, ...,  0.04272974,
                0.02849132,  0.0142471 ])
```

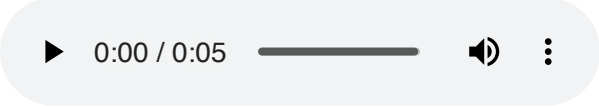
```
In [18]: ipd.Audio(x01_ts02, rate=f_samp_02)
```

Out[18]: 

```
In [19]: ipd.Audio(x02_ts02, rate=f_samp_02)
```

Out[19]: 

```
In [20]: ipd.Audio(x03_ts02, rate=f_samp_02)
```

Out[20]: 



imgflip.com

JAKE-CLARK.TUMBLR

from Imgflip Meme Generator

TODO : write report

Ans:

Problem 4.3

why many of audio file use sampling rate 44.1 kHz

Ans: