

1. Stability in quick sort - we choose not to swap if equal

First partitioning

10 15(x) 5 20 18 15(y)

Curr = 0

10

Curr = 1. No swap if equal to pivot.

10 15(x)

Curr = 1

10 15(x)

10 5 15(x)

Curr = 2

10 5 15(x) 20 18

Final : 10 5 || 15(y) || 18 20 15(x) -> Please note that in the class it was swapped incorrectly in the last step. We can see the out-of-order 15 values. This proves the sorting is not stable.

2. Worst case scenario - time complexity is $O(n^2)$

Starting array: 10 9 8 7 6 5 4 3 2 1

Partitioning step 1: ____ || 1 || 9 8 7 6 5 4 3 2 10 -> 9 -> $n - 1$

Partitioning step 2: Left arr -> quicksort({ }) and Right arr -> quicksort({ 9, 8, 7 6 5 4 3 2 10 }) -> 8 -> $n - 2$

Step 3: 7 -> $n - 3$

Step 4: 6 -> $n - 4$

...

Last step: 1

Total #comparisons = $1 + 2 + \dots + (n - 2) + (n - 1)$

= $n(n-1) / 2 = n^2 / 2 - n / 2 = O(n^2)$

EXERCISES

1. Come up with an example where this algorithm reverses the order of equal numbers

2. Implement median of 3 partitioning - median (arr[low], arr[(low + high) / 2], arr[high])

3. Implement kth() without recursion