

ΔH

i - rock, j - paper, k - scissors, N - i - j - k + players

$$H = -x(1-x)$$

$$\Delta H = \Delta H(t+1) - \Delta H(t),$$

$$\Delta H = -x_{t+1}(1 - x_{t+1}) - (-x_t(1 - x_t))$$

$$\Delta H = -x_{t+1}(1 - x_{t+1}) + x_t(1 - x_t)$$

$$\Delta H = x_t(1 - x_t) - x_{t+1}(1 - x_{t+1})$$

Rough equation:

$$\langle \Delta H \rangle = \sum_{i,j,k} (\Delta H_s - \Delta H_{s'}) T^{s \rightarrow s'}$$

$$\begin{aligned} \langle \Delta H \rangle = & \frac{1}{N^6} \sum_{i=1}^N \sum_{j=1}^N \sum_{k=1}^N \left[(N - i - j - k)(1 - N + i + j + k)(T^{R+} + T^{P+} + T^{S+} + T^{+R} + T^{+P} + T^{+S}) \right. \\ & - (N - i - j - k + 1)(-N + i + j + k)T^{R+} \\ & - (N - i - j - k + 1)(-N + i + j + k)T^{P+} \\ & - (N - i - j - k - 1)(2 - N + i + j + k)T^{+R} \\ & - (N - i - j - k - 1)(2 - N + i + j + k)T^{+P} \\ & \left. - (N - i - j - k - 1)(2 - N + i + j + k)T^{+S} \right] \end{aligned} \quad (1)$$

Ignoring some of the transition probabilities not including + as they would cancel out as they are just cycling within RPS and have no effect on ΔH_{SD} . Factorise this, then replace i,j,k with $x = i/N$, $y = j/N$... etc then replace sums with integrals.