ASSIGNMENT 1

CS21BTECH11053

Problem. 6c, ICSE Math Paper (2017):

If $\frac{7m+2n}{7m-2n} = \frac{5}{3}$ use properties of proportion to find:

(i)
$$\frac{m}{n}$$

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 (ii) $\frac{m^2+n^2}{m^2-n^2}$

Solution:

We are given,

$$\frac{7m+2n}{7m-2n} = \frac{5}{3} \tag{1}$$

From componendo - dividendo, we know

$$\frac{a}{b} = \frac{c}{d} \Rightarrow \frac{a+b}{a-b} = \frac{c+d}{c-d} \tag{2}$$

From (1) and (2)

$$\frac{(7m+2n)+(7m-2n)}{(7m+2n)-(7m-2n)} = \frac{5+3}{5-3} \implies \frac{14m}{4n} = \frac{8}{2}$$

$$\Rightarrow \frac{7m}{2n} = \frac{4}{1}$$

$$\Rightarrow \frac{m}{n} = \frac{8}{7}$$
(3)

From (3)

$$\left(\frac{m}{n}\right)^2 = \left(\frac{8}{7}\right)^2$$

$$\Rightarrow \frac{m^2}{n^2} = \frac{8^2}{7^2} = \frac{64}{49} \tag{4}$$

From (2) and (4)

$$\Rightarrow \frac{m^2 + n^2}{m^2 - n^2} = \frac{64 + 49}{64 - 49} = \frac{113}{15} \tag{5}$$

$$\therefore \frac{m}{n} = \frac{8}{7} \text{ and } \frac{m^2 + n^2}{m^2 - n^2} = \frac{113}{15}$$