

ASSIGNMENT 1

CS21BTECH11053

Abstract—From ICSE 2018 Class 12 Mathematics Examination

Problem (19.b). Find the coefficient of correlation from the regression lines

$$x - 2y + 3 = 0 \quad (1)$$

$$4x - 5y + 1 = 0 \quad (2)$$

Solution:

We shall assume that (1) is the regression line of y on x and (2) is the regression line of x on y .

From (1)

$$y = \frac{x}{2} + \frac{3}{2} \quad (3)$$

From (2)

$$x = \frac{5y}{4} - \frac{1}{4} \quad (4)$$

From (3) and (4), we evaluate regression coefficients b_{yx} and b_{xy} as

$$b_{yx} = \frac{1}{2} \quad (5)$$

$$b_{xy} = \frac{5}{4} \quad (6)$$

Given b_{yx} and b_{xy} , we can find the coefficient of correlation r as

$$r = \pm \sqrt{b_{yx} \times b_{xy}} \quad (7)$$

Note that b_{yx} , b_{xy} and r have the same sign and $|r| \leq 1$.

From (5), (6), (7)

$$r = \pm \sqrt{\frac{1}{2} \times \frac{5}{4}} = \pm \sqrt{\frac{5}{8}} \quad (8)$$

Since $b_{yx} > 0$ and $b_{xy} > 0$, $r > 0$. Also note that $|r| \leq 1$. Hence our initial assumption was correct.

$$\therefore r = \sqrt{\frac{5}{8}} \quad (9)$$

