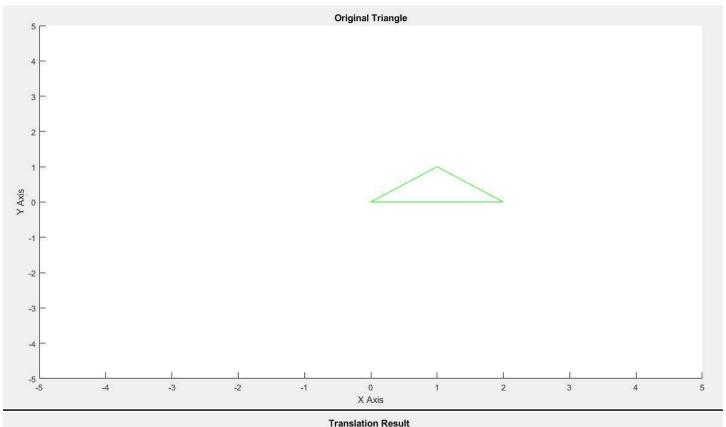
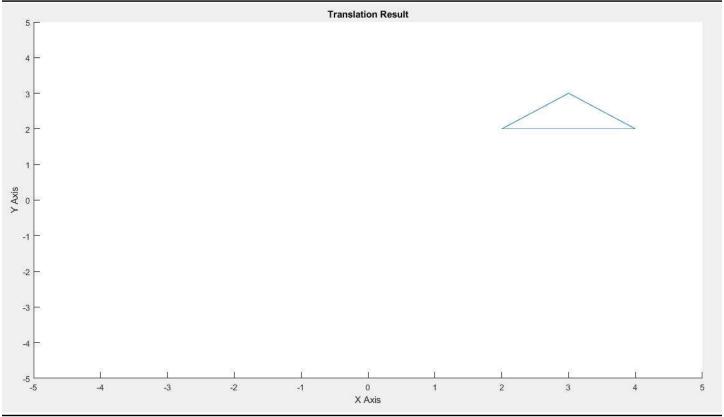
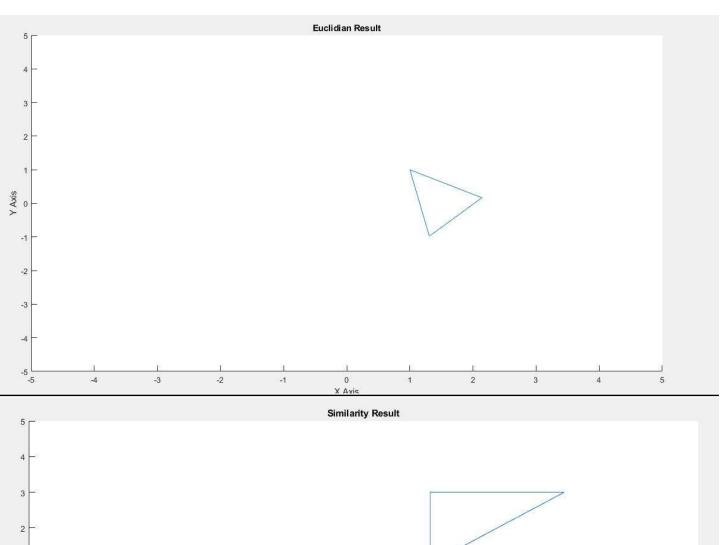
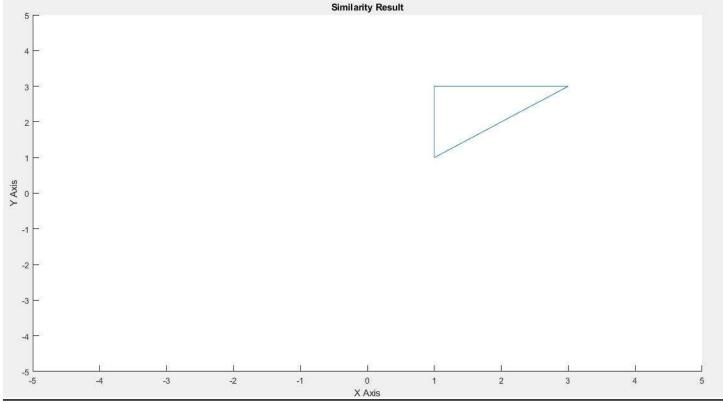
Answer (1):

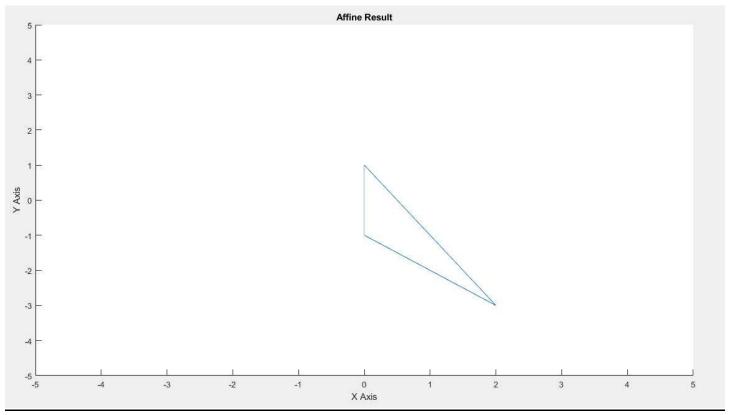
Transformations for Equilateral Triangle

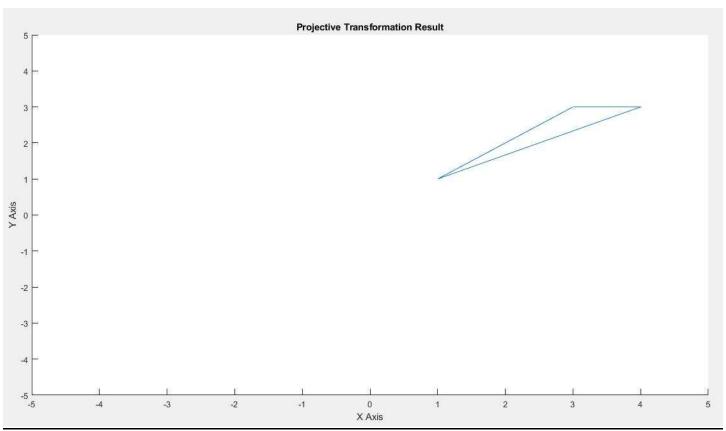




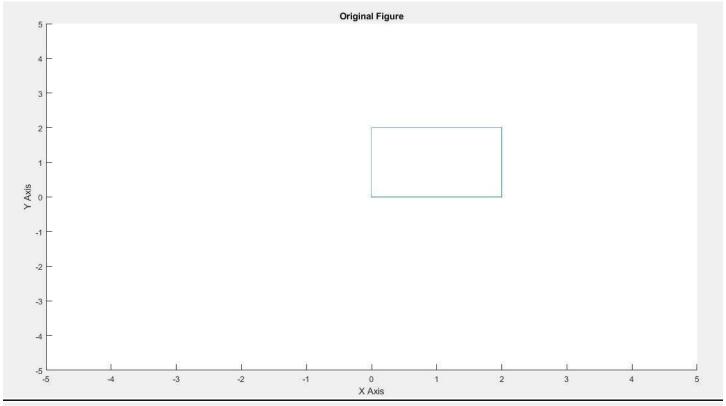


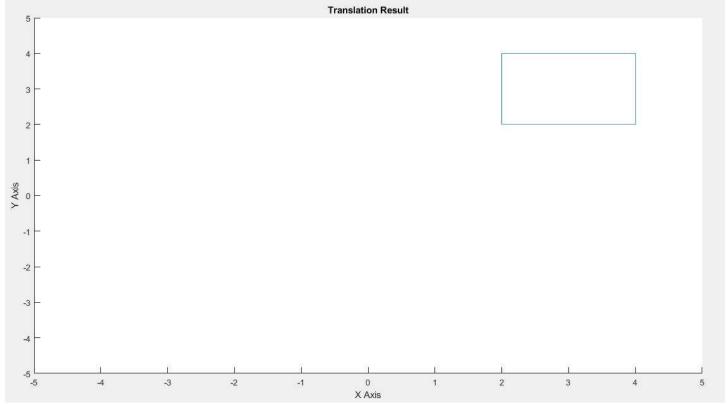


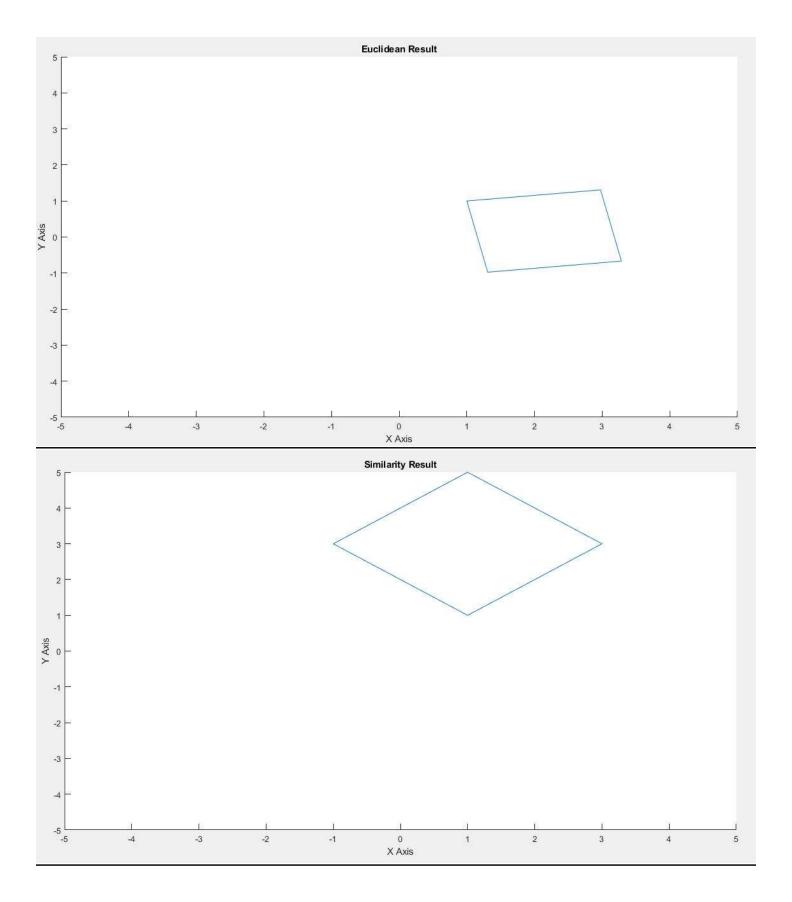


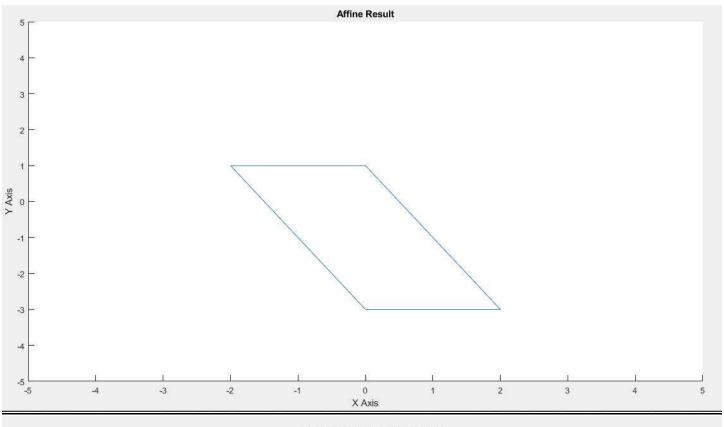


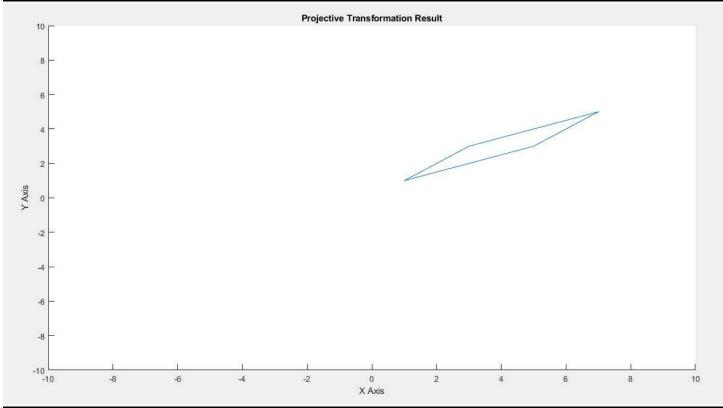
Transformations For Square



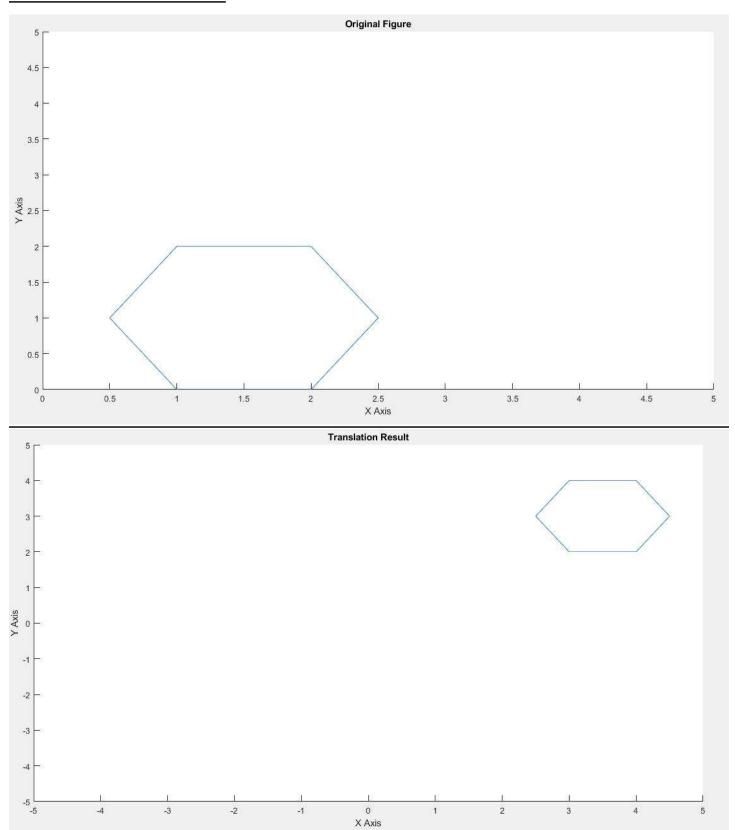


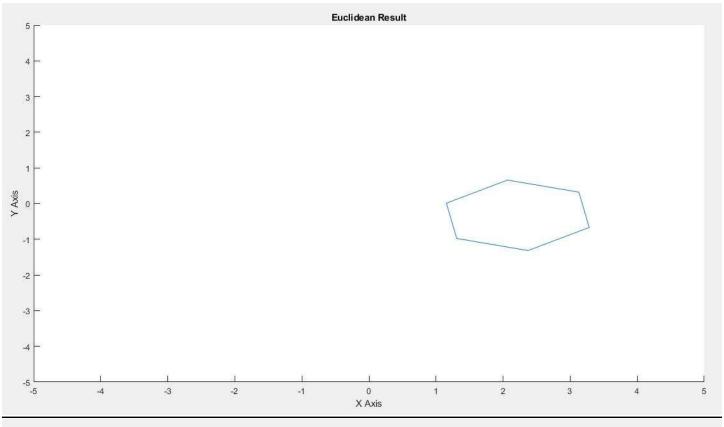


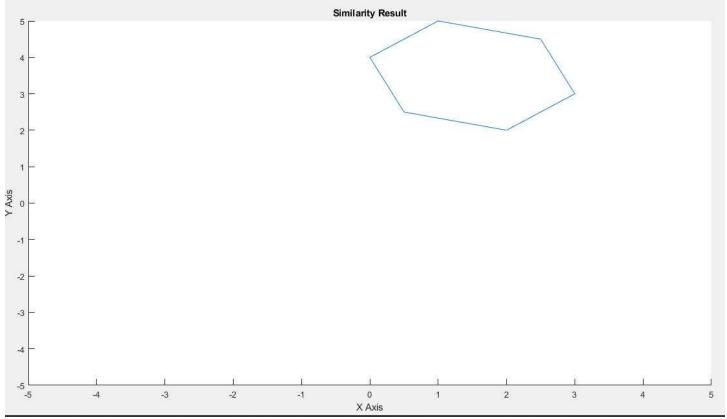


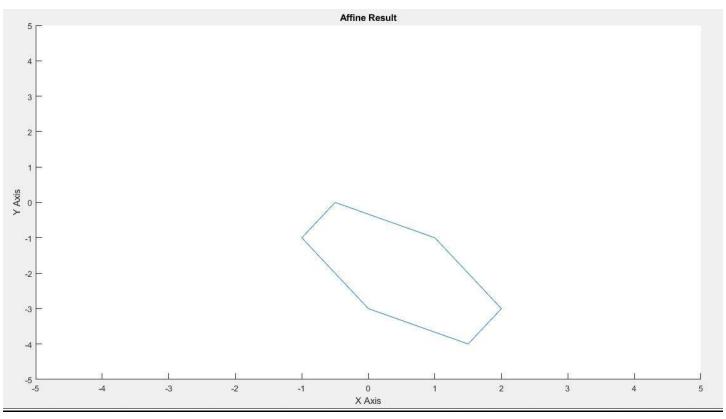


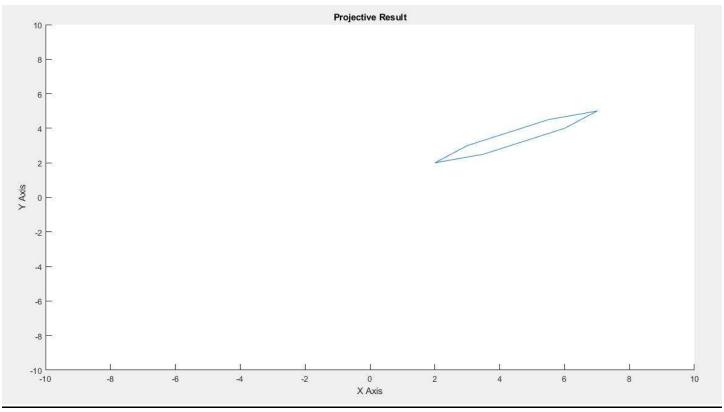
Transformations For HEXAGON:











Answer (2):

1. Translation:

After Translation Transformation, Characteristic which remain unchanged are

- Length of Sides,
- Angle between the lines
- Orientation are preserved.

2. Euclidian:

After Euclidian Transformation, Characteristic which remain unchanged are

- Length of Sides
- Angle between the lines are preserved.

3. Similarity:

After Similarity Transformation, Characteristic which remain unchanged is

• Angle between the lines is preserved.

4. Affine:

After Affine Transformation, Characteristic which remain unchanged are

• Parallel lines stays parallel.

5. Projective:

After Projective Transformation, Characteristic which remain unchanged are

0 1.0000];

• Straight lines stay straight.

Answer (3):

Translation Matrix

Matrices for transformations

```
t = [1\ 0\ 2;\ 0\ 1\ 2;\ 0\ 0\ 1]; Euclidian Matrix R = [0.1543\quad 0.9880\quad 1.0000;\ -0.9880\quad 0.1543\quad 1.0000;\ 0 Similarity Matrix
```

```
E = [1 -1 1; 1 1 1; 0 0 1];
```

Affine Matrix

$$A = [1 -1 0; -2 0 1; 0 0 1];$$

Projective Matrix

$$P = [1 \ 2 \ 1; \ 1 \ 1 \ 1; \ 2 \ 2 \ 1];$$

Answer (4):

Coordinates of Equilateral Triangle:

Cartesian coordinate for an Equilateral Triangle x = [0; 0]

Cartesian coordinate for an Equilateral Triangle y=[2; 0]

Cartesian coordinate for an Equilateral Triangle z=[1; 1]

Homogenous coordinate for an Equilateral Triangle x1 = [0; 0; 1]

Homogenous coordinate for an Equilateral Triangle y1= [2; 0; 1]

Homogenous coordinate for an Equilateral Triangle z1 = [1; 1; 1]

Coordinates of Square:

Cartesian coordinate for a Square A=[0; 0]

Cartesian coordinate for a Square C=[2; 0]

Cartesian coordinate for a Square C=[2; 2]

Cartesian coordinate for a Square D= [0; 2]

Homogenous coordinate for a Square a1=[0; 0; 1]

Homogenous coordinate for a Square b1=[2; 0; 1]

Homogenous coordinate for a Square c1= [2; 2; 1]

Homogenous coordinate for a Square d1 = [0; 2; 1]

Coordinates of Hexagon:

Cartesian coordinate for a Hexagon A=[1; 0];

Cartesian coordinate for a Hexagon B=[2; 0];

Cartesian coordinate for a Hexagon C=[2.5; 1];

Cartesian coordinate for a Hexagon D= [2; 2];

Cartesian coordinate for a Hexagon E=[1; 2];

Cartesian coordinate for a Hexagon F=[0.5; 1];

Homogenous coordinate for a Hexagon a1=[1; 0; 1];

Homogenous coordinate for a Hexagon b1=[2; 0; 1];

Homogenous coordinate for a Hexagon c1=[2.5; 1; 1]

Homogenous coordinate for a Hexagon d1=[2; 2; 1]

Homogenous coordinate for a Hexagon e1=[1; 2; 1]

Homogenous coordinate for a Hexagon f1 = [0.5; 1; 1]

Homogeneous Coordinates of Vertices of Transformed Triangle:

Translation:

Cartesian Coordinates

- t1 = [2; 2]
- t2 = [3; 3]
- t3 = [4; 2;]

Homogeneous Coordinates

- t1 = [2; 2; 1]
- t2 = [3; 3; 1]
- t3 = [4; 2; 1]

Euclidian:

Cartesian Coordinates

- R1 = [1; 1]
- R2 = [2.14; 0.16]
- R3 = [1.30; -0.97]

Homogeneous Coordinates

- R1 = [1; 1; 1]
- R2 = [2.14; 0.16; 1]
- R3 = [1.30; -0.97; 1]

Similarity:

Cartesian Coordinates

- S1 = [1; 1]
- S2 = [1; 3]
- S3 = [3; 3]

Homogeneous Coordinates

- S1 = [1; 1; 1]
- S2 = [1; 3; 1]
- S3 = [3; 3; 1]

Affine:

Cartesian Coordinates

- A1 = [0; 1]
- A2 = [1; -1]
- A3 = [2; -3]

Homogeneous Coordinates

- A1 = [0; 1; 1]
- A2 = [1; -1; 1]
- A3 = [2; -3; 1]

Projective:

Cartesian Coordinates

- P1 = [1; 1]
- P2 = [4; 3]
- P3 = [3; 3]

Homogeneous Coordinates

- P1 = [1; 1; 1]
- P2 = [4; 3; 2]
- P3 = [3; 3; 1]

Vertices of Transformed Square:

Translation:

- t1 = [2; 2]
- t2 = [4; 2]
- t3 = [4; 4]
- t4 = [2; 4]

Homogeneous Coordinates

- t1 = [2; 2; 1]
- t2 = [4; 2; 1]
- t3 = [4; 4; 1]
- t4 = [2; 4; 1]

Euclidian:

Cartesian Coordinated

- R1 = [1; 1]
- R2 = [1.31; -0.98]
- R3 = [3.28; -0.67]
- R4 = [2.97; 1.30]

Homogeneous Coordinates

- R1 = [1; 1; 1]
- R2 = [1.31; -0.98; 1]
- R3 = [3.28; -0.67; 1]
- R4 = [2.97; 1.30; 1]

Similarity:

- E1 = [1; 1]
- E2 = [5; 5]
- E3 = [1; 9]
- E4 = [-3; 5]

- E1 = [1; 1; 1]
- E2 = [5; 5; 1]
- E3 = [1; 9; 1]
- E4 = [-3; 5; 1]

Affine:

Cartesian Coordinated

- A1 = [1; 1]
- A2 = [3; 3]
- A3 = [1; 5]
- A4 = [-1; 3]

Homogeneous Coordinates

- A1 = [1; 1; 1]
- A2 = [3; 3; 1]
- A3=[1;5;1]
- A4 = [-1; 3; 1]

Projective:

Cartesian Coordinated

- P1 = [1; 1]
- P2 = [3; 3]
- P3 = [7; 5]
- P4 = [5; 3]

Homogeneous Coordinates

- P1 = [1; 1; 1]
- P2 = [3; 3; 1]
- P3 = [7; 5; 1]
- P4 = [5; 3; 1]

Vertices of Transformed Hexagon:

Translation:

Cartesian Coordinated

- t1 = [3; 2]
- t2 = [4; 2]
- t3 = [4.5; 3]
- t4 = [4; 4]
- t5 = [3; 4]
- t6 = [2.5, 3]

Homogeneous Coordinates

- t1 = [3; 2; 1]
- t2 = [4; 2; 1]
- t3 = [4.5; 3; 1]
- t4 = [4; 4; 1]
- t5 = [3; 4; 1]
- t6 = [2.5, 3, 1]

Euclidian

- t1 = [1.15; 0.01]
- t2 = [1.30; -0.97]
- t3 = [2.37; -1.31]
- t4 = [3.28; -0.66]
- t5 = [3.13; 0.32]
- t6 = [2.06; 0.66]

$$t1 = [1.15; 0.01; 1]$$

$$t2 = [1.30; -0.97; 1]$$

$$t3 = [2.37; -1.31; 1]$$

$$t4 = [3.28; -0.66; 1]$$

$$t5 = [3.13; 0.32; 1]$$

$$t6 = [2.06; 0.66; 1]$$

Similarity

Cartesian Coordinated

$$E1 = [2; 2]$$

$$E2 = [3; 3]$$

$$E3 = [2.5; 4.5]$$

$$E4 = [1; 5]$$

$$E5 = [0; 4]$$

$$E6 = [0.50; 2.50]$$

Homogeneous Coordinates

$$E1 = [2; 2; 1]$$

$$E2 = [3; 3; 1]$$

$$E3 = [2.50; 4.50; 1]$$

$$E4 = [1; 5; 1]$$

$$E5 = [0; 4; 1]$$

$$E6 = [0.50; 2.50; 1]$$

Affine

$$A1 = [1; -1]$$

$$A2 = [2; -3]$$

$$A3 = [1.5; -4]$$

$$A4 = [0; -3]$$

$$A5 = [-1; -1]$$

$$A6 = [-0.50; 0]$$

Homogeneous Coordinates

$$A1 = [1; -1; 1]$$

$$A2 = [2; -3; 1]$$

$$A3 = [1.50; -4.0; 1]$$

$$A4 = [0; -3; 1]$$

$$A5 = [-1; -1; 1]$$

$$A6 = [-0.50; 0; 1]$$

Perspective Transformation

Cartesian Coordinated

$$A1 = [2; 2]$$

$$A2 = [3; 3]$$

$$A3 = [5.5; 4.5]$$

$$A4 = [7; 5]$$

$$A5 = [6; 4]$$

$$A6 = [3.50; 2.50]$$

Homogeneous Coordinates

$$A1 = [2; 2; 1]$$

$$A2 = [3; 3; 1]$$

$$A3 = [5.5; 4.5; 1]$$

$$A4 = [7; 5; 1]$$

$$A5 = [6; 4; 1]$$

$$A6 = [3.50; 2.50; 1]$$

```
clc;
clear all;
close all;
display('Answer-1')
display('Transformations For Equilateral Triangle')
% Equilateral Triangle Points
x = [0,0];
y = [1,1];
z = [2,0];
display('Original Poins are')
[x' y' z']
figure(1)
axis([-5 5 -5 5])
line([x(1),y(1)],[x(2),y(2)],'color','green');
line([x(1),z(1)],[x(2),z(2)],'color','green');
line([y(1),z(1)],[y(2),z(2)],'color','green');
xlabel('X Axis')
ylabel('Y Axis')
title('Original Triangle')
w=1;
x1 = [x'; w];
y1 = [y'; w];
z1 = [z'; w];
disp('Transformation Matrix is')
                          %Translation Matrix
t=[1 0 2; 0 1 2; 0 0 1]
x2=t*x1;
y2=t*y1;
z2=t*z1;
disp('Points after Translation')
[x2(1:2) y2(1:2) z2(1:2)]
figure(2)
axis([-5 5 -5 5])
line([x2(1),y2(1)],[x2(2),y2(2)])
line([x2(1), z2(1)], [x2(2), z2(2)])
line ([y2(1), z2(1)], [y2(2), z2(2)])
xlabel('X Axis')
ylabel('Y Axis')
title('Translation Result')
 % Euclidian Transformation
 theta= 30;
 disp('Euclidian Transformation Matrix is')
 R=[cos(theta) -sin(theta) 1;sin(theta) cos(theta) 1;0 0 1] %Euclidean Matrix
 R1=R*x1;
 R2=R*y1;
 R3=R*z1;
 disp('Points after Euclidian Transformation')
 [R1(1:2) R2(1:2) R3(1:2)]
 figure(3)
 axis([-5 5 -5 5])
 line([R1(1),R2(1)],[R1(2),R2(2)])
 line([R1(1),R3(1)],[R1(2),R3(2)])
 line([R2(1),R3(1)],[R2(2),R3(2)])
 xlabel('X Axis')
 ylabel('Y Axis')
 title('Euclidian Transformation Result')
```

```
% Similarity transformation
disp('Similarity Transformation Matrix is')
E=[1 -1 1 ;1 1 1;0 0 1] %similarity Matrix
E1=E*x1;
E2=E*y1;
E3=E*z1;
disp('Points after Similarity Transformation')
[E1(1:2) E2(1:2) E3(1:2)]
figure (4)
axis([-5 5 -5 5])
line([E1(1),E2(1)],[E1(2),E2(2)])
line([E1(1),E3(1)],[E1(2),E3(2)])
line([E2(1),E3(1)],[E2(2),E3(2)])
xlabel('X Axis')
vlabel('Y Axis')
title('Similarity TransformationResult')
% Affine Transformation
disp('Affin Transformation Matrix is')
A=[1 -1 0 ; -2 0 1; 0 0 1]
A1=A*x1;
A2=A*y1;
A3=A*z1;
disp('Points after Affine Transformation')
[A1(1:2) A2(1:2) A3(1:2)]
figure (5)
axis([-5 5 -5 5])
line([A1(1),A2(1)],[A1(2),A2(2)])
line([A1(1),A3(1)],[A1(2),A3(2)])
line([A2(1),A3(1)],[A2(2),A3(2)])
xlabel('X Axis')
ylabel('Y Axis')
title('Affine Transformation Result')
% projective transformation
disp('Projective Transformation Matrix is')
H=[1 2 1;1 1 1;2 2 1]
H1=H*x1;
H2=H*v1;
H3=H*z1;
disp('Points after Projective Transformation')
[H1(1:2) H2(1:2) H3(1:2)]
figure(6)
axis([-5 5 -5 5])
line([H1(1),H2(1)],[H1(2),H2(2)])
line([H1(1),H3(1)],[H1(2),H3(2)])
line([H2(1),H3(1)],[H2(2),H3(2)])
xlabel('X Axis')
ylabel('Y Axis')
title('Projective Transformation Result')
display('Transformations For Square')
display('Original points are')
a = [0;0];
b = [2;0];
c = [2;2];
d = [0;2];
```

```
[a b c d]
figure (7)
axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title('Original Figure')
line([a(1),b(1)],[a(2),b(2)]);
line([b(1),c(1)],[b(2),c(2)]);
line([c(1),d(1)],[c(2),d(2)]);
line([d(1),a(1)],[d(2),a(2)]);
w=1;
a1=[a;w];
b1=[b;w];
c1=[c;w];
d1=[d;w];
display('Transformation Matrix is')
t = [1 \ 0 \ 2 \ ; \ 0 \ 1 \ 2 \ ; \ 0 \ 0 \ 1] \ %translation
t1=t*a1;
t2=t*b1;
t3=t*c1;
t4=t*d1;
disp('Points after Translation')
 [t1(1:2) t2(1:2) t3(1:2) t4(1:2)]
figure(8)
axis([-5 5 -5 5])
line([t1(1),t2(1)],[t1(2),t2(2)]);
line([t2(1),t3(1)],[t2(2),t3(2)]);
line([t3(1),t4(1)],[t3(2),t4(2)]);
line([t4(1),t1(1)],[t4(2),t1(2)]);
xlabel('X Axis')
ylabel('Y Axis')
title('Translation Result')
%Euclidian Transformation
theta = 30;
display('Euclidian Transformation Matrix is')
R=[cos(theta) -sin(theta) 1; sin(theta) cos(theta) 1;0 0 1]
%euclidean=translation+rotation
R1=R*a1;
R2=R*b1;
R3=R*c1;
R4=R*d1;
disp('Points after Euclidian Transformation')
[R1(1:2) R2(1:2) R3(1:2) R4(1:2)]
figure(9)
axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title ('Euclidean Transformation Result')
line([R1(1),R2(1)],[R1(2),R2(2)]);
line([R2(1),R3(1)],[R2(2),R3(2)]);
line([R3(1),R4(1)],[R3(2),R4(2)]);
line([R4(1),R1(1)],[R4(2),R1(2)]);
%similarity transform
display('Similarity Transformation Matrix is')
E = [1 -1 1; 1 1 1; 0 0 1]
E1=E*a1;
E2=E*b1;
E3=E*c1;
E4=E*d1;
disp('Points after Similarity Transformation')
 [E1(1:2) E2(1:2) E3(1:2) E4(1:2)]
```

```
figure (10)
axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title('Similarity TransformationResult')
line([E1(1),E2(1)],[E1(2),E2(2)]);
line([E2(1),E3(1)],[E2(2),E3(2)]);
line([E3(1), E4(1)], [E3(2), E4(2)]);
line([E4(1),E1(1)],[E4(2),E1(2)])
% AFFINE Transformation
disp('Affin Transformation Matrix is')
A=[1 -1 0 ; -2 0 1 ; 0 0 1]
A1=A*a1;
A2=A*b1;
A3=A*c1;
A4=A*d1;
disp('Points after Affine Transformation')
[A1(1:2) A2(1:2) A3(1:2) A4(1:2)]
figure (11)
axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title('Affine TransformationResult')
line([A1(1),A2(1)],[A1(2),A2(2)]);
line([A2(1),A3(1)],[A2(2),A3(2)]);
line([A3(1),A4(1)],[A3(2),A4(2)]);
line([A4(1),A1(1)],[A4(2),A1(2)]);
%projective transformation
disp('Projective Transformation Matrix is')
P = [1 \ 2 \ 1; 1 \ 1 \ 1; 2 \ 2 \ 1]
P1=P*a1;
P2=P*b1;
P3=P*c1;
P4=P*d1;
disp('Points after Projective Transformation')
[P1(1:2) P2(1:2) P3(1:2) P4(1:2)]
figure (12)
axis([-10 10 -10 10])
xlabel('X Axis')
ylabel('Y Axis')
title('Projective Transformation Result')
line([P1(1),P2(1)],[P1(2),P2(2)]);
line([P2(1),P3(1)],[P2(2),P3(2)]);
line([P3(1),P4(1)],[P3(2),P4(2)])
line([P4(1),P1(1)],[P4(2),P1(2)])
display('Hexagon Transformation')
a = [1;0];
b = [2;0];
c = [2.5;1];
d = [2;2];
e = [1;2];
f = [0.5;1];
display('Original Poins are')
[abcdef]
figure (13)
axis([0 5 0 5])
xlabel('X Axis')
```

```
ylabel('Y Axis')
 title('Original Figure')
line([a(1),b(1)],[a(2),b(2)]);
line([b(1),c(1)],[b(2),c(2)]);
line([c(1),d(1)],[c(2),d(2)]);
line([d(1), e(1)], [d(2), e(2)]);
 line([e(1),f(1)],[e(2),f(2)]);
 line([f(1),a(1)],[f(2),a(2)]);
w=1;
a1=[a;w];
b1=[b;w];
c1=[c;w];
d1=[d;w];
e1=[e;w];
f1=[f;w];
% Translation
disp('Transformation Matrix is')
t = [1 \ 0 \ 2 \ ; \ 0 \ 1 \ 2 \ ; \ 0 \ 0 \ 1] \ %translation
t1=t*a1;
t2=t*b1;
t3=t*c1;
t4=t*d1;
t5=t*e1;
t6=t*f1;
disp('Points after Translation')
 [t1(1:2) t2(1:2) t3(1:2) t4(1:2) t5(1:2) t6(1:2)]
 figure (14)
 axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title('Translation Result')
line([t1(1), t2(1)], [t1(2), t2(2)]);
line([t2(1),t3(1)],[t2(2),t3(2)]);
 line([t3(1),t4(1)],[t3(2),t4(2)]);
line([t4(1), t5(1)], [t4(2), t5(2)]);
line([t5(1),t6(1)],[t5(2),t6(2)]);
line([t6(1),t1(1)],[t6(2),t1(2)]);
 % Euclidian Transformation
theta= 30;
disp('Euclidian Transformation Matrix is')
R = [\cos(\text{theta}) - \sin(\text{theta}) \ 1; \sin(\text{theta}) \ \cos(\text{theta}) \ 1; 0 \ 0
11%euclidean=translation+rotation
R1=R*a1;
R2=R*b1;
R3=R*c1;
R4=R*d1;
R5=R*e1;
R6=R*f1;
disp('Points after Euclidian Transformation')
 [R1(1:2) R2(1:2) R3(1:2) R4(1:2) R5(1:2) R6(1:2)]
 figure (15)
axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title ('Euclidean TransformationResult')
line([R1(1),R2(1)],[R1(2),R2(2)]);
 line([R2(1),R3(1)],[R2(2),R3(2)]);
line([R3(1),R4(1)],[R3(2),R4(2)]);
line([R4(1),R5(1)],[R4(2),R5(2)]);
```

```
line([R5(1),R6(1)],[R5(2),R6(2)]);
line([R6(1),R1(1)],[R6(2),R1(2)]);
%similarity transform
disp('Similarity Transformation Matrix is')
E = [1 -1 1; 1 1 1; 0 0 1]
E1=E*a1;
E2=E*b1;
E3=E*c1;
E4=E*d1;
E5=E*e1;
E6=E*f1;
disp('Points after Similarity Translation')
[E1(1:2) E2(1:2) E3(1:2) E4(1:2) E5(1:2) E6(1:2)]
figure (16)
axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title('Similarity Transformation Result')
line([E1(1),E2(1)],[E1(2),E2(2)]);
line([E2(1),E3(1)],[E2(2),E3(2)]);
line([E3(1),E4(1)],[E3(2),E4(2)]);
line([E4(1),E5(1)],[E4(2),E5(2)]);
line([E5(1),E6(1)],[E5(2),E6(2)]);
line([E6(1),E1(1)],[E6(2),E1(2)]);
% AFFINE Transformation
disp('Affine Transformation Matrix is')
A=[1 -1 0 ; -2 0 1 ; 0 0 1]
A1=A*a1;
A2=A*b1;
A3=A*c1;
A4=A*d1;
A5=A*e1;
A6=A*f1;
disp('Points after Affine Transformation')
[A1(1:2) A2(1:2) A3(1:2) A4(1:2) A5(1:2) A6(1:2)]
figure (17)
axis([-5 5 -5 5])
xlabel('X Axis')
ylabel('Y Axis')
title('Affine Transformation Result')
line([A1(1),A2(1)],[A1(2),A2(2)]);
line([A2(1),A3(1)],[A2(2),A3(2)]);
line([A3(1),A4(1)],[A3(2),A4(2)]);
line([A4(1),A5(1)],[A4(2),A5(2)]);
line([A5(1),A6(1)],[A5(2),A6(2)]);
line([A6(1),A1(1)],[A6(2),A1(2)]);
%projective transformation
disp('Projective Transformation Matrix is')
P = [1 \ 2 \ 1; 1 \ 1 \ 1; 2 \ 2 \ 1]
P1=P*a1;
P2=P*b1;
P3=P*c1;
P4=P*d1;
P5=P*e1;
disp('Points after Projective Transformation')
[P1(1:2) P2(1:2) P3(1:2) P4(1:2) P5(1:2) P6(1:2)]
figure (18)
axis([-10 10 -10 10])
```

```
xlabel('X Axis')
ylabel('Y Axis')
title('Projective Result')
line([P1(1),P2(1)],[P1(2),P2(2)]);
line([P2(1),P3(1)],[P2(2),P3(2)]);
line([P3(1),P4(1)],[P3(2),P4(2)])
line([P4(1),P5(1)],[P4(2),P5(2)]);
line([P5(1),P6(1)],[P5(2),P6(2)]);
line([P6(1),P1(1)],[P6(2),P1(2)]);
```