

# ISYE6414 2019 Summer Midterm

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## Terms in this set (166)

The prediction intervals need to be corrected for simultaneous inference when multiple predictions are made jointly.

...

The estimated versus predicted regression line for a given  $x^*$

...

If the confidence interval for a regression coefficient contains the value zero, we interpret that the regression coefficient is definitely equal to zero.

False

The larger the coefficient of determination or R-squared, the higher the variability explained by the simple linear regression model.

True

The estimators of the error term variance and of the

True

The one-way ANOVA is a linear regression model with one qualitative predicting variable.

True

We can assess the assumption of constant-variance in multiple linear regression by plotting the standardized residuals against fitted values.

True

If one confidence interval in the pairwise comparison includes zero under ANOVA, we conclude that the two corresponding means are plausibly equal.

True

We do not need to assume normality of the response variable for making inference on the regression coefficients.

False

Assuming the model is a good fit, the residuals in simple linear regression have constant variance.

True

We cannot estimate a multiple linear regression model if the predicting variables are linearly independent.

False

If a predicting variable is categorical with 5 categories in a linear regression model without intercept, we will include 5 dummy variables in the model.

True

In the ANOVA, the number of degrees of freedom of the chi-squared distribution for the variance estimator is  $N-k-1$  where  $k$  is the number of groups.

False

The prediction of the response variable has higher uncertainty than the estimation of the mean response.

True

In linear regression, outliers do not impact the estimation of the regression coefficients.

False

Multicollinearity in multiple linear regression means that the columns in the design matrix are (nearly) linearly dependent.

True

The statistical inference for linear regression under normality relies on large size of sample data.

False

If the non-constant variance assumption does not hold in multiple linear regression, we apply a transformation to the predicting variables.

False

The only assumptions for a linear regression model are linearity, constant variance, and normality.

False

In the regression model, the variable of interest for study is the predicting variable.

False

The constant variance is diagnosed using the quantile-quantile normal plot.	False
$\beta_1$ is an unbiased estimator for $\beta_0$ .	False
The estimator $\sigma^2$ is a fixed variable.	False
The linear regression model with a qualitative predicting variable with $k$ levels/classes will have $k + 1$ parameters to estimate	True
Under the normality assumption, the estimator for $\beta_1$ is a linear combination of normally distributed random variables.	True
A negative value of $\beta_1$ is consistent with an inverse relationship between $x$ and $y$ .	True
In the simple linear regression model, we lose three degrees of freedom because of the estimation of the three model parameters $\beta_0, \beta_1, \sigma^2$ .	False
The regression coefficient is used to measure the linear dependence between two variables.	False
If the constant variance assumption in ANOVA does not hold, the inferences on the equality of the means	True

If one confidence interval in the pairwise comparison does not include zero, we conclude that the two means are plausibly equal.	False
The mean sum of square errors in ANOVA measures variability within groups.	True
Only the log-transformation of the response variable can be used when the normality assumption does not hold.	False
If one confidence interval in the pairwise comparison includes only positive values, we conclude that the difference in means is statistically significantly positive.	True
The number of degrees of freedom of the $\chi^2$ (chi-square) distribution for the variance estimator is $N - k + 1$ where $k$ is the number of samples.	False
For assessing the normality assumption of the ANOVA model, we can use the quantile-quantile normal plot and the histogram of the residuals.	True
The ANOVA is a linear regression model with one or more qualitative predicting variables.	True

The sampling distribution for the variance estimator in ANOVA is $\chi^2$ (chi-square) regardless of the assumptions of the data.	False
We assess the assumption of constant-variance by plotting the residuals against fitted values.	True
Prediction is the only objective of multiple linear regression.	False
The number of parameters to estimate in the case of a multiple linear regression model containing 5 predicting variables and no intercept is 6.	True
The equation to find the estimated variance of the error terms can be obtained by summing up the squared residuals and dividing that by $n - p - 1$ , where $n$ is the sample size and $p$ is the number of predictors.	True
The regression coefficient corresponding to one predictor is interpreted in a multiple regression in terms of the estimated expected change in the response variable when there is a change of one unit in the corresponding predicting variable.	False
In case of multiple linear regression, controlling variables are used to control for sample bias.	True

Observational studies allow us to make causal inference.	False
For a given predicting variable, the estimated coefficient of regression associated with it will likely be different in a model with other predicting variables or in the model with only the predicting variable alone.	True
For estimating confidence intervals for the regression coefficients, the sampling distribution used is a normal distribution.	False
The regression coefficients that are estimated serve as unbiased estimators.	True
For testing if a regression coefficient is zero, the normal test can be used.	False
Studying the relationship between a single response variable and more than one predicting quantitative and/or qualitative variable is termed as Multiple linear regression.	True
Before making statistical inference on regression coefficients, estimation of the variance of the error terms is necessary.	True

Partial F-Test can also be defined as the hypothesis test for the scenario where a subset of regression coefficients are all equal to zero.	True
The causation of a predicting variable to the response variable can be captured using Multiple linear regression, conditional of other predicting variables in the model.	False
For a linearly dependent set of predictor variables, we should not estimate a multiple linear regression model.	True
An example of a multiple regression model is Analysis of Variance (ANOVA).	True
Given a categorial predictor with 4 categories in a linear regression model with intercept, 4 dummy variables need to be included in the model.	False
Assuming that the data are normally distributed, under the simple linear model, the estimated variance has the following sampling distribution:	Chi-square with $n-2$ degrees of freedom
The fitted values are defined as:	The regression line with parameters replaced with the estimated regression coefficients.
The estimators of the linear regression model are	Minimizing the sum of squared differences between observed and expected values

The estimators for the regression coefficients are:	Unbiased regardless of the distribution of the data.
The assumption of normality:	It is needed for the sampling distribution of the estimators of the regression coefficients and hence for inference.
The estimated versus predicted regression line for a given $x^*$ :	Have the same expectation
The variability in the prediction comes from:	The variability due to a new measurement and due to estimation.
We detect departure from the assumption of constant variance	When the residuals vs fitted values are larger in the ends but smaller in the middle.
The pooled variance estimator is:	The sample variance estimator assuming equal variances.
The total sum of squares divided by N-1 is	The sample variance estimator assuming equal means and equal variances
The mean squared errors (MSE) measures:	The within-treatment variability.
The objective of the residual analysis is	To evaluate departures from the model assumptions
The objective of the pairwise comparison is	To identify the statistically significantly different means.
The objective of multiple linear regression is	<ol style="list-style-type: none"> <li>1. To predict future new responses</li> <li>2. To model the association of explanatory variables to a response variable accounting for controlling factors.</li> <li>3. To test hypothesis using statistical inference on the model</li> </ol>

A multiple linear regression model with p predicting variables but no intercept has p model parameters.	False
The interpretation of the regression coefficients is the same whether or not interaction terms are included in the model.	False
Multiple linear regression is a general model encompassing both ANOVA and simple linear regression.	True
The regression coefficients can be estimated only if the predicting variables are not linearly dependent.	True
The estimated regression coefficient $\hat{\beta}_i$ is interpreted as the change in the response variable associated with one unit of change in the i-th predicting variable .	False
The estimated regression coefficients will be the same under marginal and conditional model, only their interpretation is not.	False
Causality is the same as association in interpreting the relationship between the response and the predicting variables.	False

The estimated variance of the error term has a  $\chi^2$  distribution regardless of the distribution assumption of the error terms.

False

The number of degrees of freedom for the  $\chi^2$  distribution of the estimated variance is  $n-p-1$  for a model without intercept.

False

The sampling distribution of the mean squared error is different of that of the estimated variance.

False

The sampling distribution of the estimated regression coefficients is centered at the true regression parameters.

True

The sampling distribution of the estimated regression coefficients is the t-distribution assuming that the variance of the error term is unknown and replaced by its estimate.

True

The sampling distribution of the estimated regression coefficients is dependent on the design matrix.

True

We can test for a subset of regression coefficients using the F statistic test of the overall regression.

False

We can test for a subset of regression coefficients only if we are interested whether additional explanatory variables should be considered in addition to the controlling variables.

False

We can test for a subset of regression coefficients to evaluate whether all regression coefficients corresponding to the predicting variables excluded from the reduced model are statistically significant.

False

The prediction intervals need to be corrected for simultaneous inference when multiple predictions are made jointly.

True

The prediction intervals are centered at the predicted value.

True

The sampling distribution of the prediction of a new response is a t-distribution.

True

In evaluating a multiple linear model the F test is used to evaluate the overall regression.

True

In evaluating a multiple linear model the coefficient of variation is interpreted as the percentage of variability in the response variable explained by the

True

In evaluating a multiple linear model residual analysis is used for goodness of fit assessment.

True

In the presence of near multicollinearity, the coefficient of variation decreases.

False

In the presence of near multicollinearity, the regression coefficients will tend to be identified as statistically significant even if they are not.

False

If the linearity assumption with respect to one or more predictors does not hold, then we use transformations of the corresponding predictors to improve on this assumption.

True

If the normality assumption does not hold, we transform the response variable, commonly using the Box-Cox transformation.

True

If the constant variance assumption does not hold, we transform the response variable.

True

The residuals have constant variance for the multiple linear regression model.

False

The residuals vs fitted can be used to assess the assumption of independence.

False

The residuals have a t-distribution distribution if the error term is assumed to have a normal distribution.	False
Independence assumption can be assessed using the residuals vs fitted values.	False
Independence assumption can be assessed using the normal probability plot.	False
Residual analysis can only be used to assess uncorrelated errors.	True
If a departure from normality is detected, we transform the predicting variable to improve upon the normality assumption.	False
If a departure from the independence assumption is detected, we transform the response variable to improve upon this assumption.	False
The Box-Cox transformation is commonly used to improve upon the linearity assumption.	False
In evaluating a simple linear model there is a direct relationship between coefficient of variation and the correlation between the predicting and response variables.	True

In evaluating a simple linear model the coefficient of variation is interpreted as the percentage of variability in the response variable explained by the model.

True

In evaluating a simple linear model residual analysis is used for goodness of fit assessment.

True

The means of the k populations is a model parameter in ANOVA.

False

The sample means of the k populations is a model parameter in ANOVA.

False

The sample means of the k samples is a model parameter in ANOVA.

False

If we reject the test of equal means, we conclude that all treatment means are not equal.

False

If we do not reject the test of equal means, we conclude that means are definitely all equal

False

If we reject the test of equal means, we conclude that some treatment means are not equal.

True

Residual analysis can only be used to assess

True

The variability in the prediction comes from	The variability due to a new measurement and due to estimation.
The estimated versus predicted regression line for a given $x^*$	Have the same expectation
The fitted values are defined as	The regression line with parameters replaced with the estimated regression coefficients.
In evaluating a multiple linear model, the F test is used to evaluate the overall regression.	True
In evaluating a multiple linear model, the coefficient of variation is interpreted as the percentage of variability in the response variable explained by the model.	True
In evaluating a multiple linear model, Residual analysis is used for goodness of fit assessment.	True
In the presence of near multicollinearity, the coefficient of variation decreases.	False
In the presence of near multicollinearity, the regression coefficients will tend to be identified as statistically significant even if they are not.	False
In the presence of near multicollinearity, the	False

When do we use transformations?	If the linearity assumption with respect to one or more predictors does not hold, then we use transformations of the corresponding predictors to improve on this assumption. If the normality assumption does not hold, we transform the response variable, commonly using the Box-Cox transformation. If the constant variance assumption does not hold, we transform the response variable.
The sampling distribution of the estimated regression coefficients is Centered at the true regression parameters.	True
The sampling distribution of the estimated regression coefficients is the t-distribution assuming that the variance of the error term is unknown and replaced by its estimate.	True
The estimators for the regression coefficients are Unbiased regardless of the distribution of the data. correct	True
Multiple linear regression is a general model encompassing both ANOVA and simple linear regression. correct	True
The regression coefficients can be estimated only if the predicting variables are not linearly dependent.	True

1. The means of the k populations  
2. The sample means of the k populations  
3. The sample means of the k samples  
are NOT all the model parameters in ANOVA

True

The only assumptions for a simple linear regression model are linearity, constant variance, and normality.

False

In a simple linear regression model, the variable of interest is the response variable.

True

The constant variance assumption is diagnosed by plotting the predicting variable vs. the response variable.

False

LaTeX:  $\hat{\beta}_1$  is an unbiased estimator for  $\beta_1$ :  
 $\hat{\beta}_0$  is an unbiased estimator for  $\beta_0$ .

False

The estimator  $\hat{\sigma}^2$  is a fixed variable.

False

The ANOVA model with a qualitative predicting variable with  $k$  levels/classes will have  $k+1$  parameters to estimate.

True

Under the normality assumption, the estimator for  $\hat{\beta}_1$  is a linear combination of normally distributed random variables.

True

A negative value of  $\beta_1$  is consistent with an inverse relationship between  $x$  and  $y$ .

True

In the simple linear regression model, we lose three degrees of freedom because of the estimation of the three model parameters  $\beta_0, \beta_1, \sigma^2$ .

False

If the constant variance assumption in ANOVA does not hold, the inference on the equality of the means will not be reliable.

True

Only the log-transformation of the response variable should be used when the normality assumption does not hold.

False

If one confidence interval in the pairwise comparison includes only positive values, we conclude that the difference in means is positive, and statistically significant.

True

The number of degrees of freedom of the  $\chi^2$  distribution for the pooled variance estimator is  $N-k+1$  where  $k$  is the number of samples.

False

The sampling distribution for the variance estimator in ANOVA is LaTeX:  $\chi^2$  (chi-square) with  $N - k$  degrees of freedom.

False

In simple linear regression, we can diagnose the assumption of constant-variance by plotting the residuals against fitted values.

True

If response variable Y has a quadratic relationship with a predictor variable X, it is possible to model the relationship using multiple linear regression.

True

The LaTeX: R<sup>2</sup> value represents the percentage of variability in the response that can be explained by the linear regression on the predictors. Models with higher LaTeX: R<sup>2</sup> are always preferred over models with lower LaTeX: R<sup>2</sup>.

True

For the model LaTeX:

$y = \beta_0 + \beta_1 x_1 + \dots + \beta_p x_p + \epsilon$ , where LaTeX:  $\epsilon \sim N(0, \sigma^2)$ , there are  $p+1$  parameters to be estimated

False

The F-test can be used to evaluate the relationship between two qualitative variables.

False

The Partial F-Test can test whether a subset of

True

In multiple linear regression, controlling variables are used to control for sample bias.

True

In a multiple regression model with 7 predicting variables, the sampling distribution of the estimated variance of the error terms is a chi-squared distribution with  $n-8$  degrees of freedom.

True

There are four assumptions needed for estimation with multiple linear regression: mean zero, constant variance, independence, and normality.

False

Let LaTeX:  $\hat{Y}$  \* be the predicted response at LaTeX:  $\hat{x}$  \*. The variance of LaTeX:  $\hat{Y}$  \* given LaTeX:  $\hat{x}$  \* depends on both the value of LaTeX:  $\hat{x}$  \* and the design matrix.

True

Suppose  $x_1$  was not found to be significant in the model specified with  $lm(y \sim x_1 + x_2 + x_3)$ . Then  $x_1$  will also not be significant in the model  $lm(y \sim x_1 + x_2)$ .

False

When estimating confidence values for the mean response for all instances of the predicting variables, we should use a critical point based on the F-distribution to correct for the simultaneous inference.

True

In a multiple linear regression model with quantitative predictors, the coefficient corresponding to one predictor is interpreted as the estimated expected change in the response variable when there is a one unit change in that predictor.

False

It is possible to produce a model where the overall F-statistic is significant but all the regression coefficients have insignificant t-statistics.

True

Analysis of Variance (ANOVA) is an example of a multiple regression model.

True

For a multiple regression model, both the true errors  $\epsilon$  and the estimated residuals  $\hat{\epsilon}$  have a constant mean and a constant variance.

False

If the p-value of the overall F-test is close to 0, we can conclude all the predicting variable coefficients are significantly nonzero.

False

The causation effect of a predicting variable to the response variable can be captured using multiple linear regression, conditional of other predicting variables in the model.

False

A high Cook's distance for a particular observation suggests that the observation could be an influential point.

True

A no-intercept model with one qualitative predicting variable with 3 levels will use 3 dummy variables.

True