Here's a variational characterization of the absolute value of a number.

$$|x| = \min_{y>0} \frac{1}{2}\big(x^2/y + y\big)$$