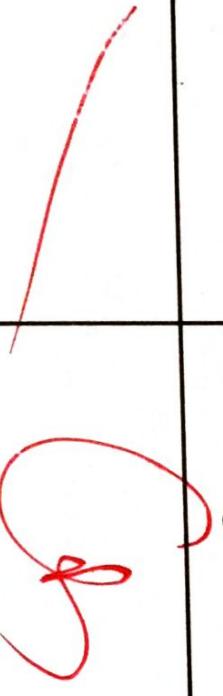
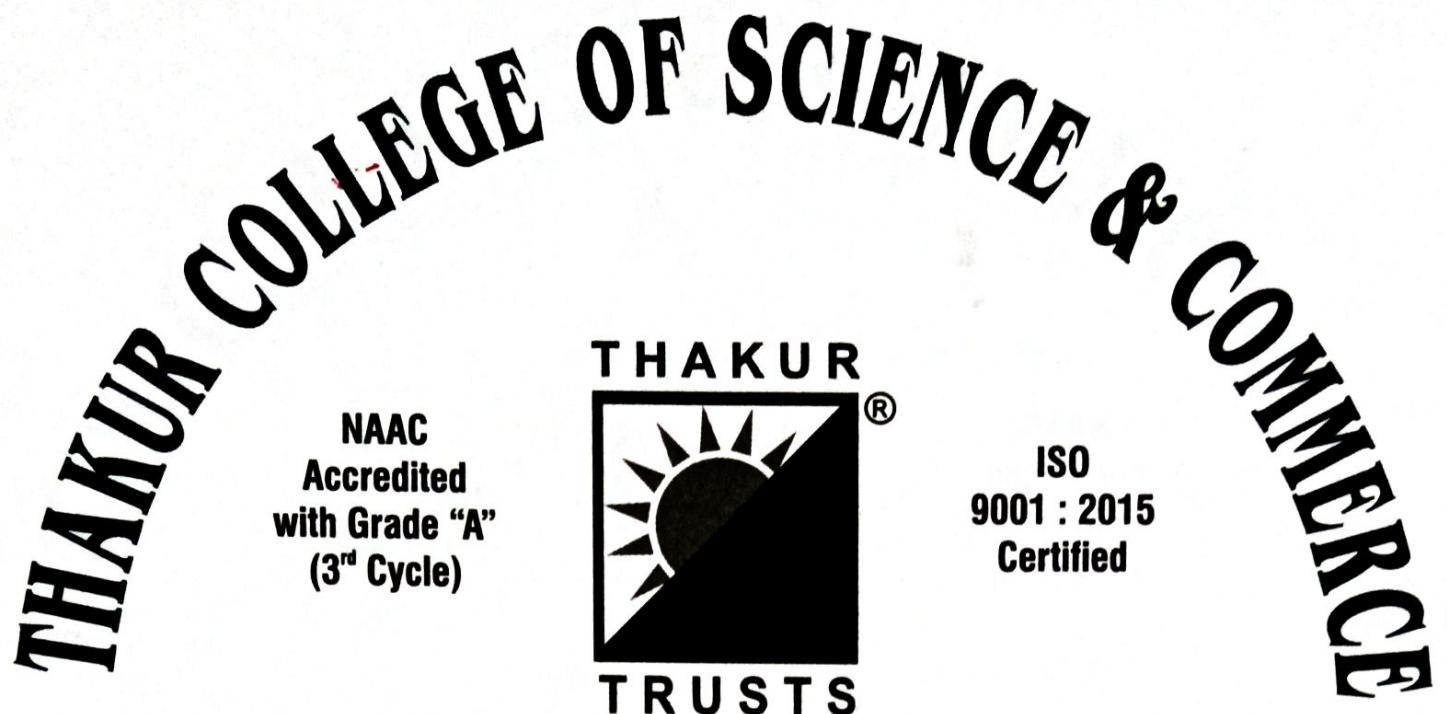


# PERFORMANCE

Term	Remarks	Staff Member's Signature
I		
II	Complete	A.M-



Degree College  
**Computer Journal**  
**CERTIFICATE**

SEMESTER II UID No. \_\_\_\_\_

Class F-X CS Roll No. 1840 Year 1840 2019-2020

This is to certify that the work entered in this journal  
is the work of Mst. / Ms. Pushpraj ojha

who has worked for the year 2019-2020 in the Computer  
Laboratory.

A. Venkatesh  
Teacher In-Charge

Head of Department

Date : 4.3.20

Examiner

**★ ★ INDEX ★ ★**

Sem - 2

27/11/19

Practical No: 1

029

27/11/19

## Basic of R Software

- 1) R is a software for Data analysis & Statistical computing.
- 2) this software is used for effective Data handling & output Storage is possible.
- 3) It is capable of Graphical Display.
- 4) It is a free software

```
> 2^2 + sqrt(25) + 35  
[1] 44  
> 2*5*3 + 62/5 + sqrt(49)  
[1] 49.4  
> sqrt(76 + (4*2) + (9/5))  
[1] 9.262829  
> 43 + abs(-10) + 7^2 + 3^9  
[1] 129
```

```
> x=20  
> y=30  
> x+y  
[1] 50  
> x^2 + y^2  
[1] 1300  
> sqrt(y^3 - x^3)  
[1] 137.8405
```

\* find the Sum, Product, maximum, minimum of the 030 values 5, 8, 6, 7, 9, 10, 15, 5

```
> abs(x-y)
[1] 10

> c(2,3,4,5)^2
[1] 4 9 16 25

> c(4,5,6,8)^*3
[1] 12 15 18 24

> c(2,3,5,7)*c(-2,-3,-5,-4)
[1] -4 -9 -25 -28

> c(2,3,5,7)*c(8,9)
[1] 16 27 40 63

> c(2,3,5,7)*c(1,2,3)
[1] 2 6 15^7 warning message
in c(2,3,7)*c(1,2,3) longer object length is not a multiple of shorter object length

> c(1,2,3,4,5,6,7,8)
[1] 1 2 3 4 5 6 7 8
```

# Matrix:

```
> f<-matrix(nrow=4,ncol=2,Data=c(1,2,3,4,5,6,7,8))
> f
```

[1,]	1
[2,]	2
[3,]	3
[4,]	4

$$\begin{aligned} & * \quad X = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}, Y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix} \end{aligned}$$

find:  $x+y, x*y, 2x+3y$

```
> x<-matrix(nrow=3,ncol=3,data=c(2,-2,1,4,8,6,10,-11,-12))
> y<-matrix(nrow=3,ncol=3,data=c(1,2,3,4,5,6,7,8,9))
```

```
> x+y
[1,] [,1] [,2] [,3]
[1] 3 8 17
[2] 6 13 -3
```

080  
 $x * y$

```
[1] 2 16 70
[2] -4 40 -88
[3] 30 36 108
```

>  $2^x + 3^y$

```
[1,] 8 20 44
[2,] -2 34 -17
[3,] 36 30 64
```

# Table:

>  $\omega = c(2, 4, 6, 1, 3, 5, 7, 18, 16, 14, 17, 19, 3, 3, 2, 5, 0, 15, 9, 14, 18, 10, 12)$

> length( $\omega$ )  
[1] 23  
> a = table( $\omega$ )  
> transform(a)

b	freq
[0, 5]	8
[5, 10]	5
[10, 15]	4
[15, 20]	6

↑  
✓

1 ω freq

1	0	1
2	1	1
3	2	2
4	3	3
5	4	1
6	5	2
7	6	0
8	7	0
9	8	0
10	9	0
11	10	0
12	11	0
13	12	-1
14	13	0
15	14	0
16	15	0
17	16	0
18	17	0
19	18	-1

> breaks = seq(0, 25, 5)  
> b = cut(x ~ ω, breaks, right = FALSE)  
> c = table(b)  
> transform(c)

PRACTICAL NO: 2

$$\begin{aligned} &= (4-2) - (2-0.5) \\ &= 2 - 1.5 \\ &= 0.5 \end{aligned}$$

+1

Q.1 Can the following be P.d.f. :-

i)  $f(x) = \begin{cases} 2-x & ; 1 \leq x \leq 2 \\ 0 & ; \text{otherwise} \end{cases}$

ii)  $f(x) = \begin{cases} 3x^2 & ; 0 < x < 1 \\ 0 & ; \text{otherwise} \end{cases}$

$\therefore$  This is not a P.d.f

Solutions:-

iii)  $f(x) = \begin{cases} \frac{3x}{2}(1-\frac{x}{2}) & ; 0 \leq x \leq 2 \\ 0 & ; \text{otherwise} \end{cases}$

$\therefore$  To prove  $f(x) = \begin{cases} 2-x & ; 1 \leq x \leq 2 \\ 0 & ; \text{otherwise} \end{cases}$

$$\begin{aligned} &\int f(x) dx \\ &= \int_{0}^{2} (2-x) dx \\ &= 3 \int_{0}^{2} x^2 dx \\ &= 3 \left[ \frac{x^3}{3} \right]_0^2 \\ &= 3 \left( \frac{1^3}{3} - \frac{0^3}{3} \right) \\ &= \frac{3}{3} \\ &= 1 \end{aligned}$$

$\therefore$  This is a P.d.f

iv)

$$f(x) = \begin{cases} \frac{3x}{2}(1-\frac{x}{2}) & ; 0 \leq x \leq 2 \\ 0 & ; \text{otherwise} \end{cases}$$

$$\int 2dx - \int x dx$$

$$= 2x \Big|_0^2 - \frac{x^2}{2} \Big|_0^2$$

$$= \int_{0}^2 \frac{3x}{2}(1-\frac{x}{2}) dx$$

Can the following be P.m.f

i)

$x$	1	2	3	4	5
$P(x)$	0.1	0.3	-0.1	0.5	0.1

ii)

$x$	10	20	30	40	50
$P(x)$	0.2	0.3	0.3	0.2	0.2

iii)

$x$	1	2	3	4	5
$P(x)$	0.1	0.3	0.2	0.1	0.1

Solutions:

1) Since One Probability is negative  
Hence it is not a P.m.f

2) Since  $P(x) \geq 0$   $\forall x$  ✓  
and  $\sum P(x) = 1$

∴ It is a P.m.f

∴ This is P.d.f

$$\begin{aligned}
 &= \int_0^2 \left[ \frac{3x}{2} - \frac{3x^2}{4} \right] dx \\
 &= \int_0^2 \frac{3x}{2} dx - \int_0^2 \frac{3x^2}{4} dx \\
 &= \frac{3}{2} \int_0^2 x dx - \frac{3}{4} \int_0^2 x^2 dx \\
 &= \frac{3}{2} \left[ \frac{x^2}{2} \right]_0^2 - \frac{3}{4} \left[ \frac{x^3}{3} \right]_0^2 \\
 &= \frac{3}{2} \left[ \frac{4}{2} - 0 \right] - \frac{3}{4} \left[ \frac{8}{3} - 0 \right] \\
 &= \left( \frac{3}{2} \times 2 \right) - \frac{3}{4} \left( \frac{8}{3} \right) \\
 &= \frac{3}{2} \left[ \frac{4}{2} - 0 \right] - \frac{3}{4} \left[ \frac{8}{3} - 0 \right] \\
 &= \left( \frac{3}{2} \times 2 \right) - \frac{3}{4} \left( \frac{8}{3} \right) \\
 &= 3 - 2 \\
 &= 1
 \end{aligned}$$

$$\begin{aligned}
 &\text{1)} \quad x = \{0, 1, 2, 3, 4, 5\} \\
 &\quad P_{prob} = \{0.1, 0.3, 0.2, 0.2, 0.1, 0.1\} \\
 &\quad \sum P_{prob} = 1
 \end{aligned}$$

$$\therefore P(2 \leq x < 4) = 0.4$$

3)  
 a)  $c(10, 20, 30, 40, 50)$   
 $\Rightarrow P_{\text{Prob1}} = c(0.2, 0.3, 0.3, 0.2, 0.2)$   
 $\Rightarrow \text{Sum } (P_{\text{Prob1}})$

[ii] 1.2  
 $\nabla$

Since  $\sum P(\text{Prob1}) > 1$   
 $\therefore g_2$  is not a p.m.f

$x$	0	1	2	3	4	5	6
$P(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

find:  
 $P(x \leq 2)$   
 $P(2 \leq x < 4)$

$P(\text{at least } 4)$   
 $P(3 < x < 6)$

Solutions:-

$x$	10	12	14	16	18
$P(x)$	0.2	0.1	0.1	0.2	0.1

Q.4

$x$	0	1	2	3	4	5	6
$P(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\therefore P(3 < x < 6) = 0.3$$

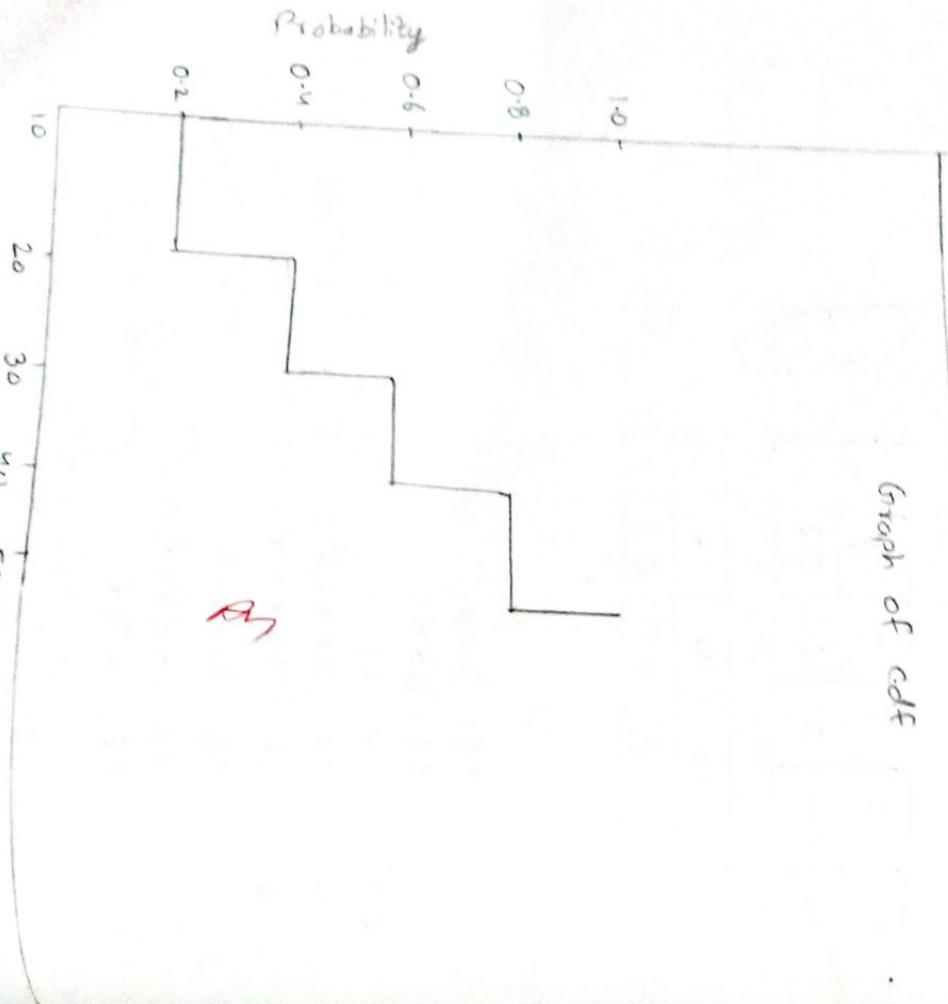
$$\begin{aligned} P(\text{at least } 4) &= P(4) + P(5) + P(6) \\ &\quad \nabla \\ &= 0.1 + 0.2 + 0.1 \\ &\quad \therefore P(\text{at least } 4) = 0.4 \\ P(3 < x < 6) &= P(4) + P(5) \\ &\quad \nabla \\ &= 0.1 + 0.2 \\ &= 0.3 \end{aligned}$$

$$\begin{aligned} P(2 \leq x < 4) &= P(2) + P(3) \\ &\quad \nabla \\ &= 0.2 + 0.2 \\ &= 0.4 \end{aligned}$$

$$\therefore P(x \leq 2) = 0.4$$

### Practical 3

2)  $f(x) = \begin{cases} 0 & \text{if } x < 0 \\ 0.2 & \text{if } 0 \leq x < 10 \\ 0.7 & \text{if } 10 \leq x < 12 \\ 0.0 & \text{if } 12 \leq x < 16 \\ 0.9 & \text{if } 16 \leq x < 18 \\ 1 & \text{if } 18 \leq x < 20 \end{cases}$



Graph of cdf

$F(X)$	10	20	30	40	50
$P(x)$	0.15	0.05	0.3	0.2	0.1
$> X = r(10, 24, 30, 40, 50)$					
$> prop = c(0.15, 0.25, 0.3, 0.2, 0.1)$					
$> Cumsum$					

[1] 0.15 0.25 0.30 0.20 0.10  
 $> Cumsum(prop)$

[1] 0.15 0.25 0.30 0.20 0.10

$> plot(x, Cumsum(prop), xlab = "values", ylab = "Probability", main = "graph of cdf", s)$

- Q2 Suppose there are 12 mcs in a test. Each question has 5 options. If only one of them is correct, find the probability of having
- i) 5 correct answer
  - ii) Almost 4 correct answer

Solution:

It is given that  
 $n = 12, P = \frac{1}{5}, q = \frac{4}{5}$

X = Total number of correct answers  
 $X \sim B(n, p)$

$$\geq n=12$$

$$\geq p=1/5$$

$$\geq q=4/5$$

$$\geq x=5$$

$\geq \text{a} = \text{dbinom}(5, 12, 1/5)$

$$\geq a$$

$$\boxed{\text{[1]} \quad 0.05315022}$$

$\geq b = \text{pbinom}(4, 12, 1/5)$

$$\boxed{\text{[1]} \quad 0.9274445}$$

Q) find the C.d.f & draw the graph

x	0	1	2	3	4	5	6
p(x)	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$\geq x=c(0, 1, 2, 3, 4, 5, 6)$   
 $\geq \text{prob}=c(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)$

$\geq \text{CumSum}(\text{prob})$   
 $\boxed{\text{[1]} \quad 0.1 \quad 0.2 \quad 0.4 \quad 0.6 \quad 0.7 \quad 0.9 \quad 1.0}$   
 $\geq \text{plot}(x, \text{CumSum}(\text{prob}), \text{xlab}=\text{"values"}, \text{ylab}=\text{"Probability"}, \text{main}=\text{"Graph of cdf", "5"})$

Graph of cdf

Solution:-

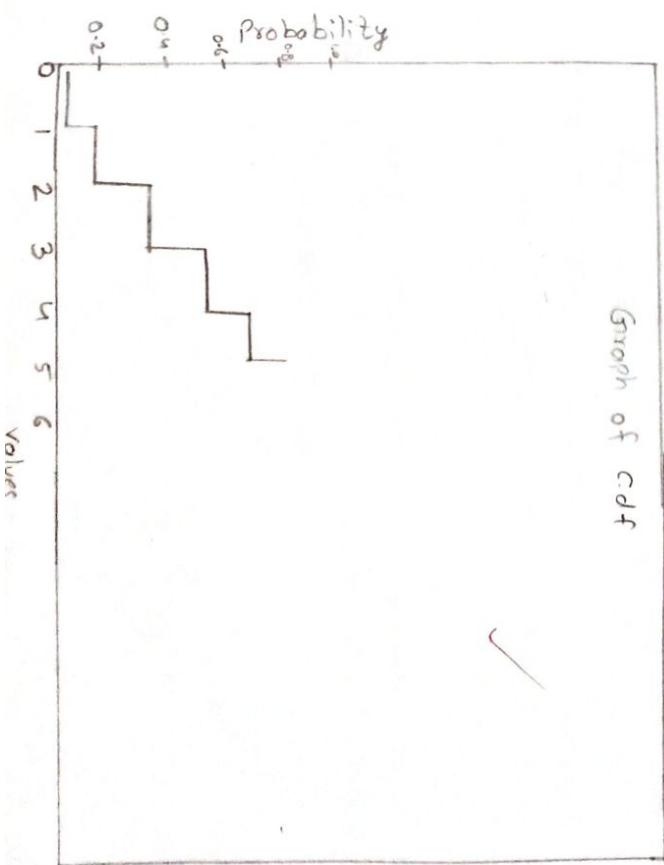
$$n=10$$

$$p=0.9$$

$$q=0.1$$

X = Total no of members attended  
 $\sim \text{B}(n, p)$

$$\begin{aligned} &\geq n=10 \\ &\geq p=0.9 \\ &\geq q=0.1 \end{aligned}$$



✓

11.12.19

### Binomial Distribution

i) find the complete b.d when  $n=5$ ,  $P=0.1$

ii) find Probability of exactly 10 success in 100 trial with  $P=0.1$

Q3 X follows B.D with  $n=12$ ,  $P=0.25$  find

- i)  $P(x=9)$
- ii)  $P(x \leq 5)$
- iii)  $P(x > 7)$
- iv)  $P(5 < x < 7)$

~~Q4~~ The probability of Salesman make a sale to customer is 0.15. Find the Probability:

- i) No Sale for 10 customers
- ii) More than 3 Sale in 20 customers

Q5 A student write 5 mcq each question has 4 options out of which 1 is correct. Calculate the Probability for at least 3 correct answers.

Note:-

$$\begin{aligned} \text{i)} & n = 12 \\ & p = 0.25 \\ & x = 5 \\ & \rho \text{binom}(5, 12, 0.25) \\ \text{ii)} & [1] 0.9455978 \end{aligned}$$

$$\left\{ \begin{array}{l} \text{Note:-} \\ \text{i)} \rho(x > 7) = 1 - \rho(x \leq 7) \\ = 1 - \rho \text{binom}(7, 12, 0.25) \\ \text{ii)} \rho(x \geq 7) = 1 - \rho(x \leq 6) \end{array} \right.$$

- i) To find the value of  $x$  for which the probability is  $\rho$ , the command is  
 $\rho(x = 0) = \text{dbinom}(x, n, p)$   
 ii)  $\rho(X \leq x) = \rho \text{binom}(x, n, p)$   
 iii)  $\rho(X > x) = 1 - \rho \text{binom}(x, n, p)$

Solutions:-

$$\begin{aligned} \text{i)} & n = 12 \\ & p = 0.25 \\ & x > 7 \\ & \cancel{\rho \text{binom}(6, 12, 0.25)} \\ & [1] 0.0027815 \end{aligned}$$

ii)  $\rho(x = 0)$

$$\begin{aligned} > n = 5, \quad p = 0.1 \\ > \text{dbinom}(0:5, 5, 0.1) \\ [1] 0.59069 \quad 0.32805 \quad 0.7290 \quad 0.00810 \quad 0.00045 \quad 0.00001 \end{aligned}$$

iii)  $\rho(x = 10)$

iv)  $\rho(x = 10)$

$$\begin{aligned} > \text{dbinom}(10, 1000, 0.1) \\ [1] 0.1318653 \end{aligned}$$

v)  $\rho(x = 12)$

vi)  $\rho(x = 12)$

vii)  $\rho(x = 12)$

viii)  $\rho(x = 12)$

$$\begin{aligned} > \text{dbinom}(5, 12, 0.25) \\ [1] 0.1032414 \end{aligned}$$

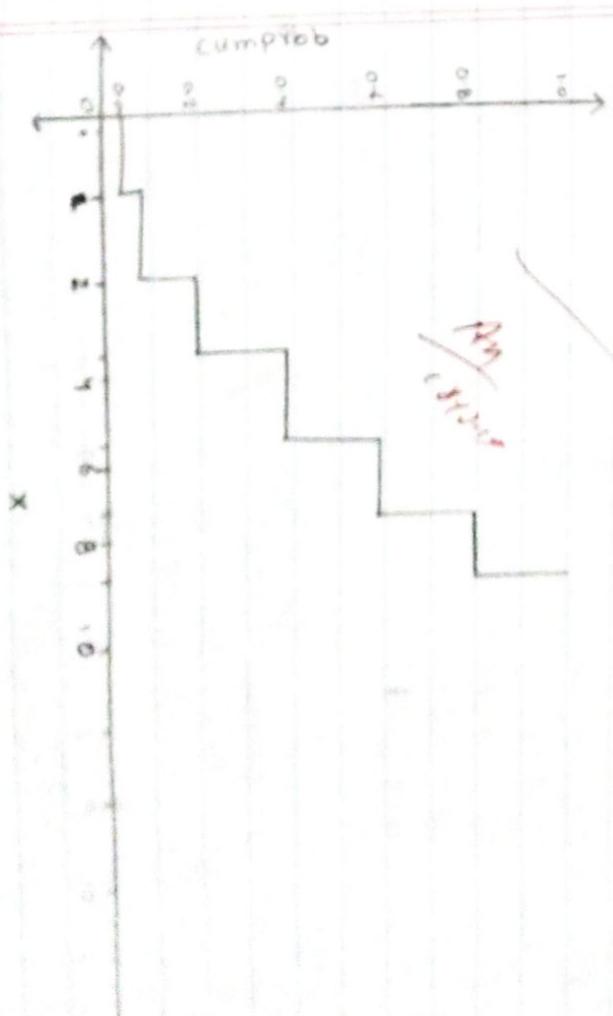
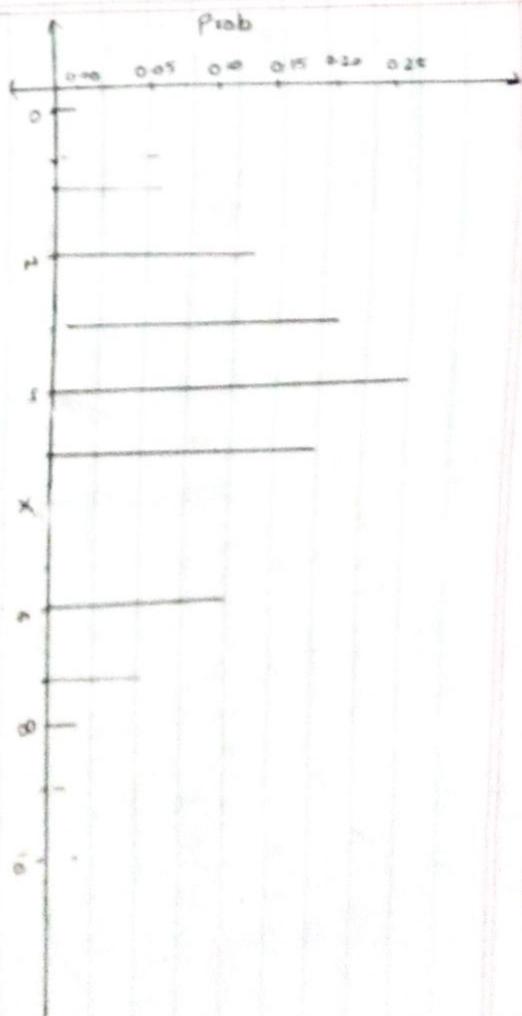
x follows binomial distribution with n=10, p=0.4

Plot the graph of Pmk vs CDF

Solution :-

```
> n=10
> p=0.4
> x=0:n
> prob=dbinom(x,n,p)
> Cumprob=pbinom(x,n,p)
> d=data.frame(c(x,values="x","Probability":prob))
> print(d)
```

x-values	Probability
0	0.00060468176
1	0.000307840
2	0.01209323520
3	0.04808224560
4	0.12065812480
5	0.20065812480
6	0.11147673480
7	0.0424673280
8	0.010468320
9	0.0015728640
10	0.0001048576



```
> plot(x,Cumprob,"s")
```

# Ex 5 Practical: 5

040

Ques:- Normal Distribution

- ①  $P[X = x] = \text{dnorm}(x, \mu, \sigma)$
  - ②  $P[X \leq x] = \text{pnorm}(x, \mu, \sigma)$
  - ③  $P[X > x] = 1 - \text{pnorm}(x, \mu, \sigma)$
  - ④  $P[x_1 < x < x_2] = \text{pnorm}(x_2, \mu, \sigma) - \text{pnorm}(x_1, \mu, \sigma)$
  - ⑤ To find the value of  $K$  so that  $P[X \leq K] = p$ ;
- To generate  $n$  random numbers  $\text{rnorm}[n, \mu, \sigma]$

Ques:-

$$X \sim N(\mu=50, \sigma^2=100)$$

find.

i)  $P(X \leq 40)$

ii)  $P(X > 55)$

iii)  $P(42 \leq X \leq 60)$

iv)  $P(X \leq K) = 0.7$ ;  $K = ?$

Sol:-

- ①  $a = \text{pnorm}(40, 50, 10)$
- ②  $\text{cat}("P(X <= K) = 0.7, K = ", d)$
- ③  $P(X <= K) = 0.7$ ,  $K = 55.2440$

Ans:-

- ①  $b = 1 - \text{pnorm}(55, 50, 10)$
- ②  $\text{cat}("P(X <= 40) = ", a)$
- ③  $P(X <= 40) = 0.1586553$

Ans:-

- ①  $d = \text{pnorm}(55, 50, 10)$
- ②  $\text{cat}("P(X > 55) = ", b)$
- ③  $P(X > 55) = 0.3085375$

Ans:-

- ①  $e = \text{pnorm}(105, 100, 6)$
- ②  $\text{cat}("P(X \leq K) = 0.4, K = ", c)$
- ③  $P(95 \leq X \leq 105) = 0.953432$

Ans:-

- ①  $f = \text{pnorm}(105, 100, 6) - \text{pnorm}(95, 100, 6)$
- ②  $\text{cat}("P(95 \leq X \leq 105) = ", d)$
- ③  $P(95 \leq X \leq 105) = 0.953432$

Ans:-

- ①  $g = \text{pnorm}(95, 100, 6)$
- ②  $\text{cat}("P(X \leq K) = 0.4, K = ", e)$
- ③  $P(X \leq K) = 0.4$ ,  $K = 98.47992$

Ques:-

- ①  $d = \text{pnorm}(0.7, 50, 10)$
- ②  $\text{cat}("P(42 \leq X \leq 60) = ", c)$
- ③  $P(42 \leq X \leq 60) = 0.6294893$

Ques:-

- ①  $d = \text{pnorm}(0.7, 50, 10)$
- ②  $\text{cat}("P(X <= K) = 0.7, K = ", d)$
- ③  $P(X <= K) = 0.7$ ,  $K = 55.2440$

Ques:-

- ①  $d = \text{pnorm}(0.7, 50, 10)$
- ②  $\text{cat}("P(X \leq 110) = ", i)$
- ③  $P(X \leq 110) = 0.7$
- ④  $\text{cat}("P(X \geq 95) = ", j)$
- ⑤  $P(X \geq 95) = 1 - 0.7 = 0.3$
- ⑥  $\text{cat}("P(95 \leq X \leq 105) = ", k)$
- ⑦  $P(95 \leq X \leq 105) = 0.2023284$

Ques:-

- ①  $d = \text{pnorm}(115, 100, 6)$
- ②  $\text{cat}("P(X \leq 95) = ", b)$
- ③  $P(X \leq 95) = 0.2023284$

Ques:-

- ①  $d = 1 - \text{pnorm}(115, 100, 6)$
- ②  $\text{cat}("P(X > 115) = ", c)$
- ③  $P(X > 115) = 0.005209665$

Ques:-

- ①  $d = \text{pnorm}(105, 100, 6) - \text{pnorm}(95, 100, 6)$
- ②  $\text{cat}("P(95 \leq X \leq 105) = ", d)$
- ③  $P(95 \leq X \leq 105) = 0.953432$

Ques:-

- ①  $d = \text{pnorm}(95, 100, 6)$
- ②  $\text{cat}("P(X \leq K) = 0.4, K = ", e)$
- ③  $P(X \leq K) = 0.4$ ,  $K = 98.47992$

Q40 From normal Distribution calculate Sample mean.

- a) Generate 10 random numbers with mean = 60 &  $S_d = 5$  also calculate variance, median & standard Deviation

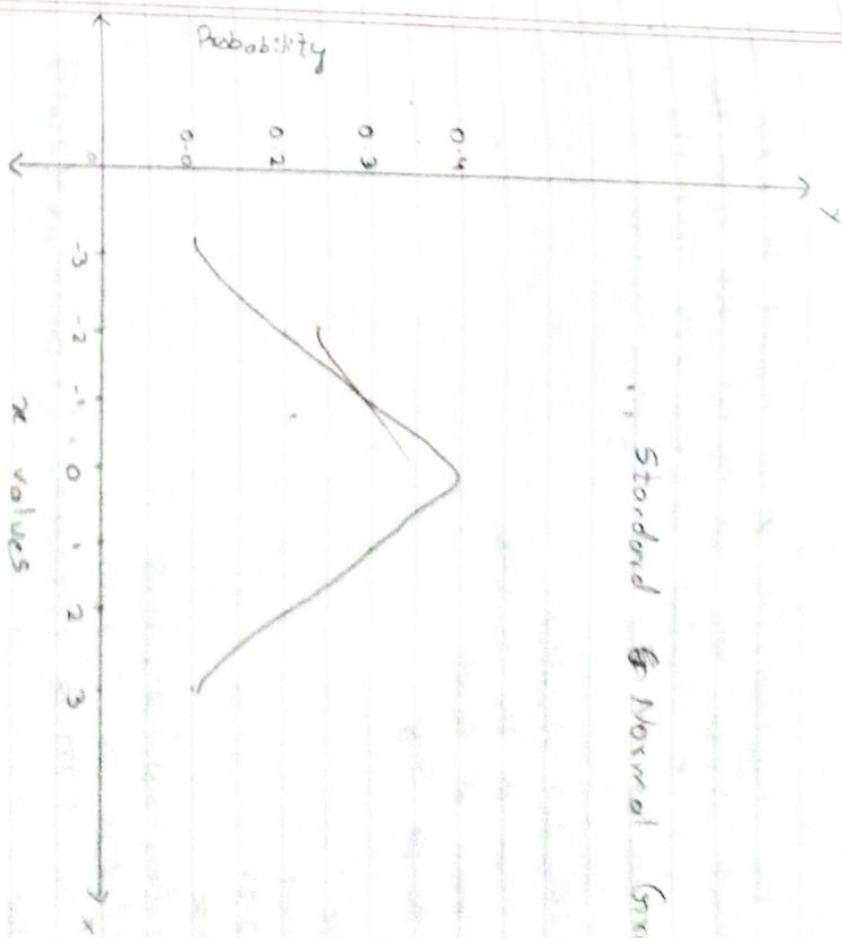
Solution:

```
> x = rnorm(10, 60, 5)
> m = mean(x)
> s_m
[1] 60.01123
> me = median(x)
> me
[1] 59.86623
> n = 10
> Variance = (n - 1) * var(x)/n
> Variance
[1] 44.45974
> SD = sqrt(Variance)
> SD
[1] 6.667814
```

Q41 Draw the graph of standard normal Distribution

Solution:

```
> n = seq(-3, 3, by = 0.1)
> y = dnorm(n)
> plot(x, y, xlab = "x values", ylab = "Probability", main =
"Standard Normal Graph")
```



## Practical: 6 : Z Distribution

1) Test the hypothesis ( $H_0$ ):  $\mu = 10$  against  $H_1: \mu \neq 10$   
A Sample of size 100 we selected which gives the  
mean 10.2  $\beta$  standard deviation 2.25 Test the  
hypothesis at 5% level of Significance Significance

S.D = Standard deviation

$m_0$  = mean of the population

$m_x$  = mean of sample

n = Sample Size

$m_0 = 10$

$m_x = 10.2$

$s_d = 2.25$

$n = 100$

$Z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$

$Z_{cal}$  is = "Zcal"

$Z_{cal}$  is =  $1.777778 > pvalue = 2 * (1 - norm(abs(Zcal)))$

$pvalue$

[1] 0.07549036

>

Value accepted ✓

2) Test the hypothesis ( $H_0$ ):  $\mu = 25$  against ( $H_1: \mu \neq 25$ ) at 5% level  
of significance the following sample is 30 selected

20	24	27	30	46	35	26	27	10	20
22	30	37	35	21	23	24	25	26	27
19	28	29	30	39	27	15	22	20	18
20	24	27	30	46	35	26	27	10	20

$x = c(20, 24, 27, 30, 46, 35, 26, 27, 10, 20, 22, 30, 37, 35, 21, 23, 24, 25, 26, 27, 19, 28, 29, 30, 39, 27, 15, 22, 20, 18)$

$m_x = mean(x)$

$m_x$

[1] 26.06667

$n = length(x)$

$n$

30

$Variance = (n-1) * var(x)/n$

Since 0.07549036 is more than 0.05 we will  
accept the  $H_0$

```

> Variance
[1] 52.99556
> sd = sqrt(Variance)
> sd
[1] 7.279805
> m0 = 25
> zcal = (mx - m0) / (sd / sqrt(n))
> cat("zcal is ", zcal)
zcal is 0.8025459
> Pvalue = 2 * (1 - pnorm(abs(zcal)))
> Pvalue
[1] 0.4222375

```

Value accepted

~~Rejected~~

c) Test the hypothesis ( $H_0$ ):  $\rho = 0.5$  against  $H_1: \rho < 0.5$ . A sample of 200 is selected from the sample proportion is calculated as  $\hat{\rho} = 0.56$ . Test the hypothesis at 1% level of significance.

```

> n = 200
> rho = 0.5
> rho = 0.56
> n = 200

```

> zcal =  $(\hat{\rho} - \rho) / (\sqrt{\rho(1-\rho)/n})$

> cat("zcal is ", zcal)

zcal is 1.697056

> Pvalue = 2 \* (1 - pnorm(abs(zcal)))

> Pvalue

[1] 0.08968602

P

[1] 0.56

$H_0$  ~~Rejected~~ accepted

```

> rho = 0.5
> n = 200
> p = 50/n
> rho = 1 - p
> zcal = (p - rho) / (sqrt(p * (1 - p) / n))
> cat("zcal is ", zcal)
zcal is -3.75
> Pvalue = 2 * (1 - pnorm(abs(zcal)))
> Pvalue
[1] 0.0001768346
> p
[1] 0.125

```

Value ~~Rejected~~

## Practical 7 Large Sample Tests

Q) A study of noise level in two hospital is calculated below Test the hypothesis that the noise level in two hospital are same or not

No of Sample obs  
Mean SD

No. A  
84  
61  
7

No. B  
34  
5  
8

$H_0$  - the noise levels are same

```

> mx = 64
> m2 = 68
> my = 59
> sdx = 7
> sdy = 8
> n1 = 84
> n2 = 61
> mx = 61
> my = 59
> sdx = 7
> sdy = 8
> z = (mx - my) / sqrt((sdx^2/n1) + (sdy^2/n2))
  
```

[1] 1.273682

$\times$  calculated is = 2

> pvalue

[1] 2.417564e-07

Since  $p\text{value} > 0.5$ , we accept  $H_0$  at 5% level of significance.

Q) In fy BSC 20% of a random sample of 400 students had defective eye sight in S-X class 15.5% of 500 students have the same defect; is the difference of the proportion is same?

$H_0$  - The proportion of the population are equal

```

> n1 = 400
> n2 = 500
> p1 = 0.2
> p2 = 0.155
> p = (n1*p1 + n2*p2)/(n1+n2)
  
```

[1] 0.175

> z = ( $p_1 - p_2$ ) /  $\sqrt{p_1 * p_2 * (1/n_1 + 1/n_2)}$

[1] 1.76547

Since  $p\text{value} < 0.05$ , we reject  $H_0$  at 5% level of significance

$\text{rat}^{\prime\prime 2}$  calculated is = 1.76547  
 $Z$  calculated is = 1.76547  
 $P\text{value} = 2 * (1 - \text{norm}(\text{abs}(z)))$

$P\text{value}$

[1] 0.07748487

Since  $P\text{value} > 0.05$  we accept  $H_0$  at 5% level of Significance

From each of the box of the apples a sample size of 200 is collected. It is found that there are 14 bad apples in first sample. Test the hypothesis that the two boxes are equivalent in term of Bad apples.

$H_0$ : The two box are equivalent

$n_1 = 200$   
 $n_2 = 200$   
 $p_1 = n_1/200$   
 $p_2 = 30/200$   
 $p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

$p = 0.185$

$q = 1 - p$

$q = 0.815$

$Z = (p_1 - p_2) / \sqrt{(p * q * (1/n_1 + 1/n_2))}$

$Z = 2$

$|Z| = 1.802741$

$P\text{value} = 2 * (1 - \text{norm}(\text{abs}(z)))$

$P\text{value}$

[1] 0.07142888

Since  $P\text{value} > 0.05$ , we accept  $H_0$  at 5% level of Significance

5) In MA class out of a sample of 60 mean height is 63.5 inches with a SD = 2.5. In a M.com class out of 50 students mean height is 69.5 inches with a SD = 2.5. Test the hypothesis that the mean of MA & M.com class are same.

$H_0$ : Heights of two classes are same

$n_1 = 60$   
 $n_2 = 50$

$m_x = 63.5$

$m_y = 69.5$

$s_{dx} = 2.5$

$s_{dy} = 2.5$

$sdy = \sqrt{(m_x - m_y)^2 / (n_1 + n_2)}$

$Z = 2$

[1] -12.53359

$P\text{value} = 2 * (1 - \text{norm}(\text{abs}(z)))$

$P\text{value}$

[1] 0

Since  $P\text{value} < 0.05$ , we reject  $H_0$  at 5% level of Significance.

Ans

## Practical-8 Small Sample Test

046

$\rightarrow y = ((x_0, \dots, x_n), w, v)$   
 $\rightarrow t \cdot \text{test}(x, y)$

### Welch Two Sample t-test

The tens are selected & height are found to be 63, 68, 69, 71, 72 cms. Test hypothesis that mean height is 66cm or not at 1%.

$H_0$ :

Mean = 66 cms  
 $\Rightarrow$  mean = 66  
 $\Rightarrow x = c(63, 68, 69, 71, 72)$

$\Rightarrow t \cdot \text{test}(x)$

One Sample t-test  
 data:  $x$   $y$   
 $t = 4.794$ ,  $df = 6$ ,  $p\text{-value} = 5.22e-09$

alternative hypothesis: true mean is not equal to 66

95 percent confidence interval:  
 64.66479 71.62092

Sample estimates:

mean of  $x$   
 68.14286

$\therefore p\text{-value} < 0.01$  is rejected on  $H_0$  in 1% level of significance

Two random sample was drawn from two different population

Sample 1 = 8, 10, 12, 11, 16, 15, 18, 7  
 Sample 2 = 20, 15, 18, 9, 8, 10, 11, 12

Test the hypothesis that there is no difference between the population mean at 5%. los

$H_0$ : there is no difference in the population mean

Q3 following are the weights of 10 people

Before: (100, 125, 95, 96, 98, 102, 115, 104, 109, 110)  
 After: (95, 80, 95, 98, 90, 100, 110, 85, 100, 101)  
 $H_0$ : The Diet program is not effective

$\Rightarrow x = c(100, 125, 95, 96, 98, 102, 115, 104, 109, 110)$   
 $\Rightarrow y = c(95, 80, 95, 98, 90, 100, 110, 85, 100, 101)$   
 $\Rightarrow t \cdot \text{test}(x, y, \text{paired} = T, \text{alternative} = 'less')$

Paired t-test

data:  $x$  and  $y$   
 $t = 2.3215$ ,  $df = 9$ ,  $p\text{-value} = 0.9773$

alternative hypothesis: true difference in means is less than 0

95 percent confidence interval: 17.89635

Sample estimates:  
 mean of the differences 10

$p\text{-value} < 0.01$  is accepted in  $H_0$  on 1% level of significance

Q3 Marks before & after a training program is given below

before = 20, 25, 32, 28, 27, 36, 35, 25  
after = 30, 35, 32, 37, 37, 40, 40, 23

Test the hypothesis that training program is effective or not

$H_0$ : The training program is not effective

$> x = c(20, 25, 32, 28, 27, 36, 35, 25)$

$> y = c(30, 35, 32, 37, 37, 40, 40, 23)$   
 $> t.test(x, y, paired = T, alternative = "greater")$

Paired t-test

data: x and y

$t = -3.3859$ ,  $df = 7$ ,  $p\text{-value} = 0.9942$

alternative hypothesis: true difference in means is greater than

95 percent confidence interval

- 8.967309 Inf

Sample estimates:

mean of the difference

- 5.75

$p\text{-value} < 0.01$  is accepted in  $H_0$  at 1% level

Q5 Two random sample were drawn from two rounds population A & the

values are

A = 66, 67, 75, 76, 82, 84, 88, 90, 92

B = 64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97

Test whether the population have same variance at 5% level of sig

$H_0$ : variances of the population are equal

$> x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$

$> y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

$> var.test(x, y)$

F test to compare two variances

data: x and y

$F = 0.70686$ , num  $df = 9$ , denom  $df = 10$ ,  $p\text{-value} = 0.6359$   
alternative hypothesis: true ratio of variances is not equal to 1

95 percent confidence interval

0.1833662 3.0360303

Sample estimates:

ratio of variances

0.7068567

$p\text{-value} \neq 0.7068567$  is accepted in  $H_0$  at 1% level of significance

The SP of sample 100 observation is 52 if SD is 7  
test the hypothesis that the population mean 55 or not at 5% of level of significance.

$H_0$ : Population mean = 55

$> m = 100$

$> mx = 52$

$> mo = 55$

$> Sd = 7$

$> Zcal = (mx - mo) / (Sd / \sqrt{n})$

$> Pvalue = 2 * (1 - pnorm(zabs(Zcal)))$

$> Pvalue$

[1] 1.82153e-05

$p\text{-value} < 0.01$  is accepted in  $H_0$  at 1% level of significance

M  
12.2.20

## Practical 9

Aim: Chi Square Distribution & ANOVA

use the following data to test whether the cleanliness of the home depends on the child

Condition of child	Condition of Home	
	Clean	Dirty
Fairly clean	80	20
Dirty	35	45

$H_0$ : condition of the home & child are independent

>  $X = c(70, 80, 35, 50, 20, 45)$

>  $m = 3$

>  $n = 2$

>  $y = matrix(x, nrow = m, col = n)$

>  $y$

[1, ]	[2, ]	[3, ]
70	80	35
50	20	45

>  $PV = chisq.test(y)$

>  $PV$

Pearson's chi-squared test

data: y  
 $\chi^2$ -squared = 25.646, df = 2, p-value = 2.698e-06

∴ P-value is less than 0.05, we ~~reject~~ reject  $H_0$  at 5% LOS

Q.2 Table below shows the relation between performance of mathematic & computer of CS students

	Maths		
	M6	Mn	L6
Computer	56	71	12
L6	47	163	38
14	42	85	

$H_0$ : Performance of Mathematic & Computer are independent

>  $a = c(56, 47, 14, 71, 163, 42, 12, 38, 85)$

>  $b = 3$

>  $c = 3$

>  $z = matrix(a, b, c)$

>  $z$

[1,1]	[1,2]	[1,3]
56	71	12
47	163	38

[1,1]	[1,2]	[1,3]
14	42	85

>  $PV = chisq.test(z)$

>  $PV$

Pearson's chi-squared test

data: z  
 $\chi^2$ -squared = 145.78, df = 4, p-value < 2.2e-16

p-value < 2.2e-16 is rejected less than 0.05, we reject  $H_0$  at 5% LOS

Q3 Perform ANOVA for the following Data:-

Varieties observations

A	50, 52
B	53, 55, 53
C	60, 68, 57, 56
D	52, 54, 54, 55

$H_0$  the means of varieties ABCD are equal

```

> x1 = c(50, 52)
> x2 = c(53, 55, 53)
> x3 = c(60, 68, 57, 56)
> x4 = c(52, 54, 54, 55)
> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
> names(d)
[1] "values" "ind"
> oneway.test(values~ind, data=d, var.equal=T)
One-way analysis of means
data: values and ind
F = 11.735, num df = 3, denom df = 9, p-value = 0.00183
> anova = aov(values~ind, data=d)
> summary(anova)

      Df Sum Sq Mean Sq F values   Pr(>F)
ind     3    71.06  23.688  11.73   0.00183 ***
Residuals 9   18.17  2.019

```

$\therefore$  P-value is less than 0.05, we accept reject the  $H_0$

Q4 Perform ANOVA for the following Data

Types observations

A	6, 7, 8
B	4, 6, 5
C	8, 6, 10
D	6, 9, 9

$H_0$  the means of varieties ABCD are equal

```

> x1 = c(6, 7, 8)
> x2 = c(4, 6, 5)
> x3 = c(8, 6, 10)
> x4 = c(6, 9, 9)
> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
> names(d)
[1] "values" "ind"
> oneway.test(values~ind, data=d, var.equal=T)
One-way analysis of means
data: values and ind
F = 2.6667, num df = 3, denom df = 8, p-value = 0.1189
> anova = aov(values~ind, data=d)
> summary(anova)

      Df Sum Sq Mean Sq F values   Pr(>F)
ind     3    18      6.00  2.667   0.1189
Residuals 8

```

$\therefore$  P-value is more than 0.05, we accept the  $H_0$  value at

Q.5  
write a R command to open and edit an Excel file in R Software

>x = read.csv('S:/users/admin/Desktop/marks1.csv')

>x

Stats	col
1	40
2	45
3	42
4	15
5	37
6	36
7	49
8	59
9	20
10	27

# Practical: 10

## Non-Parametric test

051

Q1 following are amount of Sulphide oxide emitted by factory.

17, 15, 20, 29, 90, 80, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26

Apply Sign test; to test the hypothesis that the population media against the alternative it is less than 21.5

$H_0$ : Population median = 21.5

$H_1$ : It is less than 21.5

$\geq x = c(17, 15, 20, 29, 90, 80, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26)$

$m = 21.5$

$s_p = \text{length}(x[x > m])$

$s_n = \text{length}(x[x < m])$

$n = s_p + s_n$

$p_v = \text{pbinom}(s_p, n, 0.5)$

$[1] 0.7482777$

Since, p-value  $> 0.05$ , we accept the  $H_0$  at 5% level of significance.

Q2 for the observation 12, 19, 31, 28, 43, 40, 55, 49, 70, 63.

Apply sign test, to test population median 25

against the alternative more than 25.

$H_0$ : median is 25

$H_1$ : It is more than 25

$a = c(12, 19, 31, 28, \cancel{43}, 40, 55, 49, 70, 63)$

$m = 25$

$s_p = \text{length}(a[a > m])$

$s_n = \text{length}(a[a < m])$

$n = s_p + s_n$

120

~~H<sub>0</sub>~~ > n

[1] 10

>pn = pbinom (5n, n, 0.5)

>pv

0.0546845

Since, p-value > 0.05, we accept the H<sub>0</sub> at 5%.

for the following data  
 $x = c(60, 65, 63, 89, 61, 71, 58, 51, 48, 66)$   
Test the hypothesis using wilcoxon's sign of rank test. For testing the alternative it is greater than 60

H<sub>0</sub>: median is 60  
H<sub>1</sub>: It is less than 60

$x = c(12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 10)$   
wilcox.test(x, alter="less", mu=12)

wilcoxon signed rank test with continuity correction

data: x  
v = 25, p-value = 0.2521

alternative hypothesis: true location is less than 12  
Since, p-value > 0.05. we accept the H<sub>0</sub> at 5% los

~~11. 720~~

wilcox.signed rank test with continuity correction

data: x

v = 29, p-value = 0.2386

alternative hypothesis: true location is greater than 60

Since p-value > 0.05, we accept the H<sub>0</sub> at 5%.  
Note: If the alternative is less, we have to write wilcox.test(x, alter="less", mu=60).  
If the alternative is not equal to we have to write wilcox.test(x, alter="two-sided", mu=60).

~~052~~