

Practical - 1

Brief Basis of R-software

- (1) It is a software for statistical analysis, data computing.
- (2) It is an effective data handling software and automatic storage is possible.
- (3) It is capable of graphical display.
- (4) It is a free software.

(5) Solve the following :-

$$\begin{aligned}
 & (1) 4+6+8 \div 2 = 5 \\
 & \quad 4+6+8 / 2 = 5 \\
 & \rightarrow 9
 \end{aligned}$$

$$\begin{aligned}
 & (2) 2^2 + 1-31 + \sqrt{45} \\
 & \quad 2^2 + (1-31) + \sqrt{45} \\
 & \rightarrow 23.7682
 \end{aligned}$$

$$\begin{aligned}
 & (3) 5^3 + 7 \times 5 \times 8 + 46 / 5 \\
 & \quad 5^3 + 7 \times 5 \times 8 + 46 / 5 \\
 & \rightarrow 414.2
 \end{aligned}$$

$$\begin{aligned}
 & (4) \sqrt{4^2 + 5 \times 3} + 7 / 6 \\
 & \rightarrow 5.671
 \end{aligned}$$

$$\begin{aligned}
 & (5) \text{round}(46.17) + 9 \times 9 \\
 & \rightarrow 79
 \end{aligned}$$

Q2) $(12, 3, 5, 7) * 2$
 Ans 6 10 14
 Q3) $((2, 3, 5, 7) + (2, 3))$
 Ans 9 10 21
 Q4) $(2, 3, 5, 7) * ((2, 3, 1, 6, 1, 2))$
 Ans 9 36 14
 Q5) $((1, 6, 1, 3) * ((-2) - 3, -4, 1))$
 Ans -2 -18 -8 -3
 Q6) $(1, 2, 1, 3, 1, 5, 1, 7) / 2$
 Ans 4 25 49
 Q7) $((4, 1, 6, 1, 8, 1, 9, 1, 4, 1, 5)) \wedge ((1, 2, 1, 3))$
 Ans 4 36 512 9 16 125
 Q8) $((1, 6, 1, 2, 1, 7, 1, 5)) / ((4, 5))$
 Ans 1.50 0.40 1.75 1.00
Q9)
 Q10) $x = 20, y = 30, z = 2$
 Q11) $z^2 + y^3 + z$
 Ans 72402
 Q12) $\sqrt{x^2 + y}$
 Ans 20.73644
 Q13) $x^2 + y^2$
 Ans 1300
 Q14)
 Ans $\text{xx} = \text{matrix}(\text{nrow} = 4, \text{ncol} = 2, \text{data} = c(1, 1, 2, 1, 3, 1, 4, 1))$
 Ans x

[1,1] [1,1] [1,2]
 [2,1] 1 5
 [2,2] 6
 [3,1] 3
 [3,2] 7
 [4,1] 4
 [4,2] 8

(Q5) Find $x+y$ & $2x+3y$, where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$ $y = \begin{bmatrix} 10 & -5 & 1 \\ 12 & -4 & 7 \\ 15 & -6 & 9 \\ 16 & -5 & 1 \end{bmatrix}$
 $x <- \text{matrix}[\text{nrow}=3, \text{ncl}=3, \text{data}=\text{c}(4, 7, 9, -2, 0, 7, 15, -6, 9, 16)]$

x [1,1] [1,2] [1,3]
 [1,1] 10 -5 7
 [2,1] 12 -4 9
 [3,1] 15 -6 5
 [4,1] 16 -5 1

y <- matrix[nrow=3, ncol=3, data=c(10, 12, 15, -5, -4, 7, 16, -6, 9, 1)]

x [1,1] [1,2] [1,3]
 [1,1] 4 -2 6
 [2,1] 7 0 7
 [3,1] 9 -5 3

> x+y [1,1] [1,2] [1,3]

[1,1] 14 -7 13
 [2,1] 19 -4 16
 [3,1] 24 -11 8

> 2*x + 3*y

[1,1] [1,2] [1,3]
 [1,1] 34 -19 33
 [2,1] 50 -12 41
 [3,1] 63 -28 21

(Q6) Marks of 8 students of C.8

x = c(89, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 32, 36, 29, 35, 39)

> breaks = seq(20, 60, 5)

a = cut(x, breaks, right = FALSE)

C	a	Frq
1	[20, 25)	3
2	[25, 30)	2
3	[30, 35)	1
4	[35, 40)	4
5	[40, 45)	1
6	[45, 50)	3
7	[50, 55)	2
8	[55, 60)	4

Frq
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Practical - 2

Aim:- Probability Distribution

(Q1) Check whether the following are PMF or not

x	$p(x)$
0	0.1
1	0.2
2	-0.5
3	0.4
4	0.3
5	0.5

x	1	2	3	4	5
$p(x)$	0.2	0.2	0.3	6.2	0.2

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

Ans

(Q1). If the given data is PMF then,

$$\sum p(x) = 1$$

Hence

$$\begin{aligned}\sum p &= p(1) + p(2) + p(3) + p(4) + p(5) \\ &= 0.1 + 0.2 + (-0.5) + 0.4 + 0.3 + 0.1 \\ &= 1.0.\end{aligned}$$

Since $p(2) = -0.5$,

It cannot be a probability mass function as in PMF $p(x) \geq 0$.

$$(2) \sum p(x) = 1$$

$$(3) p(x) \geq 0$$

$$(1) \sum p(x) = 1$$

$$\begin{aligned}p &= p(10) + p(20) + p(30) + p(40) + p(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1\end{aligned}$$

The given data is P.M.F.

Q1P:

$$\text{prob} = ([0.2, 0.2, 0.35, 0.15, 0.1])$$

sum(prob).

(Q2) Find C.D.F.

(1) Find C.D.F for the foll p.m.f and sketch the graph:-

x	10	20	30	40	50
$p(x)$	0.2	0.2	0.35	0.15	0.1

CDF:

cumsum (prob)

$$\rightarrow p(x) = 0 \quad x < 10$$

$$0.2 \quad 10 \leq x < 20$$

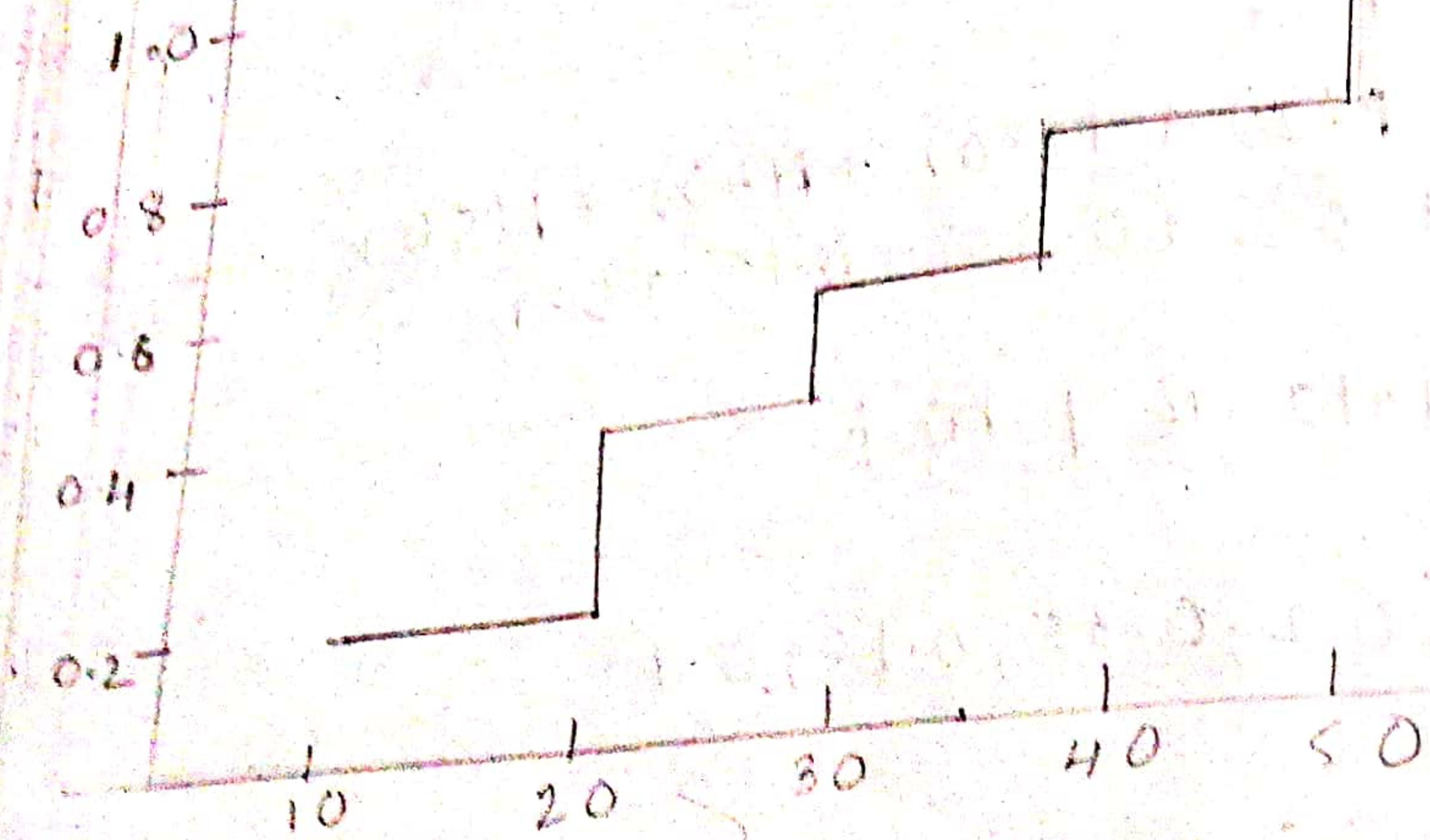
$$0.4 \quad 20 \leq x < 30$$

$$0.75 \quad 30 \leq x < 40$$

$$0.95 \quad 40 \leq x < 50$$

$$1.0 \quad 50 \leq x$$

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(Q2) Find the i.d.f w/ sketch the graph

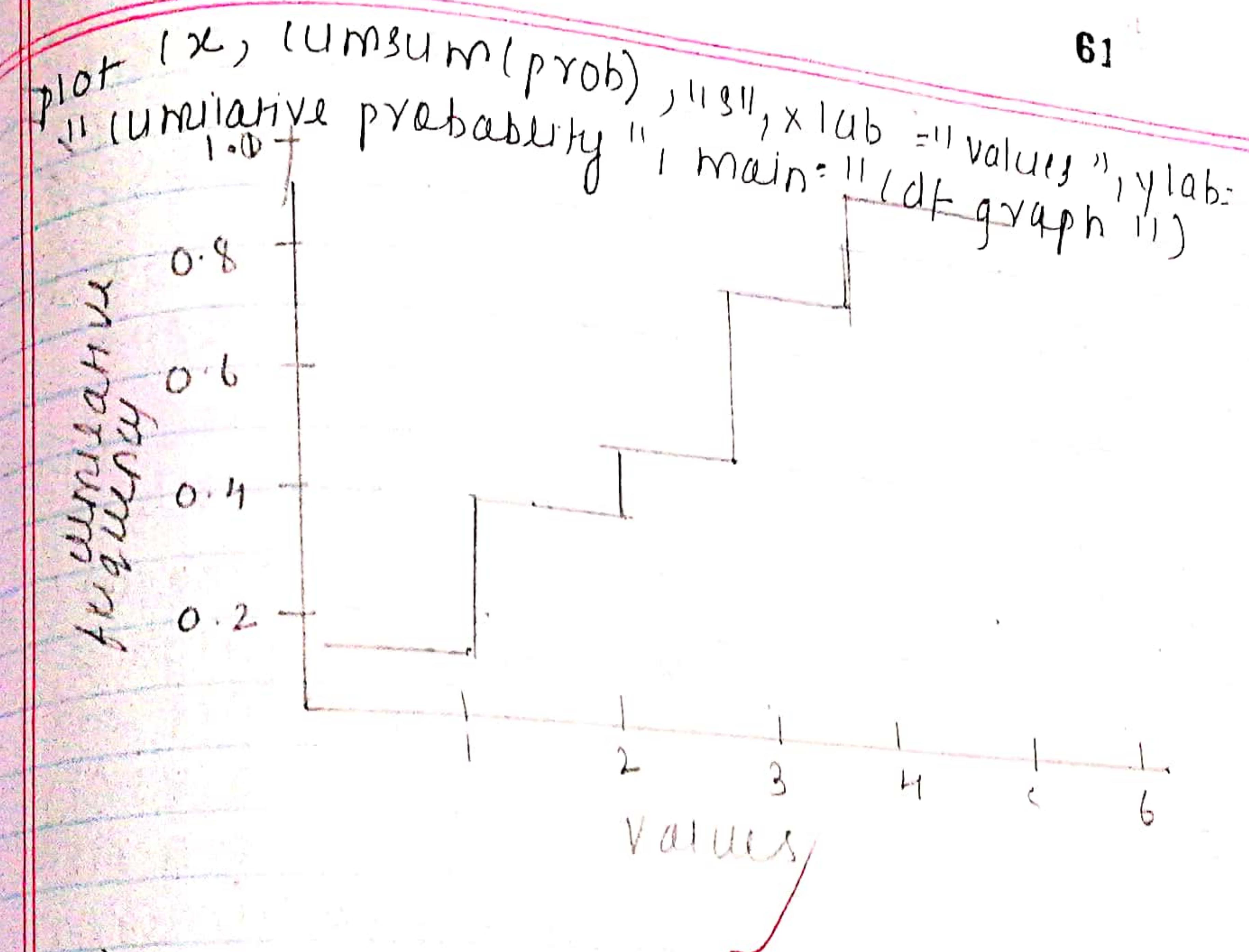
x	1	2	3	4	5	6
$p(x)$	0.15	0.25	0.1	0.2	0.2	0.1

$F(x) = 0$	$x < 1$
0.15	$1 \leq x < 2$
0.40	$2 \leq x < 3$
0.50	$3 \leq x < 4$
0.70	$4 \leq x < 5$
0.90	$5 \leq x < 6$
1.00	$x \geq 6$

CODE:

```
> prob = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)
> sum(prob)
[1] 1
> cumsum(prob)
[1] 0.15, 0.40, 0.50, 0.70, 0.90, 1.00
x = c(1, 2, 3, 4, 5, 6)
```

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(Q3)

$$(1) F(x) = 3 - 2x ; 0 \leq x \leq 1$$

$$\int x^n f(x) dx = \frac{x^{n+1}}{n+1}$$

$$\int_0^1 (3 - 2x) dx$$

$$\int_0^1 3 dx - \int_0^1 2x dx$$

$$= [3x - x^2]_0^1 = 2$$

Practical - 3

TOPIC: BINOMIAL DISTRIBUTION

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$$(1) P(X = x) = \text{dbinom}(x, n, p)$$

$$(2) P(X \leq x) = \text{pbinom}(x, n, p)$$

$$(3) P(X > x) = 1 - \text{pbinom}(x, n, p)$$

(4) If x is unknown

$$P_1 = P(X \leq x) = \text{qbinom}(p_1, n, p)$$

(i) Find the probability of exactly 10 success in 100 trials with $p = 0.1$

(ii) Suppose there are 12 MCQ's. Each question has 5 options out of which one is correct. Find the probability of having

(i) Exactly 4 correct answer

(ii) Atmost 4 correct answer

(iii) More than 5 correct answer

(iii) Find the complete distribution where $n=5$, $p=0.1$

(iv) $n=12$, $p=0.25$. Find the following probability,

(i) $P(X=5)$ (ii) $P(X>7)$

(iii) $P(X \leq 5)$ (iv) $P(5 < X \leq 7)$

(v) The probability of a sales man making a sell to a customer is 0.25. Find a probability of $x=10$

(i) No sales out of 10 customer

(ii) More than 3 sales out of 20 customer

a

$$(iii) f(x) = 3x^2 ; 0 \leq x \leq 1$$

$$\int f(x)$$

$$= \int 3x^2$$

$$= 3 \int (x^2)$$

$$= 0$$

$$= 3 \int \left(\frac{x^3}{3}\right)$$

$$\therefore x^n = \frac{x^{n+1}}{n+1}$$

$$= x^3$$

$$= 1$$

The $\int f(x) = 1$ \therefore It is a pdf

M

(Q6) A salesman has a 20% probability of making a sale to a customer out of 30 customers what minimum number of sales he can make with 88% probability.

(Q7) x follows binomial distribution with $n=10$, $p=0.3$, Plot the graph of pmf and cdf.

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[0] > dbinom(10, 100, 0.1)
[1] 0.1318653

[2] > dbinom(4, 12, 0.2)
[1] 0.1328756

[3] > pbinom(4, 12, 0.2)
[1] 0.9274445

[4] > 1 - pbinom(5, 12, 0.2)
[1] 0.01440528

[5] > dbinom(0:5, 5, 0.1)

[1] 0.59049 0.32805 0.07290
0.00810 0.00045 0.00001

[6] > dbinom(5, 12, 0.25)
[1] 0.1032414 ✓

[7] > pbinom(5, 12, 0.25)
[1] 0.9455978

[8] > 1 - pbinom(7, 12, 0.25)
[1] 0.0008782414

[9] > ubinom(6, 12, 0.25)
[1] 0.04014945

8a₂

(5) (i) $> \text{dbinom}(0, 10, 0.15)$
[1] 0.1968744

(ii) $> 1 - \text{pbisnom}(3, 10, 0.15)$
[1] 0.3522748

(6) $\text{qbinom}(0.98, 30, 0.2)$
[1] 9.

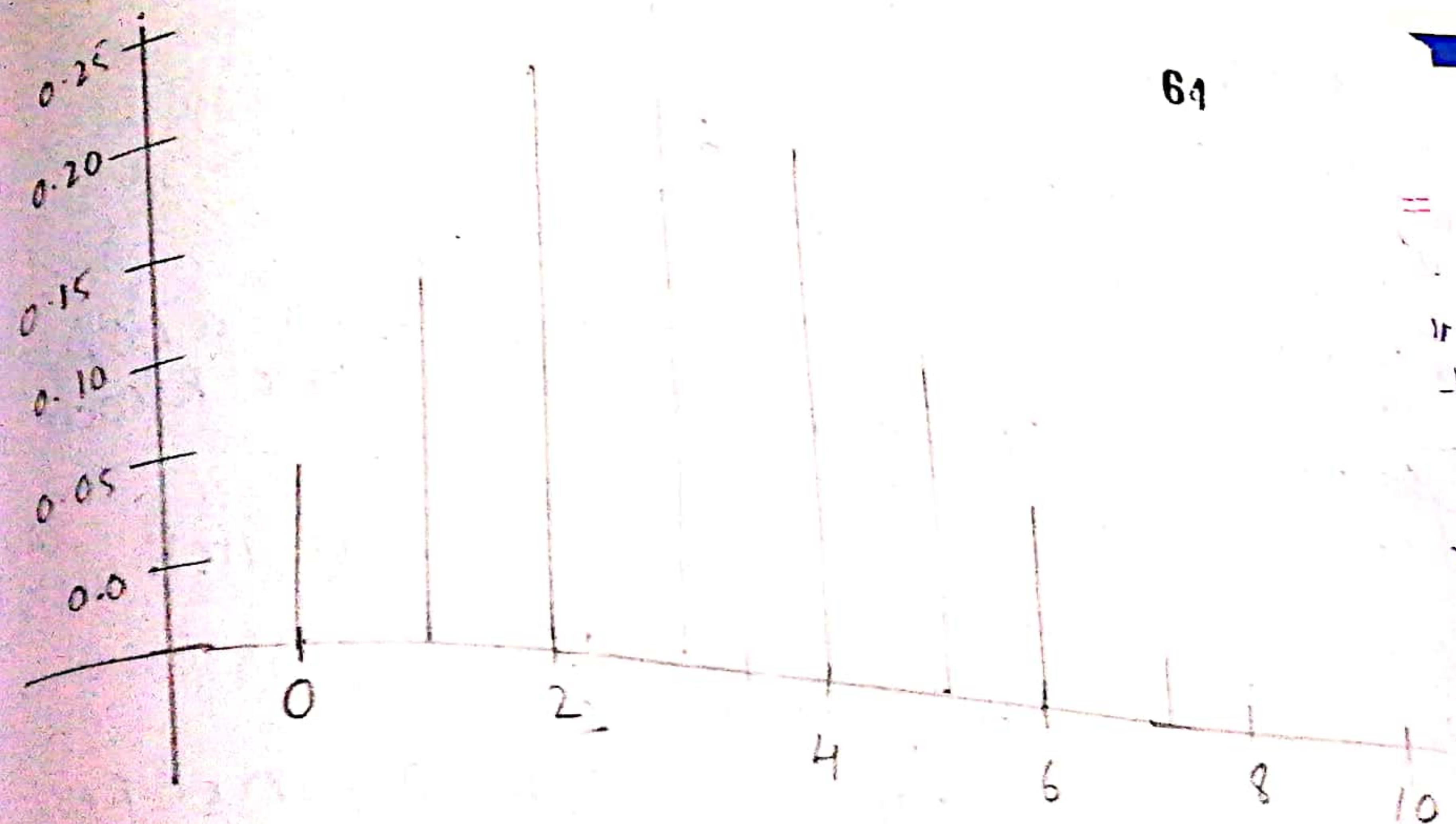
(7) $> n = 10$
 $> p = 0.3$
 $> z = 0.5$
 $> prob = \text{dbinom}(x, n, p)$
 $> cumprob = \text{pbisnom}(x, n, p)$
 $> d = \text{data.frame}(\text{"x values": } x, \text{"probability":}$
 $\text{prob})$
 $> \text{print}(d)$

x values probability

1	0	0.0282
2	1	0.1210
3	2	0.2334
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.367
8	7	0.690
9	8	0.6014
10	9	0.6001
11	10	0.6000

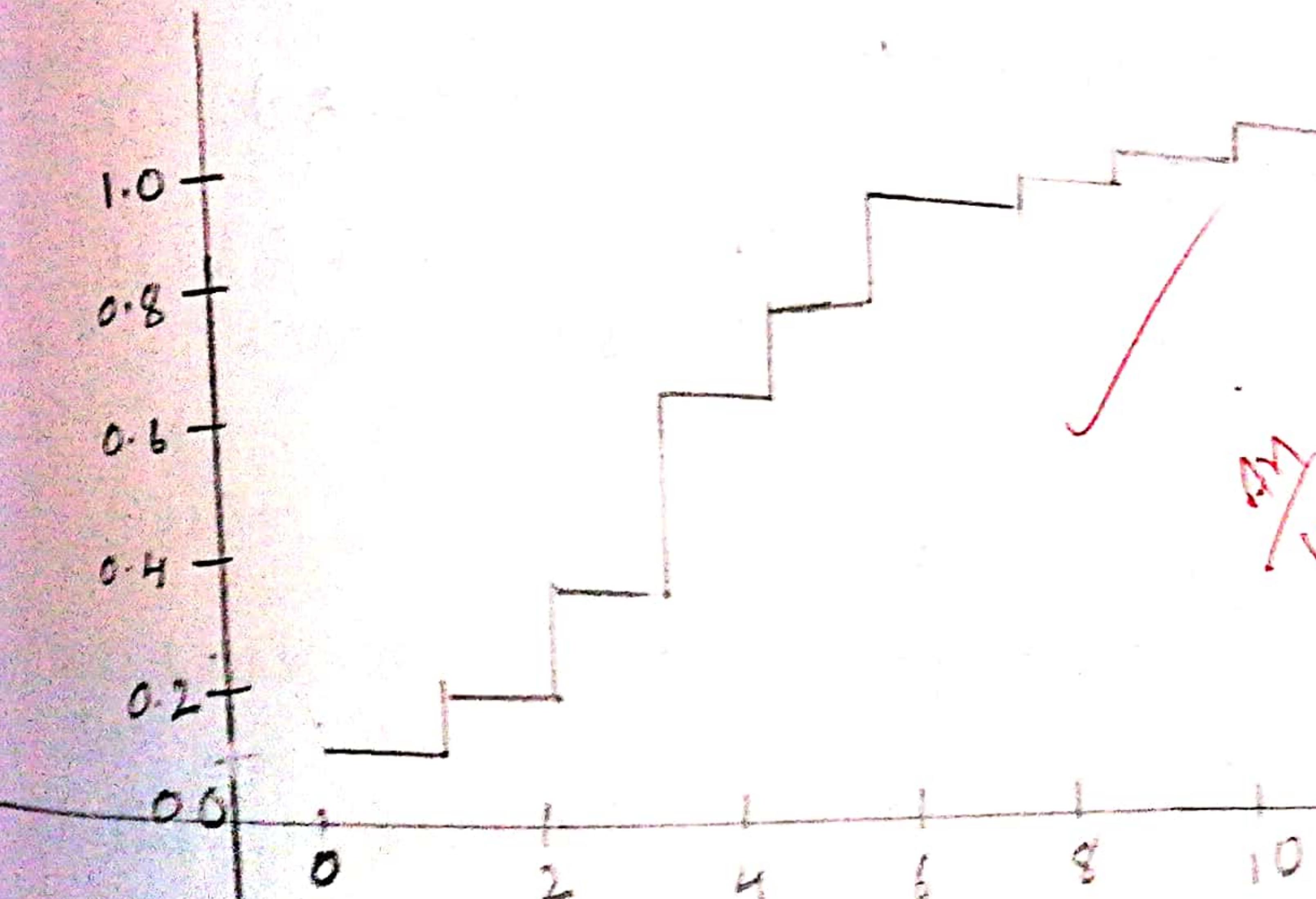
> plot(x, cumprob, "h")

6a



> plot(x, cumprob, "s")

8a
19/21



Practical 4

Topic: Normal Distribution

Formula:

$$(1) P(x=x) = \text{dnorm}(x, \mu, \sigma^2)$$

$$(2) P(x < x) = \text{pnorm}(x, \mu, \sigma^2)$$

$$(3) P(x > x) = 1 - \text{pnorm}(x, \mu, \sigma^2)$$

(4) To generate random numbers from a normal distribution (n random numbers) the R code is:

$$is = rnorm(n, \mu, \sigma^2)$$

If random variable x follows normal dist with mean = $\mu = 10$ and SD = $\sigma = 3$. Find

$$(1) P(x \leq 15) \quad (3) P(x > 14)$$

$$(2) P(10 \leq x \leq 13) \quad (4) Generate 5 observations (RN)$$

$$(1) \text{pnorm}(15, 10, 3)$$

$$[1] 0.8413447$$

$$> cat("P(x \leq 15) = ", 1, p1)$$

$$[1] 0.8413447$$

$$(1) P(x \leq 15) = \text{pnorm}(10, 12, 3)$$

$$> p2 = \text{pnorm}(13, 12, 3)$$

$$> cat("P(10 \leq x \leq 13) = ", 2, p2)$$

$$[1] 0.37080661$$

$$(1) P(10 \leq x \leq 13) = 0.37080661$$

$$> p3 = 1 - \text{pnorm}(14, 12, 3)$$

$$> cat("P(x > 14) = ", 3, p3)$$

$$[1] 0.2524925$$

$$> rnorm(5, 12, 3)$$

$$[1] 12.639812 \quad 13.041270 \quad 7.920397$$

$$9.888882 \quad 6.965470$$

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- x follows normal distribution with $\mu = 10, \sigma = 2$
- Find
 (i) $P(x \leq 7)$ (ii) $P(5 < x < 12)$
 (ii) $P(x > 12)$ (iv) Generate 10 observations
 (v) Find K such that $P(x < K = 0.4)$

$$> h1 = \text{pnorm}(7, 10, 2)$$

$$[1] 0.668072$$

$$> h2 = \text{pnorm}(15, 10, 2)$$

$$[1] -0.8351351 \quad \text{pnorm}(12, 10, 2)$$

$$> h3 = 1 - \text{pnorm}(12, 10, 2)$$

$$[1] 0.1586553$$

$$> h4 = rnorm(10, 10, 2)$$

$$[1] 10.266550 \quad 10.596867 \quad 10.547316$$

$$9.045449 \quad 9.978724 \quad 5.756808$$

$$11.989820 \quad 5.833428 \quad 8.564714$$

$$11.123124$$

$$> h5 = qnorm(0.4, 10, 2)$$

$$[1] 9.493306$$

- (3) Generate 5 random variables with mean=15, SD = 4

Find: (i) sample mean, median, SD, print it

- (4) x follows $(x \sim$

Find (i) $P(x \leq 40)$

(ii) $P(25 < x < 35)$

a3.

iii) find K such that $P(X < K) = 0.6$.

04

$d1 = \text{pnorm}(140, 30, 10)$

$d1 [1] 0.8413447$

$d2 = 1 - \text{pnorm}(35, 30, 10)$

$d2 [1] 0.3085375$

$d3 = \text{pnorm}(25, 30, 10) - \text{pnorm}(35, 30,$

$d3 [1] -0.3829249$

$d4 = \text{qnorm}(0.6, 30, 10)$

$d4 [1] 32.53347$

03

$x = \text{rnorm}(5, 15, 4)$

[1] 12.73337 12.30235 16.62240
23.24364 13.08828

$x = \text{rnorm}(5, 15, 4)$

am: mean(x)

am [1] 15.33276

mede: median(x)

mede [1] 14.86556

n = 5

v = (n - 1) * var(x) / n

v

2.574805

s d = sqrt(v)

s d

[1] 1.60462

cat "sample mean", am
sample mean 15.33276

cat "sample median", me
sample median 14.86556

cat "sample sd", sd
sample sd 1.60462

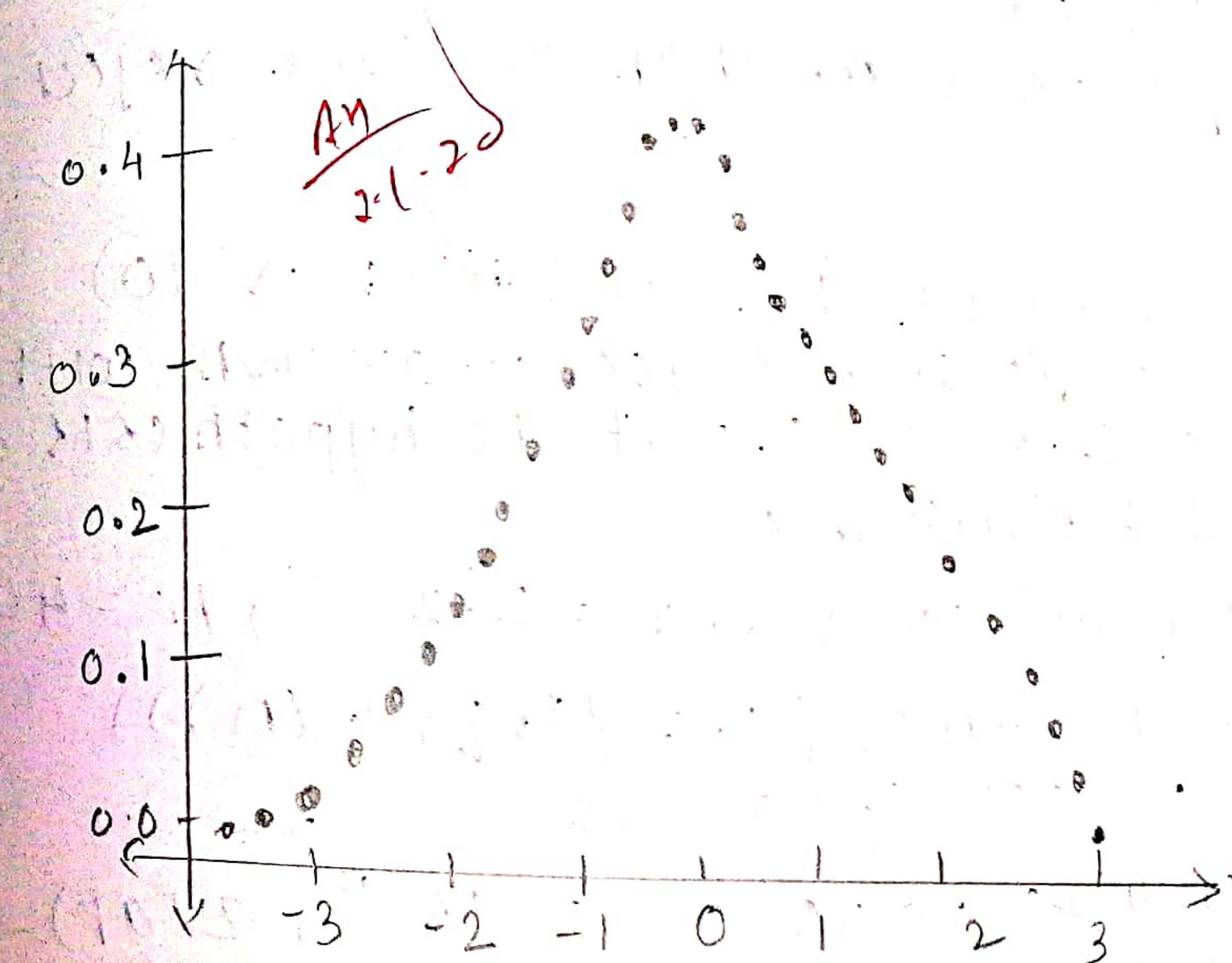
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b5) plot the standard normal graph

x = seq(-3, 3, by = 0.1)

y = dnorm(x)

plot(x, y, xlab = "x values", ylab = "probability")
main "standard normal graph")



Practical - 5

Aim: Normal and t-test

- Test the hypothesis ($H_0: \mu = 15$), $H_1: \mu \neq 15$
Random sample of size 400 is drawn and its mean is 14 by SD = 3. Test the hypothesis at 5% level of significance
 $m_0 = 15, m_x = 14, s_d = 3, n = 400$

Ans: $z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$
 $\geq z_{\text{cal}} = [1] - 6.66667$
 $\geq \text{cat} (" \text{calculate value at } z \text{ is } ", z_{\text{cal}})$
 $\geq \text{cat} (" \text{calculate value at } z \text{ is } ", -6.66667)$
 $\geq \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $\geq \text{pvalue}$

[1] 2.61679e-11
 since p value is less than 0.05 we reject $H_0: \mu = 15$

- Test the hypothesis ($H_0: \mu = 10$), $H_1: \mu \neq 10$
Random sample of size 400 is drawn with mean = 10.2, SD = 2.25. Test the hypothesis at 5% level of significance.

$m_0 = 10, m_x = 10.2, s_d = 2.25, n = 400$

$\geq z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$
 $\geq z_{\text{cal}} = [1] 1.777778$
 $\geq \text{cat} (" \text{calculate value at } z \text{ is } ", z_{\text{cal}})$
 $\geq \text{calculate value at } z \text{ is } 1.777778$
 $\geq \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $\geq \text{pvalue}$

[1] 0.07544036
 since p value more than 0.05 we accept $H_0: \mu = 10$

87

Test the hypothesis $H_0: \text{proportion of smokers in a college is } 0.2$
A sample is collected and its calculated at 5% level of significance (sample size = 400).

$\geq p = 0.2, P = 0.125$
 $\geq z_{\text{cal}} = (p - P) / (\sqrt{P(1-P)/n})$
 $\geq z_{\text{cal}} = [1] - 3.75$
 since

$\geq \text{cat} (" \text{calculate value at } z \text{ is } ", z_{\text{cal}})$

last year farmers lost 20% of their crop. random sample of 60 field are collected and it is found that 9 fields crops are insect polluted. Test the hypothesis at 1% level of significance

$p = 0.2, P = 9/60, n = 60, Q = 1 - p$
 $\geq \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$
 $\geq \text{pvalue} = [1] 0.3329216$
 $\geq z_{\text{cal}} = (p - P) / (\sqrt{P(1-P)/n})$
 $\geq z_{\text{cal}} = [1] - 0.9682458$

Test the hypothesis $H_0: \mu = 12.5$ from the full sample at 5% level of significance

$\underline{\underline{p = 0.2}}$

$x = ([1] 12.25, 11.47, 12.15, 12.08, 12.31, 12.28, 11.94, 11.49, 12.16, 12.04)$

$n = \text{length}(x)$
 $n = 10$
 $mx = \text{mean}(x)$
 $mx = [1] 12.107$
 $\text{varience} = (n-1) * \text{var}(x)/n$
 $\text{varience} = [1] 0.01952$
 $sd = \sqrt(\text{varience})$
 $sd = [1] 0.1397176$
 $m_0 = 12.5$
 $t = (mx - m_0) / (sd / \sqrt(n))$
 $t = [1] -8.894909$
 $pvalue = 2 * (1 - \text{pnorm}(\text{abs}(t)))$
 $pvalue = [1] 0$

 AM
 16.170

6

Q1) Large sample test: 68

Let the population mean (amount spent by customer in a restaurant) is 250. A sample of 100 (test selected). Sample mean is calculated as 275 w/ \$10.30; test the hypothesis that the pop mean is 250 or not at 5% level of significance.

Q2) In a random sample of 1000 students it is found that 750 use blue pen. Test the hypothesis that the population proportion is 0.8 at 1 level of significance.

$m_0 = 250$, $sd = 30$
 $mx = 275$, $n = 100$
 $z_{cal} = (mx - m_0) / (sd / \sqrt(n))$
 $z_{cal} = [1] 8.3333$
 $pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$
 $pvalue = [1] 0$

`>zat("zcal:", zcal)`
`zcal: 8.3333`
`>zat("pvalue:", pvalue)`
`pvalue: 0>`

$P = 0.8$, $n = 1000$
 $P = 0.8$, $Q = 1 - P$
 $P = 750 / 1000$
 $z_{cal} = (P - P) / \sqrt(P * Q / n)$
 $z_{cal} = [1] -3.952847$

>pvalue = 2 * (1 - pnorm(abs(z(a1)))
>pvalue [1] 7.72268e-05

Q3 2 random sample of size 1000 & 2000 are drawn from 2 population with the same SD=2.5. The sample means are 67.5 & 68 resp. Test the hypothesis $H_0: \mu_1 = \mu_2$ at 5% LOS.

Q4 A study of noise level in 2 hospital is given below. Test the claim that the 2 hospitals ~~are~~ have same level of noise at 0.05% LOS.

	Hosp A	Hosp B
size	84	34
mean	61.2	59.4
SD	7.9	7.5

Q5 In a sample of 600 students in a college, 400 use blue ink in another college from a sample of 900 students, 450 use blue ink. Test the hypothesis that the proportion of students using blue ink in 2 colleges are equal or not at 1% LOS.

Q3: $n_1 = 1000, n_2 = 2000$

$$m_{x1} = 67.5, m_{x2} = 67.5$$

$$s_{d1} = 2.5, s_{d2} = 2.5$$

$$z(a) = (m_{x1} - m_{x2}) / (\sqrt{s_{d1}^2/n_1 + s_{d2}^2/n_2})$$

$$>z(a) [1] -5.163978$$

$$>cat("z(a): ", z(a))$$

$$z(a): -5.163978$$

>pvalue = 2 * (1 - pnorm(abs(z(a1)))

>pvalue [1] 2.417564e-07

>cat("pvalue: ", pvalue)

pvalue: 2.417564e-07

p value > 0.05

value - accepted.

Q4

$$n_1 = 84, n_2 = 34$$

$$m_{x1} = 61.2, m_{x2} = 59.4$$

$$s_{d1} = 7.9, s_{d2} = 7.5$$

$$z(a) = (m_{x1} - m_{x2}) / \sqrt{(s_{d1}^2/n_1 + s_{d2}^2/n_2)}$$

$$[1] 1.162528$$

>pvalue = 2 * (1 - pnorm(abs(z(a1)))

>pvalue [1] 6.2450211

p value > 0.05 value - rejected

Q5.

$$H_0: p_1 = p_2 \quad H_A: p_1 \neq p_2$$

$$n_1 = 600$$

$$n_2 = 900$$

$$p_1 = 400/600$$

$$p_2 = 450/900$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$[1] 0.566667$$

$$q = 1 - p$$

$$>z(a) = \sqrt{p_1 * p_2 * q * (1 - q) / (n_1 + n_2)}$$

$$[1] 6.341534$$

Q8

> pvalue = 2 * (1 - pnorm(zabs(zcal)))

> pvalue
[1] 1.753222e-10

pvalue > 0.05, value accepted

~~Q6~~

> pvalue = 2 * (1 - pnorm(zabs(zcal)))
[1] 1.753222e-10

> p1 = 44/200, p2 = 30/200

> p = (p1 + p2) / (n1 + n2)

> q = 1 - p

> zcal = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))

> pvalue = 2 * (1 - pnorm(zabs(zcal)))

[1] 1.402741

> pvalue

[1] 0.07142888

pvalue > 0.05, value accepted

~~✓~~ 27/10

Q9: small sample test

The marks of 10 students are given by 63, 62, 66, 69, 68, 69, 70, 70, 71, 72. Test the hypothesis that the sample comes from population with the avg. 66. There is no significant difference.

avg = 66
n = 10
x = c(63, 63, 66, 67, 68, 69, 70, 70, 71, 72)

t-test(x)

ONE SAMPLE t-test

data: x
t = 6.8, df = 9, p value = 1.558e-13

alternative hypothesis: true mean is not equal to 65 percent confidence interval:

65.65171 70.14829

sample estimates:

mean of x

67.9

p > 0.05 ∴ H0 is rejected

> if (1.558e-13 > 0.05) {cat("H0 is accepted") } else {

{cat("H0 is rejected") }

> reject = NO

11

Q2 2 groups of students score the following marks between T-test the hypothesis that there is no significant diff between the 2 groups.

Grp 1 - 19, 22, 21, 17, 20, 17, 23, 20, 22, 21
Grp 2 - 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

H₀ - There is no difference between 2 grps

H₁ - There is no difference between 2 grps

> x = c(19, 22, 21, 17, 20, 17, 23, 20, 22, 21)
> y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

> t.test(x, y)

- Welch two sample t-test

data: x and y
t = 2.2573, df = 16.376, pvalue = 0.03798

alternative hypothesis: true diff in means is not equal to zero
95 percent confidence interval:

0.1628205 5.037145

sample estimates:

mean of x mean of y

20.1 17.5

> if (pvalue >= 0.05) { cat("accept no") } else { cat("reject no") }

> reject no

Q3 The sales data of 6 shops before by after.

Before: 53, 28, 31, 48, 50, 42

After: 54, 29, 30, 55, 56, 45

Test the hypothesis is effective or not.

There is no significant difference before and after the sales.

> x = c(53, 28, 31, 48, 50, 42)

> y = c(54, 29, 30, 55, 56, 45)

> t.test(x, y, paired = T, alternative = "greater")

Paired t-test

data: x and y

t = -2.7815, df = 5

alternative hypothesis: true difference in means is greater than 0.

95 percent confidence interval:

-6.0355 47

sample estimates:

mean of the differences

-3.5

p-value = 0.9806 > 0.05

if (0.9806 > 0.05) { cat("accept no") } else { cat("reject no") }

reject no

Q4 Two medicines are applied to two groups of patients resp.

Grp 1: - 10, 12, 13, 11, 14

Grp 2: - 8, 9, 12, 14, 15, 10, 9

Is there any significant diff between 2 medicine?

No:

x = c(10, 12, 13, 11, 14)

y = c(8, 9, 12, 14, 15, 10, 9)

H₀: There is no significant difference.

> t.test(x, y)

> pvalue = 0.4406

> if (0.4406 > 0.05) { cat("accept no") } else { cat("reject no") }

reject no

\rightarrow The value is accepted.

Q5 The foll are the weight before & after the diet program. Is the diet program effective?

before: 120, 125, 115, 130, 123, 119

after: 100, 114, 95, 90, 115, 99

H₀: There is no significant difference.

$\rightarrow x = c(120, 125, 115, 130, 123, 119)$

$\rightarrow y = c(100, 114, 95, 90, 115, 99)$

$\rightarrow t.test(x, y, paired = T, alternative = "less")$

\rightarrow data: x and y

t = 4.3458, df = 5, p-value = 0.9963

alternative hypothesis: true difference in means is less than 0

95 percent confidence interval:

-Inf 29.0295

Sample Estimates:

mean of the differences

19.83333

\rightarrow if $|0.9963| > 0.05 \} \{ \text{cat } "accept no"} \} \{ \text{use}$

$\text{cat } "reject no"} \} \{ \text{q.a.}$

\rightarrow reject no

Practical - 8

73

Q: Large and small sample test.

$$\mu = 55$$

$$\mu \neq 55$$

100

$$x = 52, m_0 = 55, s_d = 7$$

$$z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$$

$$z_{\text{cal}} = 1.4, z_{\text{tab}} = 1.96$$

$$z_{\text{cal}} < z_{\text{tab}}$$

$$z_{\text{cal}} < z_{\text{tab}}$$

$$\text{p-value} = 2 * (1 - \text{pnorm}(z_{\text{cal}}))$$

$$\text{p-value} = 1 - 0.82153 = 0.1785$$

As p-value is smaller than 0.05. Hence rejects the no

$$H_0: \mu = 112$$

$$n = 100, p = 350/700$$

$$\alpha = 0.5$$

$$\alpha = 1 - p$$

$$\text{p-value} = (p - p_0) / \text{sgyr}(p \neq 0.5 / n)$$

$$z_{\text{cal}} = 1.70$$

$$\text{p-value} = 2 * (1 - \text{pnorm}(z_{\text{cal}}))$$

$$\text{p-value} = 0.171$$

As p-value > 0.05 we accept

$\mu_0 = (63, 63, 68, 69, 71, 71, 72)$

$\sigma^2 = 47.94$, d.f. = 6, p-value = 5.522e-09
 alternative hypothesis: true mean is not equal to 0
 95 percent confidence interval: 71.62092

sample estimates:
 mean of \bar{x}

68.14286

pvalue > 0.05 Hence rejects

$\mu_0 = 1200$

$\mu_0 = 1200$, $m_x = 1150$

$s_d = 125$, $n = 100$

$z_{\text{cal}} = (m_x - \mu_0) / (s_d / \sqrt{n})$

$z_{\text{cal}} = [1] -4$

pvalue = $2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$

pvalue = [1] 6.33428e-05

pvalue ≥ 0.05 it rejects.

$\mu_0: \bar{x}_1 = 62$

$x = (166, 67, 75, 76, 82, 84, 88, 90, 92)$

$y = (64, 66, 74, 78, 82, 85, 87, 92, 93, 95)$

var. tst $t(x, y)$

F test to compare two variances

55

$$\begin{aligned} H_0: & p = p_2 \\ n_1 &= 1000 \\ n_2 &= 1500 \end{aligned}$$

$$p_1 = 20/1000$$

$$p_2 = 15/1500$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p = [1] 0.014$$

$$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * (1 - p) * (1/n_1 + 1/n_2)}$$

$$> z_{\text{cal}} = [1] 2.081283$$

$$> pvalue = 1 - \text{pnorm}(\text{abs}(z_{\text{cal}}))$$

$$> pvalue = [1] 0.018704$$

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> pvalue$$

$$[1] 0.0374080$$

pvalue < 0.05 we reject

$$\mu_0: \bar{y} = 100$$

$$(4) n = 100$$

$$m_x = 99, m_0 = 100$$

$$var = 64, s_d = 8$$

$$z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$$

$$z_{\text{cal}} = [1] -2.5$$

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> pvalue = [1] 0.01241933$$

pvalue < 0.05 we reject

data: x and y
 $F = 0.70686$, num df = 4, denom df = 10, p-value = 0.6359.

alternative hypothesis: true ratio of valuenus is not equal to 1
 95 percent confidence interval:
 0.1433662 3.0360393

sample estimates:
 ratio of valuenus = 0.7068567.
 pvalue > 0.05 we accept H0

$$108) H_0: p_1 = p_2$$

$$> n1 = 200 \quad n2 = 300$$

$$p1 = 44/200 \quad p2 = 56/300$$

$$P = (p1 * p1 - n2 * p2) / (n1 + n2)$$

$$q = 1 - P$$

$$q = 0.2$$

$$> z(a) = (p1 - p2) / \sqrt{p1 * q1 / (1/n1 + 1/n2)}$$

$$> z(a) = 1.70.9128709$$

$$> pvalue = 2 * (1 - pnorm(abs(z(a))))$$

$$> pvalue$$

$$[1] 0.3613104$$

pvalue > 0.05 we accept H0

$$\chi^2$$

Practical 9

76

Aim:- chi square and ANOVA

use the following data to test whether the condition of home by child are independent or not.

		condition of home	
		clean	dirty
condition child	clean	70	50
	dirty	80	20
dirty child	clean	35	45
	dirty		

H0: condition of home and child are independent

Soln:

$$> x = c(70, 80, 35, 50, 20, 45)$$

$$> m = 3, n = 2$$

$$> y = matrix(x, nrow = m, ncol = n)$$

$$> y$$

55

		[1,1]	[1,2]
[1,1]		50	
[2,1]		20	
[3,1]		45	

$\geq PV = \text{chi2}.\text{test}(Y)$

Pearson's chi-squared HST

data = Y
 χ^2 -squared = 25.646, df = 2, p-value = 2.698

since p-value > 0.05, we reject H₀.

(Q2) Test hypothesis that vaccination and disease are dependent or not

DISEASE		VACCINE	
		NOT affected	Affected
NOT Affected	Affected	70	46
	NOT Affected	35	37

Disease by Vaccine are independent

= 6170, 35, 46, 37
 $n = 2$, nrow = m, ncol = n
matrix(x, nrow = m, ncol = n)

[1,1] [1,2]

70 46

[1,3] [1,4]

35 37

PV = chi2.test(Y)

PV

0.6

0.6

0.6

0.6

0.6

0.6

0.6

0.6

0.6

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0.6

75

Pearson's chi-squared test with Yates' continuity correction

data = Y
 χ^2 -squared = 2.0275; df = 1, p-value = 0.1545

pvalue > 0.05, hence we reject.

b) Perform a ANOVA for a foll data.

TYPE	observation			
	A	B	C	D
A	50, 52			
B		53, 55, 53		
C			60, 58, 57, 56	
D				52, 54, 54, 55

H₀: The 'mean' are equal of A, B, C, D

X₁ = ((50, 52))

X₂ = ((53, 55, 53))

X₃ = ((60, 58, 57, 56))

X₄ = ((52, 54, 54, 55))

```

> d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
> names(d)
[1] "values" "ind"
> oneway.test(values~ind, data=d, var.equal=T)
one-way analysis of means

data: values and ind
F = 11.735, num df = 3, denom df = 9, p-value = 0.01837

```

	df	sum	mean	sq	F value	Pr(>F)
ind	3	71.06	23.688	11.73	0.001837	
residuals	9	19.17	2.019			
						--

signif. codes: 0 '***' 0.001 '**' 0.05 '*' 0.1 '.'

> pvalue > 0.05, hence we reject

Q4 The full data gives the life of the tyres of 4 brands.

Type	Life
a	20, 28, 18, 17, 18, 22, 24
b	19, 15, 17, 20, 16, 17
c	21, 19, 22, 17, 20
d	15, 14, 16, 14, 14, 16

11. Average life of tyres are equal.

$x_1 = \{20, 23, 18, 17, 18, 22, 24\}$
 $x_2 = \{19, 15, 17, 20, 16, 17\}$
 $x_3 = \{21, 19, 22, 17, 16, 17\}$
 $x_4 = \{15, 14, 16, 14, 14, 16\}$

```

d = stack(list(b1=x1, b2=x2, b3=x3, b4=x4))
names(d)
[1] "values" "ind"
[1] "one-way" "analysis" "of" "means"
data: values and ind
P = 3.2464 | num df = 3 | denom df = 18,
p-value = 7.45e-11

```

Q5

$x = read.csv("C:/Users/Administrator/Desktop/mark8.csv")$
 $\rightarrow print(x)$

STATISTICS & MATHEMATICS
03/06/18

AY
20-21

78

40r
625

maths

0
8
17
0
5
7
1

)

H(p)

tg)

Practical - 10

(where parent value is not given).

Aim:- Non-parametric test.

Q1) Following are the amounts of sulphur oxides emitted by some industry in 20 days.

Applied sign test to HST the hypothesis that the population median is 21.5 at 5% LOS.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24

14, 15, 23, 24, 26.

H_0 : Population median is 21.5

$x = ((17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20), 17, 6,$
 $24, 14, 15, 23, 24, 26)$

$> m_e = 21.5$

$> s_p = \text{length}(x[x > m_e])$

$> s_n = \text{length}(x[x < m_e])$

$> n = s_p + s_n$

$> p$

[1] 20

$> p_v = \text{pbinom}(s_p, n, 0.5)$

$> p_v [1] 0.4119015$

\Rightarrow P-value > 0.05 , hence we accept the H_0 .

NOTE:- If the alternative is $m_e \neq$ or $m_e <$

$H_1: m_e >$

$> v = \text{pbinom}(s_n, n, 0.5)$

Q2) Following is the data of 10 observations sign test to HST the hypothesis that the population median is 62.5 against the hypothesis that the population median is more than 62.5 at 5% LOS.

79

$H_0:$

$x = ((612, 619, 631, 628, 643, 640, 655, 649, 670,$
 $663))$

H_0 : Population median is 62.5.

$s_p = \text{length}(x[x > m_e])$

$s_n = \text{length}(x[x < m_e])$

$n = s_p + s_n$

[1] 10

$> p_v = \text{pbinom}(s_p, n, 0.5)$

[1] 0.0546875

$> \text{p.value} > 0.05$ Hence we accept the val.

Q3) Following are the values of a sample. Test the hypothesis that the population median is 60 against the alternative, it is more than 60 at 5% LOS, using wilcoxon signed rank test.

H_0 : Population median is 60.

$x = ((63, 65, 60, 89, 61, 71, 58, 51, 69, 62, 63, 39,$
 $72, 69, 48, 66, 72, 63, 67, 69))$

$> \text{wilcox.test}(x, alt = "greater", mu = 60)$

65

wilcoxon signed rank test with continuity correction

data: x

v = 145, p-value = 0.02298

alternative hypothesis: true location is greater than 60

p-value < 0.05 we reject the H_0

NOTE: if the alternative $<$ - altv = "less"
alternative \neq altv = "two.sided"

(Q4)

using WSRT ; test the population median is 12 or less than 12

x = c(15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26)

> wilcox.tst(x, altv = "less", mu = 12)

wilcoxon signed rank test with continuity correction

data: x

v = 66, p-value = 0.9986

alternative hypothesis: true location is less than 12

p-value > 0.05 we accept H_0

The weights of a student stopped smoking before and after WSRT test that there is no significant change.

weights before	weights after
65	72
75	74
75	72
62	66
72	73

H_0 : Before & After there is no change

H_1 : change

x = c(65, 75, 75, 62, 72)

y = c(72, 74, 72, 66, 73)

wilcox.tst(d, altv = "two.sided", mu = 0)

wilcoxon signed rank test with continuity correction

data: d

v = 4.5, p-value = 0.4982

alternative hypothesis: true location is not equal to 0.

$p < 0.05$, we accept H_0 .

AM
51.02%