

Learning outcomes

At the end of this chapter, Learners will:

- Find the total surface area of cylinder and triangular prism
- Calculate the volume of cylinder and triangular prism
- Describe density
- Calculate density of regular objects

CONCISE INFORMATION

Total Surface Area of Cylinder and Triangular prism

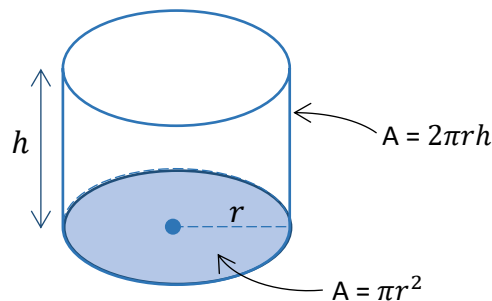
The Total Surface Area (T.S.A) of a cylinder is given by:

(a) Open Cylinder

The total surface area of an open cylinder is the sum of a circle and the curved surface.

$$\text{T.S.A} = \pi r^2 + 2\pi rh \text{ for an open cylinder}$$

$$\text{T.S.A} = \pi r(r + 2h)$$



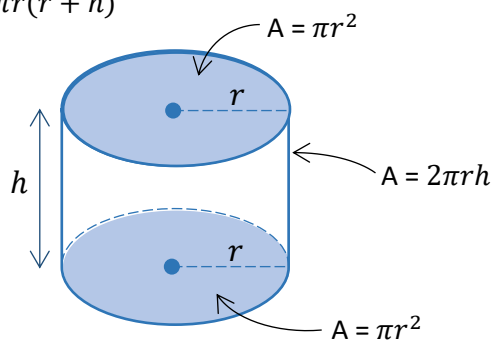
(b) Closed Cylinder

The total surface area of a closed cylinder is the sum of the two congruent circles and the curved surface.

$$\text{T.S.A} = \pi r^2 + \pi r^2 + 2\pi rh \text{ for an closed cylinder}$$

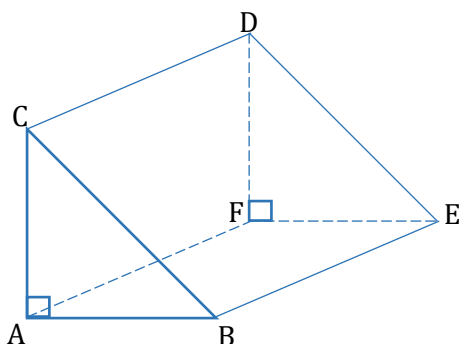
$$\text{T.S.A} = 2\pi r^2 + 2\pi rh$$

$$\text{T.S.A} = 2\pi r(r + h)$$



(c) Triangular prism

The total surface area is the sum of the two congruent triangles and the three rectangles.



Note:

The two congruent triangles are $\triangle ABC$ and $\triangle FED$.

The three rectangles are $ACDF$, $BCDE$ and $ABEF$.

$$\begin{aligned} \text{T.S.A} &= \text{Area of two congruent triangles} + \text{Area of three rectangles} \\ &= 2 \left(\frac{1}{2} \times AB \times BC \right) + \text{Area of } ACDF + \text{Area of } BCDE + \text{Area of } ABEF \end{aligned}$$

Volume of Cylinder and Triangular Prism

(a) *Cylinder*

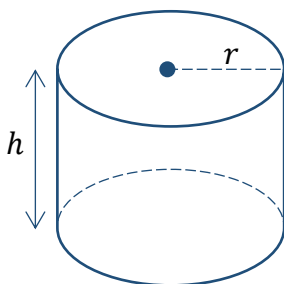
The volume of a cylinder is given by:

Volume = *Base Area* \times *Perpendicular Height*

Or

Volume = *Cross sectional Area* \times *Perpendicular Height*

$$\text{Volume} = \pi r^2 h$$



(b) *Triangular Prism*

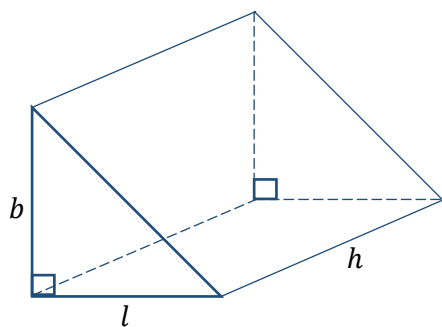
The volume of a triangular prism is given by:

Volume = *Base Area* \times *Perpendicular Height*

Or

Volume = *Cross sectional Area* \times *Perpendicular Height*

$$\text{Volume} = \frac{1}{2} \times l \times b \times h$$



Note:

The cross sectional (base) area in a triangular prism is covered by a triangle.

where,

l is the length of the triangle

b is the breadth of the triangle

h is the perpendicular height of the prism

Density of regular objects

The density of an object or a solid is the ratio of its mass to the volume. It is the amount mass per unit volume. Thus density is given by:

$$\text{Density} = \frac{\text{Mass}}{\text{Volume}}$$

Alternatively,

$$\text{Mass} = \text{Density} \times \text{Volume}$$

Or

$$\text{Volume} = \frac{\text{Mass}}{\text{Density}}$$