

## Problem 1

### 1.a.

Transition probability matrix:

```
[[ 0.5  0.5  0. ]
 [ 0.25 0.5  0.25]
 [ 0.   0.5  0.5 ]]
```

Transition probabilities after 2 steps

```
[[ 0.375 0.5  0.125]
 [ 0.25  0.5  0.25 ]
 [ 0.125 0.5  0.375]]
```

Transition probabilities after 5 steps

```
[[ 0.26562 0.5  0.23438]
 [ 0.25    0.5  0.25    ]
 [ 0.23438 0.5  0.26562]]
```

Transition probabilities after 10 steps

```
[[ 0.25049 0.5  0.24951]
 [ 0.25    0.5  0.25    ]
 [ 0.24951 0.5  0.25049]]
```

Transition probabilities after 25 steps

```
[[ 0.25 0.5  0.25]
 [ 0.25 0.5  0.25]
 [ 0.25 0.5  0.25]]
```

### 1.b.

Transition probability matrix with absorbing states:

```
[[ 1.   0.   0. ]
 [ 0.25 0.5  0.25]
 [ 0.   0.   1. ]]
```

Transition probabilities after 2 steps

```
[[ 1.   0.   0. ]
 [ 0.375 0.25 0.375]
 [ 0.   0.   1. ]]
```

Transition probabilities after 5 steps

```
[[ 1.   0.   0. ]
 [ 0.48438 0.03125 0.48438]
 [ 0.   0.   1. ]]
```

Transition probabilities after 10 steps

```
[[ 1.   0.   0. ]
 [ 0.49951 0.00098 0.49951]
 [ 0.   0.   1. ]]
```

Transition probabilities after 25 steps

```
[[ 1.   0.   0. ]
 [ 0.5  0.   0.5]
 [ 0.   0.   1. ]]
```

If a rat starts in room B it will end up in room A with probability .5 and room C with probability .5.

### 1.c.

After 84 iterations the rat has is in Room A with probability over 95% regardless of starting state. By 125<sup>th</sup> iteration that probability is over 99% regardless of starting state. In the limit, the rat will always end up in room A.

Transition probability matrix:

```
[[ 1.    0.    0.    0.    0. ]
 [ 0.25  0.5   0.25  0.    0. ]
 [ 0.    0.25  0.5   0.25  0. ]
 [ 0.    0.    0.25  0.5   0.25]
 [ 0.    0.    0.    0.5   0.5 ]]
```

Transition probabilities after 84 iterations:

```
[[ 1.    0.    0.    0.    0. ]
 [ 0.98153 0.00281 0.0052 0.00679 0.00367]
 [ 0.96587 0.0052 0.0096 0.01255 0.00679]
 [ 0.9554 0.00679 0.01255 0.01639 0.00887]
 [ 0.95173 0.00735 0.01358 0.01774 0.0096 ]]
```

Transition probabilities after 125 iterations:

```
[[ 1.    0.    0.    0.    0. ]
 [ 0.99624 0.00057 0.00106 0.00138 0.00075]
 [ 0.99305 0.00106 0.00196 0.00256 0.00138]
 [ 0.99091 0.00138 0.00256 0.00334 0.00181]
 [ 0.99017 0.0015 0.00277 0.00361 0.00196]]
```

## Problem 2.

a.

Transition probability matrix:

```
      0      1
0      0.876158  0.123842
1      0.428688  0.571312
```

b.

### Logit Regression Results

```
=====
Dep. Variable:      union      No. Observations:      21766
Model:              Logit      Df Residuals:      21758
Method:              MLE       Df Model:      7
Date:                Sat, 25 Oct 2014      Pseudo R-squ.:      0.1847
Time:                17:27:04      Log-Likelihood:      -9462.5
converged:           True       LL-Null:      -11606.
LLR p-value:         0.000
=====
```

	coef	std err	z	P> z	[95.0% Conf. Int.]
Intercept	-2.2960	0.385	-5.959	0.000	-3.051 -1.541
prior_union	2.1210	0.038	56.117	0.000	2.047 2.195
year	-0.0114	0.007	-1.700	0.089	-0.024 0.002
age	0.0237	0.006	3.846	0.000	0.012 0.036
grade	0.0464	0.008	5.911	0.000	0.031 0.062
south	-0.6630	0.042	-15.734	0.000	-0.746 -0.580
black	0.5797	0.043	13.404	0.000	0.495 0.664
smsa	0.0476	0.043	1.099	0.272	-0.037 0.132

```
=====
```

c., d., e.

Parts c. and d. do not ask for output. Steps shown in code file.

Markov transition matrix using the logistic model:

```
0.87142  0.12858
0.46298  0.53702
```

f.

Steady state distribution:

```
0.78264  0.21736
```

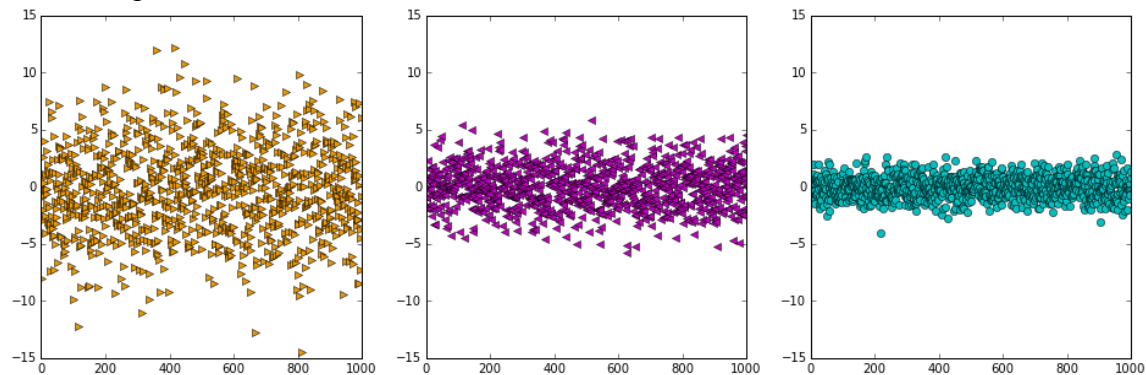
0.78264 0.21736

Data are probably available to compare the model's prediction to real outcomes. During a short search I could not find a summary of NLSW data that came from the same or similar source as the data we are given. Unsummarized NLSW data are available up to year 2003, but I wasn't confident I could aggregate and meaningfully summarize them to check prediction error.

### Problem 3.

#### 3.a.

The three plots below are of random normal vectors with variances 4, 2, and 1.



#### 3.b.

For this exercise I thought it would be fun to get a very low P-value, so I did not set seed and ran the code until I got the OLS with a P-value below 0.05. Naturally, it occurs about 5% of the time, so it didn't take long.

```

=====
                        OLS Regression Results
=====
Dep. Variable:          y      R-squared:                0.008
Model:                  OLS    Adj. R-squared:            0.007
Method:                 Least Squares    F-statistic:          8.435
Date:                   Sat, 25 Oct 2014    Prob (F-statistic):    0.00376
Time:                   18:33:53    Log-Likelihood:       -1460.1
No. Observations:      1000    AIC:                  2924.
Df Residuals:          998    BIC:                  2934.
Df Model:               1
=====

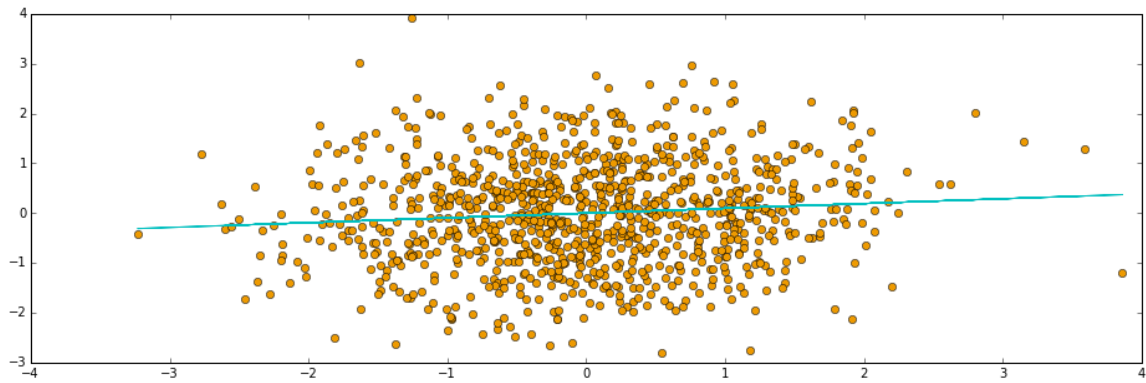
```

	coef	std err	t	P> t	[95.0% Conf. Int.]	
const	-0.0014	0.033	-0.042	0.967	-0.066	0.063
x1	0.0960	0.033	2.904	0.004	0.031	0.161

```

=====
Omnibus:                2.243    Durbin-Watson:          2.051
Prob(Omnibus):           0.326    Jarque-Bera (JB):        2.315
Skew:                    0.105    Prob(JB):                 0.314
Kurtosis:                2.894    Cond. No.                 1.02
=====

```

**3.c.**

Since all of the OLS conditions are met, the slope coefficients have a t-distribution. The histogram is consistent with a t-distribution.

