

# MANTRA — Manifold-Aware Network TRAI Model

---

A research-grade framework for **geometry-aware gene regulatory modeling** using:

- **EGGFM** (Energy-Guided Geometric Flow Model) to learn a *cell-state manifold* from unperturbed K562 cells
- **GNN-based GRN propagation** for regulator → gene → program → trait inference
- **cNMF program discovery** for gene programs
- **SMR-derived trait readout vectors**
- A systematic **ablation pipeline** evaluating manifold constraints, GRN structure, HVG choices, and embedding choice (HVG expression vs PCA-50, etc.).

This README is designed for new researchers, LLM agents, or collaborators who need a **full conceptual overview** of the system architecture, motivations, inductive biases, and experimental protocol.

---

## 1. Scientific Context

The central objective of MANTRA is to model how **perturbations to gene regulators propagate through the gene regulatory network (GRN), alter cellular programs, and ultimately impact hematopoietic traits** (MCH, RDW, IRF).

We integrate two main data sources:

1. **GWPS (Regulator →  $\Delta$ Gene expression)**

Provides causal  $\beta$ -like effects of targeted regulator perturbations on downstream gene expression ( $\Delta E$ ).

2. **SMR RBC trait genetics (Gene → trait effect sizes)**

Provides trait-weight vectors learned from human genetic burden studies, mapping gene expression shifts to trait shifts.

These together enable a *predictive causal chain*:

**Regulator →  $\Delta$ Expression →  $\Delta$ Programs →  $\Delta$ Traits**

The core MANTRA innovation is adding a **manifold constraint** so that predicted  $\Delta E$  respects the geometry of actual transcriptomic variation learned from **unperturbed** K562 cell states.

---

## 2. Overall Architecture

### 2.1 Conceptual pipeline

```

Regulator
  ↓ (GWPS  $\Delta E$ )
Predicted  $\Delta$ Gene Expression ( $\Delta E$ )
  ↓ (optional manifold regularization via EGGFM)
Geometry-constrained  $\Delta E$ 
  ↓ (cNMF  $W^T$ )
 $\Delta$ Program Activity ( $\Delta a$ )
  ↓ (SMR-derived  $\theta^{\text{trait}}$ )
 $\Delta$ Trait Prediction
  
```

Each layer is **separately testable** and participates in ablation experiments.

## 3. EGGFM: Geometry Learning on Unperturbed K562

EGGFM is trained via **denoising score matching (DSM)** on *unperturbed* (non-targeting control) K562 cells.

It learns a smooth energy function ( $E(x)$ ) whose gradient ( $-\nabla E(x)$ ) acts as a **score field** and induces a **geometry / metric** on the cell-state manifold.

You can train EGGFM either on **HVG expression** (`ad.X` in the HVG-restricted space) or directly in a **precomputed embedding** stored in `ad.obsm` (e.g. `"X_pca"` or `"X_diffmap"`). This allows a clean comparison between:

- EGGFM in raw HVG space, versus
- EGGFM on top of a classical embedding (e.g. PCA-50).

### 3.1 HVG selection and ablations

We start from a QC'd K562 AnnData with  $\sim 3k$  HVGs annotated. We then subselect smaller HVG panels for EGGFM:

- $HVG \in \{50, 75, 100, 150, 200, 250, 500, 3000\}$

Empirically:

- Very large HVG counts ( $>500$ – $3000$ ) yield unstable DSM optimization and noisy geometry.
- Moderately sized HVG panels ( $\approx 75$ – $150$ ) provide a good tradeoff between:
  - expressiveness
  - stable DSM loss
  - computational tractability
  - reduced curvature pathologies

We currently focus on **HVG=75** and **HVG=100** as main EGGFM spaces, and compare them via:

- DSM loss curves
- Downstream GRN training behavior (expr vs geo loss)

One of these will be chosen as the **baseline HVG space**; the other remains as an explicit ablation.

Typical DSM hyperparameters (in `configs/params.yml` under `eggfm_model` / `eggfm_train`):

- $\sigma$  (**DSM noise scale**)  $\sim 0.15$ – $0.2$
- Hidden dimensions: e.g. `[256, 256]` MLP
- Early stopping on DSM loss with patience and min-delta

### 3.2 EGGFM outputs

Each `train_energy.py` run produces an EGGFM checkpoint:

- `state_dict` (EnergyMLP weights)
- `model_cfg` (hidden dims, etc.)
- `n_genes` (dimensionality of the feature space)
- `var_names` (HVG gene names used for this model)
- `mean`, `std` (standardization stats **in the chosen feature space**)
- `space` (e.g. "hvg" or "X\_pca")

Examples:

- `out/models/eggfm/eggfm_energy_k562_hvg_hvg75.pt`
- `out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt`
- `out/models/eggfm/eggfm_energy_k562_X_pca_hvg50.pt` (*EGGFM in PCA-50 space*)

These checkpoints are then used both as:

- **Energy priors** in the GRN loss (geometry term), and
- **Sources of HVG gene lists / feature names** for NPZ construction and cNMF alignment.

## 4. HVG Ablation Summary

Note: numbers below are indicative / in-progress; final values will be reported in the project report.

HVG Count	Training Stability	DSM Loss (rough)	Interpretability	Notes
3000	fails	$\sim 1e5$	too noisy	geometry not learned
500	fails early	$\sim 1e4$	unstable	curvature too high
250	moderate	$\sim 3.8e3$	decent	borderline
200	good	$\sim 2.9e3$	strong	viable
150	very good	$\sim 2.0e3$	excellent	strong candidate

HVG Count	Training Stability	DSM Loss (rough)	Interpretability	Notes
100	very strong	~1.2e3	excellent	good coverage + stability
75	extremely good	~8.3e2	very good	slightly lower gene coverage
50	over-simplified	~4.3e2	poor coverage	geometry too compressed

We keep **HVG=75** and **HVG=100** as main baselines, and explicitly compare:

- DSM loss curves
- GRN training loss decomposition (expr vs geo vs prog)
- Downstream  $\Delta$ Trait performance.

## 5. Dimensionality Reductions & Embedding Ablations

After QC and HVG extraction (3k HVGs), we compute several **manifold baselines** on the HVG subset using `scripts/hvg_embed.py`. These embeddings are stored in `.obs` of:

- `data/interim/k562_gwps_unperturbed_hvg_embeddings.h5ad`

### 5.1 Included views in `.obs`

- `X_hvg_trunc` — raw expression of top-k HVGs (e.g. 150)
- `X_pca` — Scanpy PCA (e.g. 20 or 50 PCs)
- `X_diffmap` — Diffusion Map (20D)
- `X_umap` — UMAP on PCA space (20D)
- `X_phate` — PHATE (optional, if installed)
- `X_isomap` — Isomap (optional, slower)
- `X_spectral` — Laplacian eigenmaps (optional)

### 5.2 Excluded / future work

- **Dcol PCA** — too slow at this scale for now
- **Palantir** — pseudotime, not a pure embedding

These embeddings serve as **comparison manifolds** for:

- GRN propagation
- Trait prediction
- Geometry quality metrics (ARI, kNN overlap, geodesic distortion)

## 6. GRN Model (Regulator → Gene GNN)

A lightweight GNN (**GRNGNN**) propagates regulator effects through the gene network.

**Inputs per sample** (from NPZ):

- **reg\_idx** — index of the perturbed regulator
- **deltaE** — regulator-level  $\Delta E$  in HVG space  $[N, G]$
- **deltaP\_obs** — observed  $\Delta$ Program activity, if  $W$  is provided
- **deltaY\_obs** — observed  $\Delta$ Trait (currently stubbed)
- **dose** — dummy 0.0 for K562 (no explicit dose modeling yet)

**Architecture:**

- Gene embeddings (learned)
- Multi-layer message passing using adjacency  $A \in \mathbb{R}^{G \times G}$
- Optional **TraitHead** on top of program space

The GRN model is trained with a composite loss:

- **Expression term** ( $L_{\text{expr}}$ ):  $\Delta E$  reconstruction / fitting
- **Geometry term** ( $L_{\text{geo}}$ ): encourages  $\Delta E$  predictions to lie in low-energy regions under EGGFM
- **Program term** ( $L_{\text{prog}}$ ): consistency with  $\Delta P_{\text{obs}}$  via  $W$
- **Trait term** ( $L_{\text{trait}}$ ): trait supervision once  $\Delta$ Trait labels are wired

Ablations test:

1. **Vanilla GRN** (no geometry term)
2. **GRN + EGGFM geometry prior**
3. **GRN + alternate manifolds** (e.g. PCA-50 vs raw HVG)
4. **Geometry-only baselines** (no GRN).

## 7. Trait Mapping (cNMF Programs + SMR)

We run **consensus NMF (cNMF)** on **unperturbed QC cells** to learn program loadings  $W$ .

We intentionally **align the gene space to the EGGFM HVG space** by using the EGGFM checkpoint's **var\_names** and subsetting the QC AnnData before running cNMF. This guarantees:

- Rows of  $W$  correspond exactly to the genes and order used by  $\Delta E$  and the energy prior.

### 7.1 cNMF outputs

For a given HVG space (e.g. 75 or 100 genes), cNMF produces:

- **W\_consensus.npy** —  $[G, K]$  consensus gene-program loadings
- **programs\_all.npy** — stacked program vectors across runs  $[R \times K, G]$
- **cluster\_labels.npy** — cluster assignment per run-program
- optional: **program\_counts.npy**, **run\_coverage.npy** for stability diagnostics

- `genes.npy`, `cells.npy` — the gene and cell IDs used
- `manifest.yml` — lightweight YAML manifest with shapes, RMSE per run, etc.

We store these under e.g.:

- `out/programs/k562_hvg75_*`
- `out/programs/k562_hvg100_*`

$W$  is used to map  $\Delta E \rightarrow \Delta \text{Program activity}$ :

$$[\Delta a = W^{\text{top}} \Delta E.]$$

## 7.2 Trait readout via SMR

Trait vectors  $\theta^{(t)}$  (per trait  $t \in \{\text{MCH, RDW, IRF}\}$ ) are derived from SMR:

- SMR yields **gene-level trait effects**.
- We regress these onto  $W$  to obtain trait weight vectors in program space:

$$[g^{(t)} \approx W \theta^{(t)}.]$$

Predicted trait deltas:

$$[\widehat{\Delta \text{Trait}}^{(t)} = \langle \theta^{(t)}, \Delta a \rangle.]$$

cNMF hyperparameters live in `configs/params.yml` under a dedicated `cnmf` block.

## 8. NPZ Construction (Streaming GWPS $\rightarrow \Delta E$ NPZs)

Because the K562 GWPS file (`data/raw/k562_gwps.h5ad`) is large ( $\sim 2\text{M}$  cells), we construct **NPZ datasets** via a streaming script:

- `scripts/make_grn_npz.py`

For a given EGGFM checkpoint (which defines the HVG gene list), we:

1. Load the checkpoint and extract `var_names` (HVG genes).
2. Map these genes into `raw.var_names` of `k562_gwps.h5ad`.
3. Apply QC on **per-cell obs** (e.g. `mitopercent`, `UMI_count`).
4. Split cells into **control** (`reg == 'non-targeting'`) vs **perturbed**.
5. Compute a **global control mean** in HVG space.
6. For each regulator  $r$  with enough QC'd cells:
  - Average its perturbed cells in HVG space  $\rightarrow (x_r)$
  - Compute  $\Delta E_r = x_r - \bar{x}_{\text{ctrl}}$
7. Optionally map  $\Delta E \rightarrow \Delta P_{\text{obs}}$  via  $W$  (if `--cnmf-W` is passed).
8. Stub  $\Delta Y_{\text{obs}}$  for trait deltas (later replaced by real trait labels).
9. Split into train/val and write NPZs:

- `data/interim/grn_k562_gwps_hvg75_npz/{train.npz, val.npz}`
- `data/interim/grn_k562_gwps_hvg100_npz/{train.npz, val.npz}`

Each NPZ contains:

- `reg_idx` — regulator indices (int64)
- `deltaE` —  $\Delta E$  [N, G] (float32)
- `deltaP_obs` —  $\Delta P_{\text{obs}}$  [N, K] if `W` provided, else  $\Delta E$
- `deltaY_obs` —  $\Delta \text{Trait stubs}$  [N, T]
- `dose` — dummy (0.0) for K562 (no dose modeling)

## 9. Ablation Matrix

We evaluate a **2×2 GRN × Manifold grid**, plus HVG and embedding ablations:

		Manifold Constraint?	
		No	Yes
GRN?			
No		Program-only baseline	Manifold-smoothed $\Delta E$
Yes		GRN baseline ( $\Delta E$ )	GRN + EGGFM (full model)

Additional axes:

- **HVG ablations:** 75 vs 100
- **Embedding ablations:** raw HVG vs PCA-50 EGGFM
- **$\sigma$  (noise) ablations**
- **Model-depth ablations** (GNN layers, hidden dims).

## 10. Repository Structure

```
data/  
  raw/  
    k562_gwps.h5ad          # Full perturbed + control GWPS  
  (backed)  
  interim/  
    k562_gwps_unperturbed_qc.h5ad  # QC'd non-targeting controls, 3k  
HVGs  
    k562_gwps_unperturbed_hvg_embeddings.h5ad  
                                          # PCA, DiffMap, UMAP, PHATE, etc.  
  grn_k562_gwps_hvg75_npz/  
    train.npz  
    val.npz  
  grn_k562_gwps_hvg100_npz/  
    train.npz  
    val.npz  
out/  
  models/  
    eggfm/  
      eggfm_energy_k562_hvg_hvg75.pt  
      eggfm_energy_k562_hvg_hvg100.pt  
      eggfm_energy_k562_X_pca_hvg50.pt  # PCA-50 EGGFM ablation
```

```

    grn/
      hvg75/
        grn_k562_energy_prior.pt
      hvg100/
        grn_k562_energy_prior.pt
  programs/
    k562_hvg75_W_consensus.npy
    k562_hvg100_W_consensus.npy
  configs/
    params.yml
    env.yml
  scripts/
    qc.py                # QC + HVG selection on raw GWPS
    hvg_embed.py         # PCA / DiffMap / UMAP / PHATE on HVGs
    train_energy.py      # EGGFM (HVG or embedding space)
    make_grn_npz.py      # Streaming  $\Delta E$  NPZ construction
    cnmf_programs.py     # cNMF program discovery (W aligned to EGGFM genes)
    train_grn.py         # GRN GNN training with energy prior
  src/
    mantra/
      eggfm/             # EGGFM models, trainer, dataset, inference
      grn/               # GRN GNN, priors, trainer, dataset
      programs/          # cNMF config + utilities
      embeddings/        # embedding config helpers
      qc/                # QC/provenance helpers
      utils/             # misc utilities

```

## 11. Current Status Summary

### Completed

- ✓ Full QC + HVG selection (3k HVGs) for unperturbed K562
- ✓ Dimensionality reductions computed (PCA, DiffMap, UMAP, PHATE, etc.)
- ✓ EGGFM training across HVG ablations (50-500, 3000)
- ✓ HVG=75 & HVG=100 identified as leading candidates
- ✓ Streaming NPZ construction ( $\Delta E$  per regulator) aligned to EGGFM HVG space
- ✓ cNMF program discovery wiring (W aligned with EGGFM HVGs)
- ✓ GRN training loop with energy prior and loss decomposition (expr / geo / prog / trait stubs)
- ✓ Repo packaging, CLI scripts, and config-driven reproducibility

### In Progress

- ⌚ Final comparison HVG-75 vs HVG-100 (DSM and GRN metrics)
- ⌚ PCA-50 EGGFM ablations (energy in PCA space)
- ⌚ Wiring real  $\Delta$ Trait targets and trait loss
- ⌚ Full GRN  $\times$  Manifold ablation grid

### Next Steps



1. Choose baseline HVG (75 vs 100) based on:
    - DSM loss curves
    - GRN loss behavior and generalization
  2. Train GRN with:
    - HVG-EGGFM prior
    - PCA-50 EGGFM priorand compare  $\Delta\text{Trait}$  performance.
  3. Produce figures:
    - DSM loss curves across HVGs
    - Embedding visualizations (PCA, DiffMap, UMAP, EGGFM)
    - Trait prediction scatter plots
    - Performance deltas vs ablations
  4. Integrate SMR-derived  $\theta^{\text{(trait)}}$  and evaluate end-to-end Reg  $\rightarrow \Delta\text{Trait}$ .
- 

## 12. How to Train Models (Canonical Commands)

### 12.1 QC + HVG selection (unperturbed controls)

```
python scripts/qc.py \  
  --params configs/params.yml \  
  --ad data/raw/k562_gwps.h5ad \  
  --out data/interim/k562_gwps_unperturbed_qc.h5ad \  
  --pet # restrict to non-targeting controls
```

### 12.2 Embeddings (PCA-50)

```
python scripts/hvg_embed.py \  
  --ad data/interim/k562_gwps_unperturbed_qc.h5ad \  
  --out data/interim/k562_gwps_unperturbed_hvg_embeddings.h5ad \  
  --n-components 50 \  
  --n-neighbors 30 \  
  --seed 7
```

### 12.3 Train EGGFM (HVG space; main DSM ablations)

```
# HVG = 75  
python scripts/train_energy.py \  
  --params configs/params.yml \  
  --ad data/interim/k562_gwps_unperturbed_qc.h5ad \  
  --out out/models/eggfm \  
  --space hvg  
  
# HVG = 100  
# (set eggfm_train.max_hvg: 100 in configs/params.yml before this run)  
python scripts/train_energy.py \  
  --space hvg
```

```
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
--out out/models/eggfm \
--space hvg
```

## 12.4 Train EGGFM (PCA-50 ablation)

```
python scripts/train_energy.py \
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_hvg_embeddings.h5ad \
--out out/models/eggfm \
--space X_pca
```

## 12.5 Build GRN NPZs ( $\Delta E$ per regulator)

```
# HVG 75 NPZ
python scripts/make_grn_npz.py \
--ad-raw data/raw/k562_gwps.h5ad \
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg75.pt \
--out-dir data/interim/grn_k562_gwps_hvg75_npz \
--reg-col gene \
--control-value non-targeting \
--max-pct-mt 0.2 \
--min-umi 2000 \
--min-cells-per-group 10 \
--val-frac 0.2 \
--seed 7

# HVG 100 NPZ
python scripts/make_grn_npz.py \
--ad-raw data/raw/k562_gwps.h5ad \
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt \
--out-dir data/interim/grn_k562_gwps_hvg100_npz \
--reg-col gene \
--control-value non-targeting \
--max-pct-mt 0.2 \
--min-umi 2000 \
--min-cells-per-group 10 \
--val-frac 0.2 \
--seed 7
```

## 12.6 Build W (cNMF programs) for HVG-75 and HVG-100

```
# HVG 75: build W aligned to the 75-gene EGGFM / NPZ space
python scripts/cnmf_programs.py \
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
```

```
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg75.pt \  
--out-prefix out/programs/k562_hvg75  
  
# HVG 100: build W aligned to the 100-gene EGGFM / NPZ space  
python scripts/cnmf_programs.py \  
--params configs/params.yml \  
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \  
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt \  
--out-prefix out/programs/k562_hvg100
```

## 12.7 Train GRN (GNN with energy prior)

```
# Example for HVG 100  
python scripts/train_grn.py \  
--params configs/params.yml \  
--out out/models/grn/hvg100 \  
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \  
--train-npz data/interim/grn_k562_gwps_hvg100_npz/train.npz \  
--val-npz data/interim/grn_k562_gwps_hvg100_npz/val.npz \  
--adj data/interim/A_k562_hvg100.npy \  
--cnmf-W out/programs/k562_hvg100_W_consensus.npy \  
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt
```

---

## 13. Citation Notes

If using this repo in research, please cite:

- GWPS foundational papers
- SMR methods for trait mapping
- cNMF / gene program discovery work
- Any future MANTRA preprint or publication

---

*End of README*