

# MANTRA — Manifold-Aware Network TRAit Model

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A research-grade framework for **geometry-aware gene regulatory modeling** using:

- **EGGFM** (Energy-Guided Geometric Flow Model) to learn a *cell-state manifold* from unperturbed K562 cells
- **GNN-based GRN propagation** for regulator → gene → program → trait inference
- **cNMF program discovery** for gene programs
- **SMR-derived trait readout vectors**
- A systematic **ablation pipeline** evaluating manifold constraints, GRN structure, HVG choices, and embedding choice (HVG expression vs PCA-50, etc.).

This README is designed for new researchers, LLM agents, or collaborators who need a **full conceptual overview** of the system architecture, motivations, inductive biases, and experimental protocol.

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## 1. Scientific Context

The central objective of MANTRA is to model how **perturbations to gene regulators propagate through the gene regulatory network (GRN), alter cellular programs, and ultimately impact hematopoietic traits** (MCH, RDW, IRF).

We integrate two main data sources:

### 1. GWPS (Regulator → ΔGene expression)

Provides causal β-like effects of targeted regulator perturbations on downstream gene expression ( $\Delta E$ ).

### 2. SMR RBC trait genetics (Gene → trait effect sizes)

Provides trait-weight vectors learned from human genetic burden studies, mapping gene expression shifts to trait shifts.

These together enable a *predictive causal chain*:

**Regulator → ΔExpression → ΔPrograms → ΔTraits**

The core MANTRA innovation is adding a **manifold constraint** so that predicted  $\Delta E$  respects the geometry of actual transcriptomic variation learned from **unperturbed** K562 cell states.

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## 2. Overall Architecture

### 2.1 Conceptual pipeline

```

Regulator
  ↓ (GWPS ΔE)
Predicted ΔGene Expression (ΔE)
  ↓ (optional manifold regularization via EGGFM)
Geometry-constrained ΔE
  ↓ (cNMF WT)
ΔProgram Activity (Δa)
  ↓ (SMR-derived θ^(trait))
ΔTrait Prediction

```

Each layer is **separately testable** and participates in ablation experiments.

## 3. EGGFM: Geometry Learning on Unperturbed K562

EGGFM is trained via **denoising score matching (DSM)** on *unperturbed* (non-targeting control) K562 cells.

It learns a smooth energy function ( $E(x)$ ) whose gradient ( $-\nabla E(x)$ ) acts as a **score field** and induces a **geometry / metric** on the cell-state manifold.

You can train EGGFM either on **HVG expression** (`ad.X` in the HVG-restricted space) or directly in a **precomputed embedding** stored in `ad.obsm` (e.g. "`X_pca`" or "`X_diffmap`"). This allows a clean comparison between:

- EGGFM in raw HVG space, versus
- EGGFM on top of a classical embedding (e.g. PCA-50).

### 3.1 HVG selection and ablations

We start from a QC'd K562 AnnData with ~3k HVGs annotated. We then subselect smaller HVG panels for EGGFM:

- HVG  $\in \{50, 75, 100, 150, 200, 250, 500, 3000\}$

Empirically:

- Very large HVG counts ( $>500$ -3000) yield unstable DSM optimization and noisy geometry.
- Moderately sized HVG panels ( $\approx 75$ -150) provide a good tradeoff between:
  - expressiveness
  - stable DSM loss
  - computational tractability
  - reduced curvature pathologies

We currently focus on **HVG=75** and **HVG=100** as main EGGFM spaces, and compare them via:

- DSM loss curves
- Downstream GRN training behavior (expr vs geo loss)

One of these will be chosen as the **baseline HVG space**; the other remains as an explicit ablation.

Typical DSM hyperparameters (in `configs/params.yml` under `eggfm_model` / `eggfm_train`):

- **$\sigma$  (DSM noise scale)** ~ 0.15-0.2
- Hidden dimensions: e.g. [256, 256] MLP
- Early stopping on DSM loss with patience and min-delta

### 3.2 EGGFM outputs

Each `train_energy.py` run produces an EGGFM checkpoint:

- `state_dict` (EnergyMLP weights)
- `model_cfg` (hidden dims, etc.)
- `n_genes` (dimensionality of the feature space)
- `var_names` (HVG gene names used for this model)
- `mean, std` (standardization stats **in the chosen feature space**)
- `space` (e.g. "hvg" or "X\_pca")

Examples:

- `out/models/eggfm/eggfm_energy_k562_hvg_hvg75.pt`
- `out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt`
- `out/models/eggfm/eggfm_energy_k562_X_pca_hvg50.pt` (*EGGFM in PCA-50 space*)

These checkpoints are then used both as:

- **Energy priors** in the GRN loss (geometry term), and
- **Sources of HVG gene lists / feature names** for NPZ construction and cNMF alignment.

## 4. HVG Ablation Summary

Note: numbers below are indicative / in-progress; final values will be reported in the project report.

HVG Count	Training Stability	DSM Loss (rough)	Interpretability	Notes
3000	fails	~1e5	too noisy	geometry not learned
500	fails early	~1e4	unstable	curvature too high
250	moderate	~3.8e3	decent	borderline
200	good	~2.9e3	strong	viable
150	very good	~2.0e3	excellent	strong candidate

HVG Count	Training Stability	DSM Loss (rough)	Interpretability	Notes
100	<b>very strong</b>	~1.2e3	<b>excellent</b>	good coverage + stability
75	<b>extremely good</b>	~8.3e2	very good	slightly lower gene coverage
50	over-simplified	~4.3e2	poor coverage	geometry too compressed

We keep **HVG=75** and **HVG=100** as main baselines, and explicitly compare:

- DSM loss curves
- GRN training loss decomposition (expr vs geo vs prog)
- Downstream ΔTrait performance.

## 5. Dimensionality Reductions & Embedding Ablations

After QC and HVG extraction (3k HVGs), we compute several **manifold baselines** on the HVG subset using `scripts/hvg_embed.py`. These embeddings are stored in `.obsm` of:

- `data/interim/k562_gwps_unperturbed_hvg_embeddings.h5ad`

### 5.1 Included views in `.obsm`

- `X_hvg_trunc` — raw expression of top-k HVGs (e.g. 150)
- `X_pca` — Scanpy PCA (e.g. 20 or 50 PCs)
- `X_diffmap` — Diffusion Map (20D)
- `X_umap` — UMAP on PCA space (20D)
- `X_phate` — PHATE (optional, if installed)
- `X_isomap` — Isomap (optional, slower)
- `X_spectral` — Laplacian eigenmaps (optional)

### 5.2 Excluded / future work

- **Dcol PCA** — too slow at this scale for now
- **Palantir** — pseudotime, not a pure embedding

These embeddings serve as **comparison manifolds** for:

- GRN propagation
- Trait prediction
- Geometry quality metrics (ARI, kNN overlap, geodesic distortion)

## 6. GRN Model (Regulator → Gene GNN)

A lightweight GNN (**GRNGNN**) propagates regulator effects through the gene network.

**Inputs per sample** (from NPZ):

- `reg_idx` — index of the perturbed regulator
- `deltaE` — regulator-level  $\Delta E$  in HVG space [N, G]
- `deltaP_obs` — observed  $\Delta P_{\text{Program}}$  activity, if W is provided
- `deltaY_obs` — observed  $\Delta T_{\text{Trait}}$  (currently stubbed)
- `dose` — dummy 0.0 for K562 (no explicit dose modeling yet)

**Architecture:**

- Gene embeddings (learned)
- Multi-layer message passing using adjacency  $A \in \mathbb{R}^{G \times G}$
- Optional **TraitHead** on top of program space

The GRN model is trained with a composite loss:

- **Expression term** ( $L_{\{\text{expr}\}}$ ):  $\Delta E$  reconstruction / fitting
- **Geometry term** ( $L_{\{\text{geo}\}}$ ): encourages  $\Delta E$  predictions to lie in low-energy regions under EGGFM
- **Program term** ( $L_{\{\text{prog}\}}$ ): consistency with  $\Delta P_{\text{obs}}$  via W
- **Trait term** ( $L_{\{\text{trait}\}}$ ): trait supervision once  $\Delta T_{\text{Trait}}$  labels are wired

Ablations test:

1. **Vanilla GRN** (no geometry term)
  2. **GRN + EGGFM geometry prior**
  3. **GRN + alternate manifolds** (e.g. PCA-50 vs raw HVG)
  4. **Geometry-only baselines** (no GRN).
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## 7. Trait Mapping (cNMF Programs + SMR)

We run **consensus NMF (cNMF)** on **unperturbed QC cells** to learn program loadings **W**.

We intentionally **align the gene space to the EGGFM HVG space** by using the EGGFM checkpoint's `var_names` and subsetting the QC AnnData before running cNMF. This guarantees:

- Rows of W correspond exactly to the genes and order used by  $\Delta E$  and the energy prior.

### 7.1 cNMF outputs

For a given HVG space (e.g. 75 or 100 genes), cNMF produces:

- `W_consensus.npy` — [G, K] consensus gene-program loadings
- `programs_all.npy` — stacked program vectors across runs [R\*K, G]
- `cluster_labels.npy` — cluster assignment per run-program
- optional: `program_counts.npy`, `run_coverage.npy` for stability diagnostics

- `genes.npy`, `cells.npy` — the gene and cell IDs used
- `manifest.yml` — lightweight YAML manifest with shapes, RMSE per run, etc.

We store these under e.g.:

- `out/programs/k562_hvg75_*`
- `out/programs/k562_hvg100_*`

$W$  is used to map  $\Delta E \rightarrow \Delta$ Program activity:

[  $\Delta a = W^T \Delta E$ . ]

## 7.2 Trait readout via SMR

Trait vectors  $\Theta^{(t)}$  (per trait  $t \in \{MCH, RDW, IRF\}$ ) are derived from SMR:

- SMR yields **gene-level trait effects**.
- We regress these onto  $W$  to obtain trait weight vectors in program space:

[  $g^{(t)} \approx W \Theta^{(t)}$ . ]

Predicted trait deltas:

[  $\widehat{\Delta a}^{(t)} = \langle \Theta^{(t)}, \Delta E \rangle$ . ]

cNMF hyperparameters live in `configs/params.yml` under a dedicated `cnmf` block.

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## 8. NPZ Construction (Streaming GWPS $\rightarrow \Delta E$ NPZs)

Because the K562 GWPS file (`data/raw/k562_gwps.h5ad`) is large (~2M cells), we construct **NPZ datasets** via a streaming script:

- `scripts/make_grn_npz.py`

For a given EGGFM checkpoint (which defines the HVG gene list), we:

1. Load the checkpoint and extract `var_names` (HVG genes).
2. Map these genes into `raw.var_names` of `k562_gwps.h5ad`.
3. Apply QC on **per-cell obs** (e.g. `mitopercent`, `UMI_count`).
4. Split cells into **control** (`reg == 'non-targeting'`) vs **perturbed**.
5. Compute a **global control mean** in HVG space.
6. For each regulator  $r$  with enough QC'd cells:
  - Average its perturbed cells in HVG space  $\rightarrow (x_r)$
  - Compute  $(\Delta E_r = x_r - \bar{x}_{ctrl})$
7. Optionally map  $\Delta E \rightarrow \Delta P_{obs}$  via  $W$  (if `--cnmf-W` is passed).
8. Stub  $\Delta Y_{obs}$  for trait deltas (later replaced by real trait labels).
9. Split into train/val and write NPZs:
  - `data/interim/grn_k562_gwps_hvg75_npz/{train.npz, val.npz}`
  - `data/interim/grn_k562_gwps_hvg100_npz/{train.npz, val.npz}`

Each NPZ contains:

- `reg_idx` — regulator indices (int64)
- `deltaE` —  $\Delta E$  [N, G] (float32)
- `deltaP_obs` —  $\Delta P_{obs}$  [N, K] if W provided, else  $\Delta E$
- `deltaY_obs` —  $\Delta Trait$  stubs [N, T]
- `dose` — dummy (0.0) for K562 (no dose modeling)

## 9. Ablation Matrix

We evaluate a **2×2 GRN × Manifold grid**, plus HVG and embedding ablations:

		Manifold Constraint?	
		No	Yes
GRN?	No	Program-only baseline	Manifold-smoothed $\Delta E$
	Yes	GRN baseline ( $\Delta E$ )	GRN + EGGFM (full model)

Additional axes:

- **HVG ablations:** 75 vs 100
- **Embedding ablations:** raw HVG vs PCA-50 EGGFM
- **$\sigma$  (noise) ablations**
- **Model-depth ablations** (GNN layers, hidden dims).

## 10. Repository Structure

```

data/
  raw/
    k562_gwps.h5ad                      # Full perturbed + control GWPS
  (backed)
    interim/
      k562_gwps_unperturbed_qc.h5ad      # QC'd non-targeting controls, 3k
HVGs
      k562_gwps_unperturbed_hvg_embeddings.h5ad
                                         # PCA, DiffMap, UMAP, PHATE, etc.
    grn_k562_gwps_hvg75_npz/
      train.npz
      val.npz
    grn_k562_gwps_hvg100_npz/
      train.npz
      val.npz
out/
  models/
    eggfm/
      eggfm_energy_k562_hvg_hvg75.pt
      eggfm_energy_k562_hvg_hvg100.pt
      eggfm_energy_k562_X_pca_hvg50.pt  # PCA-50 EGGFM ablation

```

```

grn/
  hvg75/
    grn_k562_energy_prior.pt
  hvg100/
    grn_k562_energy_prior.pt
programs/
  k562_hvg75_W_consensus.npy
  k562_hvg100_W_consensus.npy
configs/
  params.yml
  env.yml
scripts/
  qc.py          # QC + HVG selection on raw GWPS
  hvg_embed.py   # PCA / DiffMap / UMAP / PHATE on HVGs
  train_energy.py # EGGFM (HVG or embedding space)
  make_grn_npz.py # Streaming ΔE NPZ construction
  cnmf_programs.py # cNMF program discovery (W aligned to EGGFM genes)
  train_grn.py   # GRN GNN training with energy prior
src/
  mantra/
    eggfm/        # EGGFM models, trainer, dataset, inference
    grn/          # GRN GNN, priors, trainer, dataset
  programs/
  embeddings/
  qc/            # embedding config helpers
  utils/         # QC/provenance helpers
                # misc utilities

```

## 11. Current Status Summary

### Completed

- ✓ Full QC + HVG selection (3k HVGs) for unperturbed K562
- ✓ Dimensionality reductions computed (PCA, DiffMap, UMAP, PHATE, etc.)
- ✓ EGGFM training across HVG ablations (50–500, 3000)
- ✓ HVG=75 & HVG=100 identified as leading candidates
- ✓ Streaming NPZ construction ( $\Delta E$  per regulator) aligned to EGGFM HVG space
- ✓ cNMF program discovery wiring (W aligned with EGGFM HVGs)
- ✓ GRN training loop with energy prior and loss decomposition (expr / geo / prog / trait stubs)
- ✓ Repo packaging, CLI scripts, and config-driven reproducibility

### In Progress

- ⌚ Final comparison HVG-75 vs HVG-100 (DSM and GRN metrics)
- ⌚ PCA-50 EGGFM ablations (energy in PCA space)
- ⌚ Wiring real  $\Delta$ Trait targets and trait loss
- ⌚ Full GRN × Manifold ablation grid

### Next Steps

1. Choose baseline HVG (75 vs 100) based on:
    - DSM loss curves
    - GRN loss behavior and generalization
  2. Train GRN with:
    - HVG-EGGFM prior
    - PCA-50 EGGFM prior
    - and compare  $\Delta$ Trait performance.
  3. Produce figures:
    - DSM loss curves across HVGs
    - Embedding visualizations (PCA, DiffMap, UMAP, EGGFM)
    - Trait prediction scatter plots
    - Performance deltas vs ablations
  4. Integrate SMR-derived  $\theta^\wedge(\text{trait})$  and evaluate end-to-end Reg  $\rightarrow \Delta$ Trait.
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## 12. How to Train Models (Canonical Commands)

### 12.1 QC + HVG selection (unperturbed controls)

```
python scripts/qc.py \
--params configs/params.yml \
--ad data/raw/k562_gwps.h5ad \
--out data/interim/k562_gwps_unperturbed_qc.h5ad \
--pet # restrict to non-targeting controls
```

### 12.2 Embeddings (PCA-50)

```
python scripts/hvg_embed.py \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
--out data/interim/k562_gwps_unperturbed_hvg_embeddings.h5ad \
--n-components 50 \
--n-neighbors 30 \
--seed 7
```

### 12.3 Train EGGFM (HVG space; main DSM ablations)

```
# HVG = 75
python scripts/train_energy.py \
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
--out out/models/eggfm \
--space hvg

# HVG = 100
# (set eggfm_train.max_hvg: 100 in configs/params.yml before this run)
python scripts/train_energy.py \
```

```
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
--out out/models/eggfm \
--space hvg
```

## 12.4 Train EGGFM (PCA-50 ablation)

```
python scripts/train_energy.py \
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_hvg_embeddings.h5ad \
--out out/models/eggfm \
--space X_pca
```

## 12.5 Build GRN NPZs ( $\Delta E$ per regulator)

```
# HVG 75 NPZ
python scripts/make_grn_npz.py \
--ad-raw data/raw/k562_gwps.h5ad \
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg75.pt \
--out-dir data/interim/grn_k562_gwps_hvg75_npz \
--reg-col gene \
--control-value non-targeting \
--max-pct-mt 0.2 \
--min-umi 2000 \
--min-cells-per-group 10 \
--val-frac 0.2 \
--seed 7

# HVG 100 NPZ
python scripts/make_grn_npz.py \
--ad-raw data/raw/k562_gwps.h5ad \
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt \
--out-dir data/interim/grn_k562_gwps_hvg100_npz \
--reg-col gene \
--control-value non-targeting \
--max-pct-mt 0.2 \
--min-umi 2000 \
--min-cells-per-group 10 \
--val-frac 0.2 \
--seed 7
```

## 12.6 Build W (cNMF programs) for HVG-75 and HVG-100

```
# HVG 75: build W aligned to the 75-gene EGGFM / NPZ space
python scripts/cnmf.py \
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
```

```
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg75.pt \
--out out/programs/k562_hvg75

# HVG 100: build W aligned to the 100-gene EGGFM / NPZ space
python scripts/cnmf.py \
--params configs/params.yml \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt \
--out out/programs/k562_hvg100
```

## 12.7 Train GRN (GNN with energy prior)

```
# Example for HVG 100
python scripts/train_grn.py \
--params configs/params.yml \
--out out/models/grn/hvg100 \
--ad data/interim/k562_gwps_unperturbed_qc.h5ad \
--train-npz data/interim/grn_k562_gwps_hvg100_npz/train.npz \
--val-npz data/interim/grn_k562_gwps_hvg100_npz/val.npz \
--adj data/interim/A_k562_hvg100.npy \
--cnmf-W out/programs/k562_hvg100_W_consensus.npy \
--energy-ckpt out/models/eggfm/eggfm_energy_k562_hvg_hvg100.pt
```

## 13. Citation Notes

If using this repo in research, please cite:

- GWPS foundational papers
- SMR methods for trait mapping
- cNMF / gene program discovery work
- Any future MANTRA preprint or publication

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*End of README*