

```

(* Step *)

Quit[]

Off[General::spell1];
ψ1I = Exp[i k1 x];
ψ1R = BB Exp[-i k1 x];
ψ1 = ψ1I + ψ1R;
ψ2 = CC Exp[i k2 x];
ψ = Piecewise[{{ψ1, x < x1}, {ψ2, x1 ≤ x}}];
eqns = {ψ1 == ψ2 /. x → x1, ∂x ψ1 == ∂x ψ2 /. x → x1};

soln =
{BB, CC} = FullSimplify[{BB, CC} /. Solve[eqns, {BB, CC}], Assumptions → {x1 ∈ Reals}][[1]]
{  $\frac{e^{2 i k_1 x_1} (k_1 - k_2)}{k_1 + k_2}$ ,  $\frac{2 e^{i (k_1 - k_2) x_1} k_1}{k_1 + k_2}$  }

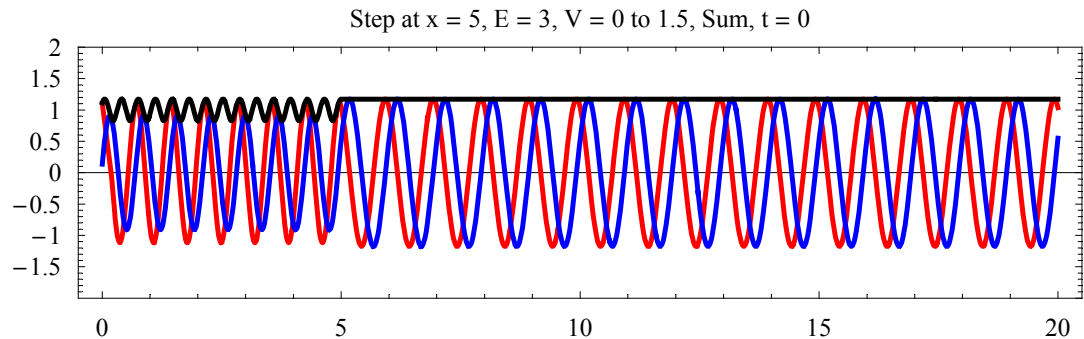
CForm[soln]

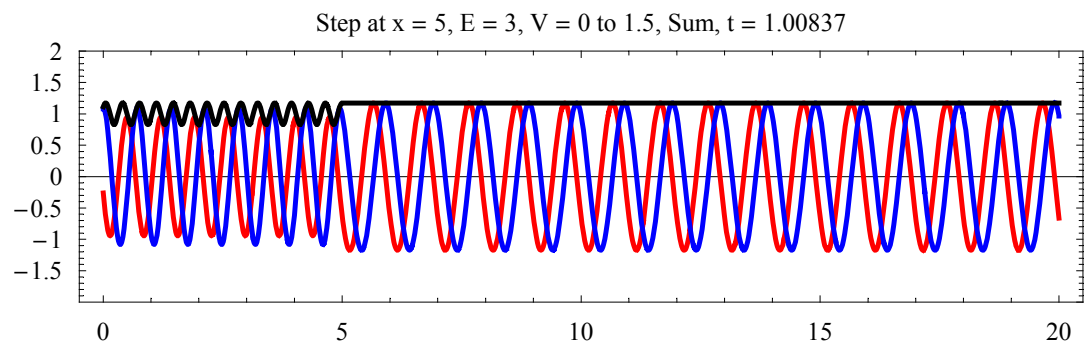
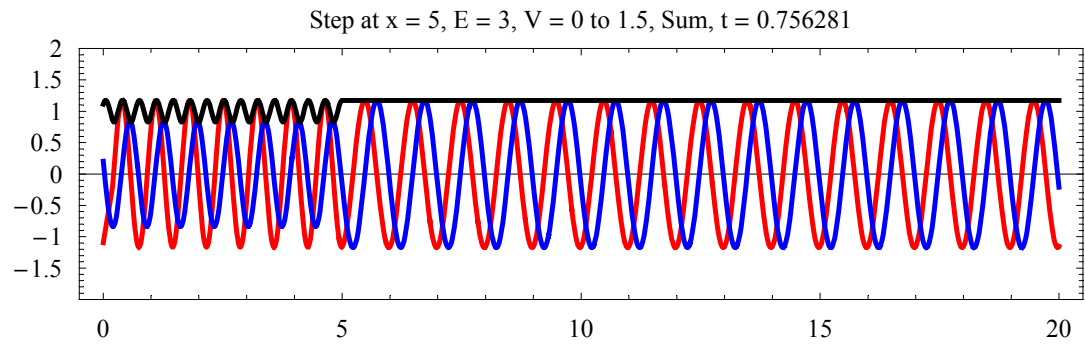
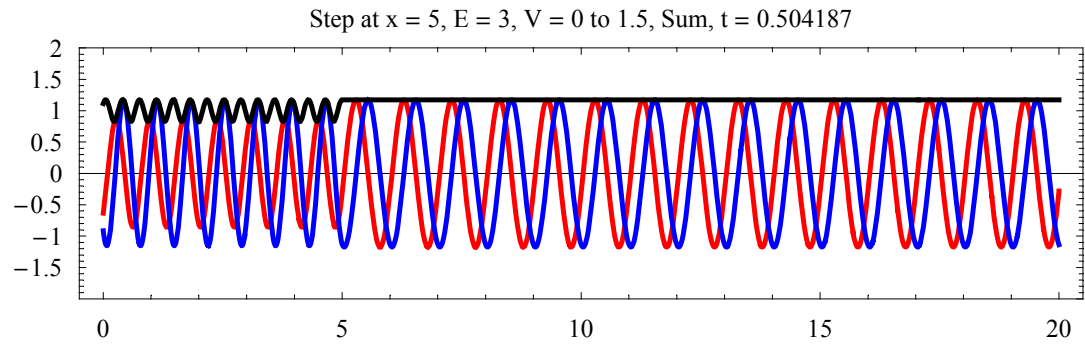
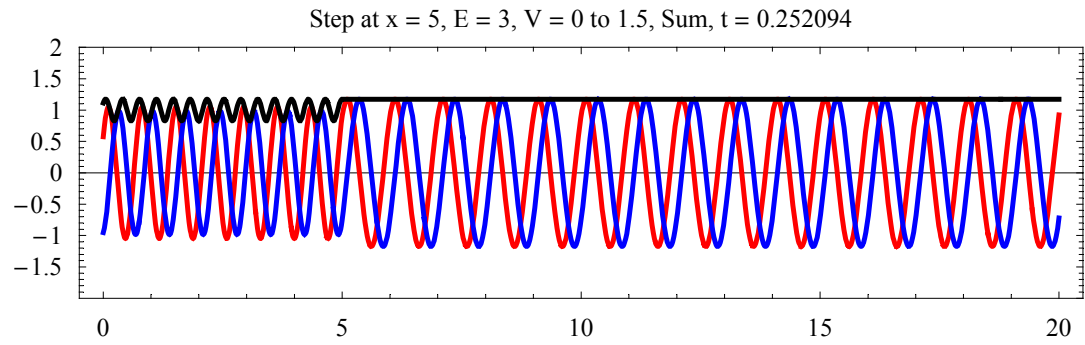
List((Power(E, 2*I*k1*x1)*(k1 - k2))/(k1 + k2), (2*Power(E, I*(k1 - k2)*x1)*k1)/(k1 + k2))

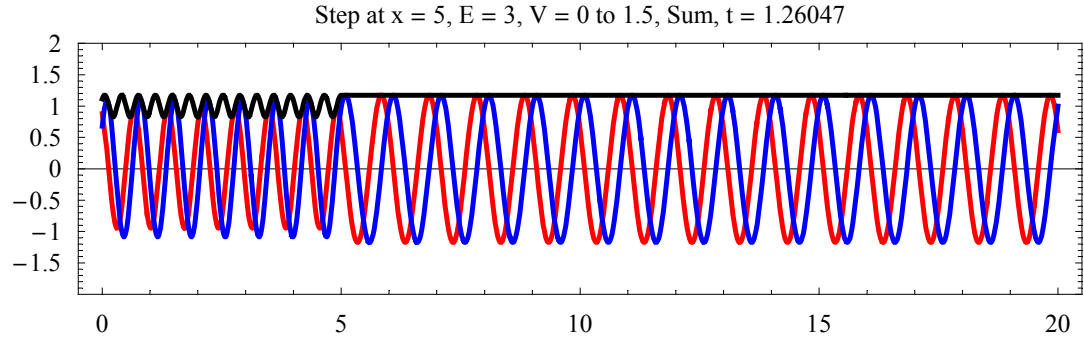
EE = 3; (* eV *)
V = 1.5; (* eV *)
m = 0.511*106 (hbar/197)2; (* eV/c2 *)
hbar = 0.658; (* eV fs *)
k1 =  $\sqrt{2 m EE / \hbar^2}$ ;
k2 =  $\sqrt{2 m (EE - V) / \hbar^2}$ ;
period = 2 π hbar / E;
x1 = 5;
$TextStyle = {FontFamily → "Times", FontSize → 12};

movie =
Table[Plot[{Re[ψ Exp[-i EE t / hbar]], Im[ψ Exp[-i EE t / hbar]], Abs[ψ Exp[-i EE t / hbar]]},
{x, 0, 20}, PlotRange → {-2, 2}, PlotPoints → 100, PlotStyle →
{{Thickness[0.005], Red}, {Thickness[0.005], Blue}, {Thickness[0.005], Black}},
PlotLabel → StringJoin["Step at x = 5, E = 3, V = 0 to 1.5, Sum, t = ",
ToString[t]], Frame → True, AspectRatio → 1 / 4, ImageSize → 9 * 72,
PlotPoints → 100], {t, 0, period - (period + 1) / 10, (period + 1) / 10}];

```

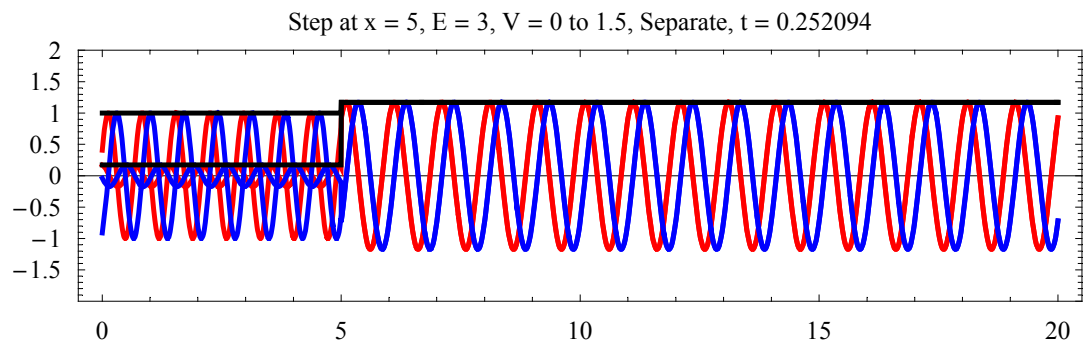
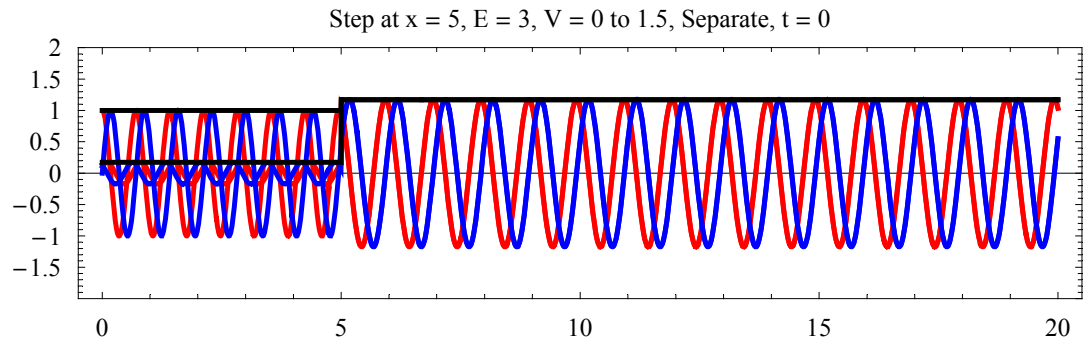


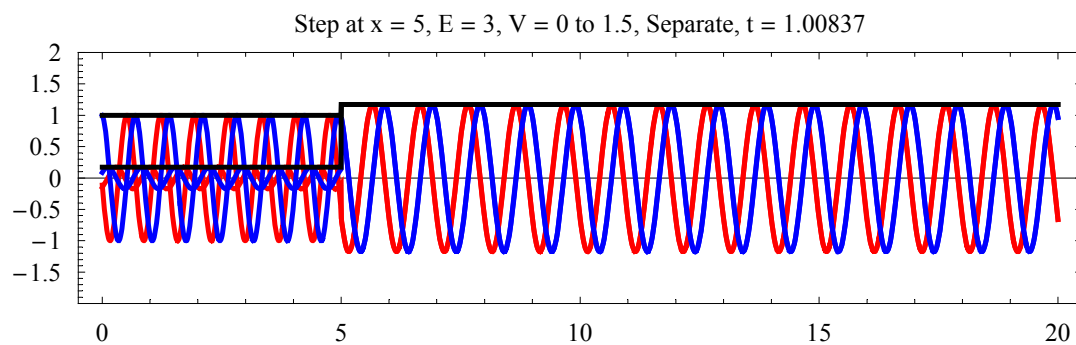
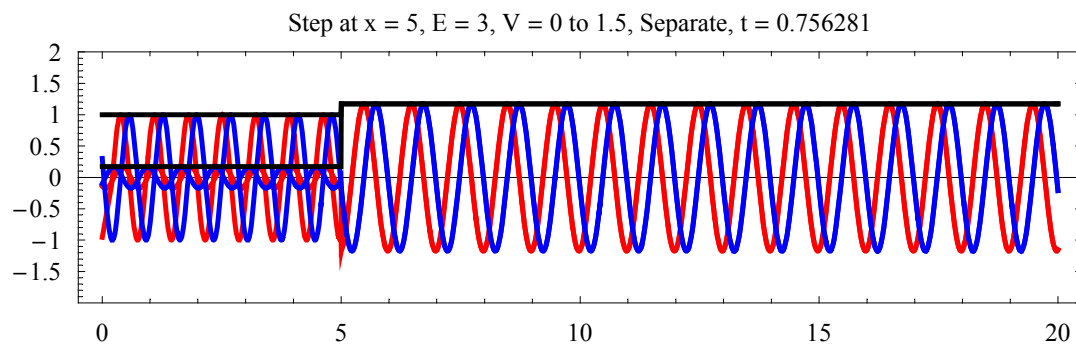
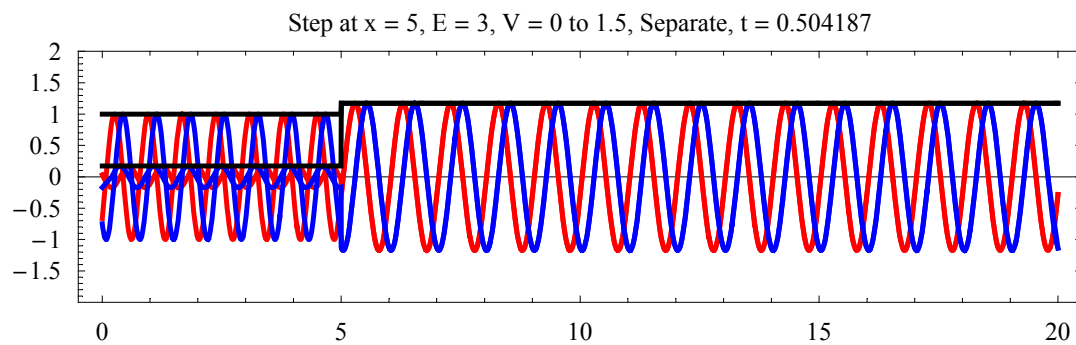


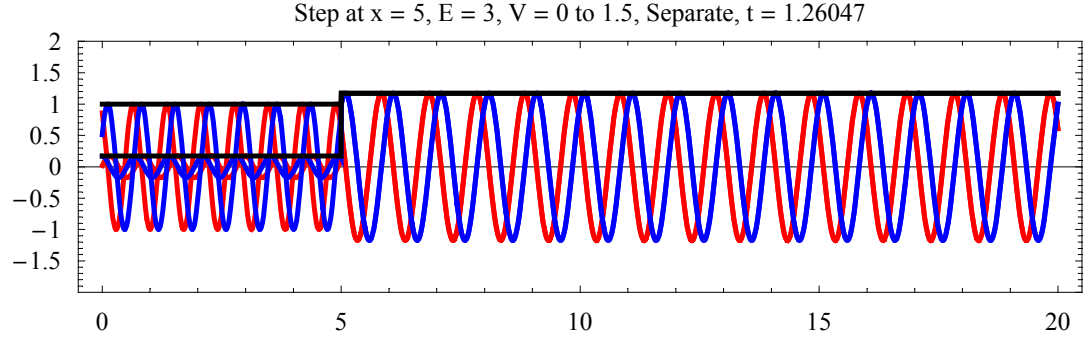


movie =

```
Table[Plot[Evaluate[{Re[{If[x ≤ x1, ψ1I, ψ2], If[x ≤ x1, ψ1R, ψ2]} Exp[-i EE t / hbar]],
  Im[{If[x ≤ x1, ψ1I, ψ2], If[x ≤ x1, ψ1R, ψ2]} Exp[-i EE t / hbar]],
  Abs[{If[x ≤ x1, ψ1I, ψ2], If[x ≤ x1, ψ1R, ψ2]} Exp[-i EE t / hbar]]}],
{x, 0, 20}, PlotRange → {-2, 2}, PlotStyle → {{Thickness[0.005], Red},
  {Thickness[0.005], Red}, {Thickness[0.005], Blue}, {Thickness[0.005], Blue},
  {Thickness[0.005], Black}, {Thickness[0.005], Black}}, PlotLabel →
StringJoin["Step at x = 5, E = 3, V = 0 to 1.5, Separate, t = ", ToString[t]],
Frame → True, AspectRatio → 1 / 4, ImageSize → 9 * 72, PlotPoints → 100],
{t, 0, period - (period + 1) / 10, (period + 1) / 10}];
```







(* barrier *)

In[1]:= Quit[]

In[1]:= Off[General::spell1];

$\psi_{1I} = \text{Exp}[i k_1 x];$

$\psi_{1R} = \text{BB Exp}[-i k_1 x];$

$\psi_1 = \psi_{1I} + \psi_{1R};$

$\psi_{2I} = \text{CC Exp}[i k_2 x];$

$\psi_{2R} = \text{DD Exp}[-i k_2 x];$

$\psi_2 = \psi_{2I} + \psi_{2R};$

$\psi_3 = \text{FF Exp}[i k_3 x];$

$\psi = \text{Piecewise}[\{\{\psi_1, x < x_1\}, \{\psi_2, x_1 \leq x < x_2\}, \{\psi_3, x \geq x_2\}\}];$

eqns =

$\{\psi_1 == \psi_2 /. x \rightarrow x_1, \psi_2 == \psi_3 /. x \rightarrow x_2, \partial_x \psi_1 == \partial_x \psi_2 /. x \rightarrow x_1, \partial_x \psi_2 == \partial_x \psi_3 /. x \rightarrow x_2\};$

In[11]:= soln = {BB, CC, DD, FF} = FullSimplify[{BB, CC, DD, FF} /. Solve[eqns, {BB, CC, DD, FF}], Assumptions -> {x1 ∈ Reals, x2 ∈ Reals}][[1]]

$$\text{Out}[11] = \left\{ \frac{e^{2 i k_1 x_1} (e^{2 i k_2 x_2} (k_1 + k_2) (k_2 - k_3) - e^{2 i k_2 x_1} (-k_1 + k_2) (k_2 + k_3))}{-e^{2 i k_2 x_2} (-k_1 + k_2) (k_2 - k_3) + e^{2 i k_2 x_1} (k_1 + k_2) (k_2 + k_3)}, \right. \\ \frac{2 e^{i (k_1 + k_2) x_1} k_1 (k_2 + k_3)}{-e^{2 i k_2 x_2} (-k_1 + k_2) (k_2 - k_3) + e^{2 i k_2 x_1} (k_1 + k_2) (k_2 + k_3)}, \\ \frac{2 e^{i ((k_1 + k_2) x_1 + 2 k_2 x_2)} k_1 (k_2 - k_3)}{-e^{2 i k_2 x_2} (-k_1 + k_2) (k_2 - k_3) + e^{2 i k_2 x_1} (k_1 + k_2) (k_2 + k_3)}, \\ \left. \frac{4 e^{i (k_1 x_1 - k_3 x_2 + k_2 (x_1 + x_2))} k_1 k_2}{-e^{2 i k_2 x_2} (-k_1 + k_2) (k_2 - k_3) + e^{2 i k_2 x_1} (k_1 + k_2) (k_2 + k_3)} \right\}$$

CForm[soln]

```
List((Power(E,2*I*k1*x1)*(Power(E,2*I*k2*x2)*(k1 + k2)*(k2 - k3) -
Power(E,2*I*k2*x1)*(-k1 + k2)*(k2 + k3)))/
(-Power(E,2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E,2*I*k2*x1)*(k1 + k2)*(k2 +
k3)),
(2*Power(E,I*(k1 + k2)*x1)*k1*(k2 + k3))/
(-Power(E,2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E,2*I*k2*x1)*(k1 + k2)*(k2 +
k3)),
(2*Power(E,I*((k1 + k2)*x1 + 2*k2*x2))*k1*(k2 - k3))/
(-Power(E,2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E,2*I*k2*x1)*(k1 + k2)*(k2 +
k3)),
(4*Power(E,I*(k1*x1 - k3*x2 + k2*(x1 + x2)))*k1*k2)/
(-Power(E,2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E,2*I*k2*x1)*(k1 + k2)*(k2 +
k3)))
```

(*** E > V ***)

EE = 3; (* eV *)

V1 = V3 = 0; (* eV *)

V2 = 1.5;

L = 2;

m = 0.511*10⁶ (hbar/197)²; (* eV/c² *)

hbar = 0.658; (* eV fs *)

k1 = $\sqrt{2m(EE - V1)/hbar^2}$;

k3 = $\sqrt{2m(EE - V3)/hbar^2}$;

k2 = $\sqrt{2m(EE - V2)/hbar^2}$;

period = 2 π hbar / E;

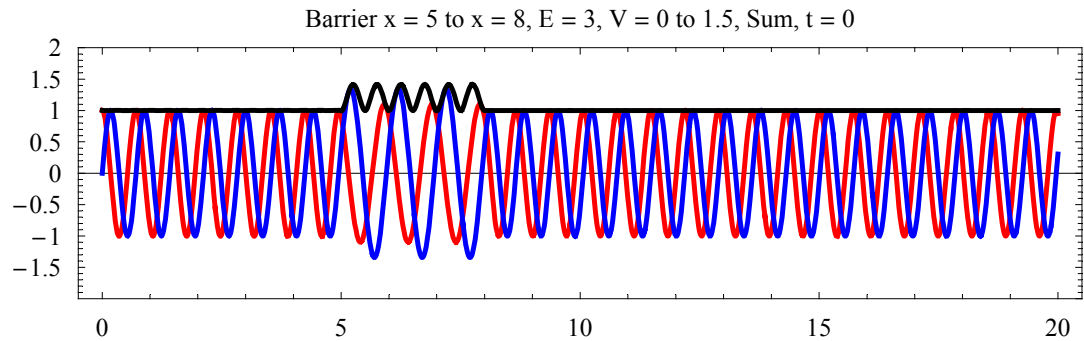
x1 = 5;

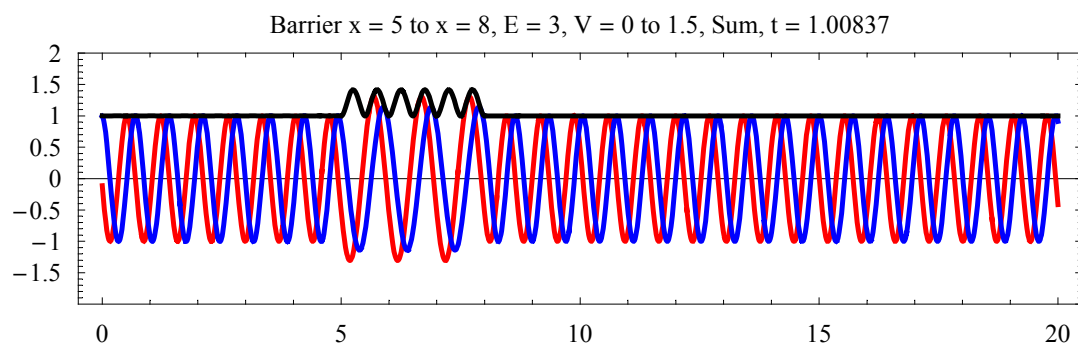
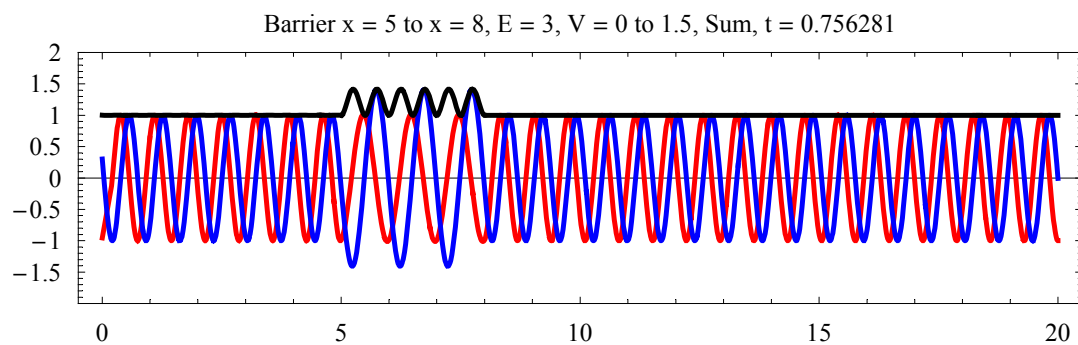
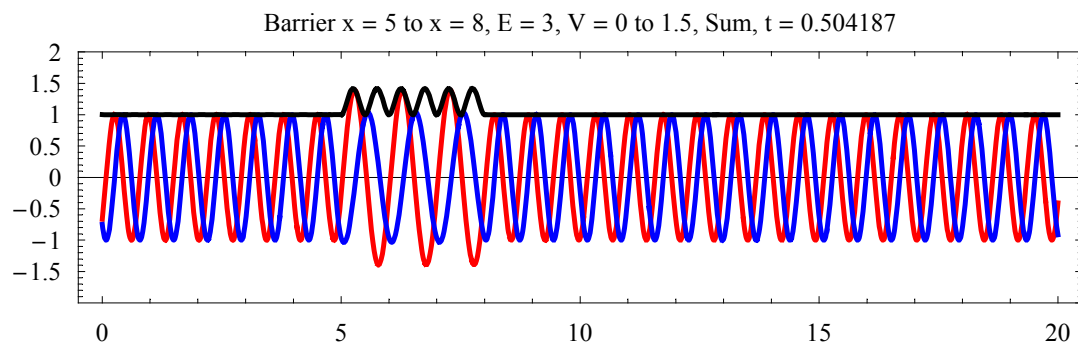
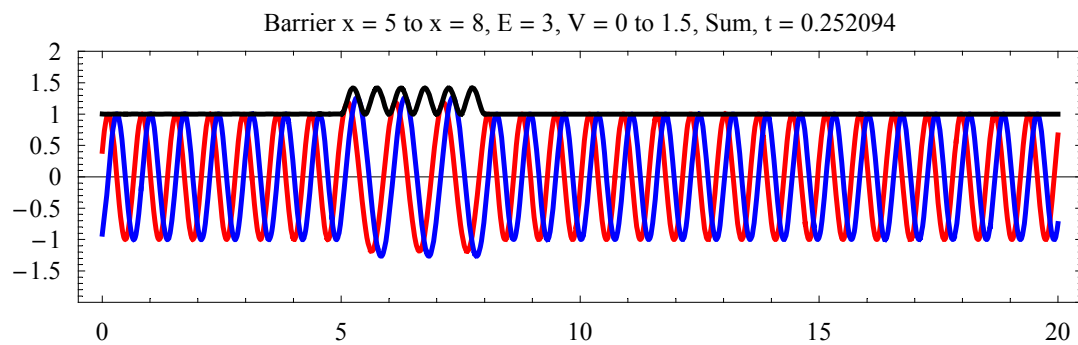
x2 = 8;

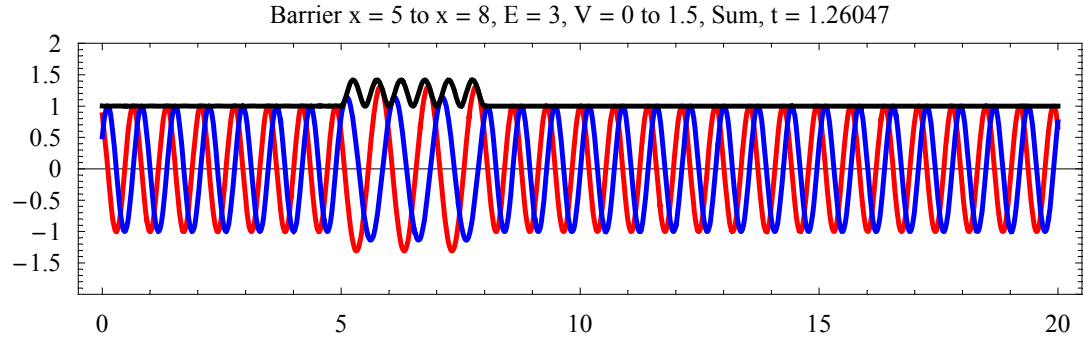
\$TextStyle = {FontFamily -> "Times", FontSize -> 12};

movie =

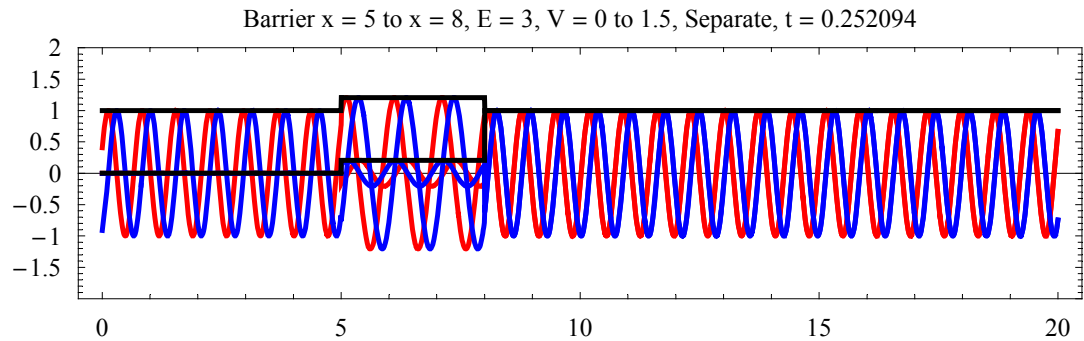
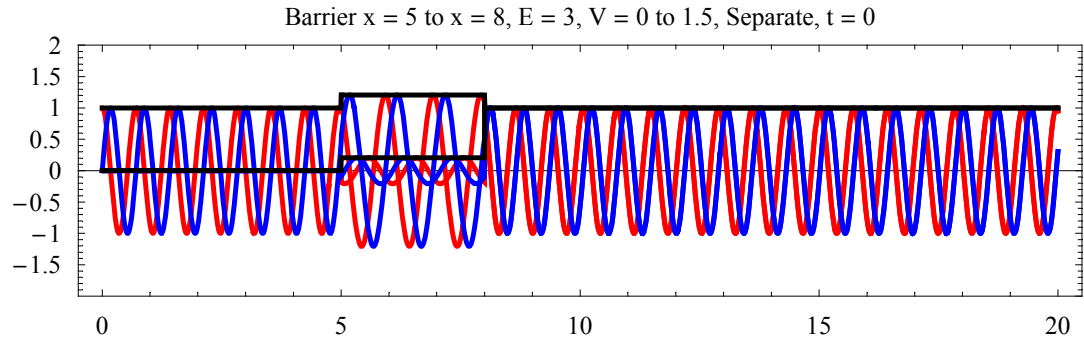
```
Table[Plot[{Re[ $\psi$  Exp[-i EE t / hbar]], Im[ $\psi$  Exp[-i EE t / hbar]], Abs[ $\psi$  Exp[-i EE t / hbar]]},
{x, 0, 20}, PlotRange -> {-2, 2}, PlotPoints -> 100, PlotStyle ->
{{Thickness[0.005], Red}, {Thickness[0.005], Blue}, {Thickness[0.005], Black}},
PlotLabel -> StringJoin["Barrier x = 5 to x = 8, E = 3, V = 0 to 1.5, Sum, t = ",
ToString[t]], Frame -> True, AspectRatio -> 1 / 4, ImageSize -> 9 * 72,
PlotPoints -> 100], {t, 0, period - (period + 1) / 10, (period + 1) / 10}];
```

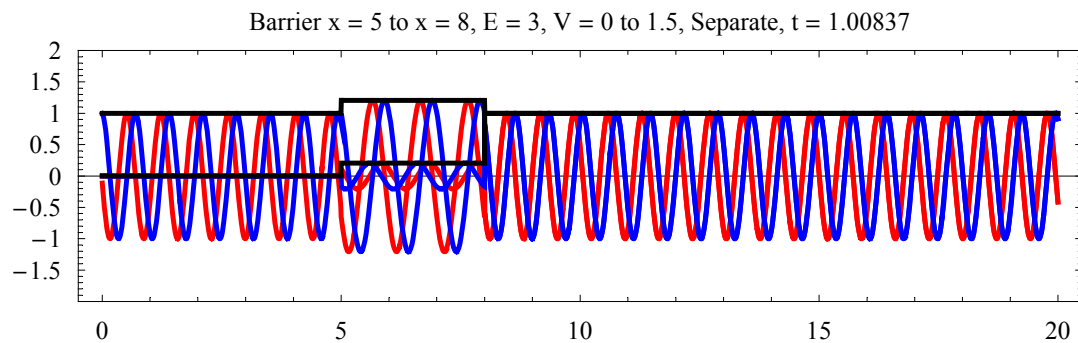
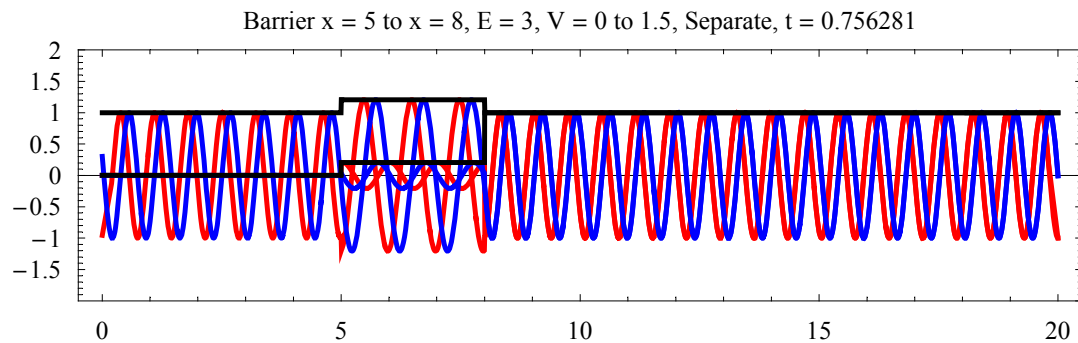
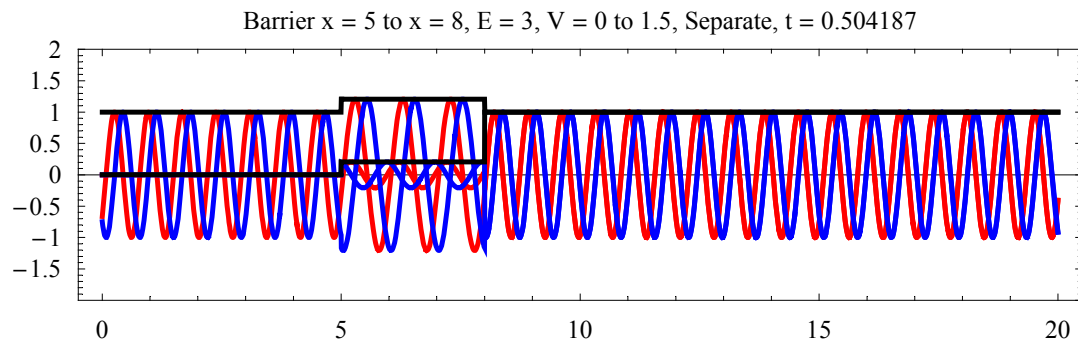


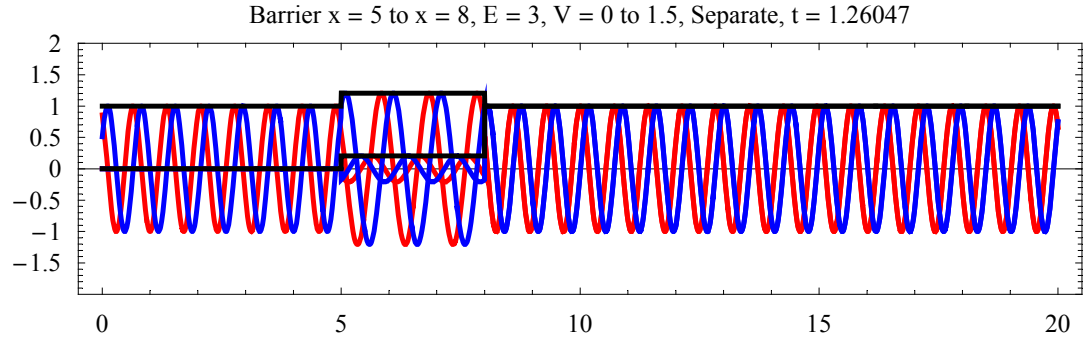




```
movie = Table[Plot[
  Evaluate[{Re[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, ψ3]], If[x ≤ x1, ψ1R, If[x ≤ x2, ψ2R, ψ3]]}
    Exp[-i EE t / hbar]], Im[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, ψ3]],
    If[x ≤ x1, ψ1R, If[x ≤ x2, ψ2R, ψ3]]} Exp[-i EE t / hbar]],
  Abs[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, ψ3]], If[x ≤ x1, ψ1R, If[x ≤ x2, ψ2R, ψ3]]}
    Exp[-i EE t / hbar]]], {x, 0, 20}, PlotRange → {-2, 2},
  PlotStyle → {{Thickness[0.005], Red}, {Thickness[0.005], Red},
    {Thickness[0.005], Blue}, {Thickness[0.005], Blue},
    {Thickness[0.005], Black}, {Thickness[0.005], Black}}, PlotLabel → StringJoin[
    "Barrier x = 5 to x = 8, E = 3, V = 0 to 1.5, Separate, t = ", ToString[t]],
  Frame → True, AspectRatio → 1 / 4, ImageSize → 9 * 72, PlotPoints → 100],
  {t, 0, period - (period + 1) / 10, (period + 1) / 10}];
```



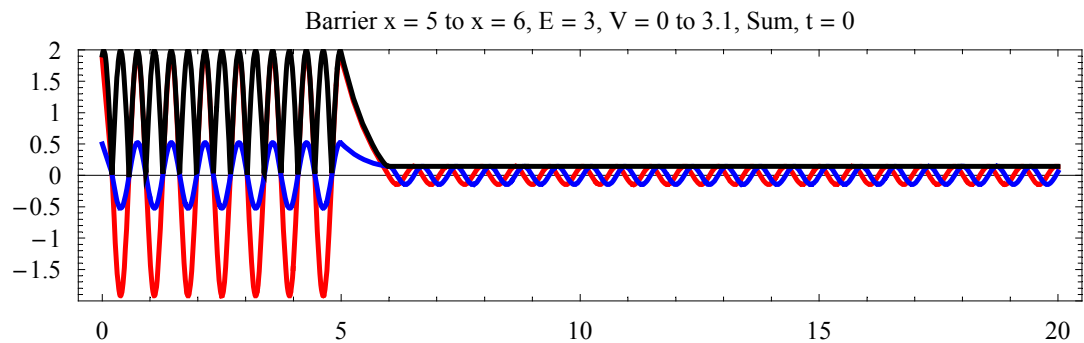


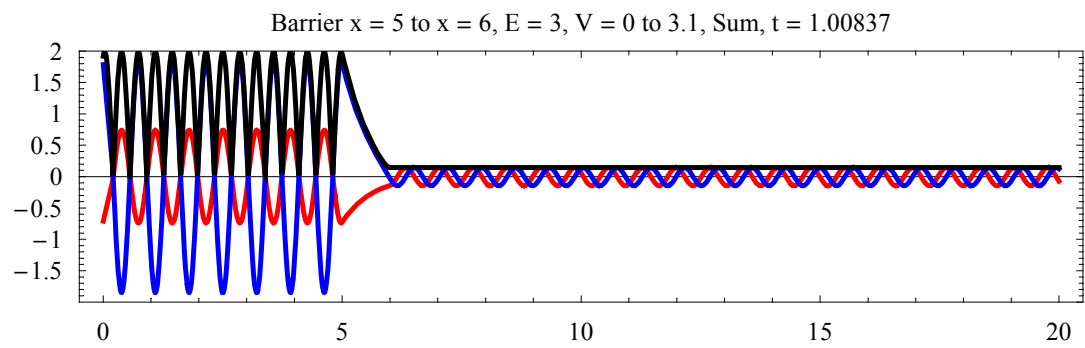
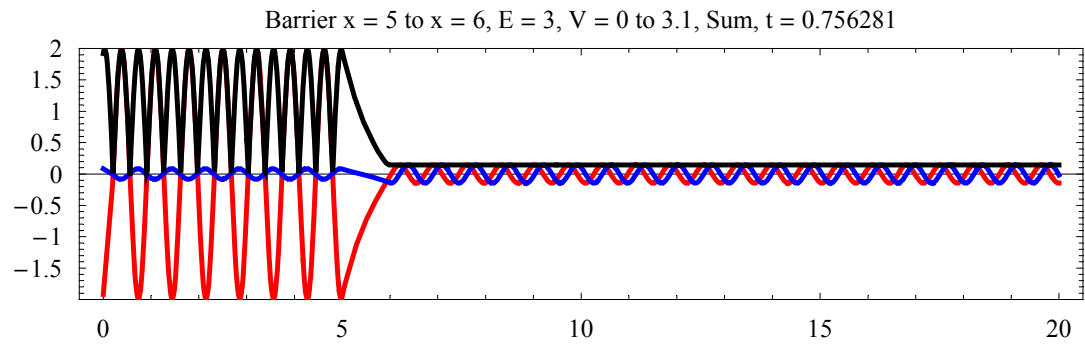
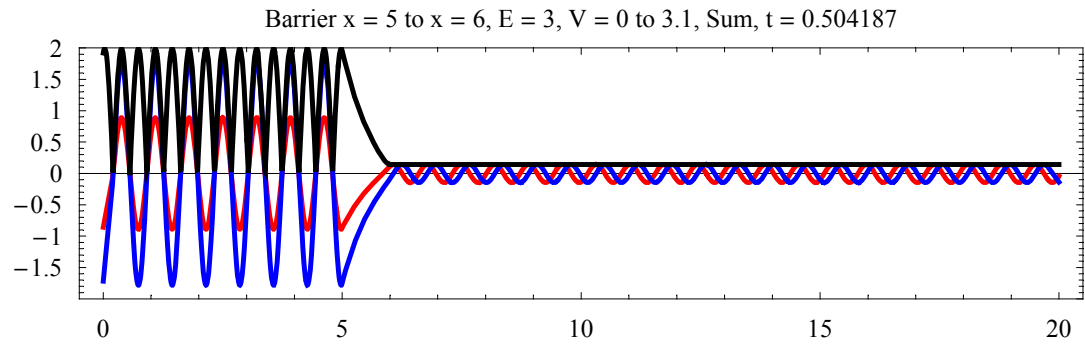
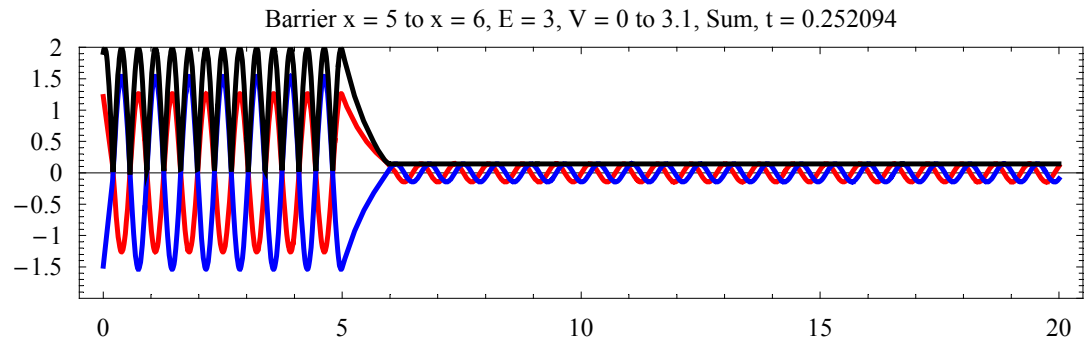


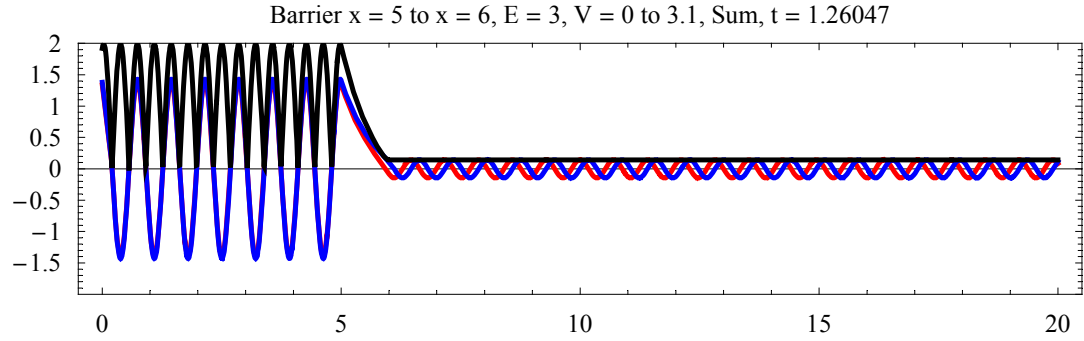
(* E < V *)

```
In[22]:= EE = 3; (* eV *)
V1 = V3 = 0; (* eV *)
V2 = 3.1;
m = 0.511 * 106 (hbar / 197)2; (* eV/c2 *)
hbar = 0.658; (* eV fs *)
k1 =  $\sqrt{2 m (EE - V1) / \hbar^2}$ ;
k3 =  $\sqrt{2 m (EE - V3) / \hbar^2}$ ;
k2 =  $\sqrt{2 m (EE - V2) / \hbar^2}$ ;
period = 2  $\pi$  hbar / E;
x1 = 5;
x2 = 6;
$TextStyle = {FontFamily -> "Times", FontSize -> 12};

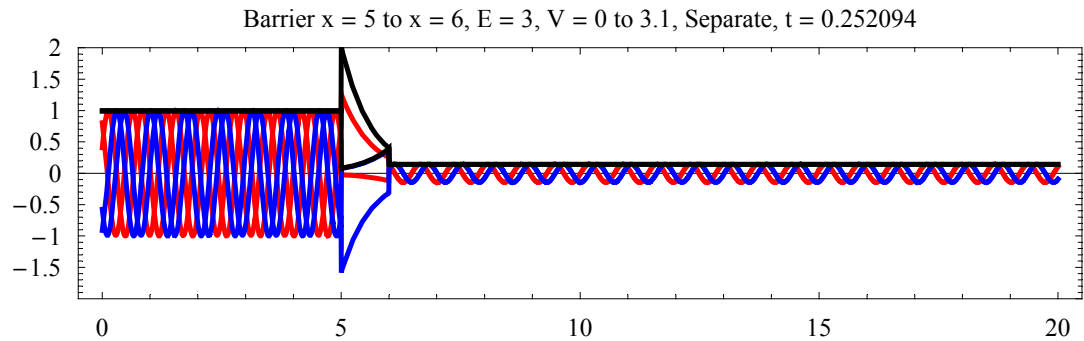
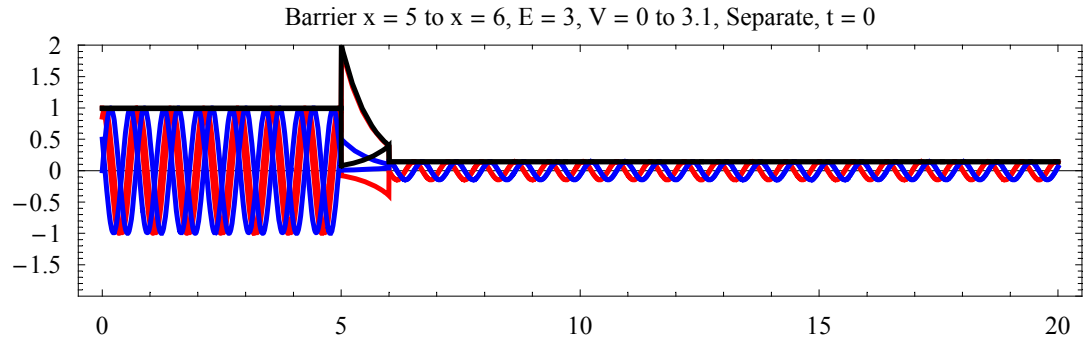
In[31]:= movie = Table[
  Plot[{Re[ $\psi \text{Exp}[-i EE t / \hbar]$ ], Im[ $\psi \text{Exp}[-i EE t / \hbar]$ ], Abs[ $\psi \text{Exp}[-i EE t / \hbar]$ ]}, {x,
    0, 20}, PlotRange -> {-2, 2}, PlotPoints -> 100, PlotStyle -> {{Thickness[0.005], Red},
      {Thickness[0.005], Blue}, {Thickness[0.005], Black}}, PlotLabel -> StringJoin[
        "Barrier x = 5 to x = 6, E = 3, V = 0 to 3.1, Sum, t = ", ToString[t]],
    Frame -> True, AspectRatio -> 1 / 4, ImageSize -> 9 * 72, PlotPoints -> 100],
  {t, 0, period - (period + 1) / 10, (period + 1) / 10}];
```

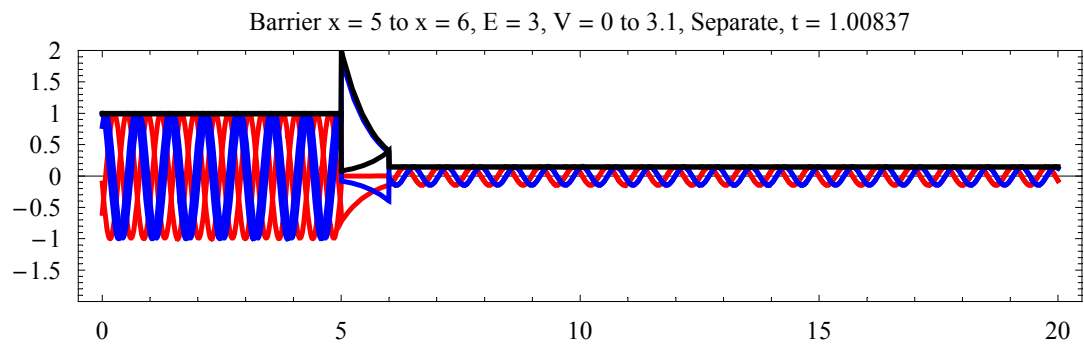
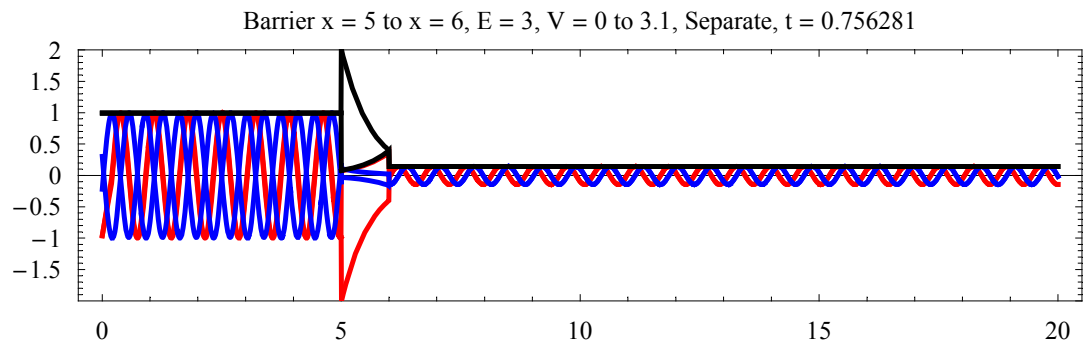
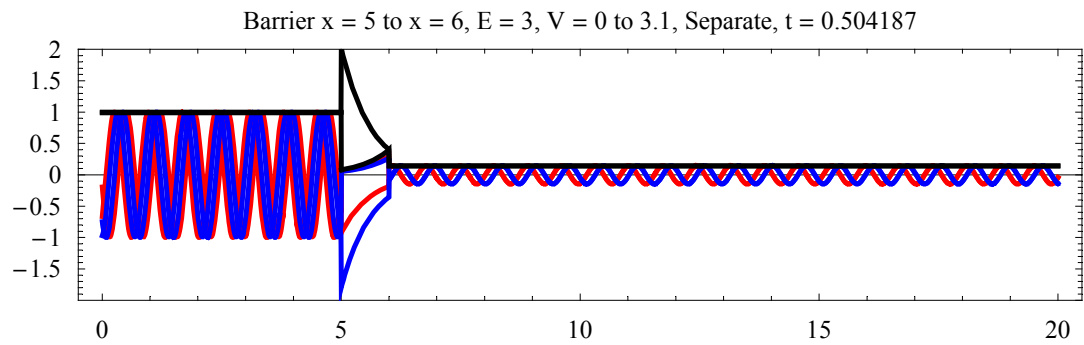


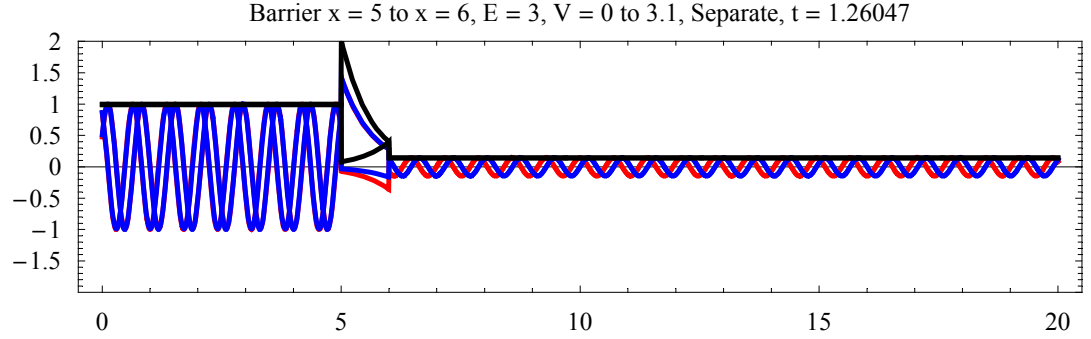




```
In[32]:= movie = Table[Plot[Evaluate[
  {Re[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, ψ3]], If[x ≤ x1, ψ1R, If[x ≤ x2, ψ2R, ψ3]]}
    Exp[-i EE t / hbar]], Im[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, ψ3]],
    If[x ≤ x1, ψ1R, If[x ≤ x2, ψ2R, ψ3]]} Exp[-i EE t / hbar]],
  Abs[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, ψ3]], If[x ≤ x1, ψ1R, If[x ≤ x2, ψ2R, ψ3]]}
    Exp[-i EE t / hbar]]], {x, 0, 20}, PlotRange → {-2, 2},
PlotStyle → {{Thickness[0.005], Red}, {Thickness[0.005], Red},
  {Thickness[0.005], Blue}, {Thickness[0.005], Blue},
  {Thickness[0.005], Black}, {Thickness[0.005], Black}}, PlotLabel → StringJoin[
  "Barrier x = 5 to x = 6, E = 3, V = 0 to 3.1, Separate, t = ", ToString[t],
Frame → True, AspectRatio → 1 / 4, ImageSize → 9 * 72, PlotPoints → 100],
{t, 0, period - (period + 1) / 10, (period + 1) / 10}];
```







(* Double barrier *)

Quit[]

Off[General::spell1];

$\psi_{1I} = \text{Exp}[i k_1 x];$

$\psi_{1R} = \text{BB Exp}[-i k_1 x];$

$\psi_1 = \psi_{1I} + \psi_{1R};$

$\psi_{2I} = \text{CC Exp}[i k_2 x];$

$\psi_{2R} = \text{DD Exp}[-i k_2 x];$

$\psi_2 = \psi_{2I} + \psi_{2R};$

$\psi_{3I} = \text{FF Exp}[i k_3 x];$

$\psi_{3R} = \text{GG Exp}[-i k_3 x];$

$\psi_3 = \psi_{3I} + \psi_{3R};$

$\psi_{4I} = \text{HH Exp}[i k_4 x];$

$\psi_{4R} = \text{II Exp}[-i k_4 x];$

$\psi_4 = \psi_{4I} + \psi_{4R};$

$\psi_5 = \text{JJ Exp}[i k_5 x];$

$\psi = \text{Piecewise}[$

$\{\{\psi_1, x < x_1\}, \{\psi_2, x_1 \leq x < x_2\}, \{\psi_3, x_2 \leq x < x_3\}, \{\psi_4, x_3 \leq x < x_4\}, \{\psi_5, x \geq x_4\}\};$

$\text{eqns} = \{\psi_1 == \psi_2 /. x \rightarrow x_1, \psi_2 == \psi_3 /. x \rightarrow x_2, \psi_3 == \psi_4 /. x \rightarrow x_3,$

$\psi_4 == \psi_5 /. x \rightarrow x_4, \partial_x \psi_1 == \partial_x \psi_2 /. x \rightarrow x_1, \partial_x \psi_2 == \partial_x \psi_3 /. x \rightarrow x_2,$

$\partial_x \psi_3 == \partial_x \psi_4 /. x \rightarrow x_3, \partial_x \psi_4 == \partial_x \psi_5 /. x \rightarrow x_4\};$

$\text{soln} = \{\text{BB}, \text{CC}, \text{DD}, \text{FF}, \text{GG}, \text{HH}, \text{II}, \text{JJ}\} = \text{FullSimplify}[$

$\{\text{BB}, \text{CC}, \text{DD}, \text{FF}, \text{GG}, \text{HH}, \text{II}, \text{JJ}\} /. \text{Solve}[\text{eqns}, \{\text{BB}, \text{CC}, \text{DD}, \text{FF}, \text{GG}, \text{HH}, \text{II}, \text{JJ}\}],$

$\text{Assumptions} \rightarrow \{x_1 \in \text{Reals}, x_2 \in \text{Reals}, x_3 \in \text{Reals}, x_4 \in \text{Reals}\}][[1]]$

$\{ (e^{2 i k_1 x_1} (e^{2 i ((k_2+k_3) x_2+k_4 x_4)} (k_1+k_2) (k_2-k_3) (k_3-k_4) (k_4-k_5) -$
 $e^{2 i (k_2 x_1+k_3 x_2+k_4 x_4)} (-k_1+k_2) (k_2+k_3) (k_3-k_4) (k_4-k_5) -$
 $e^{2 i (k_2 x_1+k_3 x_3+k_4 x_4)} (-k_1+k_2) (k_2-k_3) (k_3+k_4) (k_4-k_5) + e^{2 i (k_2 x_2+k_3 x_3+k_4 x_4)} (k_1+k_2)$
 $(k_2+k_3) (k_3+k_4) (k_4-k_5) - e^{2 i (k_2 x_1+(k_3+k_4) x_3)} (-k_1+k_2) (k_2-k_3) (k_3-k_4) (k_4+k_5) +$
 $e^{2 i (k_2 x_2+(k_3+k_4) x_3)} (k_1+k_2) (k_2+k_3) (k_3-k_4) (k_4+k_5) + e^{2 i ((k_2+k_3) x_2+k_4 x_3)} (k_1+k_2)$
 $(k_2-k_3) (k_3+k_4) (k_4+k_5) - e^{2 i (k_2 x_1+k_3 x_2+k_4 x_3)} (-k_1+k_2) (k_2+k_3) (k_3+k_4) (k_4+k_5)) /$
 $(-e^{2 i ((k_2+k_3) x_2+k_4 x_4)} (-k_1+k_2) (k_2-k_3) (k_3-k_4) (k_4-k_5) +$
 $e^{2 i (k_2 x_1+k_3 x_2+k_4 x_4)} (k_1+k_2) (k_2+k_3) (k_3-k_4) (k_4-k_5) +$
 $e^{2 i (k_2 x_1+k_3 x_3+k_4 x_4)} (k_1+k_2) (k_2-k_3) (k_3+k_4) (k_4-k_5) -$
 $e^{2 i (k_2 x_2+k_3 x_3+k_4 x_4)} (-k_1+k_2) (k_2+k_3) (k_3+k_4) (k_4-k_5) +$
 $e^{2 i (k_2 x_1+(k_3+k_4) x_3)} (k_1+k_2) (k_2-k_3) (k_3-k_4) (k_4+k_5) -$
 $e^{2 i (k_2 x_2+(k_3+k_4) x_3)} (-k_1+k_2) (k_2+k_3) (k_3-k_4) (k_4+k_5) -$
 $e^{2 i ((k_2+k_3) x_2+k_4 x_3)} (-k_1+k_2) (k_2-k_3) (k_3+k_4) (k_4+k_5) +$

$$\begin{aligned}
& e^{2i(k_2 x_2 + k_3 x_3 + k_4 x_4)} (-k_1 + k_2) (k_2 + k_3) (k_3 + k_4) (k_4 - k_5) + \\
& e^{2i(k_2 x_1 + (k_3 + k_4) x_3)} (k_1 + k_2) (k_2 - k_3) (k_3 - k_4) (k_4 + k_5) - \\
& e^{2i(k_2 x_2 + (k_3 + k_4) x_3)} (-k_1 + k_2) (k_2 + k_3) (k_3 - k_4) (k_4 + k_5) - \\
& e^{2i((k_2 + k_3) x_2 + k_4 x_3)} (-k_1 + k_2) (k_2 - k_3) (k_3 + k_4) (k_4 + k_5) + \\
& e^{2i(k_2 x_1 + k_3 x_2 + k_4 x_3)} (k_1 + k_2) (k_2 + k_3) (k_3 + k_4) (k_4 + k_5)), \\
& (16 e^{i(k_1 x_1 + k_3 x_2 + k_2(x_1 + x_2) + k_3 x_3 + k_4 x_3 + k_4 x_4 - k_5 x_4)} k_1 k_2 k_3 k_4) / \\
& (-e^{2i((k_2 + k_3) x_2 + k_4 x_4)} (-k_1 + k_2) (k_2 - k_3) (k_3 - k_4) (k_4 - k_5) + \\
& e^{2i(k_2 x_1 + k_3 x_2 + k_4 x_4)} (k_1 + k_2) (k_2 + k_3) (k_3 - k_4) (k_4 - k_5) + \\
& e^{2i(k_2 x_1 + k_3 x_3 + k_4 x_4)} (k_1 + k_2) (k_2 - k_3) (k_3 + k_4) (k_4 - k_5) - \\
& e^{2i(k_2 x_2 + k_3 x_3 + k_4 x_4)} (-k_1 + k_2) (k_2 + k_3) (k_3 + k_4) (k_4 - k_5) + \\
& e^{2i(k_2 x_1 + (k_3 + k_4) x_3)} (k_1 + k_2) (k_2 - k_3) (k_3 - k_4) (k_4 + k_5) - \\
& e^{2i(k_2 x_2 + (k_3 + k_4) x_3)} (-k_1 + k_2) (k_2 + k_3) (k_3 - k_4) (k_4 + k_5) - \\
& e^{2i((k_2 + k_3) x_2 + k_4 x_3)} (-k_1 + k_2) (k_2 - k_3) (k_3 + k_4) (k_4 + k_5) + \\
& e^{2i(k_2 x_1 + k_3 x_2 + k_4 x_3)} (k_1 + k_2) (k_2 + k_3) (k_3 + k_4) (k_4 + k_5)) \}
\end{aligned}$$

CForm[soln]

```

List((Power(E,2*I*k1*x1)*(Power(E,2*I*((k2 + k3)*x2 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3
- k4)*(k4 - k5) -
      Power(E,2*I*(k2*x1 + k3*x2 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5)
-
      Power(E,2*I*(k2*x1 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5)
+
      Power(E,2*I*(k2*x2 + k3*x3 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5)
-
      Power(E,2*I*(k2*x1 + (k3 + k4)*x3))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5)
+
      Power(E,2*I*(k2*x2 + (k3 + k4)*x3))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) +
      Power(E,2*I*((k2 + k3)*x2 + k4*x3))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) -
      Power(E,2*I*(k2*x1 + k3*x2 + k4*x3))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 +
k5)))/
      (-(Power(E,2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
+
      Power(E,2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
      Power(E,2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) -
      Power(E,2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
      Power(E,2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) -
      Power(E,2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
      Power(E,2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
      Power(E,2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)),
      (2*Power(E,I*(k1 + k2)*x1)*k1*(Power(E,2*I*(k3*x2 + k4*x4))*(k2 + k3)*(k3 -
k4)*(k4 - k5) -
      Power(E,2*I*(k3*x3 + k4*x4))*(-k2 + k3)*(k3 + k4)*(k4 - k5) - Power(E,2*I*(k3
+ k4)*x3)*(-k2 + k3)*(k3 - k4)*(k4 + k5) +
      Power(E,2*I*(k3*x2 + k4*x3))*(k2 + k3)*(k3 + k4)*(k4 + k5)))/
      (-(Power(E,2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
+
      Power(E,2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
      Power(E,2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) -
      Power(E,2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
      Power(E,2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) -
      Power(E,2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
      Power(E,2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
      Power(E,2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)),
      (-2*Power(E,I*((k1 + k2)*x1 + 2*k2*x2))*k1*(-(Power(E,2*I*(k3*x2 + k4*x4))*(-k2 +
k3)*(k3 - k4)*(k4 - k5)) +
      Power(E,2*I*(k3*x3 + k4*x4))*(k2 + k3)*(k3 + k4)*(k4 - k5) + Power(E,2*I*(k3
+ k4)*x3)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
      Power(E,2*I*(k3*x2 + k4*x3))*(-k2 + k3)*(k3 + k4)*(k4 + k5)))/

```


[illegible]

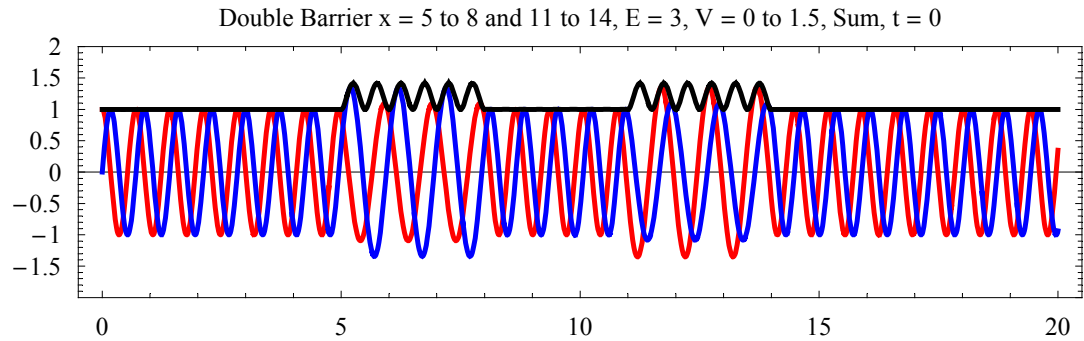
```

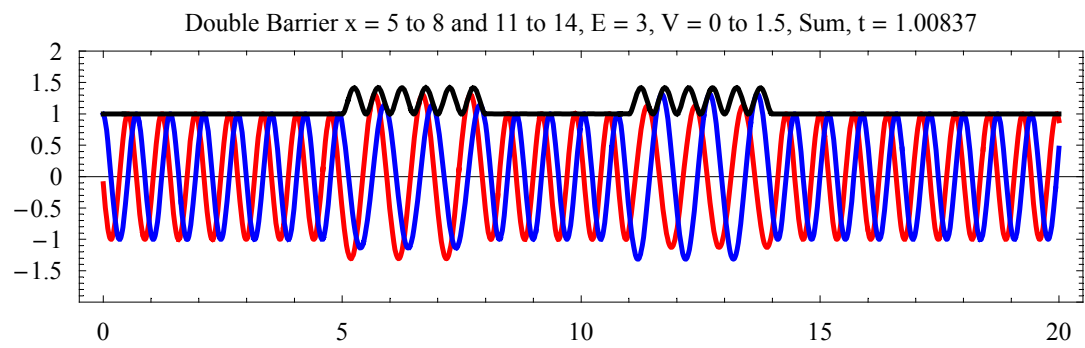
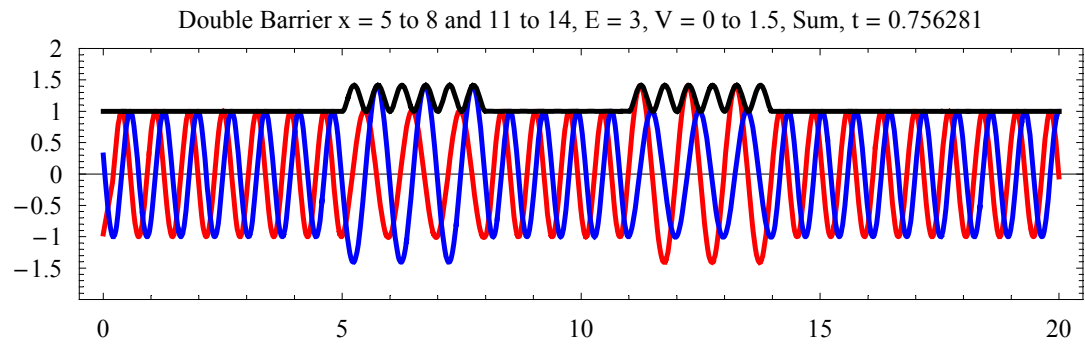
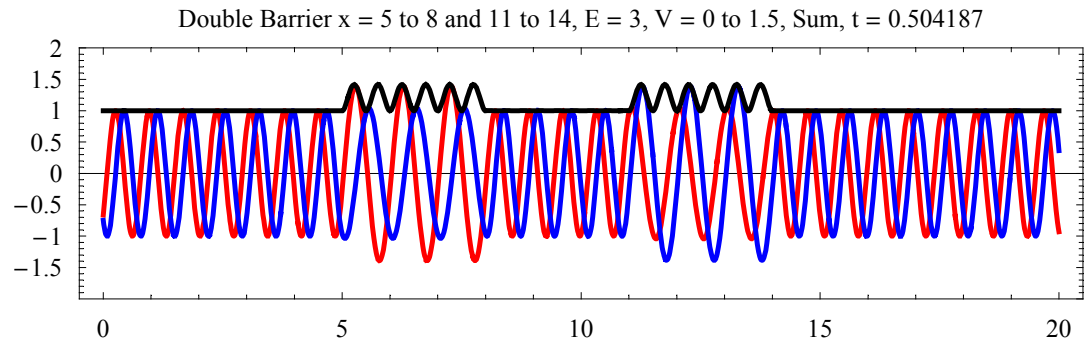
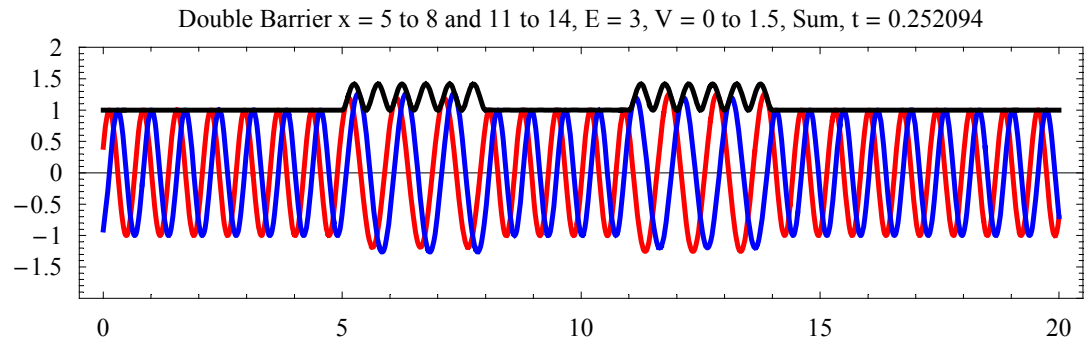
Power(E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
Power(E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
Power(E, 2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5))

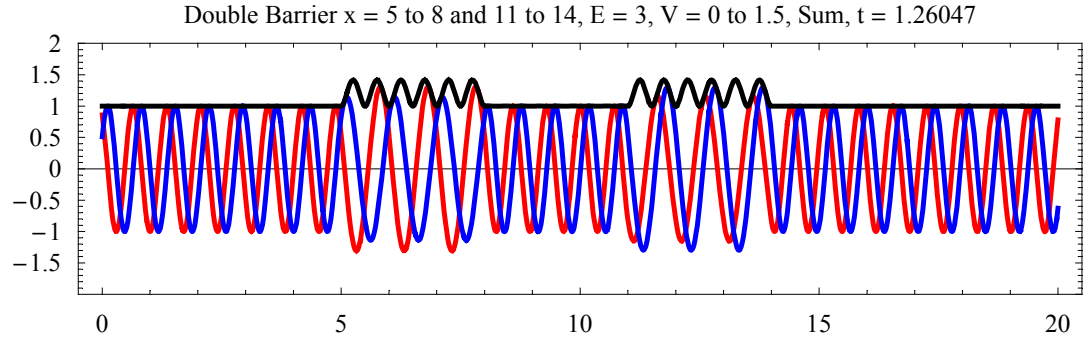
EE = 3; (* eV *)
V1 = V3 = V5 = 0; (* eV *)
V2 = V4 = 1.5;
L1 = 2;
L2 = 2;
L3 = 2;
m = 0.511*106 (hbar/197)2; (* eV/c2 *)
hbar = 0.658; (* eV fs *)
k1 =  $\sqrt{2 m (EE - V1) / hbar^2}$ ;
k2 =  $\sqrt{2 m (EE - V2) / hbar^2}$ ;
k3 =  $\sqrt{2 m (EE - V3) / hbar^2}$ ;
k4 =  $\sqrt{2 m (EE - V4) / hbar^2}$ ;
k5 =  $\sqrt{2 m (EE - V5) / hbar^2}$ ;
period = 2  $\pi$  hbar / E;
x1 = 5;
x2 = 8;
x3 = 11;
x4 = 14;
$TextStyle = {FontFamily -> "Times", FontSize -> 12};

movie =
Table[Plot[{Re[ $\psi \text{ Exp}[-i EE t / hbar]$ ], Im[ $\psi \text{ Exp}[-i EE t / hbar]$ ], Abs[ $\psi \text{ Exp}[-i EE t / hbar]$ ]},
{x, 0, 20}, PlotRange -> {-2, 2}, PlotPoints -> 100, PlotStyle ->
{{Thickness[0.005], Red}, {Thickness[0.005], Blue}, {Thickness[0.005], Black}},
PlotLabel -> StringJoin["Double Barrier x = 5 to 8 and 11 to
14, E = 3, V = 0 to 1.5, Sum, t = ", ToString[t]],
Frame -> True, AspectRatio -> 1/4, ImageSize -> 9*72, PlotPoints -> 100],
{t, 0, period - (period + 1)/10, (period + 1)/10}];

```







```
movie = Table[Plot[Evaluate[
  {Re[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, If[x ≤ x3, ψ3I, If[x ≤ x4, ψ4I, ψ5]]], If[x ≤ x1,
    ψ1R, If[x ≤ x2, ψ2R, If[x ≤ x3, ψ3R, If[x ≤ x4, ψ4R, ψ5]]]} Exp[-i EE t / hbar]],
  Im[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, If[x ≤ x3, ψ3I, If[x ≤ x4, ψ4I, ψ5]]], If[x ≤ x1,
    ψ1R, If[x ≤ x2, ψ2R, If[x ≤ x3, ψ3R, If[x ≤ x4, ψ4R, ψ5]]]} Exp[-i EE t / hbar]],
  Abs[{If[x ≤ x1, ψ1I, If[x ≤ x2, ψ2I, If[x ≤ x3, ψ3I, If[x ≤ x4, ψ4I, ψ5]]], If[x ≤ x1,
    ψ1R, If[x ≤ x2, ψ2R, If[x ≤ x3, ψ3R, If[x ≤ x4, ψ4R, ψ5]]]} Exp[-i EE t / hbar]]}],
{x, 0, 20}, PlotRange → {-2, 2}, PlotStyle → {{Thickness[0.005], Red},
  {Thickness[0.005], Red}, {Thickness[0.005], Blue}, {Thickness[0.005], Blue},
  {Thickness[0.005], Black}, {Thickness[0.005], Black}},
PlotLabel → StringJoin["Double Barrier  $x = 5$  to  $8$  and  $11$  to  $14$ ,
   $E = 3$ ,  $V = 0$  to  $1.5$ , Separate,  $t =$ ", ToString[t]],
Frame → True, AspectRatio → 1 / 4, ImageSize → 9 * 72, PlotPoints → 100],
{t, 0, period - (period + 1) / 10, (period + 1) / 10}];
```

