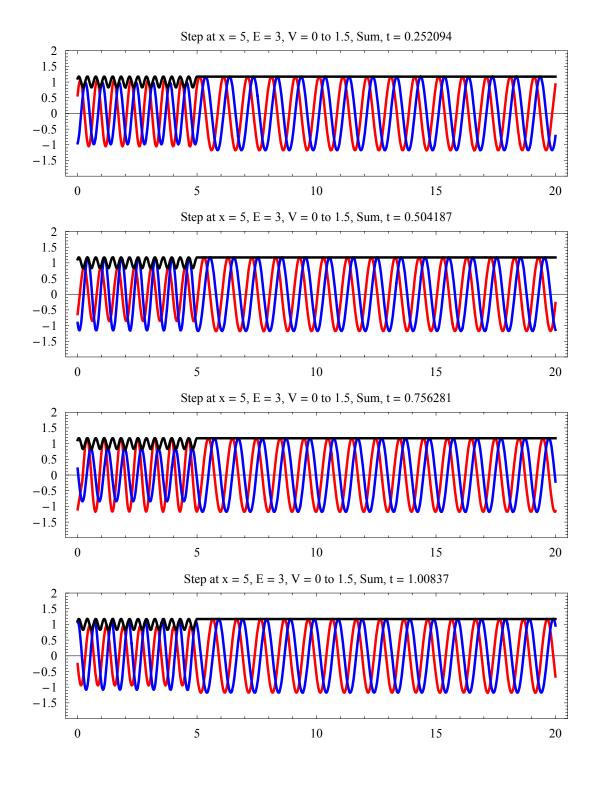
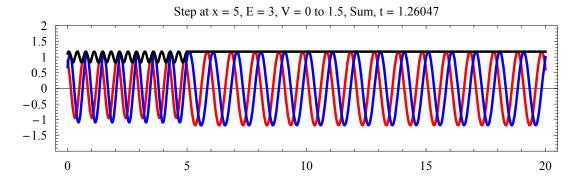
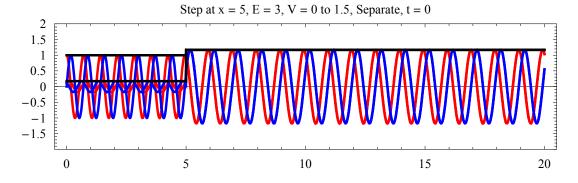
```
(* Step *)
Quit[]
Off[General::spell1];
\psi1I = Exp[ik1 x];
\psi1R = BB Exp[-ik1 x];
\psi \texttt{1} = \psi \texttt{1I} + \psi \texttt{1R} \,;
\psi2 = CC Exp[ik2x];
\psi = \texttt{Piecewise}\big[\left\{\left\{\psi\mathbf{1}\,,\;\mathbf{x} < \mathbf{x}\mathbf{1}\right\}\,,\;\left\{\psi\mathbf{2}\,,\;\mathbf{x}\mathbf{1} \leq \mathbf{x}\right\}\right\}\big]\;;
eqns = \{\psi 1 == \psi 2 /. x \rightarrow x1, \partial_x \psi 1 == \partial_x \psi 2 /. x \rightarrow x1\};
soln =
  \label{eq:bb_cc} $\{\mathtt{BB},\mathtt{CC}\} = \mathtt{FullSimplify}[\{\mathtt{BB},\mathtt{CC}\} \ /. \ \mathtt{Solve}[\mathtt{eqns}, \{\mathtt{BB},\mathtt{CC}\}] \ , \ \mathtt{Assumptions} \to \{\mathtt{x1} \in \mathtt{Reals}\}][[1]]$ }
   \frac{e^{2\,i\,k1\,x1}\,\left(k1-k2\right)}{k1+k2}\,\text{,}\  \, \frac{2\,e^{i\,\left(k1-k2\right)\,x1}\,k1}{k1+k2}\,\big\}
CForm[soln]
List((Power(E, 2*I*k1*x1)*(k1 - k2))/(k1 + k2), (2*Power(E, I*(k1 - k2)*x1)*k1)/(k1 +
k2))
EE = 3; (* eV *)
V = 1.5; (* eV *)
m = 0.511 * 10^6 (hbar/197)^2; (* eV/c^2 *)
hbar = 0.658; (* eV fs *)
k1 = \sqrt{2 m EE / hbar^2};
k2 = \sqrt{2 m (EE - V) / hbar^2};
period = 2 \pi hbar / E;
x1 = 5;
$TextStyle = {FontFamily → "Times", FontSize → 12};
movie =
    {\tt Table[Plot[\{Re[\psi\,{\tt Exp[-i}\,{\tt EE}\,\,t/\,hbar]]\,,\,\,Im[\psi\,{\tt Exp[-i}\,{\tt EE}\,\,t/\,hbar]]\,,\,\,Abs[\psi\,{\tt Exp[-i}\,{\tt EE}\,\,t/\,hbar]]\,\}\,,}
        \{x, 0, 20\}, PlotRange \rightarrow \{-2, 2\}, PlotPoints \rightarrow 100, PlotStyle \rightarrow
         \{\{Thickness[0.005], Red\}, \{Thickness[0.005], Blue\}, \{Thickness[0.005], Black\}\},
       PlotLabel \rightarrow StringJoin["Step at x = 5, E = 3, V = 0 to 1.5, Sum, t = ",
           \texttt{ToString[t]], Frame} \rightarrow \texttt{True, AspectRatio} \rightarrow \texttt{1/4, ImageSize} \rightarrow \texttt{9} * \texttt{72,}
       PlotPoints \rightarrow 100], \{t, 0, period - (period + 1) / 10, (period + 1) / 10\}];
                                                         Step at x = 5, E = 3, V = 0 to 1.5, Sum, t = 0
                   2
                 1.5
                   1
                 0.5
               -0.5
                 -1
               -1.5
                         0
                                                       5
                                                                                    10
                                                                                                                  15
                                                                                                                                               20
```

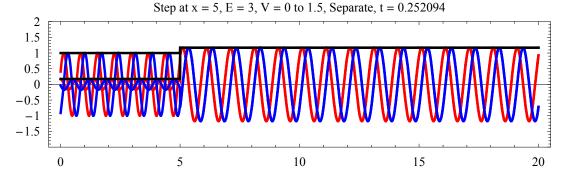


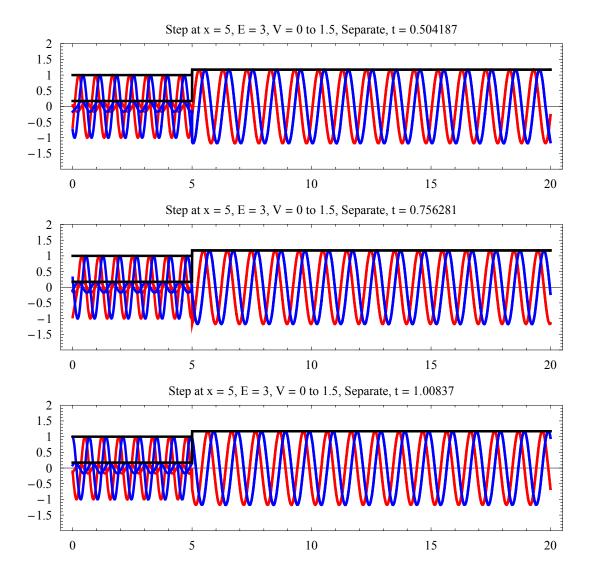


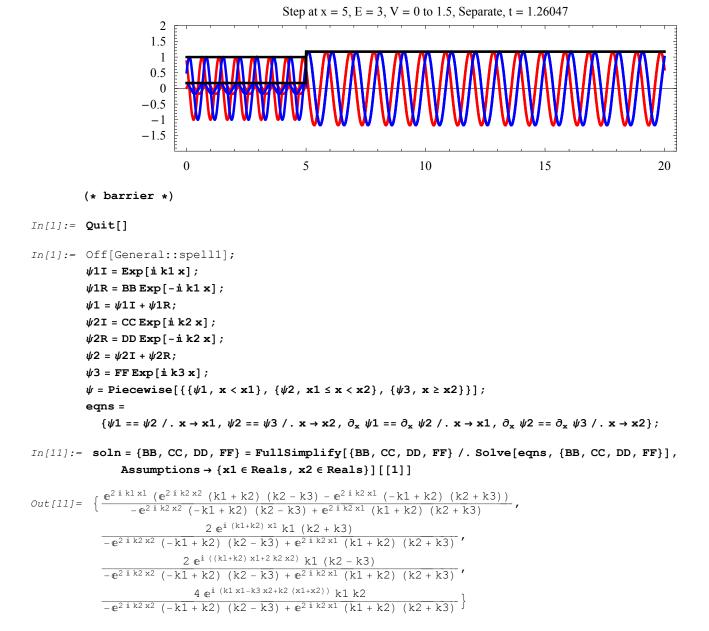
movie =

```
 \begin{split} & \text{Table}[\text{Plot}[\text{Evaluate}[\{\text{Re}[\{\text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{I}, \, \psi 2], \, \text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{R}, \, \psi 2]\} \, \text{Exp}[-i\, \text{EE}\, \, \text{t} \, / \, \text{hbar}]] \, , \\ & \text{Im}[\{\text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{I}, \, \psi 2], \, \text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{R}, \, \psi 2]\} \, \text{Exp}[-i\, \text{EE}\, \, \text{t} \, / \, \text{hbar}]] \, , \\ & \text{Abs}[\{\text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{I}, \, \psi 2], \, \text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{R}, \, \psi 2]\} \, \text{Exp}[-i\, \text{EE}\, \, \text{t} \, / \, \text{hbar}]] \, \} \, , \\ & \{\mathbf{x}, \, 0, \, 20\}, \, \text{PlotRange} \rightarrow \{-2, \, 2\}, \, \text{PlotStyle} \rightarrow \{\{\text{Thickness}[0.005], \, \text{Red}\}, \, \\ & \{\text{Thickness}[0.005], \, \text{Red}\}, \, \{\text{Thickness}[0.005], \, \text{Blue}\}, \, \{\text{Thickness}[0.005], \, \text{Blue}\}, \, \\ & \{\text{Thickness}[0.005], \, \text{Black}\}, \, \{\text{Thickness}[0.005], \, \text{Black}\}\}, \, \text{PlotLabel} \rightarrow \\ & \text{StringJoin}["Step at x = 5, \, E = 3, \, V = 0 \, \text{to} \, 1.5, \, \text{Separate}, \, t = ", \, \text{ToString}[t]], \, \\ & \text{Frame} \rightarrow \text{True}, \, \text{AspectRatio} \rightarrow 1/4, \, \text{ImageSize} \rightarrow 9 * 72, \, \text{PlotPoints} \rightarrow 100], \, \\ & \{t, \, 0, \, \text{period} - (\text{period} + 1) \, / \, 10, \, (\text{period} + 1) \, / \, 10\}]; \, \end{split}
```



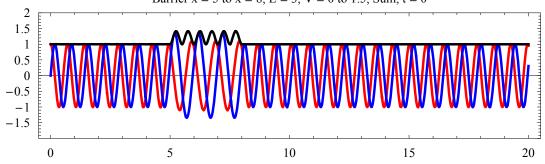


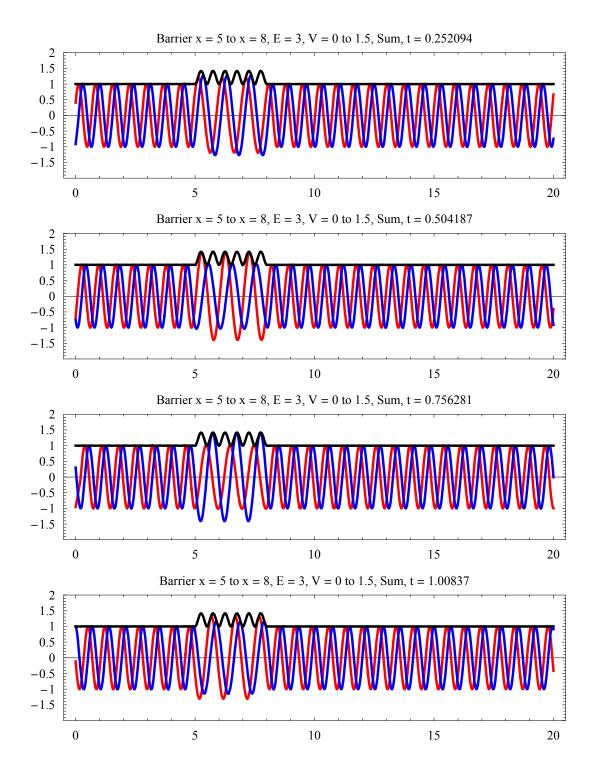


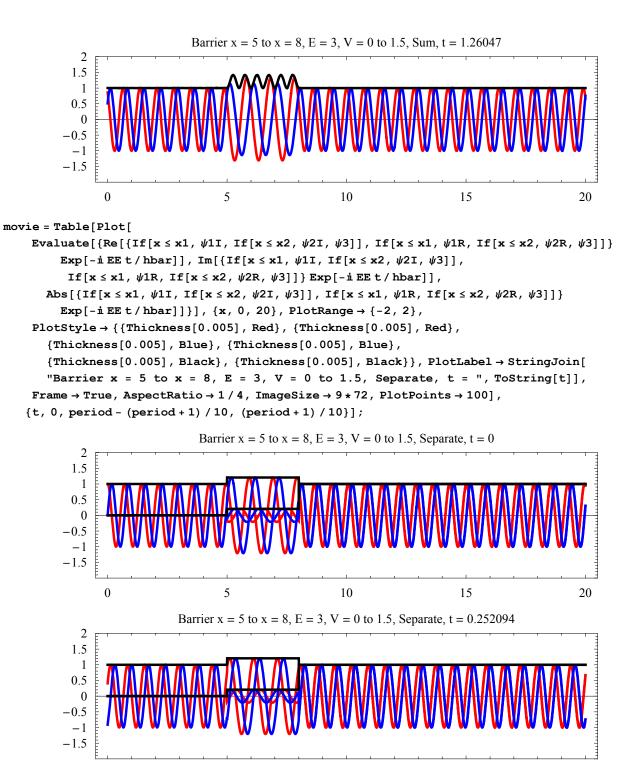


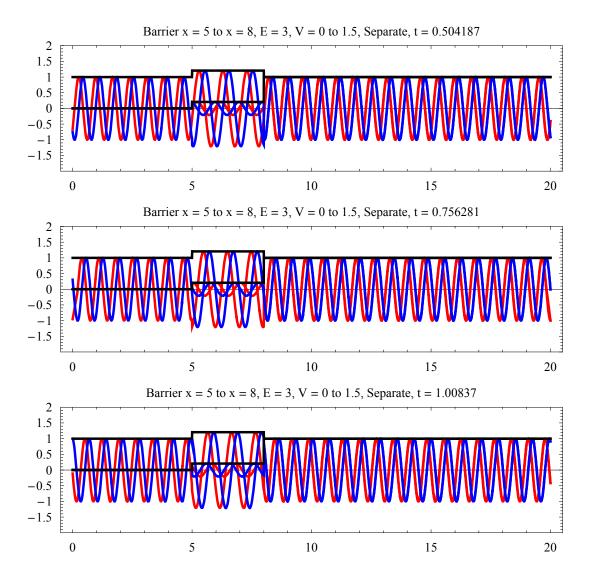
CForm[soln]

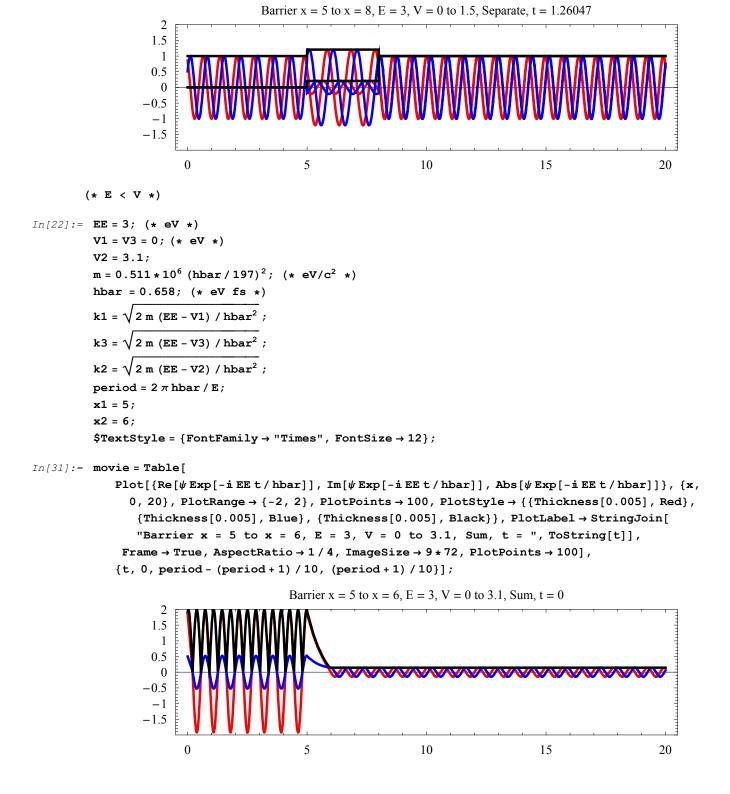
```
List((Power(E, 2 \times 1 \times k1 \times x1) * (Power(E, 2 \times 1 \times k2 \times x2) * (k1 + k2) * (k2 - k3) -
Power (E, 2*I*k2*x1)*(-k1 + k2)*(k2 + k3)))/
            (-(Power(E, 2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E, 2*I*k2*x1)*(k1 + k2)*(k2 + k3))
k3)),
         (2*Power(E,I*(k1 + k2)*x1)*k1*(k2 + k3))/
           (-(Power(E, 2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E, 2*I*k2*x1)*(k1 + k2)*(k2 + k3))
k3)),
         (2*Power(E,I*((k1 + k2)*x1 + 2*k2*x2))*k1*(k2 - k3))/
            (-(Power(E, 2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E, 2*I*k2*x1)*(k1 + k2)*(k2 + k3))
k3)),
         (4*Power(E,I*(k1*x1 - k3*x2 + k2*(x1 + x2)))*k1*k2)/
            (-(Power(E, 2*I*k2*x2)*(-k1 + k2)*(k2 - k3)) + Power(E, 2*I*k2*x1)*(k1 + k2)*(k2 + k2)*(k2 + k3))
k3)))
 (* E > V *)
 EE = 3; (* eV *)
 V1 = V3 = 0; (* eV *)
 V2 = 1.5;
 L = 2;
 m = 0.511 * 10^6 (hbar/197)^2; (* eV/c^2 *)
 hbar = 0.658; (* eV fs *)
 k1 = \sqrt{2 m (EE - V1) / hbar^2};
 k3 = \sqrt{2 m (EE - V3) / hbar^2};
 k2 = \sqrt{2 m (EE - V2) / hbar^2};
 period = 2 \pi hbar / E;
 x1 = 5;
 x2 = 8;
 $TextStyle = {FontFamily → "Times", FontSize → 12};
 movie =
      Table[Plot[{Re[\psi Exp[-i EE t/hbar]}], Im[\psi Exp[-i EE t/hbar]], Abs[\psi Exp[-i EE t/hbar]], Abs[\psi
             \{x, 0, 20\}, PlotRange \rightarrow \{-2, 2\}, PlotPoints \rightarrow 100, PlotStyle \rightarrow
               {{Thickness[0.005], Red}, {Thickness[0.005], Blue}, {Thickness[0.005], Black}},
            PlotLabel \rightarrow StringJoin["Barrier x = 5 to x = 8, E = 3, V = 0 to 1.5, Sum, t = ",
                  ToString[t]], Frame \rightarrow True, AspectRatio \rightarrow 1 / 4, ImageSize \rightarrow 9 * 72,
            PlotPoints \rightarrow 100], {t, 0, period - (period + 1) / 10, (period + 1) / 10}];
                                                                                   Barrier x = 5 to x = 8, E = 3, V = 0 to 1.5, Sum, t = 0
                               2
```

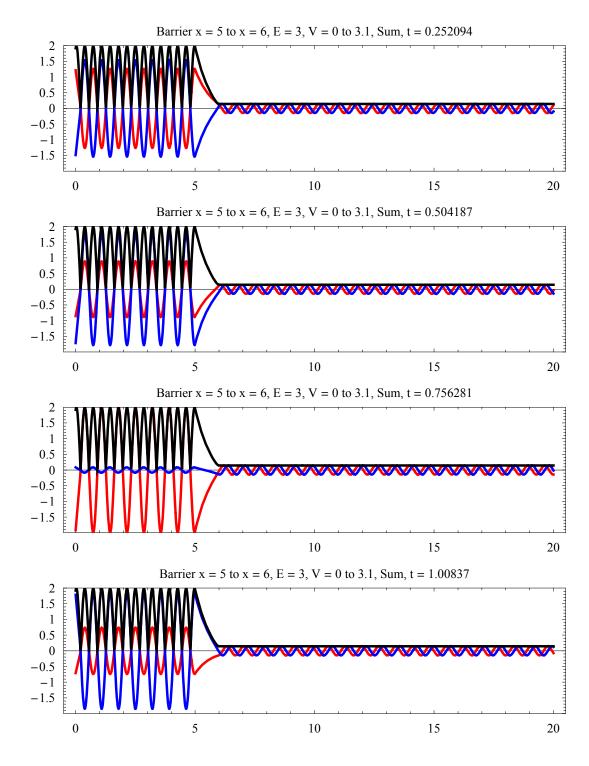


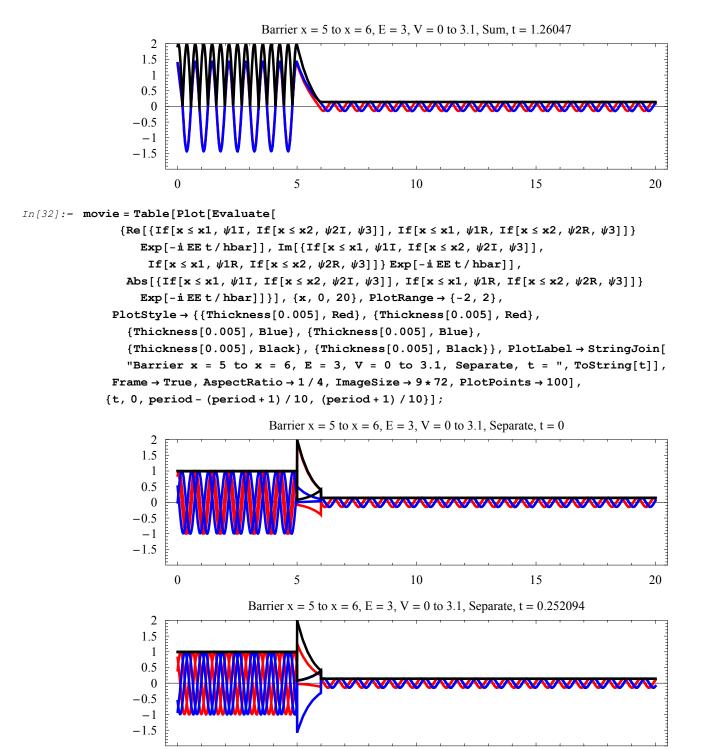


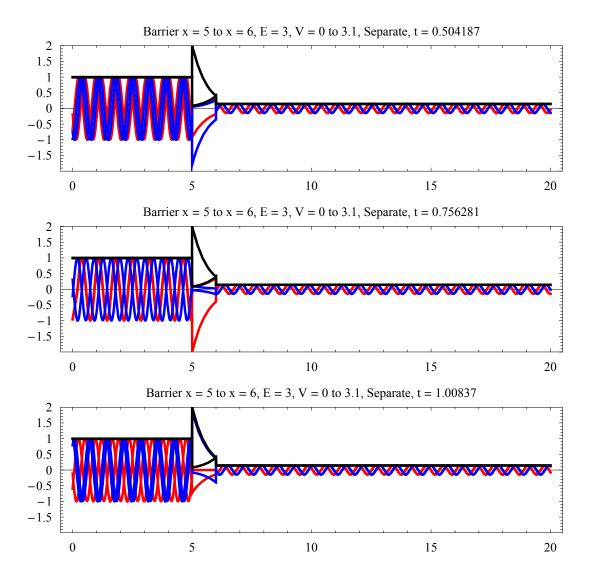












Barrier x = 5 to x = 6, E = 3, V = 0 to 3.1, Separate, t = 1.26047

```
2
                              1.5
                                   1
                              0.5
                                  0
                           -0.5
                               -1
                           -1.5
                                             0
                                                                                                   5
                                                                                                                                                        10
                                                                                                                                                                                                              15
                                                                                                                                                                                                                                                                    20
(* Double barrier *)
Quit[]
Off[General::spell1];
\psi1I = Exp[ik1x];
\psi1R = BB Exp[-ik1 x];
\psi 1 = \psi 1 I + \psi 1 R;
\psi2I = CC Exp[ik2x];
\psi2R = DD Exp[-ik2x];
\psi 2 = \psi 2I + \psi 2R;
\psi3I = FF Exp[ik3x];
\psi 3R = GG \, \text{Exp} \left[ -i \, k3 \, x \right];
\psi3 = \psi3I + \psi3R;
\psi4I = HH Exp[ik4x];
\psi4R = II Exp[-ik4 x];
\psi 4 = \psi 4 \mathtt{I} + \psi 4 \mathtt{R}\,;
\psi5 = JJ Exp[ik5 x];
\psi = Piecewise[
          \{\{\psi 1, x < x1\}, \{\psi 2, x1 \le x < x2\}, \{\psi 3, x2 \le x < x3\}, \{\psi 4, x3 \le x < x4\}, \{\psi 5, x \ge x4\}\}\}
eqns = \{\psi 1 == \psi 2 /. x \rightarrow x 1, \psi 2 == \psi 3 /. x \rightarrow x 2, \psi 3 == \psi 4 /. x \rightarrow x 3,
         \psi 4 == \psi 5 \ / \ . \ \mathbf{x} \rightarrow \mathbf{x} 4 \ , \ \partial_{\mathbf{x}} \ \psi 1 == \partial_{\mathbf{x}} \ \psi 2 \ / \ . \ \mathbf{x} \rightarrow \mathbf{x} 1 \ , \ \partial_{\mathbf{x}} \ \psi 2 == \partial_{\mathbf{x}} \ \psi 3 \ / \ . \ \mathbf{x} \rightarrow \mathbf{x} 2 \ ,
         \partial_{\mathbf{x}} \psi 3 == \partial_{\mathbf{x}} \psi 4 / . \mathbf{x} \rightarrow \mathbf{x} 3, \ \partial_{\mathbf{x}} \psi 4 == \partial_{\mathbf{x}} \psi 5 / . \mathbf{x} \rightarrow \mathbf{x} 4 \};
soln = {BB, CC, DD, FF, GG, HH, II, JJ} = FullSimplify[
             {BB, CC, DD, FF, GG, HH, II, JJ} /. Solve[eqns, {BB, CC, DD, FF, GG, HH, II, JJ}],
             Assumptions \rightarrow {x1 \in Reals, x2 \in Reals, x3 \in Reals, x4 \in Reals}][[1]]
 \{ (e^{2 i k1 x1} (e^{2 i ((k2+k3) x2+k4 x4)} (k1+k2) (k2-k3) (k3-k4) (k4-k5) - (k4-k5) (k4-k5) \} \} 
                   e^{2\ i\ (k2\ x1+k3\ x2+k4\ x4)}\ (-k1+k2)\ (k2+k3)\ (k3-k4)\ (k4-k5)\ -
                   e^{2 i (k2 x1 + k3 x3 + k4 x4)} (-k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2 i (k2 x2 + k3 x3 + k4 x4)} (k1 + k2)
                       (k2 + k3) (k3 + k4) (k4 - k5) - e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 + k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 - k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 - k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 - k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 - k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 + k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 + k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 + k5) + e^{2i(k2 \times 1 + (k3 + k4) \times 3)} (-k1 + k2) (k2 - k3) (k3 - k4) (k4 + k5) + e^{2i(k3 + k4) \times 3)} (-k1 + k2) (k4 + k5) + e^{2i(k3 + k4) \times 3)} (-k1 + k2) (k4 + k5) + e^{2i(k3 + k4) \times 3)} (-k1 + k4) (k4 + k5) + e^{2i(k3 + k4) \times 3)} (-k1 + k4) (k4 + k5) (k
                   e^{2 \ i \ (k2 \ x2 + (k3 + k4) \ x3)} \ (k1 + k2) \ (k2 + k3) \ (k3 - k4) \ (k4 + k5) \ + e^{2 \ i \ ((k2 + k3) \ x2 + k4 \ x3)} \ (k1 + k2)
                       (-e^{2 \; i \; (\,(\,k2+k3)\;\; x2+k4\; x4\,)} \;\; (-\,k1\,+\,k2\,) \;\; (\,k2\,-\,k3\,) \;\; (\,k3\,-\,k4\,) \;\; (\,k4\,-\,k5\,) \;\; +
              e^{2 \, i \, (k2 \, x1 + k3 \, x2 + k4 \, x4)} \, \left( k1 + k2 \right) \, \left( k2 + k3 \right) \, \left( k3 - k4 \right) \, \left( k4 - k5 \right) \, + \\
             e^{2\,i\,\,(k2\,\,x1+k3\,\,x3+k4\,\,x4)}\,\,\,(k1\,+\,k2)\,\,\,(k2\,-\,k3)\,\,\,(k3\,+\,k4)\,\,\,(k4\,-\,k5)\,\,-\,\,k4)
              e^{2 \ i \ (k2 \ x2 + k3 \ x3 + k4 \ x4)} \ \ (-k1 + k2) \ \ (k2 + k3) \ \ (k3 + k4) \ \ (k4 - k5) \ +
              e^{2 \ i \ (k2 \ x1 + (k3 + k4) \ x3)} \ (k1 + k2) \ (k2 - k3) \ (k3 - k4) \ (k4 + k5) \ -
              e^{2 \ i \ (k2 \ x2 + (k3 + k4) \ x3)} \ (-k1 + k2) \ (k2 + k3) \ (k3 - k4) \ (k4 + k5) \ -
             e^{2i((k2+k3) \times 2+k4 \times 3)} (-k1+k2) (k2-k3) (k3+k4) (k4+k5) +
```

```
e^{2i(k2x1+k3x2+k4x3)} (k1 + k2) (k2 + k3) (k3 + k4) (k4 + k5)), (2 e^{i(k1+k2)x1} k1
                         (e^{2i(k3\times2+k4\times4)})(k2+k3)(k3-k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times3+k4\times4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k2+k3)(k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2i(k3\times4+k4)}(-k3+k4)(k4-k5)-e^{2
                                      e^{2 i (k3+k4) \times 3} (-k2+k3) (k3-k4) (k4+k5) + e^{2 i (k3 \times 2+k4 \times 3)} (k2+k3) (k3+k4) (k4+k5)))
         (-e^{2 \ i \ ((k2+k3) \ x2+k4 \ x4)} \ (-k1+k2) \ (k2-k3) \ (k3-k4) \ (k4-k5) \ +
                        e^{2 i (k2 x1+k3 x2+k4 x4)} (k1+k2) (k2+k3) (k3-k4) (k4-k5) +
                       e^{2\,i\,\,(k2\,x1+k3\,x3+k4\,x4)}\,\,(k1+k2)\,\,(k2-k3)\,\,(k3+k4)\,\,(k4-k5)\,\,-
                        e^{2\,i\,\left(k2\,x2+k3\,x3+k4\,x4\right)}\,\,\left(-\,k1\,+\,k2\right)\,\,\left(k2\,+\,k3\right)\,\,\left(k3\,+\,k4\right)\,\,\left(k4\,-\,k5\right)\,+\,k2\,\left(k4\,-\,k5\right)\,+\,k3\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4\,\left(k4\,-\,k5\right)\,+\,k4
                        e^{2 i (k2 \times 1 + (k3 + k4) \times 3)} (k1 + k2) (k2 - k3) (k3 - k4) (k4 + k5) -
                        e^{2 \ i \ (k2 \ x2 + (k3 + k4) \ x3)} \ (-k1 + k2) \ (k2 + k3) \ (k3 - k4) \ (k4 + k5) \ -
                        e^{2 \ i \ (\,(k2+k3) \ x2+k4 \ x3)} \ (-k1+k2) \ (k2-k3) \ (k3+k4) \ (k4+k5) \ +
                       e^{2\,i\,\left(k2\,x1+k3\,x2+k4\,x3\right)}\,\left(k1+k2\right)\,\left(k2+k3\right)\,\left(k3+k4\right)\,\left(k4+k5\right))\,\text{,}
-(2e^{i(k1+k2)x1+2k2x2})k1(-e^{2i(k3x2+k4x4)}(-k2+k3)(k3-k4)(k4-k5)+
                                               e^{2 i (k3 \times 3 + k4 \times 4)} (k2 + k3) (k3 + k4) (k4 - k5) + e^{2 i (k3 + k4) \times 3} (k2 + k3) (k3 - k4) (k4 + k5) -
                                               e^{2 i (k3 x2+k4 x3)} (-k2+k3) (k3+k4) (k4+k5))) /
                 (e^{2i((k2+k3) \times 2+k4 \times 4)} (-k1+k2) (k2-k3) (k3-k4) (k4-k5) - e^{2i(k2 \times 1+k3 \times 2+k4 \times 4)} (k1+k2)
                                        (k2 + k3) (k3 - k4) (k4 - k5) - e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k2 - k3) (k3 + k4) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k4 - k5) + e^{2i(k2x1+k3x3+k4x4)} (k1 + k2) (k4 - k5) + e^{2i(k2x1+k3x4+k4x4)} (k1 + k2) (k4 - k5) + e^{2i(k2x1+k4x4)} (k1 + k2) (k4 - k3) + e^{2i(k2x1+k4x4)} (k1 + k4) + e^{2i(k2x1+k
                                e^{2 i (k2 \times 2 + k3 \times 3 + k4 \times 4)} (-k1 + k2) (k2 + k3) (k3 + k4) (k4 - k5) - \\
                               e^{2i(k2x1+(k3+k4)x3)} (k1 + k2) (k2 - k3) (k3 - k4) (k4 + k5) +
                               e^{2 i (k2 \times 2 + (k3 + k4) \times 3)} (-k1 + k2) (k2 + k3) (k3 - k4) (k4 + k5) + e^{2 i ((k2 + k3) \times 2 + k4 \times 3)} (-k1 + k2)
                                       (k2-k3)(k3+k4)(k4+k5)-e^{2i(k2x1+k3x2+k4x3)}(k1+k2)(k2+k3)(k3+k4)(k4+k5)),
  (4 e^{i((k1+k2) \times 1 + (k2+k3) \times 2)} k1 k2 (-e^{2i k4 \times 4} (-k3 + k4) (k4 - k5) + e^{2i k4 \times 3} (k3 + k4) (k4 + k5)))
         (-e^{2\ i\ ((k2+k3)\ x2+k4\ x4)}\ (-k1+k2)\ (k2-k3)\ (k3-k4)\ (k4-k5)\ +
                       e^{2 i (k2 \times 1 + k3 \times 2 + k4 \times 4)} (k1 + k2) (k2 + k3) (k3 - k4) (k4 - k5) +
                        e^{2 \; i \; (k2 \; x1 + k3 \; x3 + k4 \; x4)} \; \; (k1 + k2) \; \; (k2 - k3) \; \; (k3 + k4) \; \; (k4 - k5) \; - \; \; \\
                         e^{2 \, i \, \left(k2 \, x2 + k3 \, x3 + k4 \, x4\right)} \, \left(-k1 + k2\right) \, \left(k2 + k3\right) \, \left(k3 + k4\right) \, \left(k4 - k5\right) \, + \\
                       e^{2 \ i \ (k2 \ x1 + (k3 + k4) \ x3)} \ (k1 + k2) \ (k2 - k3) \ (k3 - k4) \ (k4 + k5) \ -
                       e^{2 i ((k2+k3) \times 2+k4 \times 3)} (-k1+k2) (k2-k3) (k3+k4) (k4+k5) +
                        e^{2\,i\,\left(k2\,x1+k3\,x2+k4\,x3\right)}\,\left(k1+k2\right)\,\left(k2+k3\right)\,\left(k3+k4\right)\,\left(k4+k5\right))\,\text{,}
   (4 e^{i (k1 x1+k2 (x1+x2)+k3 (x2+2 x3))} k1 k2 (e^{2 i k4 x4} (k3+k4) (k4-k5) - e^{2 i k4 x3} (-k3+k4) (k4+k5)))
         (-e^{2 \ i \ ((k2+k3) \ x2+k4 \ x4)} \ (-k1+k2) \ (k2-k3) \ (k3-k4) \ (k4-k5) \ +
                        e^{2 \ i \ (k2 \ x1 + k3 \ x2 + k4 \ x4)} \ (k1 + k2) \ (k2 + k3) \ (k3 - k4) \ (k4 - k5) \ +
                        e^{2 \ i \ (k2 \ x1 + k3 \ x3 + k4 \ x4)} \ (k1 + k2) \ (k2 - k3) \ (k3 + k4) \ (k4 - k5) \ -
                        e^{2 \; i \; (k2 \; x2 + k3 \; x3 + k4 \; x4)} \; \; (-k1 + k2) \; \; (k2 + k3) \; \; (k3 + k4) \; \; (k4 - k5) \; + \; \; \\
                        e^{2 \; i \; (k2 \; x1 + \, (k3 + k4) \; x3)} \; \; (k1 + k2) \; \; (k2 - k3) \; \; (k3 - k4) \; \; (k4 + k5) \; - \; \; \\
                         e^{2 \, i \, \left(k2 \, x2 + \left(k3 + k4\right) \, x3\right)} \, \left(-k1 + k2\right) \, \left(k2 + k3\right) \, \left(k3 - k4\right) \, \left(k4 + k5\right) \, - \left(k4 + k5\right) \, \left(k4 + 
                        e^{2 \; i \; (\,(k2+k3) \; x2+k4 \; x3)} \; \; (-\,k1 \; + \; k2) \; \; (k2 \; - \; k3) \; \; (k3 \; + \; k4) \; \; (k4 \; + \; k5) \; + \; (k4 \; +
                       e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)}\,\,(k1+k2)\,\,(k2+k3)\,\,(k3+k4)\,\,(k4+k5)\,)\,\text{,}
  (8 e^{i (k1 x1+k3 x2+k2 (x1+x2)+(k3+k4) x3)} k1 k2 k3 (k4+k5)) /
         (-e^{2\ i\ ((k2+k3)\ x2+k4\ x4)}\ (-k1+k2)\ (k2-k3)\ (k3-k4)\ (k4-k5)\ +
                        e^{2i(k2x_1+k3x_2+k4x_4)} (k1 + k2) (k2 + k3) (k3 - k4) (k4 - k5) +
                         e^{2 \ i \ (k2 \ x1 + k3 \ x3 + k4 \ x4)} \ (k1 + k2) \ (k2 - k3) \ (k3 + k4) \ (k4 - k5) \ -
                        e^{2 \ i \ (k2 \ x2 + k3 \ x3 + k4 \ x4)} \ \ (-k1 + k2) \ \ (k2 + k3) \ \ (k3 + k4) \ \ (k4 - k5) \ +
                        e^{2 \; i \; (k2 \; x1 + (k3 + k4) \; x3)} \; \; (k1 \; + \; k2) \; \; (k2 \; - \; k3) \; \; (k3 \; - \; k4) \; \; (k4 \; + \; k5) \; \; - \; \; \\
                        e^{2\,i\,\left(\,(k2+k3)\,\,x2+k4\,\,x3\right)} \ \left(\,-\,k1\,+\,k2\,\right) \ \left(\,k2\,-\,k3\,\right) \ \left(\,k3\,+\,k4\,\right) \ \left(\,k4\,+\,k5\,\right) \,+\, \left(\,k4\,+\,k5\,\right) \,
                        e^{2 i (k2 \times 1 + k3 \times 2 + k4 \times 3)} (k1 + k2) (k2 + k3) (k3 + k4) (k4 + k5)),
  (8 e^{i (k1 \times 1 + k3 \times 2 + k2 (x1 + x2) + k3 \times 3 + k4 \times 3 + 2 k4 \times 4)} k1 k2 k3 (k4 - k5)) /
         (-e^{2i((k2+k3) \times 2+k4 \times 4)} (-k1+k2) (k2-k3) (k3-k4) (k4-k5) +
                       e^{2 i (k2 x1+k3 x2+k4 x4)} (k1+k2) (k2+k3) (k3-k4) (k4-k5) +
                        e^{2 \; i \; (k2 \; x1 + k3 \; x3 + k4 \; x4)} \; \; (k1 + k2) \; \; (k2 - k3) \; \; (k3 + k4) \; \; (k4 - k5) \; - \; \; \\
```

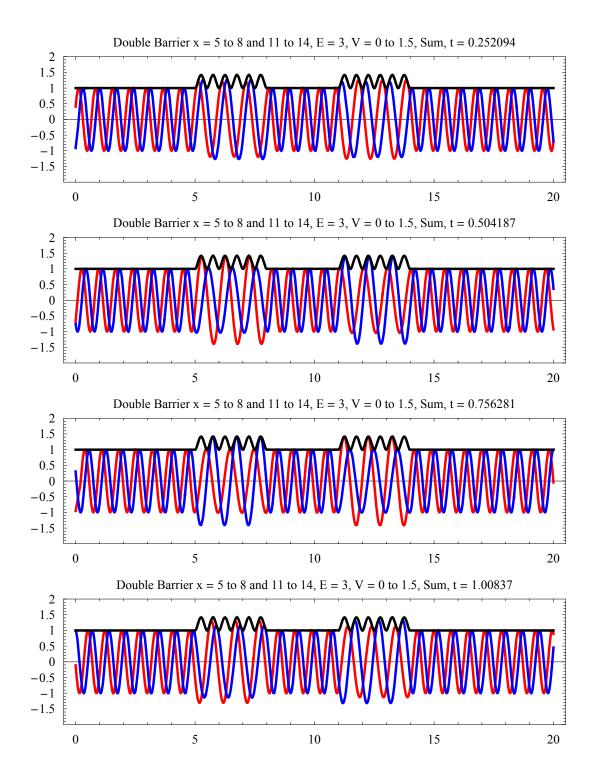
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\begin{array}{l} e^{2\,i\,\,(k2\,x2+k3\,x3+k4\,x4)} \  \, (-k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,+k4)\,\,(k4\,-k5)\,+\\ e^{2\,i\,\,(k2\,x1+\,(k3+k4)\,x3)} \  \, (k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,-k4)\,\,(k4\,+k5)\,-\\ e^{2\,i\,\,(k2\,x2+\,(k3+k4)\,x3)} \  \, (-k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,-k4)\,\,(k4\,+k5)\,-\\ e^{2\,i\,\,((k2+k3)\,x2+k4\,x3)} \  \, (-k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,,\\ (16\,e^{i\,\,(k1\,x1+k3\,x2+k2\,\,(x1+x2)+k3\,x3+k4\,x3+k4\,x4-k5\,x4)}\,\,k1\,\,k2\,\,k3\,\,k4)\,\,/\\ (-e^{2\,i\,\,((k2+k3)\,x2+k4\,x4)} \  \, (-k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,-k4)\,\,(k4\,-k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x4)} \  \, (k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,-k4)\,\,(k4\,-k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x3+k4\,x4)} \  \, (k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,+k4)\,\,(k4\,-k5)\,-\\ e^{2\,i\,\,(k2\,x2+k3\,x3+k4\,x4)} \  \, (-k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,+k4)\,\,(k4\,-k5)\,-\\ e^{2\,i\,\,(k2\,x2+(k3+k4)\,x3)} \  \, (k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,-k4)\,\,(k4\,+k5)\,-\\ e^{2\,i\,\,(k2\,x2+(k3+k4)\,x3)} \  \, (-k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,-k4)\,\,(k4\,+k5)\,-\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (-k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,-\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (-k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (-k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (k1\,+k2)\,\,(k2\,-k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (k1\,+k2)\,\,(k2\,+k3)\,\,(k3\,+k4)\,\,(k4\,+k5)\,+\\ e^{2\,i\,\,(k2\,x1+k3\,x2+k4\,x3)} \  \, (k1\,+k2)\,\,(k2\,+k
```

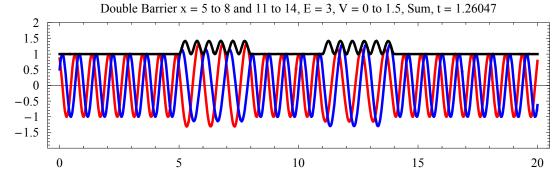
CForm[soln]

```
List((Power(E, 2 \times 1 \times 1 \times 1) \times (Power(E, 2 \times 1 \times (k2 + k3) \times 2 + k4 \times 4)) \times (k1 + k2) \times (k2 - k3) \times (k3 + k3) \times
  - k4)*(k4 - k5) -
                                                              Power (E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5)
                                                              Power(E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5)
                                                              Power (E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5)
                                                              Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5)
                                                             Power (E, 2*I*(k2*x2 + (k3 + k4)*x3))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) +
                                                             Power (E, 2*I*((k2 + k3)*x2 + k4*x3))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) -
                                                              Power (E, 2*I*(k2*x1 + k3*x2 + k4*x3))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k3)*(k4 + k4)*(k4 + k3)*(k4 + k4)*(k4 
k5)))/
                                  (-(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
                                               Power(E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
                                               Power(E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) -
                                               Power (E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
                                               Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) - k4)*(k4 + k5)*(k3 - k4)*(k4 + k5)*(k5 - k4)*(k4 + k5)*(k5 - k4)*(k5 - k4)*(k5 - k4)*(k5 - k4)*(k5 - k5)*(k5 - k5)*
                                               Power (E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
                                               Power(E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
                                               Power(E, 2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)),
                          (2*Power(E,I*(k1 + k2)*x1)*k1*(Power(E,2*I*(k3*x2 + k4*x4))*(k2 + k3)*(k3 - k3)*(k3 + k4*x4))*(k2 + k3)*(k3 + k3)*
k4)*(k4 - k5) -
                                                              Power(E, 2*I*(k3*x3 + k4*x4))*(-k2 + k3)*(k3 + k4)*(k4 - k5) - Power(E, <math>2*I*(k3)*(k3 + k4)*(k4 - k5) - Power(E, 2*I*(k3)*(k3 + k4)*(k4 - k5) - Power(E, 2*I*(k3)*(k4 - k5) - Power(E, 2*I*(k3)*(k5 -
 + k4)*x3)*(-k2 + k3)*(k3 - k4)*(k4 + k5) +
                                                               Power (E, 2*I*(k3*x2 + k4*x3))*(k2 + k3)*(k3 + k4)*(k4 + k5)))/
                                  (-(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
                                               Power (E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
                                               Power (E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) -
                                               Power (E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
                                               Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) -
                                               Power(E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) - (k4 + k5)*(k4 + k5)*(k4 + k5)*(k5 + k4)*(k4 + k5)*(k5 + k4)*(k5 + k5)*(k5 
                                               Power(E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
                                               Power (E, 2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)),
                          (-2*Power(E,I*((k1 + k2)*x1 + 2*k2*x2))*k1*(-(Power(E,2*I*(k3*x2 + k4*x4))*(-k2 + k2*x4))*(-k2 + k4*x4))*(-k2 + k4*x4))*(-k4*x4))*(-k4*x4))*(-k4*x4))*(-k4*x4)(-k4*x4))*(-k4*x4)(-k4*x4))*(-k4*x4)(-k4*x4))*(-k4*x4)(-k4*x4)(-k4*x4)(-k4*x4)(-k4*x4)(-k4*x4))*(-k4*x4)(-k4*x4)(-k4
k3)*(k3 - k4)*(k4 - k5)) +
                                                              Power (E, 2*I*(k3*x3 + k4*x4))*(k2 + k3)*(k3 + k4)*(k4 - k5) + Power (E, 2*I*(k3))*(k3 + k4)*(k4 - k5) + Power (E, 2*I*(k3))*(k2 + k3)*(k3 + k4)*(k4 - k5) + Power (E, 2*I*(k3))*(k3 + k4)*(k4 - k5) + Power (E, 2*I*(k3))*(k4 - k5) + Power (E, 2*I*(k3))*(k5 -
 + k4)*x3)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
                                                               Power (E, 2*I*(k3*x2 + k4*x3))*(-k2 + k3)*(k3 + k4)*(k4 + k5)))/
```

```
(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5) -
                            Power(E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) -
                            Power(E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) -
                            Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) +
                            Power (E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) +
                            Power (E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) -
                            Power (E, 2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)),
                (4*Power(E,I*((k1 + k2)*x1 + (k2 + k3)*x2))*k1*k2*
                              (-(Power(E, 2*I*k4*x4)*(-k3 + k4)*(k4 - k5)) + Power(E, 2*I*k4*x3)*(k3 + k4)*(k4 - k5))
+ k5)))/
                    (-(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
                            Power (E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) -
                            Power (E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) - k4)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k5 - k4)*(k4 + k5)*(k5 - k4)*(k5 - k4)*(k5 - k4)*(k5 - k5)*(k5 - k5)*
                            Power(E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
                            Power(E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
                             \text{Power}(\texttt{E}, 2*\texttt{I}*(\texttt{k}2*\texttt{x}1 + \texttt{k}3*\texttt{x}2 + \texttt{k}4*\texttt{x}3))*(\texttt{k}1 + \texttt{k}2)*(\texttt{k}2 + \texttt{k}3)*(\texttt{k}3 + \texttt{k}4)*(\texttt{k}4 + \texttt{k}5)), 
                (4*Power(E,I*(k1*x1 + k2*(x1 + x2) + k3*(x2 + 2*x3)))*k1*k2*
                              (Power(E, 2*I*k4*x4)*(k3 + k4)*(k4 - k5) - Power(E, 2*I*k4*x3)*(-k3 + k4)*(k4 + k4)*
k5)))/
                    (-(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
                            Power(E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
                            Power(E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) - k4*x4*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) - k4*x4*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) - k4*x4*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) - k4*x4*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) - k4*x4*(k4 - k5)*(k4 - 
                            Power(E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) - k4)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k5 + k4)*(k5 + k4)*(k5 + k4)*(k5 + k4)*(k5 + k4)*(k5 + k5)*(k5 + k5)*
                            Power(E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
                            Power (E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
                            Power (E, 2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)),
                (8*Power(E,I*(k1*x1 + k3*x2 + k2*(x1 + x2) + (k3 + k4)*x3))*k1*k2*k3*(k4 + k5))/
                    (-(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
                            Power (E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5)
                            Power (E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) -
                            Power (E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
                            Power(E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) + k4)*(k5) + k5) + k4)*(k5) + k5) + k5)*(k5) + k5)*(k5)
                            Power(E, 2 \times 1 \times (k2 \times 1 + k3 \times 2 + k4 \times 3)) \times (k1 + k2) \times (k2 + k3) \times (k3 + k4) \times (k4 + k5)),
                (8*Power(E,I*(k1*x1 + k3*x2 + k2*(x1 + x2) + k3*x3 + k4*x3 +
2*k4*x4))*k1*k2*k3*(k4 - k5))/
                    (-(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
                            Power(E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
                            Power(E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5) -
                            Power(E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x1 + (k3 + k4)*x3))*(k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 + k5) - k4)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k4 + k5)*(k5 + k4)*(k5 + k4)*(k5 + k4)*(k5 + k4)*(k5 + k4)*(k5 + k5)*(k5 + k5)*
                            Power(E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) -
                             \text{Power}(\texttt{E},2*\texttt{I}*((\texttt{k2}+\texttt{k3})*\texttt{x2}+\texttt{k4}*\texttt{x3}))*(-\texttt{k1}+\texttt{k2})*(\texttt{k2}-\texttt{k3})*(\texttt{k3}+\texttt{k4})*(\texttt{k4}+\texttt{k5})+\\
                            Power(E,2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)),
               (16*Power(E,I*(k1*x1 + k3*x2 + k2*(x1 + x2) + k3*x3 + k4*x3 + k4*x4 -
k5*x4))*k1*k2*k3*k4)/
                    (-(Power(E, 2*I*((k2 + k3)*x2 + k4*x4))*(-k1 + k2)*(k2 - k3)*(k3 - k4)*(k4 - k5))
                            Power (E, 2*I*(k2*x1 + k3*x2 + k4*x4))*(k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 - k5) +
                            Power (E, 2*I*(k2*x1 + k3*x3 + k4*x4))*(k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 - k5)
                            Power (E, 2*I*(k2*x2 + k3*x3 + k4*x4))*(-k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 - k5) +
                            Power(E, 2 \times 1 \times (k2 \times 1 + (k3 + k4) \times 3)) \times (k1 + k2) \times (k2 - k3) \times (k3 - k4) \times (k4 + k5) - (k4 + k5) \times (k4 + k
```

```
Power (E, 2*I*(k2*x2 + (k3 + k4)*x3))*(-k1 + k2)*(k2 + k3)*(k3 - k4)*(k4 + k5) - (k4 + k5)*(k4 + k5)*(k4 + k5)*(k5 + k4)*(k4 + k5)*(k5 + k4)*(k5 + k5)*(k5 + k5)*(k5
                 Power(E, 2*I*((k2 + k3)*x2 + k4*x3))*(-k1 + k2)*(k2 - k3)*(k3 + k4)*(k4 + k5) +
                 Power(E, 2*I*(k2*x1 + k3*x2 + k4*x3))*(k1 + k2)*(k2 + k3)*(k3 + k4)*(k4 + k5)))
EE = 3; (* eV *)
V1 = V3 = V5 = 0; (* eV *)
V2 = V4 = 1.5;
L1 = 2;
L2 = 2;
L3 = 2;
m = 0.511 * 10^6 (hbar/197)^2; (* eV/c^2 *)
hbar = 0.658; (* eV fs *)
k1 = \sqrt{2 m (EE - V1) / hbar^2};
                  2 m (EE - V2) / hbar^2;
                 2 \text{ m (EE - V3) / hbar}^2;
                 2 \text{ m (EE - V4) / hbar}^2;
k5 = \sqrt{2 m (EE - V5) / hbar^2};
period = 2 \pi hbar / E;
x1 = 5;
x2 = 8;
x3 = 11;
x4 = 14;
TextStyle = {FontFamily \rightarrow "Times", FontSize \rightarrow 12};
movie =
      Table [Plot[{Re[\psi Exp[-i EE t/hbar]], Im[\psi Exp[-i EE t/hbar]], Abs[\psi Exp[-i EE t/hbar]]},
             \{x, 0, 20\}, PlotRange \rightarrow \{-2, 2\}, PlotPoints \rightarrow 100, PlotStyle \rightarrow
                \{\{Thickness[0.005], Red\}, \{Thickness[0.005], Blue\}, \{Thickness[0.005], Black\}\}, \}
            PlotLabel \rightarrow StringJoin["Double Barrier x = 5 to 8 and 11 to
                         14, E = 3, V = 0 to 1.5, Sum, t = ", ToString[t]],
            Frame \rightarrow True, AspectRatio \rightarrow 1 / 4, ImageSize \rightarrow 9 * 72, PlotPoints \rightarrow 100],
          \{t, 0, period - (period + 1) / 10, (period + 1) / 10\}];
                                                                      Double Barrier x = 5 to 8 and 11 to 14, E = 3, V = 0 to 1.5, Sum, t = 0
                                 2
                             1.5
                                 1
                             0.5
                                 0
                          -0.5
                             -1
                          -1.5
                                           0
                                                                                              5
                                                                                                                                                10
                                                                                                                                                                                                   15
                                                                                                                                                                                                                                                      20
```





movie = Table[Plot[Evaluate[

```
 \{ \text{Re}[\{\text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}2, \, \psi 2\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}3, \, \psi 3\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}4, \, \psi 4\mathbf{I}, \, \psi 5]]]\}, \, \text{If}[\mathbf{x} \leq \mathbf{x}1, \\ \psi 1\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}2, \, \psi 2\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}3, \, \psi 3\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}4, \, \psi 4\mathbf{R}, \, \psi 5]]]\} \, \text{Exp}[-\dot{\mathbf{n}} \, \text{EE} \, \mathbf{t} \, / \, \text{hbar}]], \\ \text{Im}[\{\text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}2, \, \psi 2\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}3, \, \psi 3\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}4, \, \psi 4\mathbf{I}, \, \psi 5]]]]\} \, \text{Exp}[-\dot{\mathbf{n}} \, \text{EE} \, \mathbf{t} \, / \, \text{hbar}]], \\ \text{Abs}[\{\text{If}[\mathbf{x} \leq \mathbf{x}2, \, \psi 2\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}3, \, \psi 3\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}4, \, \psi 4\mathbf{R}, \, \psi 5]]]]\} \, \text{Exp}[-\dot{\mathbf{n}} \, \text{EE} \, \mathbf{t} \, / \, \text{hbar}]]\}, \\ \text{Abs}[\{\text{If}[\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}2, \, \psi 2\mathbf{I}, \, \text{If}[\mathbf{x} \leq \mathbf{x}3, \, \psi 3\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}4, \, \psi 4\mathbf{R}, \, \psi 5]]]]\} \, \text{Exp}[-\dot{\mathbf{n}} \, \text{EE} \, \mathbf{t} \, / \, \, \text{hbar}]]\}, \\ \text{Abs}[\{\text{If}[\mathbf{x} \leq \mathbf{x}2, \, \psi 2\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}3, \, \psi 3\mathbf{R}, \, \text{If}[\mathbf{x} \leq \mathbf{x}4, \, \psi 4\mathbf{R}, \, \psi 5]]]]\} \, \text{Exp}[-\dot{\mathbf{n}} \, \text{EE} \, \mathbf{t} \, / \, \, \text{hbar}]\}, \\ \text{Als}[\{\mathbf{x} \leq \mathbf{x}1, \, \psi 1\mathbf{x}, \, \mathbf{x}, \, \psi 1\mathbf{x}, \,
```

