

Additional exercises

1 Theory

1. A mass spectrometer has a radius of 0.3 m and an acceleration voltage of 10 000 V. The magnetic field is adjusted to the various masses to be measured. Calculate the atomic mass corresponding to a field of 0.5 T.
2. What types of radioactivity are involved in the following reactions: $^{146}_{62}\text{Sm} \rightarrow ^{142}_{60}\text{Nd}$, $^{53}_{25}\text{Mn} \rightarrow ^{53}_{23}\text{Cr}$, $^{230}_{90}\text{Th} \rightarrow ^{226}_{88}\text{Ra}$?
3. Rb has two isotopes, ^{85}Rb and ^{87}Rb , which exist in a constant ratio in our Solar System: $^{85}\text{Rb}/^{87}\text{Rb} = 2.5933$. The molar mass of Rb is 85.4678. A rock contains 10pm of Rb. How many mol/g of ^{87}Rb does that correspond to?
4. Following up from the previous question: ^{87}Rb is radioactive with a half-life $t_{1/2} = 48.8$ Gyr. What was the $^{85}\text{Rb}/^{87}\text{Rb}$ -ratio 2 billion years ago?
5. The half-life of ^{14}C is 5730 years. The ^{14}C content of the atmosphere is 13.2 disintegrations per minute and per gram (dpm g^{-1}) of carbon (initial activity A_0). We wish to date an Egyptian artefact from approximately 2000 BC. What is the approximate activity (A) of this artefact? If our method can measure 1 dpm, what mass of the (probably precious) sample will have to be destroyed?
6. Consider the Rb-Sr composition of three aliquots from the same sample:

	$^{87}\text{Rb}/^{86}\text{Sr}$	$^{87}\text{Rb}/^{86}\text{Rb}$
mineral A	0.05	0.70108
mineral B	0.10	0.70215
mineral C	0.20	0.70431

How old is the sample?

7. ^{210}Pb is a short lived ($t_{1/2}=22.3$ yr) intermediate daughter of the ^{238}U decay chain. This natural radioactive lead is incorporated into ice deposited in Greenland by forming successive layers of ice which can be studied like sedimentary strata. The activity of ^{210}Pb is measured at four levels in disintegrations per hour per kilogram of ice.

	1	2	3	4
depth (m)	0	1	1.5	2.5
^{210}Pb (dph/k)	75	32	24.0	10.0

Calculate the sedimentation rate of the ice. Assuming a constant rate and a compaction factor of 5, how thick will the glacier be in 5000 years? Calculate the ^{210}Pb -content of fresh ice (in mol/kg or atoms/kg).

8. What is the expected $^{207}\text{Pb}/^{206}\text{Pb}$ -ratio of a 4.57 billion year old meteorite? Assume that the meteorite contained no initial Pb. The half-lives of ^{238}U and ^{235}U are 4.468 and 0.704 Gyr, respectively. The present-day $^{238}\text{U}/^{235}\text{U}$ -ratio is 137.818. What is the expected $^{207}\text{Pb}/^{206}\text{Pb}$ -ratio for modern uranium-ores?

9. Consider the following three aliquots from the same sample:

	$^{206}\text{Pb}/^{204}\text{Pb}$	$^{207}\text{Pb}/^{204}\text{Pb}$	$^{238}\text{U}/^{204}\text{Pb}$
aliquot A	9.0	10.0	0
aliquot B	45.4	14.5	100
aliquot C	56.8	15.1	180
aliquot D	42.6	12.4	200

- Calculate the $^{206}\text{Pb}/^{238}\text{U}$ and $^{207}\text{Pb}/^{235}\text{U}$ ages
 - Sketch a geological history for the sample (hint: consider the U-Pb composition in concordia space).
10. Consider the Pb-Pb composition of three aliquots from a meteorite:

	1	2	3
$^{206}\text{Pb}/^{204}\text{Pb}$	107.0	407	1010
$^{207}\text{Pb}/^{204}\text{Pb}$	65.8	251	622

Use the following lookup table to estimate the age of the meteorite:

age (Ma)	4450	4475	4500	4525	4550	4575	4600	4625	4650
$^{207}\text{Pb}/^{206}\text{Pb}$	0.577	0.587	0.597	0.607	0.618	0.629	0.64	0.651	0.662

Hint: think isochrons.

- The silicate Earth weighs approximately 4×10^{24} kg and contains 250 ppm potassium. How much ^{40}Ar is created in 4.5 billion years? Given that ^{40}Ar cannot escape from the Earth and the quantity of ^{40}Ar in the atmosphere is 66000 Gt, what is the “K-Ar age of the Earth’s atmosphere”? K has three isotopes with $^{39}\text{K}/^{40}\text{K} = 7771$ and $^{41}\text{K}/^{40}\text{K} = 561$. ^{40}K is radioactive and undergoes branched decay to ^{40}Ar (10.72%) and ^{40}Ca (89.28%) with a half-life of 1.248 billion years. The molar mass of K is 39.1 g/mol.
- ^{129}I is an extinct nuclide of Iodine with a half-life of 15.7 million years. It decays (or rather: decayed!) to the noble gas ^{129}Xe . Although there is no (natural) ^{129}I in the Solar System today, the nuclide did exist during its earliest stages. Iodine-rich meteorites that within the first few 10s of millions of years of Solar System history contain measurable amounts of excess of ^{129}Xe .

Consider two meteorites with $^{129}\text{Xe}/^{127}\text{I}$ ratios of 13×10^{-5} and 8×10^{-5} , respectively. What is the age difference between the two meteorites? Assume that all the ^{129}Xe is radiogenic, and that the early Solar System had a homogeneous $^{129}\text{I}/^{127}\text{I}$ -composition.

13. Analysis of a granite yields:

$^{206}\text{Pb}^*/^{238}\text{U}$ (zircon)	$^{40}\text{Ar}^*/^{40}\text{K}$ (amphibole)	$^{40}\text{Ar}^*/^{40}\text{K}$ (biotite)	$^{87}\text{Sr}^*/^{87}\text{Rb}$ (muscovite)	$^{87}\text{Sr}^*/^{87}\text{Rb}$ (biotite)
0.084	0.304	0.248	0.00659	0.00645

What is the likely age of intrusion of this granite? How reliable is the result?

2 Practicals

2.1 Intro

1. Write a function to simulate radioactive decay, following the recipe shown in slide 13 of the first theory presentation. Compare the numerical approximation with the analytical solution. Explore the effect of different time steps on the accuracy of the simulation.
2. Install the `IsoplotRgui` package and start it using the `IsoplotR()` function. Explore the Rb-Sr, Sm-Nd, Re-Os and Lu-Hf functions.

2.2 U-Pb

1. Plot the U-Pb composition of sample 91500 on a Wetherill concordia diagram.
2. Plot the U-Pb composition of sample 91500 on a Tera-Wasserburg concordia diagram ($^{207}\text{Pb}/^{206}\text{Pb}$ vs. $^{238}\text{U}/^{206}\text{Pb}$). Use a $^{238}\text{U}/^{235}\text{U}$ -ratio of 137.818 for the conversion from Wetherill to Tera-Wasserburg space.
3. Explore the U-Pb functionality of the `IsoplotRgui` package. Change the options to compare different input formats. Each row in the example datasets represents an isotopic composition that was computed from mass spectrometer data using software that is similar to the R code that you wrote to process sample 91500. Plot data as Wetherill and Tera-Wasserburg concordia diagrams.

2.3 Ar-Ar

1. Process files `smpl11.csv` through `smpl10.csv` using your Ar-Ar data reduction script. Plot the results as an Ar-Ar release spectrum, using the following function. `Ar39` and `tx` are both vectors containing the blank corrected ^{39}Ar signals and $^{40}\text{Ar}/^{39}\text{Ar}$ age estimates, respectively:

```
spectrum <- function(Ar39,tx){  
  Ar39n <- cumsum(c(0,Ar39))/sum(Ar39) # normalise  
  plot(x=Ar39n, y=c(tx[1],tx), type='s',  
       xlab=expression(''^{39}*Ar (%)"'), ylab='Ar-Ar age (Ma)')  
}
```

2. Explore the $^{40}\text{Ar}/^{39}\text{Ar}$ -functionality of `IsoplotRgui`, including the plateau and isochron functions.