Additional exercises

1 Theory

- 1. A mass spectrometer has a radius of 0.3 m and an acceleration voltage of 10~000 V. The magnetic field is adjusted to the various masses to be measured. Calculate the atomic mass corresponding to a field of 0.5 T.
- 2. What types of radioactivity are involved in the following reactions: $^{146}_{62}\mathrm{Sm} \to ^{142}_{60}\mathrm{Nd}, ^{53}_{25}\mathrm{Mn} \to ^{23}_{23}\mathrm{Cr}, ^{230}_{90}\mathrm{Th} \to ^{226}_{88}\mathrm{Ra}?$
- 3. Rb has two isotopes, 85 Rb and 87 Rb, which exist in a constant ratio in our Solar System: 85 Rb/ 87 Rb = 2.5933. The molar mass of Rb is 85.4678. A rock contains 10pm of Rb. How many mol/g of 87 Rb does that correspond to?
- 4. Following up from the previous question: 87 Rb is radioactive with a half-life $t_{1/2} = 48.8$ Gyr. What was the 85 Rb-ratio 2 billion years ago?
- 5. The half-life of 14 C is 5730 years. The 14 C content of the atmosphere is 13.2 disintegrations per minute and per gram (dpm g⁻¹) of carbon (initial activity A_0). We wish to date an Egyptian artefact from approximately 2000 BC. What is the approximate activity (A) of this artefact? If our method can measure 1 dpm, what mass of the (probably precious) sample will have to be destroyed?
- 6. Consider the Rb-Sr composition of three aliquots from the same sample:

	$^{87}\mathrm{Rb}/^{86}\mathrm{Sr}$	$^{87}\mathrm{Rb}/^{86}\mathrm{Rb}$
mineral A	0.05	0.70108
mineral B	0.10	0.70215
mineral C	0.20	0.70431

How old is the sample?

7. ^{210}Pb is a short lived ($t_{1/2}$ =22.3 yr) intermediate daughter of the ^{238}U decay chain. This natural radioactive lead is incorporated into ice deposited in Greenland by forming successive layers of ice which can be studied like sedimentary strata. The activity of ^{210}Pb is measured at four levels in disintegrations per hour per kilogram of ice.

	1	2	3	4
depth (m)	0	1	1.5	2.5
210 Pb (dph/k)	75	32	24.0	10.0

Calculate the sedimentation rate of the ice. Assuming a constant rate and a compaction factor of 5, how thick will the glacier be in 5000 years? Calculate the ²¹⁰Pb-content of fresh ice (in mol/kg or atoms/kg).

8. What is the expected $^{207}\text{Pb}/^{206}\text{Pb}$ -ratio of a 4.57 billion year old meteorite? Assume that the meteorite contained no initial Pb. The half-lives of ^{238}U and ^{235}U are 4.468 and 0.704 Gyr, respectively. The present-day $^{238}\text{U}/^{235}\text{U}$ -ratio is 137.818. What is the expected $^{207}\text{Pb}/^{206}\text{Pb}$ -ratio for modern uranium-ores?

9. Consider the following three aliquots from the same sample:

	²⁰⁶ Pb/ ²⁰⁴ Pb	$^{207}\text{Pb}/^{204}\text{Pb}$	²³⁸ U/ ²⁰⁴ Pb
aliquot A	9.0	10.0	0
aliquot A	45.4	14.5	100
aliquot C	56.8	15.1	180
aliquot D	42.6	12.4	200

- a. Calculate the $^{206}\mathrm{Pb}/^{238}\mathrm{U}$ and $^{207}\mathrm{Pb}/^{235}\mathrm{U}$ ages
- b. Sketch a geological history for the sample (hint: consider the U-Pb composion in concordia space).
- 10. Consider the Pb-Pb composition of three aliquots from a meteorite:

	1	2	3
$\frac{206 \text{Pb}/204 \text{Pb}}{207 \text{Pb}/204 \text{Pb}}$	107.0	407	1010
	65.8	251	622

Use the following lookup table to estimate the age of the meteorite:

age (Ma)	4450	4475	4500	4525	4550	4575	4600	4625	4650
$^{207}\text{Pb}/^{206}\text{Pb}$	0.577	0.587	0.597	0.607	0.618	0.629	0.64	0.651	0.662

Hint: think isochrons.

- 11. The silicate Earth weighs approximately 4×10^{24} kg and contains 250 ppm potassium. How much 40 Ar is created in 4.5 billion years? Given that 40 Ar cannot escape from the Earth and the quantity of 40 Ar in the atmosphere is 66000 Gt, what is the "K-Ar age of the Earth's atmosphere"? K has three isotopes with 39 K/ 40 K = 7771 and 41 K/ 40 K = 561. 40 K is radioactive and undergoes branched decay to 40 Ar (10.72%) and 40 Ca (89.28%) with a half-life of 1.248 billion years. The molar mass of K is 39.1 g/mol.
- 12. ¹²⁹I is an extinct nuclide of Iodine with a half-life of 15.7 million years. It decays (or rather: decayed!) to the noble gas ¹²⁹Xe. Although there is no (natural) ¹²⁹I in the Solar System today, the nuclide did exist during its earliest stages. Iodine-rich meteorites that within the first few 10s of millions of years of Solary System history contain measurable amounts of excess of ¹²⁹Xe.

Consider two meteorites with $^{129}\text{Xe}/^{127}\text{I}$ ratios of 13×10^{-5} and 8×10^{-5} , respectively. What is the age difference between the two meteorites? Assume that all the ^{129}Xe is radiogenic, and that the early Solar System had a homogeneous $^{129}\text{I}/^{127}\text{I}$ -composition.

13. Given the ${}^{40}\mathrm{Ar}/{}^{39}\mathrm{Ar}$ -data shown in the following table:

	$^{39}{ m Ar}/^{36}{ m Ar}$	$^{40}{\rm Ar}/^{36}{\rm Ar}$
	AI/ AI	AI/ AI
std	100	2536
smp1	10	820
smp2	110	5519
smp3	160	7869

'std' is a 98 Ma reference material whose inherited argon content is of atmospheric origin ($[^{40}\mathrm{Ar}/^{36}\mathrm{Ar}]_{\mathrm{atm}}=298.5$); whereas 'smp1', 'smp2' and 'smp3' are three cogenetic aliquots of a metamorphic sample of unknown age. What are the age and non-radiogenic $^{40}\mathrm{Ar}/^{36}\mathrm{Ar}$ -ratio of the sample? Recall that the half-life of $^{40}\mathrm{K}$ is 1248 Myr.

- 14. Consider a rapidly cooled (volcanic) apatite of 10 Ma with an atomic Th/U ratio of 5. What is the ratio of helium atoms to fission tracks in it? Look up the relevant decay constants in the notes.
- 15. Analysis of a granite yields:

•	²⁰⁶ Pb*/ ²³⁸ U (zircon)	$^{40}\mathrm{Ar}^{*}/^{40}\mathrm{K}$ (amphibole)	40 Ar*/ 40 K (biotite)	⁸⁷ Sr*/ ⁸⁷ Rb (muscovite)	⁸⁷ Sr*/ ⁸⁷ Rb (biotite)
	0.084	0.304	0.248	0.00659	0.00645

What is the likely age of intrusion of this granite? How reliable is the result?

2 Practicals

- 1. Write a function to simulate radioactive decay, following the recipe shown in slide 13 of the first theory presentation. Compare the numerical approximation with the analytical solution. Explore the effect of different time steps on the accuracy of the simulation.
- 2. Plot the U-Pb composition of sample 91500 on a Tera-Wasserburg concordia diagram (207 Pb/ 206 Pb vs. 238 U/ 206 Pb). Use a 238 U/ 235 U-ratio of 137.818 for the conversion from Wetherill to Tera-Wasserburg space.
- 3. Process files smpl1.csv through smpl10.csv using your Ar-Ar data reduction script. Plot the results as an Ar-Ar release spectrum, using the following function. Ar39 and tx are both vectors containing the blank corrected ³⁹Ar signals and ⁴⁰Ar/³⁹Ar age estimates, respectively:

```
spectrum <- function(Ar39,tx){
   Ar39n <- cumsum(c(0,Ar39))/sum(Ar39) # normalise
   plot(x=Ar39n, y=c(tx[1],tx), type='s',
        xlab=expression(''^39*"Ar (%)"), ylab='Ar-Ar age (Ma)')
}</pre>
```

4. Install the IsoplotRgui package and start it using the IsoplotR() function. Explore the Rb-Sr, Sm-Nd, Re-Os and Lu-Hf functions.