



# CosmoCalc: An Excel add-in for cosmogenic nuclide calculations

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[1] As dating methods using Terrestrial Cosmogenic Nuclides (TCN) become more popular, the need arises for a general-purpose and easy-to-use data reduction software. The CosmoCalc Excel add-in calculates TCN production rate scaling factors (using Lal, Stone, Dunai, and Desilets methods); topographic, snow, and self-shielding factors; and exposure ages, erosion rates, and burial ages and visualizes the results on banana-style plots. It uses an internally consistent TCN production equation that is based on the quadruple exponential approach of Granger and Smith (2000). CosmoCalc was designed to be as user-friendly as possible. Although the user interface is extremely simple, the program is also very flexible, and nearly all default parameter values can be changed. To facilitate the comparison of different scaling factors, a set of converter tools is provided, allowing the user to easily convert cut-off rigidities to magnetic inclinations, elevations to atmospheric depths, and so forth. Because it is important to use a consistent set of scaling factors for the sample measurements and the production rate calibration sites, CosmoCalc defines the production rates implicitly, as a function of the original TCN concentrations of the calibration site. The program is best suited for  $^{10}\text{Be}$ ,  $^{26}\text{Al}$ ,  $^3\text{He}$ , and  $^{21}\text{Ne}$  calculations, although basic functionality for  $^{36}\text{Cl}$  and  $^{14}\text{C}$  is also provided. CosmoCalc can be downloaded along with a set of test data from <http://cosmocalc.googlepages.com>.

**Components:** 5243 words, 4 figures, 1 table.

**Keywords:** cosmogenic nuclides; Excel; exposure dating; banana plots; calculator.

**Index Terms:** 1150 Geochronology: Cosmogenic-nuclide exposure dating (4918); 1105 Geochronology: Quaternary geochronology; 1194 Geochronology: Instruments and techniques.

**Received** 16 November 2006; **Revised** 7 February 2007; **Accepted** 1 May 2007; **Published** 9 August 2007.

Vermeesch, P. (2007), CosmoCalc: An Excel add-in for cosmogenic nuclide calculations, *Geochem. Geophys. Geosyst.*, 8, Q08003, doi:10.1029/2006GC001530.

## 1. Introduction

[2] The first applications of Terrestrial Cosmogenic Nuclide (TCN) geochronology appeared about 20 years ago [Kurz, 1986; Nishiizumi *et al.*, 1986; Phillips *et al.*, 1986]. The method has rapidly developed since those early days, truly revolutionizing geomorphology and related fields

in the process. TCN dating is no longer a specialized tool used by a small group of experienced users, but has found an ever growing base of users who are not necessarily familiar with all the details of the method. Today we are facing a paradoxical situation. On the one hand, a better understanding of cosmogenic nuclide production systematics has improved the accuracy of TCN dating. But on the other hand, many users of the method may be less

familiar with its intricacies than was the case in the pioneering days. An important example of this situation is that of the production rate scaling factors. In a landmark paper, *Lal* [1991] presented a method to calculate cosmogenic nuclide production rates as a function of latitude and elevation. *Lal*'s scaling factors are elegant and easy to use, but overestimate the importance of muons and are only valid for standard atmosphere. Later authors introduced several improvements, incorporating atmospheric effects and improved muon production systematics. The scaling factors of *Stone* [2000], *Dunai* [2000], *Desilets and Zreda* [2003], and *Desilets et al.* [2006] more accurately represent the scaling of cosmogenic nuclide production rates with latitude and elevation, but the increased sophistication of these methods is an obstacle to their widespread use.

[3] CosmoCalc is an add-in to MS-Excel developed with the intention to alleviate this problem. The CosmoCalc interface was designed to be as user friendly and easy-to-use as possible. Default parameters are set so that beginning users only have to make a minimal number of decisions. At the same time, all the default parameters can be changed so that CosmoCalc is highly customizable and also experienced users should find it useful. The program as well as a spreadsheet with test data can be downloaded from the CosmoCalc Web site <http://cosmocalc.googlepages.com>), which also provides detailed installation instructions. The add-in requires MS-Excel 2000 or higher. Because of small differences between the MS-Windows and Apple OS-X implementations of Excel, two versions of CosmoCalc are provided. The functionality of both programs is the same, but the Macintosh version is significantly slower than the PC version. [4] After installing the CosmoCalc add-in, a toolbar menu appears (Figure 1) that guides the user through the data reduction and closely follows the outline of this paper:

- Production rate scaling factors (section 2)
  - Lal* [1991]
  - Stone* [2000]
  - Dunai* [2000]
  - Desilets and Zreda* [2003]
  - Desilets et al.* [2006]
- Shielding corrections (section 3)
  - Topographic shielding
  - Self shielding
  - Snow shielding
- Banana plots (section 4)
  - <sup>26</sup>Al-<sup>10</sup>Be
  - <sup>21</sup>Ne-<sup>10</sup>Be

- Age-erosion rate calculations (section 5)
  - Single nuclide: exposure age and erosion rate calculations for <sup>26</sup>Al, <sup>10</sup>Be, <sup>21</sup>Ne, <sup>3</sup>He, <sup>36</sup>Cl and <sup>14</sup>C
  - Two nuclides: simultaneous calculation of (burial or exposure) age and erosion rate.
- Converters (section 6)
  - Convert elevation to atmospheric pressure or -depth and back, under standard and Antarctic atmosphere.
  - Convert geomagnetic latitude to -inclination or cutoff rigidity and back.
- Settings: customizing CosmoCalc (section 7)
  - Specify TCN production rate calibration sites
  - Specify the relative importance of various production pathways

[5] The following sections will provide more details about these calculations. Thus the present paper serves as an abridged review of TCN calculations, with an emphasis on the numerical methods that are needed to solve the equations. More details about the physics of TCN production are given in the review article of *Gosse and Phillips* [2001]. CosmoCalc is not the first computational tool for TCN calculations. Useful alternatives are CHLOE, an Excel spreadsheet for cosmogenic <sup>36</sup>Cl calculations [*Phillips and Plummer*, 1996] and the CRONUS-Earth Web calculator (<http://hess.ess.washington.edu/math>) (G. Balco and J. O. H. Stone, A simple, internally consistent, and easily accessible means of calculating surface exposure ages or erosion rates from <sup>10</sup>Be and <sup>26</sup>Al measurements, manuscript in preparation, 2007; hereinafter referred to as Balco and Stone, manuscript in preparation, 2007). CosmoCalc was developed independently from these other tools, except for its topographic shielding correction function, which was translated into VBA from the Matlab code of Balco and Stone (manuscript in preparation, 2007). The reader is strongly encouraged to try these other programs. CosmoCalc is optimized for <sup>26</sup>Al, <sup>10</sup>Be, <sup>21</sup>Ne and <sup>3</sup>He dating. Because geomagnetic field fluctuations and thermal neutron reactions are ignored, results for <sup>36</sup>Cl and <sup>14</sup>C may be inaccurate. CosmoCalc can be used as an exploratory tool for these nuclides, but for more accurate results, CHLOE and the spreadsheet of *Lifton et al.* [2005] are recommended.

## 2. Production Rate Scaling Factors

[6] In the simplest case (no shielding or burial), only three pieces of information are needed to



**Figure 1.** CosmoCalc's main menu guides the user through the data reduction and follows the outline of this paper.

calculate an exposure age or erosion rate: TCN concentration, half-life and production rate. Production rates are the “Achilles’ heel” of the TCN method. There exist only a few calibration sites where TCN production rates are accurately known thanks to the availability of independent age constraints [e.g., *Nishiizumi et al.*, 1989; *Niedermann et al.*, 1994; *Kubik et al.*, 1998]. These production rates are only valid for the specific conditions (latitude, elevation, age) of each particular calibration site. To apply the TCN method to other field settings, the production rates must be scaled to a common reference at sea level and high latitude (SLHL). Up to 20% uncertainty is associated with this scaling, constituting the bulk of TCN age uncertainty.

[7] Although several efforts have been made to directly measure TCN production rate scaling with latitude and elevation using artificial  $\text{H}_2\text{O}$  and  $\text{SiO}_2$  targets [*Nishiizumi et al.*, 1996; *Brown et al.*, 2000; I. J. Graham et al., Direct measurement of cosmogenic production of  $^7\text{Be}$  and  $^{10}\text{Be}$  in water targets in the southern hemisphere, manuscript in preparation, 2007], all currently used scaling models are based on neutron monitor surveys. The oldest and still most widely used scaling model is that of *Lal* [1991]. This model is a simple set of polynomial equations giving the (spallogenic + muogenic) production rate relative to SLHL as a function of geographic latitude and elevation. In CosmoCalc, *Lal*’s scaling factors can be calculated by simply selecting two columns of latitude (in degrees) and elevation (in meters) data and clicking “OK”.

[8] *Lal*’s scaling factors use elevation as a proxy for atmospheric depth, assuming a standard atmosphere approximation. *Stone* [2000] noted that this

approximation is not valid in certain areas, such as Antarctica and Iceland. To avoid the systematic errors caused by the standard atmosphere model, *Stone* [2000] recast the polynomial equations of *Lal* [1991] in terms of air pressure instead of elevation. A second improvement of the *Stone* [2000] model is the independent scaling of TCN production by slow (negative) muons [*Heisinger et al.*, 2002a, 2002b]. In spite of this added complexity, the CosmoCalc interface for *Stone* [2000] scaling factors is identical to that for *Lal* [1991] scaling: the user simply needs to provide two columns of data, one with latitude and one with air pressure (in mbar). The scaling factors of *Stone* [2000] can be different for different nuclides, because the importance of muons depends on the nuclide of interest. Because most TCN production rate calibration sites are not located at SLHL, it is crucially important to scale the production rates using the same method as the unknown sample. This is exactly what CosmoCalc does when the user selects a nuclide from the scroll-down menu of the scaling-form. Thus the program “forces” the user to be consistent. The program comes with a set of default calibration sites, but these can be changed. Also the relative importance of the production pathways (neutrons, slow and fast muons) can be changed (section 7).

[9] Behind the scaling models of both *Lal* [1991] and *Stone* [2000] lies an extensive database of neutron monitor measurements, ordered according to geomagnetic latitude. This ordering implies that Earth’s magnetic field can be accurately approximated by a simple dipole. To avoid this approximation, *Dunai* [2000] ordered the neutron monitor data according to geomagnetic inclination, which also represents the non-dipole field. Just like *Stone* [2000], *Dunai* [2000] also incorporates separate muon scaling and atmospheric effects. However, atmospheric depth ( $\text{g}/\text{cm}^2$ ) is used instead of air pressure. Using CosmoCalc it is very easy to convert air pressure to elevation or atmospheric depth and back (section 6).

[10] Ultimately, both geomagnetic latitude and inclination are merely proxies for a more fundamental physical quantity: the geomagnetic cutoff rigidity ( $R_c$ ), which is the minimum momentum per unit charge (in GV), required for a primary cosmic ray to reach the atmosphere. Ordering the neutron monitor data according to this parameter results in yet another set of scaling factors. Unfortunately, at least three different methods for calculating  $R_c$  exist in the literature. *Dunai* [2001] used a

database of horizontal magnetic field intensities and inclinations to estimate the cutoff-rigidity of an equivalent axial dipole field, for which an approximate analytical solution exists. *Desilets and Zreda* [2003] used a model based on trajectory tracing of an axial dipole field, which is done by numerically testing the feasibility of vertically incident anti-protons to travel from the top of the atmosphere back into space. Finally, *Lifton et al.* [2005] fit a cosine function to a database of geomagnetic latitudes versus trajectory traced cut-off rigidities for the 1955 magnetic field. These authors consider the scatter around their fit to be a realistic estimator of the natural variability of  $R_c$  at any given geomagnetic latitude.

[11] In order to avoid confusion, CosmoCalc currently only implements one of these three methods, namely that of *Desilets and Zreda* [2003]. The scaling model of *Desilets and Zreda* [2003] makes a distinction between slow and fast muons, each of which scales differently. In an update of their model, *Desilets et al.* [2006] did a neutron monitor survey at low latitudes, which were undersampled by previous surveys. This resulted in a slightly different set of attenuation length polynomials for spallogenic reactions. The method of *Desilets and Zreda* [2003] and *Desilets et al.* [2006] is probably the most accurate of all the scaling models implemented in CosmoCalc. It is also the most complex model, but this did not change the user interface. Using the scaling models of *Desilets and Zreda* [2003] and *Desilets et al.* [2006] is just as easy as that of *Lal* [1991] in CosmoCalc. Default values for the relative SLHL production rate contributions of neutrons, slow and fast muons can be changed in the Settings menu (section 7).

[12] The scaling models of *Dunai* [2001], *Desilets and Zreda* [2003], *Desilets et al.* [2006], *Pigati and Lifton* [2004], and *Lifton et al.* [2005] are a sensitive function of magnetic field intensity and solar activity, both of which are poorly constrained over geologic time. On the one hand, this temporal variability is the biggest downside to  $R_c$ -based models for long exposures (>20 ka [*Dunai*, 2001]). On the other hand, such models also offer the possibility to correct for secular variation of TCN production rates for short exposures. Instructions for doing so are given by *Dunai* [2001] and *Desilets and Zreda* [2003], provided a local record of paleomagnetic intensity is available. Compiling such a record is something for advanced users and falls beyond the scope of CosmoCalc. The scaling models of *Pigati and Lifton* [2004] and *Lifton et al.*

[2005] are accompanied by global data sets of magnetic field intensity, polar wander and solar activity and in principle, it would have been possible to incorporate these data sets into CosmoCalc. However, because they are very large (4 and 7 Mb, respectively) in comparison with CosmoCalc itself (~500 kb), the cost of including these scaling models was considered too high. Therefore researchers working with  $^{14}\text{C}$ , where secular variation of the magnetic field is really crucial, should use CosmoCalc only as an exploratory tool, and use the spreadsheets of *Pigati and Lifton* [2004] and *Lifton et al.* [2005] for final calculations.

### 3. Shielding Corrections

[13] The scaling factors discussed in the previous section allow the calculation of TCN production rates at any location on the Earth's surface, assuming that the sample is a slab of zero thickness taken from a horizontal planar surface. If these assumption are not fulfilled, the SLHL production rates must be multiplied by a second set of correction factors, quantifying the extent to which the cosmic rays were blocked. CosmoCalc implements three such correction factors: topographic shielding, self shielding and snow cover.

#### 3.1. Topographic Shielding

[14] Two kinds of topographic shielding corrections can be distinguished for (1) samples taken from a tilted rather than horizontal surface and (2) samples that are located in the vicinity of topographic irregularities. CosmoCalc follows the approach of Balco and Stone (manuscript in preparation, 2007) (their Matlab function skyline.m) and treats these two effects together using the following equation:

$$S_t = 1 - \int_0^{2\pi} \frac{\sin(h(\theta))^{3.5}}{2\pi} d\theta \quad (1)$$

[15] With  $h(\theta)$  the “horizon” in the azimuthal direction  $\theta$ , i.e., either the elevation (in radians) of the topography or the sloping sample surface, whichever is greatest. Sometimes, an exponent of 2.3 is used instead of 3.5 in equation (1) [*Staudacher and Allègre*, 1993]. CosmoCalc treats this exponent as a variable, which can be changed in the Settings form (section 7). In practice, the integral of equation (1) is solved by linear interpolation between a finite number of azimuth/elevation measurements. The input needed by CosmoCalc is two mandatory columns of strike and dip (in



degrees, where the strike is 90 degrees less than the direction of the dip), followed by an optional series of topographic azimuth/elevation measurements (in degrees). There is no restriction on the total number of measurements, provided they come in multiples of two.

### 3.2. Self-Shielding

[16] Cosmic rays are rapidly attenuated as they travel through matter, causing TCN production rates to vary greatly with depth below the rock/air contact. They must be integrated over the actual sample thickness and scaled to the surface production rates before an exposure age can be calculated. Different reaction mechanisms are associated with different attenuation lengths. *Gosse and Phillips* [2001] consider four kinds of thickness corrections, for spallogenic, thermal and epithermal neutrons, and muons. Because self-shielding corrections are generally small, CosmoCalc considers only the spallogenic neutron reactions:

$$S_s = \frac{\Lambda_0}{\rho z} \left(1 - e^{-\frac{\rho z}{\Lambda_0}}\right) \quad (2)$$

with  $\Lambda_0$  the spallogenic neutron attenuation length (default value 160 g/cm<sup>2</sup>),  $\rho$  the rock density (default value 2.65 g/cm<sup>3</sup>) and  $z$  the sample thickness (in cm). Neglecting the remaining pathways makes little difference, with the possible exception of <sup>36</sup>Cl, because the latter can be strongly affected by thermal neutron fluxes, which are currently ignored by CosmoCalc.

### 3.3. Snow Cover

[17] Perhaps the most popular and powerful application of TCN techniques is the dating of glacial moraines [e.g., *Gosse et al.*, 1995; *Schäfer et al.*, 1999]. These features are generally located at high latitudes or elevations, where snow cover poses a potential problem. The snow correction is similar to the self-shielding correction with the important difference that the former is highly variable with time. Given  $n$  (e.g., 12 for monthly or 4 for seasonal) measurements of average snow thickness  $z$  and density  $\rho$ , CosmoCalc computes the snow correction factor  $S_c$  as follows:

$$S_c = \frac{1}{n} \sum_{i=1}^n e^{-\frac{\rho(i)z(i)}{\Lambda_0}} \quad (3)$$

## 4. Banana Plots

[18] Before calculating an exposure age or erosion rate, it is a good idea to check if the TCN measure-

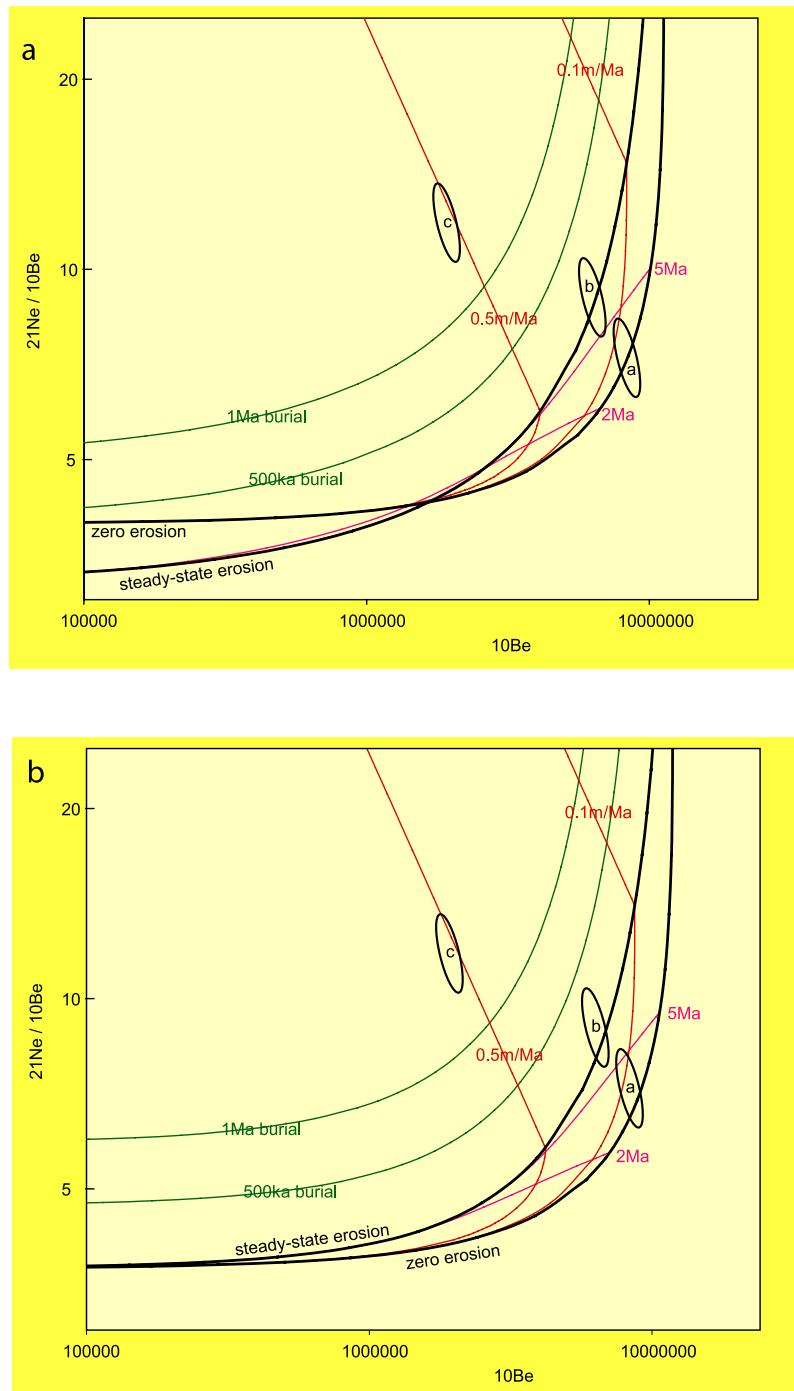
ments are consistent with a simple or complex exposure history. This can be done with two nuclides (including at least one radionuclide) using a “banana plot” [*Lal*, 1991]. CosmoCalc accommodates two types of banana plot: <sup>26</sup>Al-<sup>10</sup>Be and <sup>21</sup>Ne-<sup>10</sup>Be. Depending on whether or not a sample plots above, below or inside the so-called “steady-state erosion island” [*Lal*, 1991], one can decide whether or not to pursue the calculation of an exposure age, erosion rate or burial age. For the construction of the banana plots and the age-erosion calculations of section 5, CosmoCalc implements a modified version of the ingrowth equation of *Granger and Muzikar* [2001]:

$$N = P e^{-\lambda \tau} \sum_{i=0}^3 \frac{F_i}{\lambda + \epsilon \rho / \Lambda_i} \left(1 - e^{-(\lambda + \epsilon \rho / \Lambda_i)t}\right) \quad (4)$$

[19] With  $N$  the nuclide concentration (atoms/g),  $P$  the total surface production rate (in atoms/g/yr) at SLHL,  $\tau$  the burial age,  $\epsilon$  the erosion rate,  $t$  the exposure age and  $\lambda$  the radioactive half-life of the nuclide. Equation (4) models TCN production by neutrons, slow and fast muons by a series of exponential approximations. The first term of the summation models TCN production by spallogenic neutron reactions, the second and third terms model slow muons and the last term approximates TCN production by fast muons. Thus  $F_0, \dots, F_3$  are dimensionless numbers between zero and one, and  $\Lambda_0, \dots, \Lambda_3$  are attenuation lengths (g/cm<sup>2</sup>). The approach of *Granger and Smith* [2000] and *Granger et al.* [2001] was chosen because of its flexibility. For instance, neglecting muon production can be easily implemented by setting  $F_1, F_2$  and  $F_3$  equal to zero in equation (4). CosmoCalc uses *Granger and Smith*’s [2000] and *Granger et al.*’s [2001] recommended values of  $F_0, \dots, F_3$  for <sup>10</sup>Be and <sup>26</sup>Al, but also offers an alternative choice of pre-set values approximating either the alternative parameterization of *Schaller et al.* [2002], neglecting the contribution of muons, or only using three exponentials (for more details, see section 7). Banana plots with non-zero muon contributions feature a characteristic cross-over of the steady-state and zero erosion lines which is absent when muons are neglected (Figure 2).

[20] CosmoCalc’s banana plots are normalized to SLHL, meaning that the TCN concentrations of each sample are divided by the cumulative effect of all their correction factors, represented by the “effective scaling factor”  $S_e$ :

$$S_e = S_i \times f(S) \quad (5)$$



**Figure 2.** By using the TCN production equation of *Granger and Smith* [2000] (equation (4)), CosmoCalc's banana plots are very flexible, as illustrated by two  $^{21}\text{Ne}$ - $^{10}\text{Be}$  diagrams: (a) with default parameters as given by *Granger and Smith* [2000] and in Table 1 and (b) using only spallation by neutrons, i.e., no muons. TCN production by muons causes a characteristic cross-over of the zero-erosion and infinite exposure lines at low  $^{10}\text{Be}$  concentrations. The ellipses mark the  $2\sigma$  uncertainties of three samples (labeled a, b, and c).

with

$$S = S_p \times S_s \times S_c \quad (6)$$

where  $S_p$  is one of the production rate scaling factors of section 2 and  $S_t$ ,  $S_s$  and  $S_c$  are defined in section 3. If muon production is neglected, then  $S_e = S_t \times S_p \times S_s \times S_c$ . However, in the presence of muons, the effective scaling factor  $S_e$  may deviate from this value because the relative importance of the different production mechanisms changes as a function of age, erosion rate, elevation, latitude, sample thickness and snow cover. The exact form of the function  $f(S)$  will be defined in section 5.2.4. Note that the topographic shielding correction  $S_t$  does not “fractionate” (i.e., change the fractions  $F_0, \dots, F_3$  of) the different production mechanisms and is placed outside the scaling function  $f(S)$ . This means that, strictly speaking, the TCN concentrations should be divided by  $S_t$  prior to generating a banana plot. The input required by CosmoCalc’s “Banana” function are (1) the composite scaling factor  $S$  for the first nuclide ( $^{26}\text{Al}$  or  $^{21}\text{Ne}$ ), (2) the concentration and  $1\sigma$  measurement uncertainty of the first nuclide ( $^{26}\text{Al}$  or  $^{21}\text{Ne}$ ), both divided by  $S_t$ , (3)  $S$  for the second nuclide ( $^{10}\text{Be}$ ), and (4) the concentration and  $1\sigma$  measurement uncertainty of the second nuclide ( $^{10}\text{Be}$ ), also divided by  $S_t$ . Because topographic shielding corrections are generally small, the systematic error caused by lumping  $S_t$  together with the other correction factors is very small. Therefore, if  $S_t > \sim 0.95$ , say, it is safe to approximate equation (5) by  $S_e = f(S_t \times S_p \times S_s \times S_c)$ . In this case, the nuclide concentrations do not need to be pre-divided by  $S_t$ .

[21] The graphical output of CosmoCalc can easily be copied and pasted for editing in vector graphics software such as Adobe Illustrator or CorelDraw. The y-axis of the  $^{26}\text{Al}$ - $^{10}\text{Be}$  plot is logarithmic by default whereas the y-axis of the  $^{21}\text{Ne}$ - $^{10}\text{Be}$  plot is linear. These defaults can be changed in the “Banana Options” userform. Note that MS-Excel (versions 2000 and 2003) only allows logarithmic tick marks to have values in multiples of ten. To get around this limitation, CosmoCalc uses a “pseudo y-axis”, which cannot be edited by the usual right mouse button click. Hopefully, this limitation will not be necessary in later versions of Excel. CosmoCalc only propagates the analytical uncertainty of the measured TCN concentrations. No uncertainty is assigned to the production rate scaling factors, radioactive half-lives or other potentially ill-constrained quantities. On the banana plots, the user is offered the choice between error bars

or -ellipses with the latter being the default. Banana plots are graphs of the type  $N_1/N_2$  vs.  $N_2$  which are always associated with some degree of “spurious correlation” [Chayes, 1949]. This causes the error ellipses to be rotated according to the following correlation coefficient:

$$\rho_c = - \frac{\bar{N}_1 \sigma_{N_2}}{\sqrt{\bar{N}_2^2 \sigma_{N_1}^2 + \bar{N}_1^2 \sigma_{N_2}^2}} \quad (7)$$

[22] If  $N_1$  stands for  $^{26}\text{Al}$  or  $^{21}\text{Ne}$  and  $N_2$  for  $^{10}\text{Be}$ , then  $\bar{N}_1$  and  $\bar{N}_2$  are the measured concentrations of these respective nuclides while  $\sigma_{N_1}$  and  $\sigma_{N_2}$  are the corresponding measurement uncertainties.

## 5. Age-Erosion Rate Calculations

[23] Equation (4) has three unknowns:  $t$  (exposure age),  $\epsilon$  (erosion rate) and  $\tau$  (burial age). If only one nuclide was measured, we must assume values for two of these quantities in order to solve for the third. If two nuclides were analyzed (of which at least one is radioactive), only one assumption is needed. CosmoCalc is capable of both approaches. In this section, we will first discuss how to solve for  $\epsilon$  (assuming infinite exposure age and zero burial) and  $t$  (assuming zero erosion and burial) using a single nuclide (section 5.1). Then, numerical methods will be presented to simultaneously solve for  $t$  and  $\epsilon$  (assuming zero burial),  $t$  and  $\tau$  (assuming zero erosion) or  $\epsilon$  and  $\tau$  (assuming infinite exposure age), using two nuclides (section 5.2). Note that in the case of two nuclides ( $^{26}\text{Al}$  or  $^{21}\text{Ne}$  combined with  $^{10}\text{Be}$ ), the assumption of zero burial can be verified on the banana plot.

### 5.1. Calculations Using a Single Nuclide

[24] CosmoCalc requires three pieces of information to calculate an exposure age or erosion rate: the TCN concentration (corrected for topography), its analytical uncertainty and a composite correction factor for production rate scaling with latitude/elevation and shielding (equation (6)). We somehow need to incorporate this scaling factor into the ingrowth equation (equation (4)). This poses a problem because the scaling factor is a single number whereas equation (4) explicitly makes the distinction between neutrons, slow and fast muons. Granger and Smith [2000] avoid this problem by separately scaling the different production mechanisms:

$$N(t, \epsilon, \tau) = Pe^{-\lambda\tau} \sum_{i=0}^3 \frac{S_i F_i}{\lambda + \epsilon \rho / \Lambda_i} \left( 1 - e^{-(\lambda + \epsilon \rho / \Lambda_i)t} \right) \quad (8)$$

[25] Instead of one scaling factor, equation (8) has four, one for neutrons ( $S_0$ ), two for slow muons ( $S_1$  and  $S_2$ ) and one for fast muons ( $S_3$ ). *Granger et al.* [2001] separately calculate each of these four scaling factors. Thus the original method of *Granger and Smith* [2000] is incompatible with the common practice of lumping all production mechanisms into a single latitude/elevation scaling factor (section 2). To ensure optimal flexibility and user-friendliness, CosmoCalc uses a slightly different approach.  $S_0, \dots, S_3$  are calculated from the composite correction factor  $S$ , by approximating the total scaling by a single attenuation factor caused by a virtual layer of matter of thickness  $x$  (in  $\text{g/cm}^2$ ):

$$S_i = e^{-x/\Lambda_i} \quad \text{for } i = 0, \dots, 3 \quad (9)$$

so that

$$\sum_{i=0}^3 S_i F_i = S \quad (10)$$

with  $F_i$  and  $\Lambda_i$  as in equation (4) and  $S$  as defined in equation (6). CosmoCalc solves equation (10) iteratively using Newton's method.

[26] As said before, some assumptions are needed to solve equation (8). An exposure age ( $t$ ) can be calculated under the assumption of zero erosion and burial ( $\epsilon = 0$ ,  $\tau = 0$ ). For a radionuclide with decay constant  $\lambda$ , this yields:

$$t = -\frac{1}{\lambda} \ln \left( 1 - \frac{N\lambda}{PS} \right) \quad (11)$$

whereas for stable nuclides ( $^3\text{He}$  and  $^{21}\text{Ne}$ ):

$$t = \frac{N}{PS} \quad (12)$$

[27] Alternatively, the erosion rate ( $\epsilon$ ) can be calculated under the assumption of steady state and zero burial ( $t = \infty$ ,  $\tau = 0$ ):

$$N(\epsilon) = P \sum_{i=0}^3 \frac{S_i F_i}{\lambda + \epsilon \rho / \Lambda_i} \quad (13)$$

[28] CosmoCalc solves this equation iteratively using Newton's method. Statistical uncertainties are estimated by standard error propagation:

$$\sigma_t = \frac{\sigma_N}{PS - N\lambda} \quad (14)$$

$$\sigma_\epsilon = \frac{\sigma_N}{P \sum_{i=0}^3 \frac{S_i F_i}{((\Lambda_i/\rho)(\lambda + \epsilon \rho / \Lambda_i))^2}} \quad (15)$$

[29] These error estimates do not include any uncertainties in production rates and scaling factors, which are difficult to quantify, but can be evaluated by using a range of input parameters.

## 5.2. Calculations With Two Nuclides

[30] Equation (8) has three unknowns ( $t$ ,  $\epsilon$  and  $\tau$ ). If two nuclides have been measured (with concentrations  $N_1$  and  $N_2$ , say), only one value must be assumed in order to solve for the remaining two. By assuming zero erosion ( $\epsilon = 0$ ), CosmoCalc simultaneously calculates the exposure age and burial age (section 5.2.1); by assuming steady-state erosion ( $t = \infty$ ), the erosion rate and burial age are calculated; and by assuming zero-burial ( $\tau = 0$ ), the erosion rate and exposure age can be computed (section 5.2.2).

### 5.2.1. Burial Dating

[31] If a rock surface gets buried by sediments or covered by ice, it is shielded from cosmic rays and the concentration of cosmogenic radionuclides decays with time. Such samples plot outside the steady-state erosion island of the banana plot, in the so-called field of "complex exposure", a feature which is considered undesirable by most studies. Other studies, however, intentionally target complex exposure histories, using radionuclides to date pre-exposure and burial [e.g., *Bierman et al.*, 1999; *Fabel et al.*, 2002; *Partridge et al.*, 2003]. CosmoCalc calculates burial ages, either by assuming negligible erosion or steady state erosion ( $\epsilon = 0$  or  $t = \infty$ , respectively). It does not handle post-depositional nuclide production.

#### 5.2.1.1. Burial-Exposure Dating

[32] If  $\epsilon = 0$ , equation (8) reduces to:

$$N = e^{-\lambda\tau} \frac{SP}{\lambda} (1 - e^{-\lambda t}) \quad (16)$$

[33] The easiest case of two-nuclide dating is that of simultaneously calculating exposure age ( $t$ ) and burial age ( $\tau$ ) with one radionuclide and one stable nuclide. Because the stable nuclide is not affected by burial, it can be used to calculate the pre-exposure age, using equation (12). This age can then be used to calculate the burial age:

$$\tau = \frac{1}{\lambda} \ln \left( \frac{SP}{N\lambda} (1 - e^{-\lambda t}) \right) \quad (17)$$



[34] In the case of two radionuclides, CosmoCalc finds  $t$  by iteratively solving the following equation using Newton's method:

$$\lambda_2 \ln \left( \frac{(SP)_1}{N_1 \lambda_1} (1 - e^{-\lambda_1 t}) \right) - \lambda_1 \ln \left( \frac{(SP)_2}{N_2 \lambda_2} (1 - e^{-\lambda_2 t}) \right) = 0 \quad (18)$$

[35] With  $\lambda_1 > \lambda_2$ . The solution is then plugged into equation (17), using nuclide 1.

### 5.2.1.2. Burial-Erosion Dating

[36] Setting  $t = \infty$  in equation (8) yields the following system of non-linear equations for TCN concentrations  $N_1$  and  $N_2$ :

$$\begin{cases} f_1(\epsilon, \tau) : N_1 = P_1 e^{-\lambda_1 \tau} \sum_{i=0}^3 \frac{S_{i,1} F_{i,1}}{\lambda_1 + \epsilon \rho / \Lambda_{i,1}} \\ f_2(\epsilon, \tau) : N_2 = P_2 e^{-\lambda_2 \tau} \sum_{i=0}^3 \frac{S_{i,2} F_{i,2}}{\lambda_2 + \epsilon \rho / \Lambda_{i,2}} \end{cases} \quad (19)$$

[37] These equations are easy to solve since the variables  $\tau$  and  $\epsilon$  are separated. If nuclide 1 has the shortest half-life (largest decay constant  $\lambda$ ), the burial age is written as a function of the erosion rate  $\epsilon$ :

$$\tau = \frac{1}{\lambda_1} \ln \left( \frac{P_1}{N_1} \sum_{i=0}^3 \frac{S_{i,1} F_{i,1}}{\lambda_1 + \epsilon \rho / \Lambda_{i,1}} \right) \quad (20)$$

[38] The erosion rate is given implicitly by:

$$\begin{aligned} & \lambda_2 \ln \left( \frac{P_1}{N_1} \sum_{i=0}^3 \frac{S_{i,1} F_{i,1}}{\lambda_1 + \epsilon \rho / \Lambda_{i,1}} \right) \\ & - \lambda_1 \ln \left( \frac{P_2}{N_2} \sum_{i=0}^3 \frac{S_{i,2} F_{i,2}}{\lambda_2 + \epsilon \rho / \Lambda_{i,2}} \right) \\ & = 0 \end{aligned} \quad (21)$$

[39] CosmoCalc solves equation (21) for  $\epsilon$  using Newton's method and then plugs this value into equation (20). If  $\lambda_2 < \lambda_1$ , then  $N_2$  is used instead of  $N_1$  in equation (20).

### 5.2.2. Age-Erosion Rate Calculations

[40] Assuming zero burial ( $\tau = 0$ ) yields the following system of equations  $f_1$  and  $f_2$ :

$$\begin{cases} f_1(\epsilon, t) : N_1 = P_1 \sum_{i=0}^3 \frac{S_{i,1} F_{i,1}}{\lambda_1 + \epsilon \rho / \Lambda_{i,1}} (1 - e^{-(\lambda_1 + \epsilon \rho / \Lambda_{i,1})t}) \\ f_2(\epsilon, t) : N_2 = P_2 \sum_{i=0}^3 \frac{S_{i,2} F_{i,2}}{\lambda_2 + \epsilon \rho / \Lambda_{i,2}} (1 - e^{-(\lambda_2 + \epsilon \rho / \Lambda_{i,2})t}) \end{cases} \quad (22)$$

[41] It is impossible to solve these equations for exposure age ( $t$ ) and erosion rate ( $\epsilon$ ) separately. Instead, CosmoCalc implements the two-dimensional version of the Newton-Raphson algorithm:

$$\begin{bmatrix} \epsilon_{k+1} \\ t_{k+1} \end{bmatrix} = \begin{bmatrix} \epsilon_k \\ t_k \end{bmatrix} - \begin{bmatrix} a = \left( \frac{\partial f_1}{\partial \epsilon} \right)_k & b = \left( \frac{\partial f_1}{\partial t} \right)_k \\ c = \left( \frac{\partial f_2}{\partial \epsilon} \right)_k & d = \left( \frac{\partial f_2}{\partial t} \right)_k \end{bmatrix}^{-1} \begin{bmatrix} f_1(\epsilon_k, t_k) \\ f_2(\epsilon_k, t_k) \end{bmatrix} \quad (23)$$

[42] With  $J(\epsilon, t) = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$  the Jacobian matrix, which is also used for error propagation.

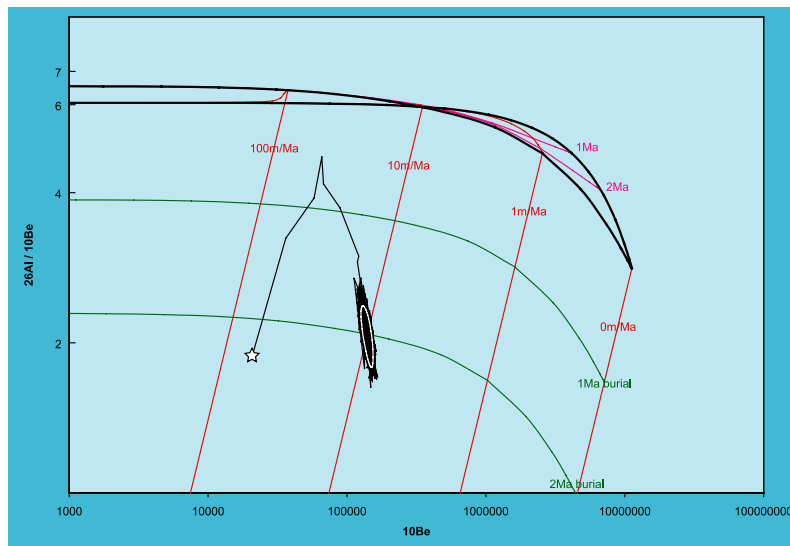
### 5.2.3. Error Propagation

[43] Error propagation is less straightforward in the two-dimensional case than in the single nuclide case (section 5.1). The bijection from  $(N_1, N_2)$ -space to  $(\epsilon, t)$ -space is not orthogonal, particularly in the case of age-erosion dating (section 5.2.2). For this reason, it is only possible to analytically compute upper bounds for  $\sigma(\epsilon)$ ,  $\sigma(\tau)$  and  $\sigma(t)$ :

$$\begin{bmatrix} \sigma(x) \\ \sigma(y) \end{bmatrix} \leq \| J(x, y)^{-1} \| \begin{bmatrix} \sigma(N_1) \\ \sigma(N_2) \end{bmatrix} \quad (24)$$

with  $x$  and  $y$  placeholders for  $\epsilon$  and  $t$  or  $\tau$ , respectively. And  $\|\cdot\|$  the absolute values of the matrix  $[\cdot]$ . In the case of age-erosion dating, the confidence intervals for  $t$  and  $\epsilon$  are very wide, often too wide to be useful. Therefore it can be more productive to solve each quantity separately instead of simultaneously. Thus, using equations (11) and (13), it is possible to estimate minimum exposure ages and maximum erosion rates [e.g., *Nishiizumi et al.*, 1991]. However, for burial dating there is no choice and we must simultaneously solve for  $\tau$  and  $\epsilon$  or  $t$ .

[44] In addition to Newton's method, CosmoCalc offers a second way of solving equations (19) and (22) by means of Monte Carlo simulation, implementing the Metropolis-Hastings algorithm [*Metropolis et al.*, 1953; *Tarantola*, 2004]. The Metropolis-Hastings algorithm is a so-called Bayesian MCMC (Markov Chain Monte Carlo) method. It not only finds the best solution to the system of non-linear equations, but actually explores the entire solution space. If the "Metropolis" option of the Age-Erosion function is selected,



**Figure 3.** Starting with a random guess (white star) for the erosion rate ( $\epsilon$ ) and burial age ( $\tau$ ), the Metropolis-Hastings algorithm quickly finds the optimal solution. It then continues to randomly sample the solution space defined by the measurement uncertainties. The white ellipse is the  $2\sigma$  confidence region, which corresponds to  $\sim 90\%$  of the bivariate ( $\epsilon, \tau$ ) solution-space. The black area contains the last 90% of the 1000 accepted values generated by the algorithm; 95% of these 900 values are used to calculate the simultaneous confidence intervals for  $\epsilon$  and  $\tau$ .

CosmoCalc generates 1000 “acceptable” solutions to equation (19) or (22), where “acceptable” is defined by the bivariate normal likelihood of the forward-modeled TCN concentrations (Figure 3). The last 900 of these solutions are then ranked according to their likelihood. For a 95% confidence interval, those solutions with the lowest 5% likelihoods of the 900 results are discarded, leaving 855 values for  $\epsilon$ ,  $t$  or  $\tau$ . The minimum and maximum values of these 855 numbers are the lower and upper bounds, respectively, of the simultaneous 95% confidence intervals. In contrast with the symmetric confidence intervals given by equation (24), the MCMC confidence limits are always positive. However, as said before, the 95% confidence intervals can be very wide especially in the case of age-erosion dating.

#### 5.2.4. A Posteriori Modification of the Banana Plots

[45] Section 4 discussed the construction of  $^{26}\text{Al}$ - $^{10}\text{Be}$  and  $^{21}\text{Ne}$ - $^{10}\text{Be}$  banana plots. To plot samples from different field locations (with different latitude, elevation and shielding conditions) together on the same banana plot, it is necessary to scale the TCN concentrations to SLHL. In other words, each TCN concentration must be divided by

an appropriate scaling factor, the so-called “effective scaling factor”  $S_e$  (equation (5)):

$$S_e = \frac{N_{meas}}{N_{SLHL}} \quad (25)$$

[46] With  $N_{meas}$  the measured TCN concentration, and  $N_{SLHL}$  the equivalent TCN concentration which would be measured had the sample been collected from SLHL. In the case of zero erosion,  $N_{SLHL} = N_{meas}/(S_p \times S_t \times S_s \times S_c)$ . This is no longer true when  $\epsilon > 0$ , because the relative contributions of neutron spallation, slow and fast muons change below the surface. This is the “fractionation” effect that was discussed in section 4 and quantified by equation (10). For example, consider the case of two high latitude, high elevation samples, one with negligible erosion ( $\epsilon = 0$ ) and one with non-zero erosion ( $\epsilon > 0$ ). Because the relative importance of neutron spallation increases with decreasing erosion rate, and neutrons are more important (relative to muons) at higher elevations,  $S_e$  will be greater for the zero erosion than for the non-zero erosion case. CosmoCalc first solves equation (19) or (22) for  $\epsilon$  and  $\tau$  or  $t$ , whichever fits the measured TCN concentrations best. Plugging these solutions into equation (4) yields the

equivalent TCN concentration at SLHL.  $S_e$  is then given by equation (25).

## 6. Converters

[47] Section 2 discussed four different models to scale TCN production rates from SLHL to any other location on Earth. All these models have in common that they require two columns of data in CosmoCalc: “latitude” and “elevation”. They differ in how they quantify these two pieces of information. The scaling factors of *Lal* [1991] are the only ones that use the actual geographical latitude (in degrees) and elevation (in meters). *Stone* [2000] also uses the geographical latitude for estimating the latitude effect, but uses atmospheric pressure (in mbar) for modeling the elevation effect. *Dunai* [2000] uses the geomagnetic inclination (in degrees) instead of latitude, and atmospheric depth (in  $\text{g/cm}^2$ ) instead of elevation. Finally, *Desilets and Zreda* [2003] and *Desilets et al.* [2006] use cut-off rigidity (in GV) for the latitude effect and atmospheric depth for the elevation effect.

[48] All these different measures of “latitude” and “elevation” are related to each other and can be converted into each other. To facilitate the comparison of the different methods and, for example, reinterpret published literature data, CosmoCalc provides a series of easy-to-use conversion tools.

### 6.1. Converting Different Measures of “Elevation”

[49] To convert elevation ( $z$ , in m) to atmospheric pressure ( $p$ , in mbar) [*Iribane and Godson*, 1992]:

$$p = p_0 \left( 1 - \frac{\beta_0 z}{T_0} \right)^{\frac{g_0}{R_d \beta_0}} \quad (26)$$

[50] With  $p_0$  the pressure at sea level,  $\beta_0$  the adiabatic lapse rate,  $T_0$  the temperature at sea level,  $g_0$  the gravitational constant and  $R_d$  the universal gas constant. In the standard atmospheric model,  $\beta_0 = 6.5 \text{ K/km}$ ,  $g_0 = 9.80665 \text{ m/s}^2$ ,  $p_0 = 1013.25 \text{ mbar}$  and  $T_0 = 288.15 \text{ K}$ . However, these values are not valid for Antarctica, where  $p_0 \approx 989.1 \text{ mbar}$  and  $T_0 \approx 250 \text{ K}$ . The modified equation (26) can be rewritten as [*Stone*, 2000]:

$$p_{ant} = 989.1 e^{-\frac{z}{7588}} \quad (27)$$

[51] Atmospheric pressure is converted to atmospheric depth ( $\text{g/cm}^2$ ) by:

$$d = 10 \frac{p}{g_0} \quad (28)$$

[52] The reverse conversions are trivial inversions of these equations.

### 6.2. Converting Different Measures of “Latitude”

[53] Converting latitude ( $L$ , in degrees) to geomagnetic inclination ( $I$ , in degrees) and back:

$$\tan I = 2 \tan L \quad (29)$$

[54] Converting latitude to geomagnetic cut-off rigidity (in GV) for a geomagnetic field strength  $M$ , compared to the 1945 reference value ( $M_0 = 8.085 \times 10^2 \text{ A m}^2$ ):

$$R_c = \sum_{i=1}^6 \left( e_i + f_i \left( \frac{M}{M_0} \right) \right) L^i \quad (30)$$

[55] The default value for  $M/M_0 = 1$ , but can be changed by clicking the “Option” button of the CosmoCalc conversion form.  $e_1, \dots, e_6$  and  $f_1, \dots, f_6$  are defined in Table 8 of *Desilets and Zreda* [2003]. The reverse operation of equation (30) does not have an analytical solution and is solved iteratively with Newton’s method.

## 7. Customizing CosmoCalc

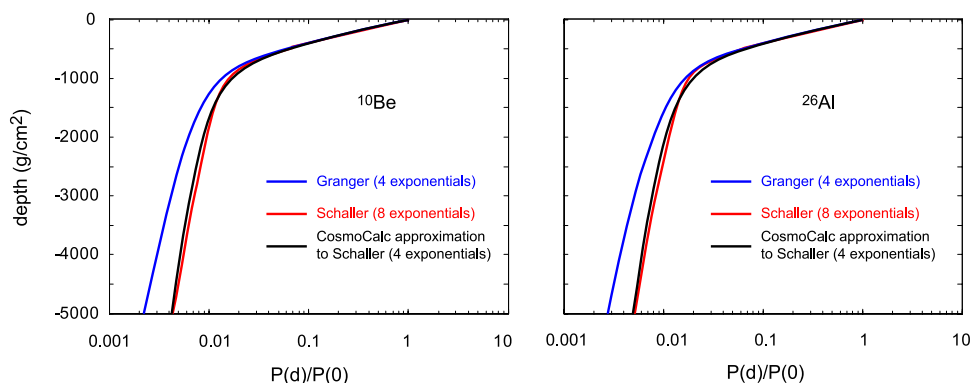
[56] The interface of CosmoCalc is very simple because default values are set for most of the parameters that occur in the various equations discussed in this paper (Table 1). This greatly reduces the chance that novice users make mistakes when reducing their TCN data. For more advanced users, the program allows nearly all the parameters to be changed.

### 7.1. Specifying the Production Rate Calibration Sites

[57] As mentioned in section 2, it is very important to use a consistent set of scaling factors for the unknown sample and the production rate calibration site. Failing to do so can cause significant systematic errors. To avoid this, CosmoCalc defines the SLHL production rates implicitly, by specifying a set of calibration sites and their measured TCN concentrations. Using the “Calibration sites” form of the “Settings” menu, these

**Table 1.** Default Values of CosmoCalc Parameters

Parameter	Symbol	Default Value	Units
Rock density	$\rho$	2.65	$\text{g/cm}^3$
Decay constant ( $^{10}\text{Be}$ )	$\lambda(^{10}\text{Be})$	4.560E-07	$\text{yr}^{-1}$
Decay constant ( $^{26}\text{Al}$ )	$\lambda(^{26}\text{Al})$	9.800E-07	$\text{yr}^{-1}$
Decay constant ( $^{36}\text{Cl}$ )	$\lambda(^{36}\text{Cl})$	2.300E-06	$\text{yr}^{-1}$
Decay constant ( $^{14}\text{C}$ )	$\lambda(^{14}\text{C})$	1.213E-04	$\text{yr}^{-1}$
Attenuation length (neutrons)	$\Lambda_0$	160	$\text{g/cm}^2$
Attenuation length (slow muons)	$\Lambda_1$	738	$\text{g/cm}^2$
Attenuation length (slow muons)	$\Lambda_2$	2688	$\text{g/cm}^2$
Attenuation length (fast muons)	$\Lambda_3$	4360	$\text{g/cm}^2$
Relative production by neutrons ( $^{10}\text{Be}$ )	$F_0(^{10}\text{Be})$	0.9724	—
Relative production by neutrons ( $^{26}\text{Al}$ )	$F_0(^{26}\text{Al})$	0.9655	—
Relative production by neutrons ( $^{14}\text{C}$ )	$F_0(^{14}\text{C})$	0.83	—
Relative production by neutrons ( $^{36}\text{Cl}$ )	$F_0(^{36}\text{Cl})$	0.903	—
Relative production by neutrons ( $^3\text{He}$ )	$F_0(^3\text{He})$	1	—
Relative production by neutrons ( $^{21}\text{Ne}$ )	$F_0(^{21}\text{Ne})$	1	—
Relative production by slow muons ( $^{10}\text{Be}$ )	$F_1(^{10}\text{Be})$	0.0186	—
Relative production by slow muons ( $^{26}\text{Al}$ )	$F_1(^{26}\text{Al})$	0.0233	—
Relative production by slow muons ( $^{14}\text{C}$ )	$F_1(^{14}\text{C})$	0.0691	—
Relative production by slow muons ( $^{36}\text{Cl}$ )	$F_1(^{36}\text{Cl})$	0.0447	—
Relative production by slow muons ( $^3\text{He}$ )	$F_1(^3\text{He})$	0	—
Relative production by slow muons ( $^{21}\text{Ne}$ )	$F_1(^{21}\text{Ne})$	0	—
Relative production by slow muons ( $^{10}\text{Be}$ )	$F_2(^{10}\text{Be})$	0.004	—
Relative production by slow muons ( $^{26}\text{Al}$ )	$F_2(^{26}\text{Al})$	0.005	—
Relative production by slow muons ( $^{14}\text{C}$ )	$F_2(^{14}\text{C})$	0.0809	—
Relative production by slow muons ( $^{36}\text{Cl}$ )	$F_2(^{36}\text{Cl})$	0.0523	—
Relative production by slow muons ( $^3\text{He}$ )	$F_2(^3\text{He})$	0	—
Relative production by slow muons ( $^{21}\text{Ne}$ )	$F_2(^{21}\text{Ne})$	0	—
Relative production by fast muons ( $^{10}\text{Be}$ )	$F_3(^{10}\text{Be})$	0.005	—
Relative production by fast muons ( $^{26}\text{Al}$ )	$F_3(^{26}\text{Al})$	0.0062	—
Relative production by fast muons ( $^{14}\text{C}$ )	$F_3(^{14}\text{C})$	0.02	—
Relative production by fast muons ( $^{36}\text{Cl}$ )	$F_3(^{36}\text{Cl})$	0	—
Relative production by fast muons ( $^3\text{He}$ )	$F_3(^3\text{He})$	0	—
Relative production by fast muons ( $^{21}\text{Ne}$ )	$F_3(^{21}\text{Ne})$	0	—
Sea level temperature	$T_0$	288.15	K
Adiabatic lapse rate	$\beta_0$	6.5	K/km
Air pressure at sea level	$P_0$	1013.25	mbar
Geomagnetic field intensity relative to 1945	$M/M_0$	1	—



**Figure 4.** To implement the TCN ingrowth equation of *Schaller et al.* [2002], CosmoCalc uses a least squares fit of the TCN ingrowth equation of *Granger and Smith* [2000] to a “virtual” depth profile defined by this alternative ingrowth equation.



concentrations are scaled to SLHL and an average production rate is calculated using one of the five scaling models of section 2. CosmoCalc comes with a default set of published production rate calibrations, some of which ( $^{10}\text{Be}$  and  $^{26}\text{Al}$ ) were borrowed from Balco and Stone (manuscript in preparation, 2007). The published data come from a variety of latitudes and elevations, yielding a presumably reliable estimate of the globally averaged production rates. This, however, is not always the best approach. For example, if a TCN study is carried out in the vicinity of one particular calibration site, then it makes more sense to use only this site to estimate the local production rate. Therefore CosmoCalc offers the user the flexibility to delete or add calibration sites at will.

## 7.2. Changing the Relative Contributions of Different Production Pathways

[58] Being based on the equation of *Granger and Smith* [2000], the TCN production equation consists of four exponentials: one for neutrons, two for slow neutrons, and one for fast neutrons (see equation (8) and section 5). These exponentials are governed by two sets of parameters: the fractions  $F_i$  and the attenuation lengths  $\Lambda_i$  (for  $i = 0, \dots, 3$ ). Default values for  $\Lambda_i$ ,  $F_i(^{10}\text{Be})$  and  $F_i(^{26}\text{Al})$  were taken from *Granger and Smith* [2000] (Table 1), but these values can be changed in the “Settings” form.

[59] In addition to equation (8), several alternative, but similar looking TCN ingrowth equations exist in the literature. *Schaller et al.* [2002] use not four but eight exponentials (two for neutrons, and three for each slow and fast muons), whereas others use three (one for each production mechanism) [e.g., *Braucher et al.*, 2003; *Miller et al.*, 2006] or only one exponential (neglecting muon production). CosmoCalc provides a separate set of default parameters for each of these alternatives. For example, the ingrowth equation of *Schaller et al.* [2002] was recast in the parameterization of *Granger and Smith* [2000] by a least squares fit of a virtual depth profile (Figure 4).

## 8. How to Report Data Reduced With CosmoCalc

[60] CosmoCalc was designed to be a user-friendly program for both novice and advanced users of TCN methods. Nearly every function comes with a set of options which allow the user to change the

default values of various parameters (section 7). Although CosmoCalc’s flexibility should be considered a positive feature, a danger exists that this may lead to confusion. Therefore it is important that the data-reduction method is well documented when reporting results. Here is an example:

[61] “Ages were calculated with CosmoCalc 1.0 (Vermeesch, 2007), using *Dunai* [2000] scaling factors and default values for all parameters with the following exceptions:  $\rho = 3.5 \text{ g/cm}^3$  and  $\lambda(^{10}\text{Be}) = 5.17 \times 10^{-7} \text{ yr}^{-1}$ ”.

[62] Clearly indicating the version number is important because CosmoCalc will be updated in the future to keep track of new developments in TCN geochronology. Older versions will always be available from the CosmoCalc Web site (<http://cosmocalc.googlepages.com>). Users with useful suggestions for improvements should feel free to contact the author by emailing to [cosmocalc@gmail.com](mailto:cosmocalc@gmail.com).

## Acknowledgments

[63] The author is financially supported by a Marie Curie Fellowship of the European Union (CRONUS-EU network, RTN project reference 511927). Many thanks to Naki Akçar for testing beta versions of CosmoCalc and making useful suggestions which simplified the user interface and made the program more user-friendly and to two anonymous reviewers for constructive comments.

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