

# Portfolio Optimization with Python3

pvhprjet

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## 1 Important Concepts

### 1.1 Return, Expected Return, and Excess return

*Return* refers to the money made or lost on an investment over a period of time. It can be expressed in terms of percentage change or money profit/loss. A positive return represents a profit whereas a negative one represents a loss. This code optimizes the portfolio with regards to the *nominal return*, which is the net profit or loss before any adjustments for taxes, fees, dividends, inflation, or any other influence on the amount [?].

A *holding period return* is an investment's return over the time it is owned by a particular investor. Holding period return may be expressed nominally or as a percentage. When expressed as a percentage, the term often used is *rate of return (RoR)* [?].

The *expected return* is the anticipated profit or loss based on known historical rates of return [?]

$$\langle R \rangle = \sum_i R_i P_i \quad (1)$$

Where  $R_i$  is the return of the  $i$ -th component of the series and  $P_i$  its corresponding probability. Equation 1 is not used in the code because we don't know the probabilities. Instead, we approximate the expected return with the mean value of the probabilities **look into the notes of prof. Nobach regarding the approximation of the mean value.**

The expected return is usually based on historical data and is therefore not guaranteed into the future; however, it does often set reasonable expectations. Therefore, the expected return figure can be thought of as a long-term weighted average of historical returns.

An *annualized total return* is the geometric average amount of money earned by an investment each year over a given time period. The annualized return formula is calculated as a geometric average to show what an investor would earn over a period of time if the annual return was compounded [?].

The *excess return* is

<https://pythonforfinance.net/2017/01/21/investment-portfolio-optimisation-with-python/>  
[http://www.stat.ucla.edu/~nchristo/statistics\\_c183\\_c283/sharpe\\_\\_mutual\\_fund\\_performance.pdf](http://www.stat.ucla.edu/~nchristo/statistics_c183_c283/sharpe__mutual_fund_performance.pdf)