

Autonomous Institution Affiliated to Visvesvaraya Technological University, Belagavi Approved by AICTE, New Delhi, Accredited By NAAC, Bengaluru And NBA, New Delhi

## **DEPARTMENT OF MATHEMATICS**

Course: Fundamentals of Linear Algebra, Calculus and Statistics	QUIZ - III	Maximum marks: 10
Course code: MAT211CT	First semester 2023-2024 Chemistry Cycle Branch: AI, BT, CS, CD, CY, IS, SPARK	Time: 20 Minutes Date: 22-01-2024

Name:	Branch:	USN:

Instructions to students: Rough work can be done at the backside of the sheet.

Q.No	Quiz questions	M	BT	CO
1.1	Rank of the matrix $\begin{bmatrix} 1 & 1 & 1 \\ 1 & -1 & 0 \\ 1 & 1 & 1 \end{bmatrix}$ is  Ans: 2	1	L1	1
1.2	For what values of K, the following system has a non-trivial solution $K^2x - y = 0$ ; $4x - y = 0$ . <b>Ans:</b> $K = \pm 2$	1	L1	1
1.3	Eigenvalues of the matrix $\begin{bmatrix} 2 & -1 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & -2 \end{bmatrix}$ are  Ans: 2,3,-2	1	L1	1
1.4	For the matrix $A = \begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}$ , determine the eigenvector corresponding to eigenvalue $\lambda = 1$ .  Ans: $\begin{bmatrix} -k \\ +k \end{bmatrix}$	1	L1	1
1.5	Express the integral $\int_0^1 \int_y^{\sqrt{y}} f(x,y) dx dy$ as an equivalent integral by changing the order of integration.  Ans: $\int_0^1 \int_{x^2}^x f(x,y) dy dx$	2	L2	2
1.6	The integral obtained by transforming $\int_0^1 \int_0^{\sqrt{1-y^2}} f(x,y)  dx  dy$ to polar coordinates is  Ans: $\int_0^{\frac{\pi}{2}} \int_0^1 f(r,\theta) r  dr  d\theta$	2	L2	2
1.7	If $(\bar{x}, \bar{y})$ is the center of gravity of the lamina bounded by the region $0 \le x \le 1$ , $-1 \le y \le 3$ with the density function $x^3y^2$ and mass $\frac{7}{3}$ , then $\bar{y}$ is  Ans: $\frac{15}{7}$	2	L2	2

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Q.No	Quiz questions	M	BT	CO
1.1	Rank of the matrix $\begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$ is	1	L1	1
	Ans: 3			
1.2	For what values of K, the following system has a non-trivial solution $Kx - 2y = 0$ ; $8x - Ky = 0$ . <b>Ans:</b> $K = \pm 4$	1	L1	1
1.3	Eigenvalues of the matrix $\begin{bmatrix} 8 & 0 & 0 \\ 0 & -6 & 0 \\ 3 & 0 & 2 \end{bmatrix}$ are  Ans: 8,-6,2	1	L1	1
1.4	For the square matrix $A = \begin{bmatrix} 2 & 1 \\ 0 & 3 \end{bmatrix}$ , determine the eigenvector corresponding to eigenvalue $\lambda = 2$ .  Ans: $\begin{bmatrix} k \\ 0 \end{bmatrix}$	1	L1	1
1.5	Express the integral $\int_0^1 \int_x^{\sqrt{x}} f(x,y) dy dx$ as an equivalent integral by changing the order of integration.  Ans: $\int_0^1 \int_{y^2}^y f(x,y) dx dy$	2	L2	2
1.6	The integral obtained by transforming $\int_{-1}^{1} \int_{0}^{\sqrt{1-x^2}} f(x,y)  dy  dx$ to polar coordinates is  Ans: $\int_{0}^{\pi} \int_{0}^{1} f(r,\theta) r dr  d\theta$	2	L2	2
1.7	If $(\bar{x}, \bar{y})$ is the center of gravity of a two dimensional plate that occupies the triangle $0 \le x \le 1, 0 \le y \le x$ with density function $xy$ and mass $\frac{1}{8}$ , then $\bar{y}$ is  Ans: $\frac{8}{15}$	2	L2	2

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Q.No	Quiz questions	M	BT	CO
1.1	Rank of the matrix $\begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$ is	1	L1	1
	$\begin{bmatrix} 1 & 0 & 1 & 15 & 15 & 15 & 15 & 15 & 15$			
	Ans: 3			
1.2	For what values of K, the following system has a non-trivial solution	1	L1	1
	9x - Ky = 0; Kx - y = 0.			
	Ans: $K = \pm 3$			
1.3	[4 0 0]	1	L1	1
1.5	Determine the value of k, if the sum of eigenvalues in matrix $A = \begin{bmatrix} 0 & 3 & 0 \\ 0 & 0 & k \end{bmatrix}$ is 9.	1	Li	1
	Ans: k=2			
1.4	For the square matrix $A = \begin{bmatrix} 2 & 0 \\ 1 & 3 \end{bmatrix}$ , determine the eigenvector corresponding to eigenvalue	1	L1	1
	$\lambda = 2$ .			
	Ans: $\begin{bmatrix} -k \\ +k \end{bmatrix}$			
1.5	Express the integral $\int_0^\infty \int_x^\infty f(x,y) dy dx$ as an equivalent integral by changing the order of	2	L2	2
	integration.			
	Ans: $\int_0^\infty \int_0^y f(x,y) dx dy$			
1.6	The integral obtained by transforming $\int_0^2 \int_0^{\sqrt{4-x^2}} (x^2 + y^2) dy dx$ to polar coordinates is	2	L2	2
	Ans: $\int_0^{\pi/2} \int_0^2 r^3 dr d\theta$			
1.7	If $(\bar{x}, \bar{y})$ is the center of gravity of the region between the curves $y = x^2$ and $y = x$ with the	2	L2	2
	density function x in the interval $0 \le x \le 1$ and mass $\frac{1}{12}$ , then $\bar{x}$ is			
	Ans: $\frac{3}{5}$			
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1.1	Rank of the matrix $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 0 \end{bmatrix}$ is	1	L1	1
	Rank of the matrix $\begin{bmatrix} 0 & 1 & 1 \\ 1 & 0 & 0 \end{bmatrix}$ is			
	Ans: 2			
1.2	For what values of K, the following system has a non-trivial solution	1	L1	1
	Kx - y = 0; -4x + Ky = 0.			
	Ans: $K = \pm 2$			
1.3	Determine value of $a$ , if the sum of eigenvalues in matrix $A = \begin{bmatrix} 6 & 0 & 0 \\ 1 & -3 & 0 \\ 0 & 0 & a \end{bmatrix}$ is 9	1	L1	1
	Ans: a=6			
1.4	For the square matrix $A = \begin{bmatrix} 2 & -5 \\ 0 & 3 \end{bmatrix}$ , determine the eigenvectors corresponding to eigenvalue	1	L1	1
	$\lambda = 2$ .			
	Ans: $\begin{bmatrix} k \\ 0 \end{bmatrix}$			
1.5	Express the integral $\int_0^\infty \int_y^\infty f(x,y) dx dy$ as an equivalent integral by changing the order of	2	L2	2
	integration.			
	Ans: $\int_0^\infty \int_0^x f(x,y) dy dx$			
1.6	The integral obtained by transforming $\int_{-1}^{1} \int_{0}^{\sqrt{1-x^2}} (x^2 + y^2)^{\frac{3}{2}} dy dx$ to polar coordinates is	2	L2	2
	Ans: $\int_0^\pi \int_0^1 r^4 dr \ d\theta$			
1.7	If $(\bar{x}, \bar{y})$ is the center of gravity of a two dimensional plate that occupies the triangle	2	L2	2
	$0 \le x \le 1, 0 \le y \le x$ with density function $xy$ and mass $\frac{1}{8}$ , then $\bar{x}$ is			
	Ans: $\frac{4}{5}$			

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