

Principal Component Analysis

Principal Component Analysis (PCA) is a linear dimensionality reduction technique that can be utilized for extracting information from a high-dimensional space by projecting it into a lower-dimensional sub-space. It tries to preserve the essential parts that have more variation of the data and remove the non-essential parts with fewer variation.

Dimensions are nothing but features that represent the data. For example, A 28 X 28 image has 784 picture elements (pixels) that are the dimensions or features which together represent that image.

One important thing to note about PCA is that it is an Unsupervised dimensionality reduction technique, you can cluster the similar data points based on the feature correlation between them without any supervision (or labels), and you will learn how to achieve this practically using Python in later sections of this tutorial!

One important thing to note about PCA is that it is an Unsupervised dimensionality reduction technique, you can cluster the similar data points based on the feature correlation between them without any supervision (or labels). PCA is a statistical procedure that uses an orthogonal transformation to convert a set of observations of possibly correlated variables (entities each of which takes on various numerical values) into a set of values of linearly uncorrelated variables called principal components. Features, Dimensions, and Variables are all referring to the same thing in this notebook.

Main usage of PCA

- **Data Visualization** When working on any data related problem, extensive data exploration like finding out how the variables are correlated or understanding the distribution of a few variables is crucial. Considering that there are a large number of variables or dimensions along which the data is distributed, visualization can be a challenge and almost impossible. Using dimensionality reduction, data can be projected into a lower dimension, thereby allowing you to visualize the data in a 2D or 3D space.
- **Speeding Machine Learning Algorithm** Since PCA's main idea is dimensionality reduction, you can leverage that to speed up your machine learning algorithm's training and testing time considering your data has a lot of features, and the ML algorithm's learning is too slow.

Principal Component

Principal components are the key to PCA; they represent what's underneath the hood of your data. In a layman term, when the data is projected into a lower dimension (assume three dimensions) from a higher space, the three dimensions are nothing but

the three Principal Components that captures (or holds) most of the variance (information) of your data.

Principal components have both direction and magnitude. The direction represents across which principal axes the data is mostly spread out or has most variance and the magnitude signifies the amount of variance that Principal Component captures of the data when projected onto that axis. The principal components are a straight line, and the first principal component holds the most variance in the data. Each subsequent principal component is orthogonal to the last and has a lesser variance. In this way, given a set of x correlated variables over y samples you achieve a set of u uncorrelated principal components over the same y samples.

The reason you achieve uncorrelated principal components from the original features is that the correlated features contribute to the same principal component, thereby reducing the original data features into uncorrelated principal components; each representing a different set of correlated features with different amounts of variation.

Each principal component represents a percentage of total variation captured from the data.

PCA on iris dataset

In this section we will decompose with PCA very simple 4-dimensional data set. This is one eg the best known pattern recognition dataset. The data set contains 3 classes of 50 instances each, where each class refers to a type of iris plant. One class is linearly separable from the other 2; the latter are NOT linearly separable from each other.

```
In [50]: import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
from sklearn.decomposition import PCA
from sklearn.preprocessing import StandardScaler
from sklearn.datasets import load_breast_cancer
import numpy as np

%matplotlib inline
```

```
In [4]: %%javascript
IPython.OutputArea.prototype._should_scroll = function(lines) {
    return false;
}
```

```
In [5]: iris_url = "https://archive.ics.uci.edu/ml/machine-learning-databases/iri
```

```
In [6]: # loading dataset into Pandas DataFrame
df_iris = pd.read_csv(
    iris_url,
    names=["sepal length", "sepal width", "petal length", "petal width",
])
```

```
In [7]: df_iris.head(15)
```

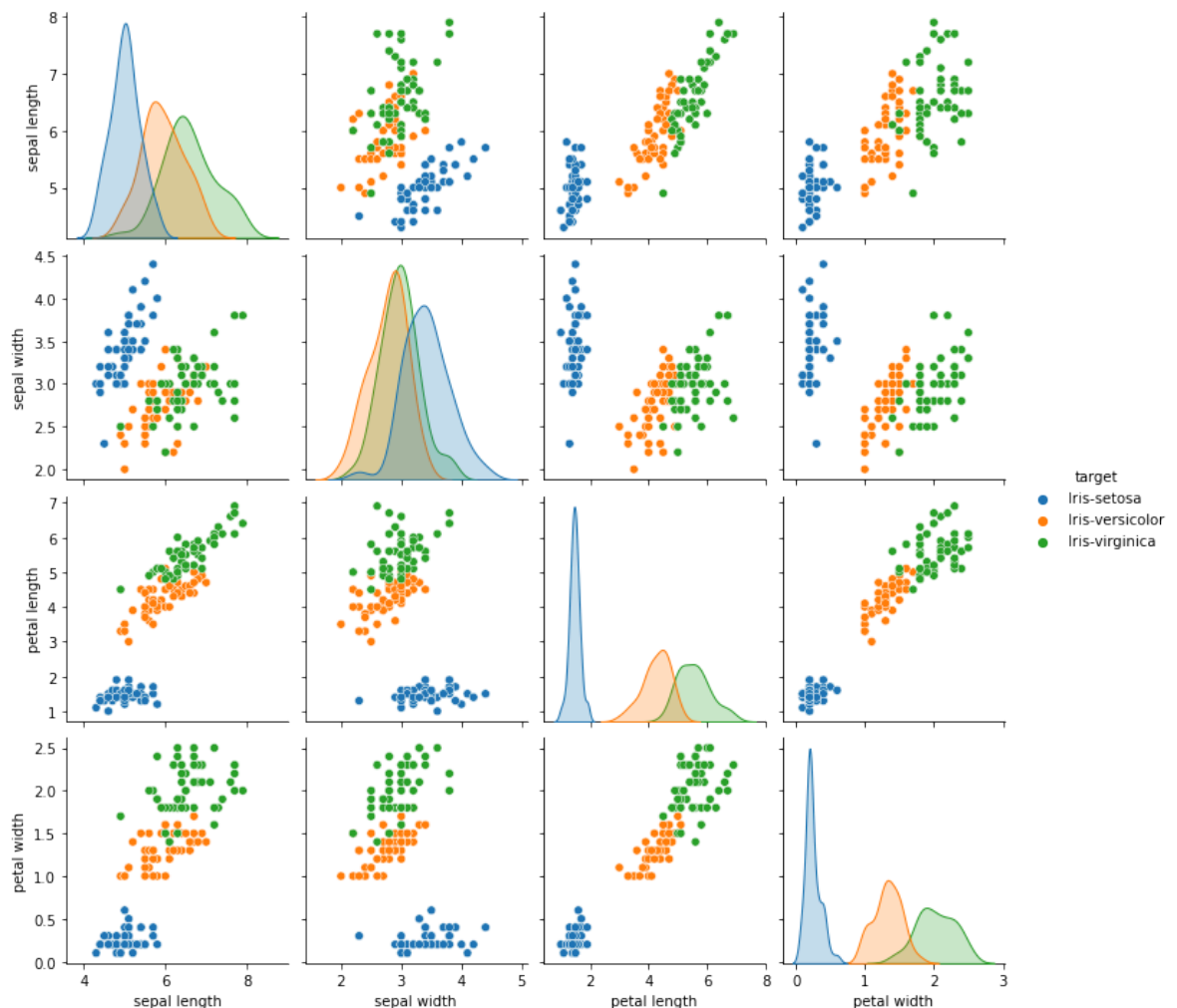
Out[7]:

	sepal length	sepal width	petal length	petal width	target
0	5.1	3.5	1.4	0.2	Iris-setosa
1	4.9	3.0	1.4	0.2	Iris-setosa
2	4.7	3.2	1.3	0.2	Iris-setosa
3	4.6	3.1	1.5	0.2	Iris-setosa
4	5.0	3.6	1.4	0.2	Iris-setosa
5	5.4	3.9	1.7	0.4	Iris-setosa
6	4.6	3.4	1.4	0.3	Iris-setosa
7	5.0	3.4	1.5	0.2	Iris-setosa
8	4.4	2.9	1.4	0.2	Iris-setosa
9	4.9	3.1	1.5	0.1	Iris-setosa
10	5.4	3.7	1.5	0.2	Iris-setosa
11	4.8	3.4	1.6	0.2	Iris-setosa
12	4.8	3.0	1.4	0.1	Iris-setosa
13	4.3	3.0	1.1	0.1	Iris-setosa
14	5.8	4.0	1.2	0.2	Iris-setosa

In the case that the dimensionality of the data allows it, it is good practice to see how each pair of features correlate with each other. In the following link you will find more methods for visualizing multidimensional data using matplotlib and seaborn libraries <https://towardsdatascience.com/the-art-of-effective-visualization-of-multi-dimensional-data-6c7202990c57>

In [8]: `sns.pairplot(df_iris, hue="target")`

Out[8]: `<seaborn.axisgrid.PairGrid at 0x7f5c7f84ad90>`



You can immediately see that the features petal length and petal width are strongly correlated

Standardize the Data

Since PCA yields a feature subspace that maximizes the variance along the axes, it makes sense to standardize the data, especially, if it was measured on different scales. Although, all features in the Iris dataset were measured in centimeters, let us continue with the transformation of the data onto unit scale (mean=0 and variance=1), which is a requirement for the optimal performance of many machine learning algorithms.

```
In [9]: features_iris = ["sepal length", "sepal width", "petal length", "petal width"]
x_iris = df_iris.loc[:, features_iris].values
```

```
In [10]: y_iris = df_iris.loc[:, ["target"]].values
```

```
In [11]: x_iris = StandardScaler().fit_transform(x_iris)
```

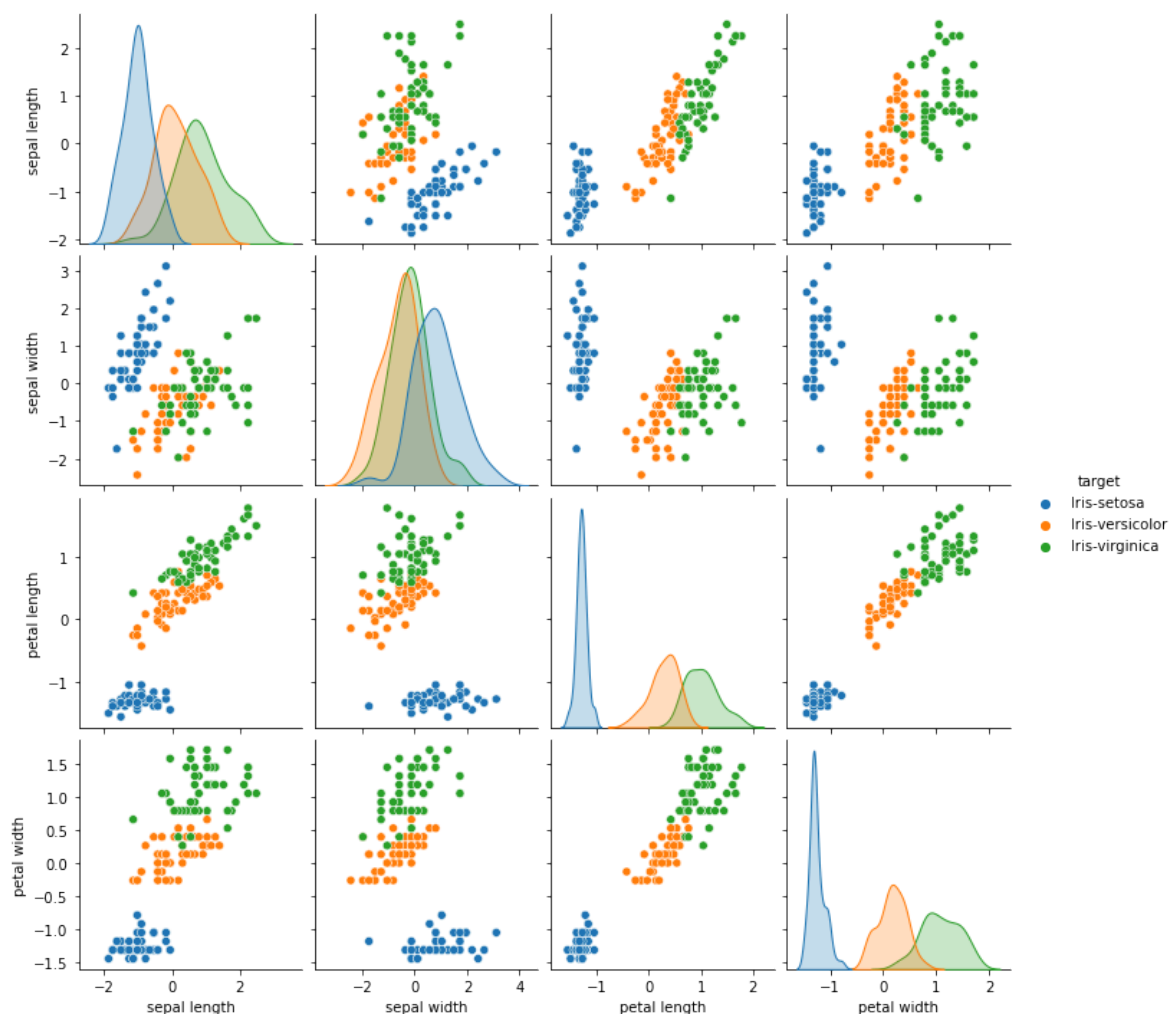
```
In [12]: df_iris_standardize = pd.DataFrame(data=x_iris, columns=features_iris)
df_iris_standardize["target"] = df_iris["target"]
df_iris_standardize.head(15)
```

Out[12]:

	sepal length	sepal width	petal length	petal width	target
0	-0.900681	1.032057	-1.341272	-1.312977	Iris-setosa
1	-1.143017	-0.124958	-1.341272	-1.312977	Iris-setosa
2	-1.385353	0.337848	-1.398138	-1.312977	Iris-setosa
3	-1.506521	0.106445	-1.284407	-1.312977	Iris-setosa
4	-1.021849	1.263460	-1.341272	-1.312977	Iris-setosa
5	-0.537178	1.957669	-1.170675	-1.050031	Iris-setosa
6	-1.506521	0.800654	-1.341272	-1.181504	Iris-setosa
7	-1.021849	0.800654	-1.284407	-1.312977	Iris-setosa
8	-1.748856	-0.356361	-1.341272	-1.312977	Iris-setosa
9	-1.143017	0.106445	-1.284407	-1.444450	Iris-setosa
10	-0.537178	1.494863	-1.284407	-1.312977	Iris-setosa
11	-1.264185	0.800654	-1.227541	-1.312977	Iris-setosa
12	-1.264185	-0.124958	-1.341272	-1.444450	Iris-setosa
13	-1.870024	-0.124958	-1.511870	-1.444450	Iris-setosa
14	-0.052506	2.189072	-1.455004	-1.312977	Iris-setosa

In [13]: `sns.pairplot(df_iris_standarize, hue="target")`

Out[13]: `<seaborn.axisgrid.PairGrid at 0x7f5c7ae7b940>`



We can see that the distributions are now standardized

PCA Projection to 2D

```
In [14]: pca_iris = PCA(n_components=2)
```

```
In [15]: principalComponents_iris = pca_iris.fit_transform(x_iris)
```

```
In [16]: principalDf_iris = pd.DataFrame(
    data=principalComponents_iris,
    columns=["principal component 1", "principal component 2"],
)
```

```
In [17]: finalDf_iris = pd.concat([principalDf_iris, df_iris[["target"]]], axis=1)
finalDf_iris.head(15)
```

Out[17]:

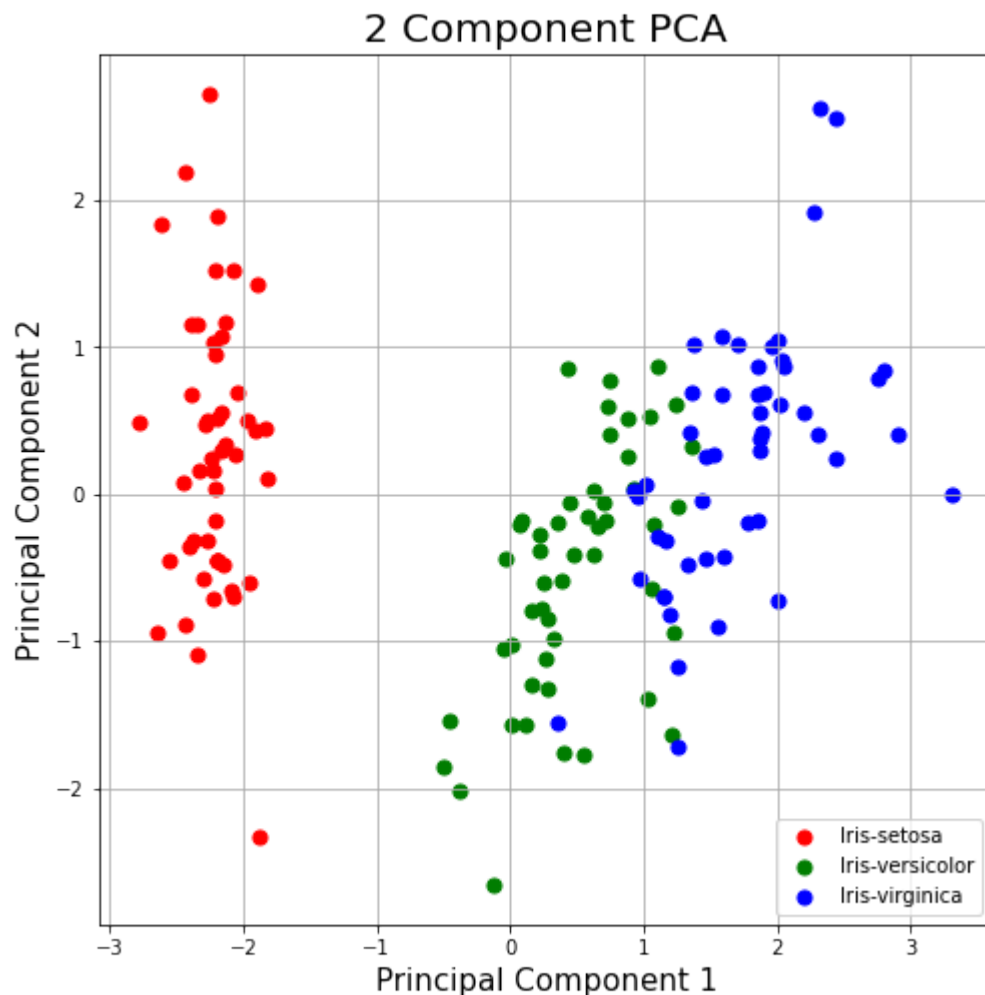
	principal component 1	principal component 2	target
0	-2.264542	0.505704	Iris-setosa
1	-2.086426	-0.655405	Iris-setosa
2	-2.367950	-0.318477	Iris-setosa
3	-2.304197	-0.575368	Iris-setosa
4	-2.388777	0.674767	Iris-setosa
5	-2.070537	1.518549	Iris-setosa
6	-2.445711	0.074563	Iris-setosa
7	-2.233842	0.247614	Iris-setosa
8	-2.341958	-1.095146	Iris-setosa
9	-2.188676	-0.448629	Iris-setosa
10	-2.163487	1.070596	Iris-setosa
11	-2.327378	0.158587	Iris-setosa
12	-2.224083	-0.709118	Iris-setosa
13	-2.639716	-0.938282	Iris-setosa
14	-2.192292	1.889979	Iris-setosa

Visualize 2D Projection

Use a PCA projection to 2d to visualize the entire data set. You should plot different classes using different colors or shapes.

```
In [18]: fig = plt.figure(figsize=(8, 8))
ax = fig.add_subplot(1, 1, 1)
ax.set_xlabel("Principal Component 1", fontsize=15)
ax.set_ylabel("Principal Component 2", fontsize=15)
ax.set_title("2 Component PCA", fontsize=20)

iris_targets = ["Iris-setosa", "Iris-versicolor", "Iris-virginica"]
colors = ["r", "g", "b"]
for target, color in zip(iris_targets, colors):
    indicesToKeep = finalDf_iris["target"] == target
    ax.scatter(
        finalDf_iris.loc[indicesToKeep, "principal component 1"],
        finalDf_iris.loc[indicesToKeep, "principal component 2"],
        c=color,
        s=50,
    )
ax.legend(iris_targets)
ax.grid()
```



iris-setosa is linearly separable from other classes

Explained Variance

The explained variance tells us how much information (variance) can be attributed to each of the principal components.

```
In [19]: pca_iris.explained_variance_ratio_
```

```
Out[19]: array([0.72770452, 0.23030523])
```

Together, the first two principal components contain 95.80% of the information. The first principal component contains 72.77% of the variance and the second principal component contains 23.03% of the variance. The third and fourth principal component contained the rest of the variance of the dataset.

limitations of PCA

- PCA is not scale invariant. check: we need to scale our data first.
- The directions with largest variance are assumed to be of the most interest
- Only considers orthogonal transformations (rotations) of the original variables

- PCA is only based on the mean vector and covariance matrix. Some distributions (multivariate normal) are characterized by this, but some are not.
- If the variables are correlated, PCA can achieve dimension reduction. If not, PCA just orders them according to their variances.

Exercises - Perform PCA for breast cancer dataset

- You can find this dataset it in the scikit learn library, import it and convert to pandas dataframe, original label are '0' and '1' for better readability change these names to: 'benign' and 'malignant'

```
In [31]: df_bc, labels_bc = load_breast_cancer(return_X_y=True, as_frame=True)

labels_bc[labels_bc == 0] = "benign"
labels_bc[labels_bc == 1] = "malignant"
```

```
In [33]: labels_bc.head(3)
```

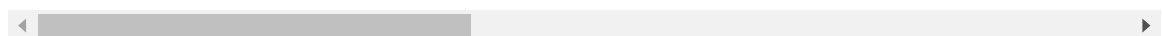
```
Out[33]: 0    benign
1    benign
2    benign
Name: target, dtype: object
```

```
In [34]: df_bc.head(3)
```

```
Out[34]:
```

	mean radius	mean texture	mean perimeter	mean area	mean smoothness	mean compactness	mean concavity	mean concave points
0	17.99	10.38	122.8	1001.0	0.11840	0.27760	0.3001	0.14710
1	20.57	17.77	132.9	1326.0	0.08474	0.07864	0.0869	0.07017
2	19.69	21.25	130.0	1203.0	0.10960	0.15990	0.1974	0.12790

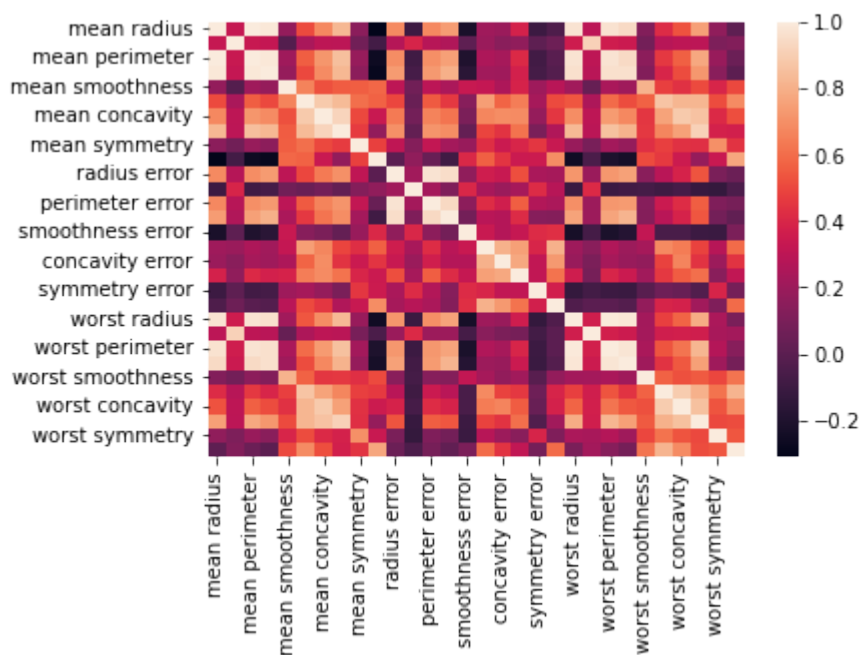
3 rows × 30 columns



- Visualizes correlations between pairs of features (due to the greater number of features use pandas corr () function instead of pairplot instead of seaborn heatmap ())

```
In [36]: sns.heatmap(df_bc.corr())
```

```
Out[36]: <Axes: >
```



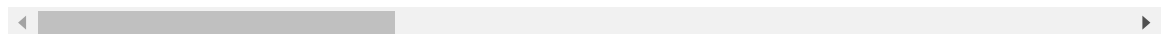
- Perform PCA and visualize the data

```
In [38]: df_bc.describe()
```

```
Out[38]:
```

	mean radius	mean texture	mean perimeter	mean area	mean smoothness	mean compactness
count	569.000000	569.000000	569.000000	569.000000	569.000000	569.000000
mean	14.127292	19.289649	91.969033	654.889104	0.096360	0.104341
std	3.524049	4.301036	24.298981	351.914129	0.014064	0.052813
min	6.981000	9.710000	43.790000	143.500000	0.052630	0.019380
25%	11.700000	16.170000	75.170000	420.300000	0.086370	0.064920
50%	13.370000	18.840000	86.240000	551.100000	0.095870	0.092630
75%	15.780000	21.800000	104.100000	782.700000	0.105300	0.130400
max	28.110000	39.280000	188.500000	2501.000000	0.163400	0.345400

8 rows × 30 columns



```
In [43]: # Just making sure we only have floats in DF
list(zip(df_bc.columns, df_bc.dtypes))
```

```
Out[43]: [('mean radius', dtype('float64')),
('mean texture', dtype('float64')),
('mean perimeter', dtype('float64')),
('mean area', dtype('float64')),
('mean smoothness', dtype('float64')),
('mean compactness', dtype('float64')),
('mean concavity', dtype('float64')),
('mean concave points', dtype('float64')),
('mean symmetry', dtype('float64')),
('mean fractal dimension', dtype('float64')),
('radius error', dtype('float64')),
('texture error', dtype('float64')),
('perimeter error', dtype('float64')),
('area error', dtype('float64')),
('smoothness error', dtype('float64')),
('compactness error', dtype('float64')),
('concavity error', dtype('float64')),
('concave points error', dtype('float64')),
('symmetry error', dtype('float64')),
('fractal dimension error', dtype('float64')),
('worst radius', dtype('float64')),
('worst texture', dtype('float64')),
('worst perimeter', dtype('float64')),
('worst area', dtype('float64')),
('worst smoothness', dtype('float64')),
('worst compactness', dtype('float64')),
('worst concavity', dtype('float64')),
('worst concave points', dtype('float64')),
('worst symmetry', dtype('float64')),
('worst fractal dimension', dtype('float64'))]
```

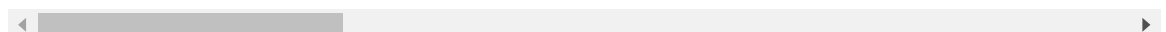
```
In [44]: # Scale features
X_bc = StandardScaler().fit_transform(df_bc)
df_bc_standardized = pd.DataFrame(data=X_bc, columns=df_bc.columns)

df_bc_standardized.describe()
```

```
Out[44]:
```

	mean radius	mean texture	mean perimeter	mean area	mean smoothness	cc
count	5.690000e+02	5.690000e+02	5.690000e+02	5.690000e+02	5.690000e+02	5.6
mean	-1.373633e-16	6.868164e-17	-1.248757e-16	-2.185325e-16	-8.366672e-16	1.
std	1.000880e+00	1.000880e+00	1.000880e+00	1.000880e+00	1.000880e+00	1.0
min	-2.029648e+00	-2.229249e+00	-1.984504e+00	-1.454443e+00	-3.112085e+00	-1.6
25%	-6.893853e-01	-7.259631e-01	-6.919555e-01	-6.671955e-01	-7.109628e-01	-7.
50%	-2.150816e-01	-1.046362e-01	-2.359800e-01	-2.951869e-01	-3.489108e-02	-2.
75%	4.693926e-01	5.841756e-01	4.996769e-01	3.635073e-01	6.361990e-01	4.
max	3.971288e+00	4.651889e+00	3.976130e+00	5.250529e+00	4.770911e+00	4.5

8 rows × 30 columns



```
In [45]: pca_bc = PCA(n_components=2)
components_bc = pca_bc.fit_transform(df_bc_standardized)
```

```
In [47]: principal_df_bc = pd.DataFrame(
        data=components_bc, columns=["principal component 1", "principal comp
    )
```

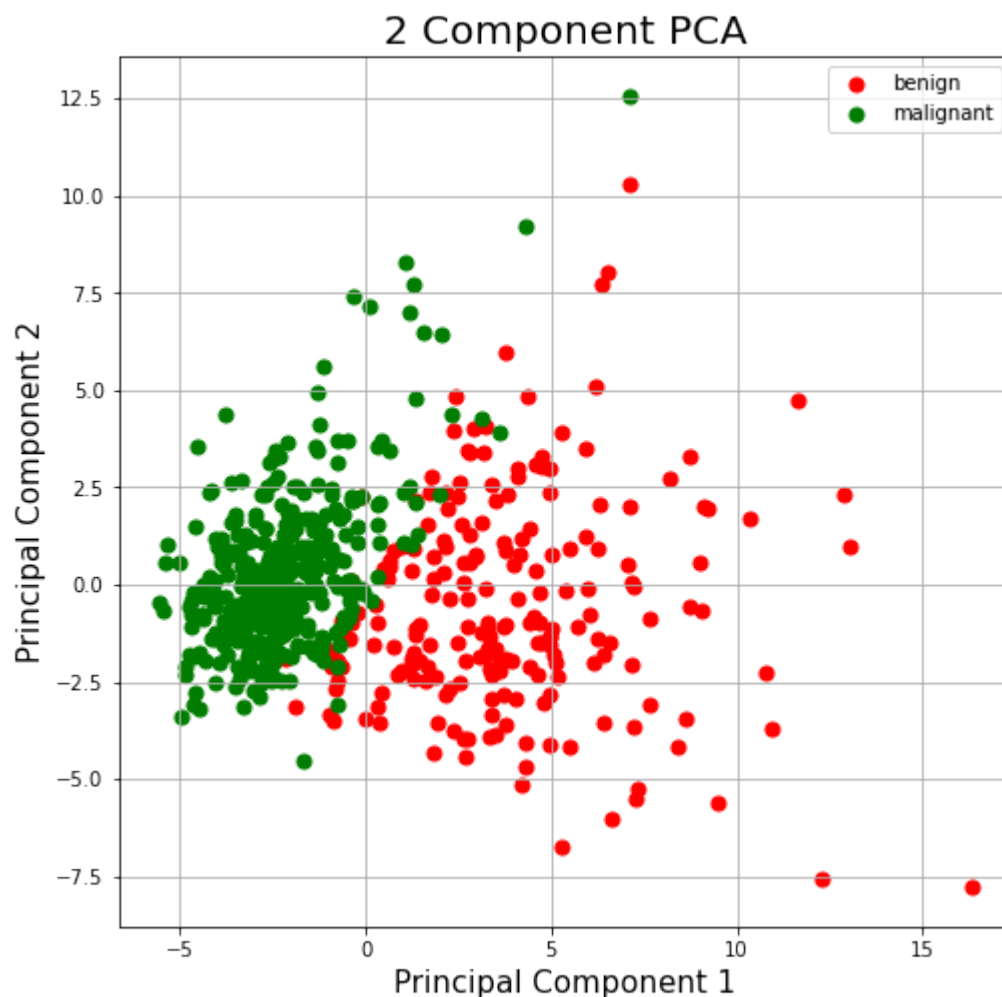
```
In [49]: final_df_bc = pd.concat([principal_df_bc, labels_bc], axis=1)
        final_df_bc.head(15)
```

```
Out[49]:
```

	principal component 1	principal component 2	target
0	9.192837	1.948583	benign
1	2.387802	-3.768172	benign
2	5.733896	-1.075174	benign
3	7.122953	10.275589	benign
4	3.935302	-1.948072	benign
5	2.380247	3.949929	benign
6	2.238883	-2.690031	benign
7	2.143299	2.340244	benign
8	3.174924	3.391813	benign
9	6.351747	7.727174	benign
10	-0.810414	-2.659275	benign
11	2.651100	0.066568	benign
12	8.185034	2.700976	benign
13	0.342126	-0.968279	benign
14	4.342379	4.861083	benign

```
In [53]: fig = plt.figure(figsize=(8, 8))
        ax = fig.add_subplot(1, 1, 1)
        ax.set_xlabel("Principal Component 1", fontsize=15)
        ax.set_ylabel("Principal Component 2", fontsize=15)
        ax.set_title("2 Component PCA", fontsize=20)

        colors = ["r", "g", "b"]
        for target, color in zip(np.unique(labels_bc), colors):
            indices_to_keep = labels_bc == target
            ax.scatter(
                final_df_bc.loc[indices_to_keep, "principal component 1"],
                final_df_bc.loc[indices_to_keep, "principal component 2"],
                c=color,
                s=50,
            )
        ax.legend(np.unique(labels_bc))
        ax.grid()
```



🔥 Comment

Class are not linearly separable. They don't overlap significantly, but there's a lot of datapoints that wouldn't be correctly separated by linear classifier.

- Examine explained variance, draw a plot showing relation between total explained variance and number of principal components used

```
In [54]: pca_bc.explained_variance_ratio_
```

```
Out[54]: array([0.44272026, 0.18971182])
```

🔥 Comment

First two components contain only ~64% of information. We'd be better off by using more components if we want to use PCA to reduce dimensionality of our data.

```
In [60]: total_explained_variance = []
         for i in range(2, len(df_bc.columns)):
             pca_bc_temp = PCA(n_components=i)
             pca_bc_temp.fit(df_bc_standardized)

             total_explained_variance.append(np.sum(pca_bc_temp.explained_variance_ratio_))

         data_to_plot = list(zip(list(range(2, len(df_bc.columns))), total_explained_variance))
```

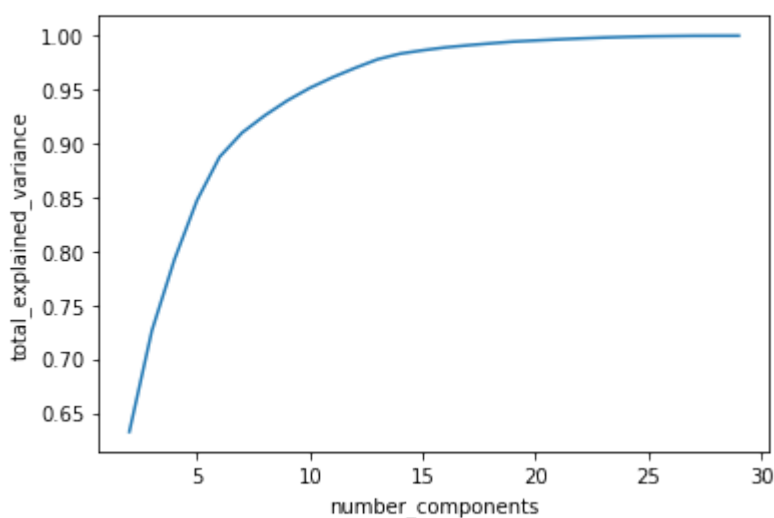
```
In [70]: df_plot = pd.DataFrame(
    data=data_to_plot,
    columns=["number_components", "total_explained_variance"],
)
df_plot.head(3)
```

```
Out[70]:
```

	number_components	total_explained_variance
0	2	0.632432
1	3	0.726364
2	4	0.792385

```
In [72]: sns.lineplot(data=df_plot, x="number_components", y="total_explained_vari
```

```
Out[72]: <Axes: xlabel='number_components', ylabel='total_explained_variance'>
```



🔥 Comment

We could successfully use PCA for dimensionality reduction with sufficiently high number of components.

- Use recursive feature elimination (available in scikit-learn module) or another feature ranking algorithm to split 30 features to on 15 "more important" and "less important" features. Then repeat the last step from the full data set - draw a plot showing relation between total explained variance and number of principal components used for all 3 cases. Explain the result briefly.

```
In [82]: from sklearn.feature_selection import RFE
from sklearn.svm import SVR

labels_bc_binary = labels_bc.copy()
labels_bc_binary[labels_bc == "benign"] = 0
labels_bc_binary[labels_bc == "malignant"] = 1

estimator = SVR(kernel="linear")
selector = RFE(estimator, n_features_to_select=15, step=1)
selector = selector.fit(df_bc_standardized, labels_bc_binary)
```

```
Out[82]:
```

	0
0	True
1	False
2	True
3	True
4	False

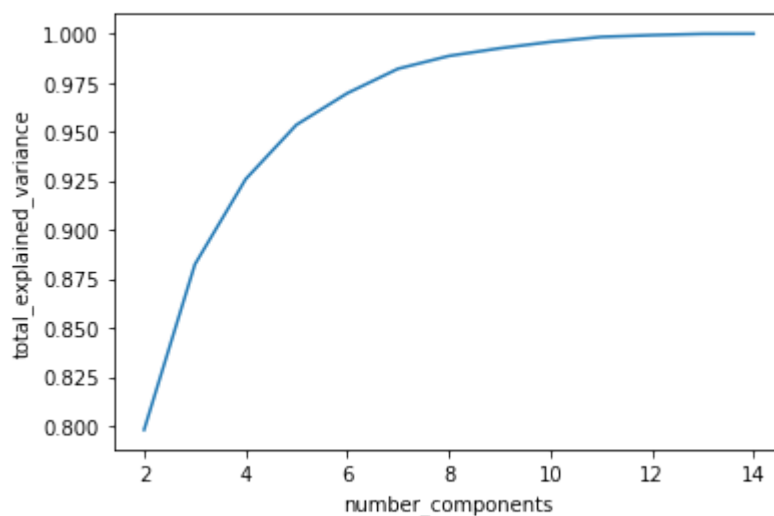
```
In [89]: df_bc_good_features = df_bc_standardized.loc[:, selector.support_]
df_bc_bad_features = df_bc_standardized.loc[:, ~selector.support_]
```

```
In [90]: total_explained_variance = []
for i in range(2, len(df_bc_good_features.columns)):
    pca_bc_temp = PCA(n_components=i)
    pca_bc_temp.fit(df_bc_good_features)

    total_explained_variance.append(np.sum(pca_bc_temp.explained_variance_))

data_to_plot = list(zip(list(range(2, len(df_bc_good_features.columns))),
df_plot = pd.DataFrame(
    data=data_to_plot,
    columns=["number_components", "total_explained_variance_good"],
)
```

```
Out[90]: <Axes: xlabel='number_components', ylabel='total_explained_variance'>
```



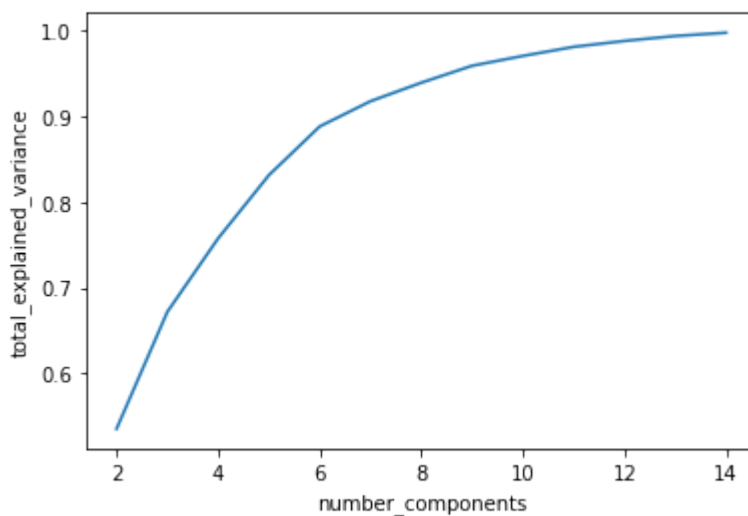
```
In [96]: total_explained_variance = []
for i in range(2, len(df_bc_bad_features.columns)):
    pca_bc_temp = PCA(n_components=i)
    pca_bc_temp.fit(df_bc_bad_features)

    total_explained_variance.append(np.sum(pca_bc_temp.explained_variance_))

data_to_plot = list(zip(list(range(2, len(df_bc_bad_features.columns))),
df_plot = pd.DataFrame(
    data=data_to_plot,
    columns=["number_components", "total_explained_variance"],
)
```

```
)
sns.lineplot(data=df_plot, x="number_components", y="total_explained_vari
```

Out[96]: <Axes: xlabel='number_components', ylabel='total_explained_variance'>



🔥 Comment

If we only use less relevant features (according to RFE), we need more principal components to contain same amount of information.

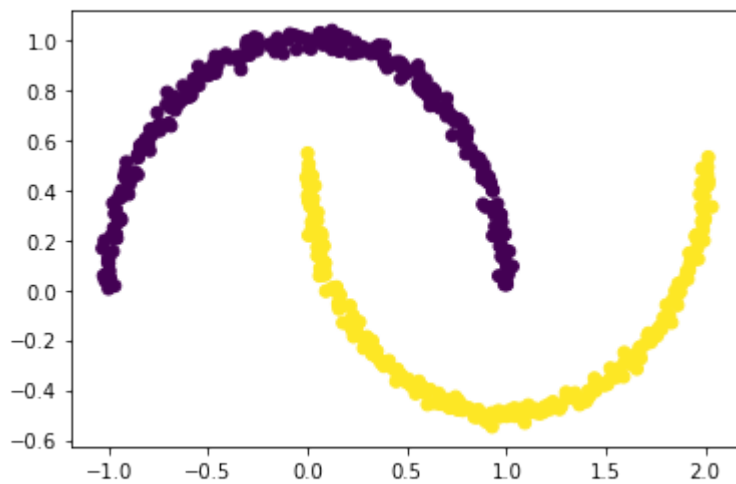
Kernel PCA

PCA is a linear method. That is it can only be applied to datasets which are linearly separable. It does an excellent job for datasets, which are linearly separable. But, if we use it to non-linear datasets, we might get a result which may not be the optimal dimensionality reduction. Kernel PCA uses a kernel function to project dataset into a higher dimensional feature space, where it is linearly separable. It is similar to the idea of Support Vector Machines.

```
In [97]: import matplotlib.pyplot as plt
from sklearn.datasets import make_moons

X, y = make_moons(n_samples=500, noise=0.02, random_state=417)

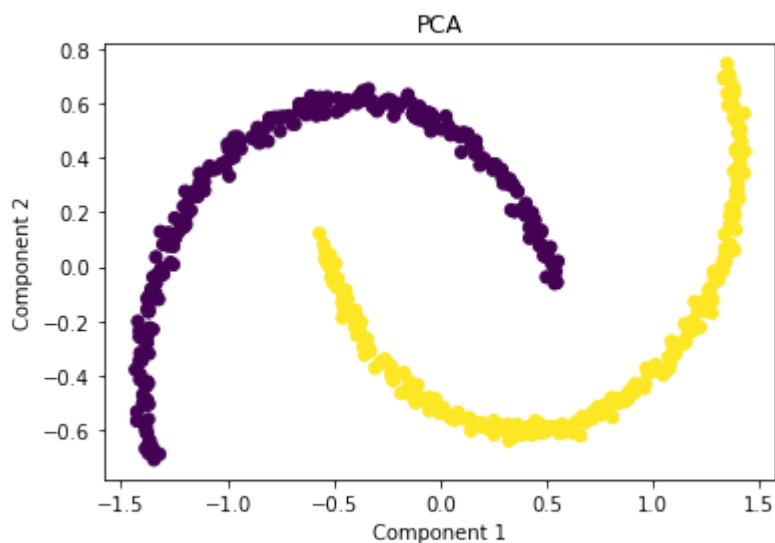
plt.scatter(X[:, 0], X[:, 1], c=y)
plt.show()
```

Let's apply PCA on this dataset

```
In [98]: pca = PCA(n_components=2)
X_pca = pca.fit_transform(X)

plt.title("PCA")
plt.scatter(X_pca[:, 0], X_pca[:, 1], c=y)
plt.xlabel("Component 1")
plt.ylabel("Component 2")
plt.show()
```

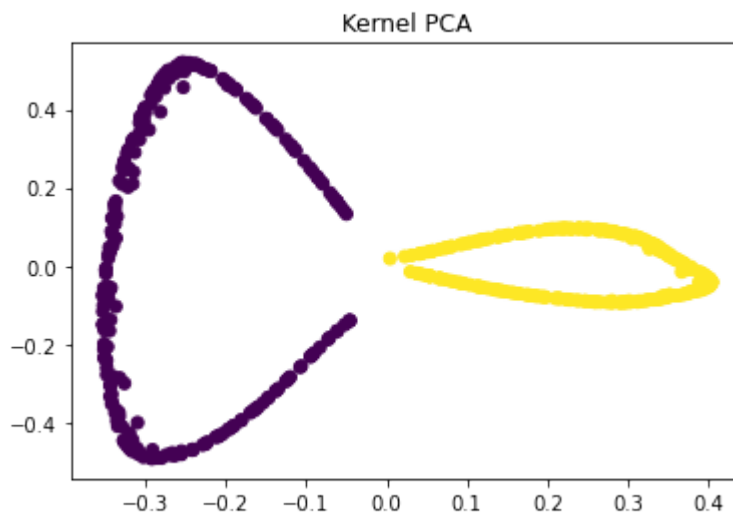


PCA failed to distinguish the two classes

```
In [99]: from sklearn.decomposition import KernelPCA

kpca = KernelPCA(kernel="rbf", gamma=15)
X_kpca = kpca.fit_transform(X)

plt.title("Kernel PCA")
plt.scatter(X_kpca[:, 0], X_kpca[:, 1], c=y)
plt.show()
```



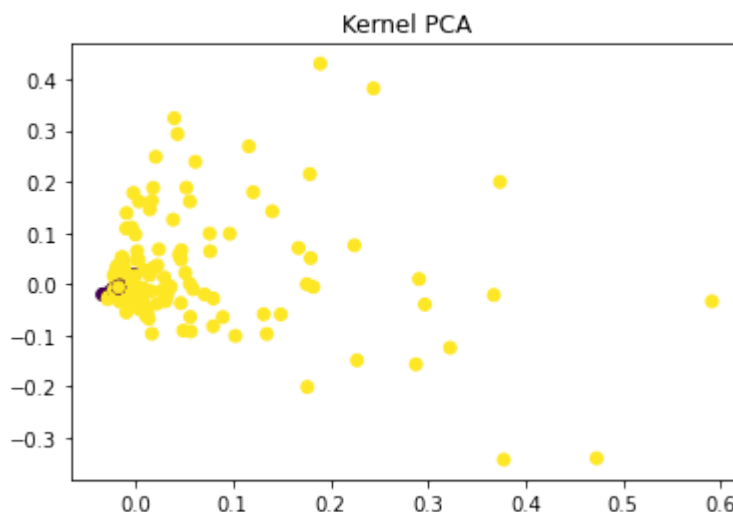
Applying kernel PCA on this dataset with RBF kernel with a gamma value of 15

KernelPCA exercises

- Visualize in 2d datasets used in this labs, experiment with the parameters of the KernelPCA method change kernel and gamma params. Docs: <https://scikit-learn.org/stable/modules/generated/sklearn.decomposition.KernelPCA.html>

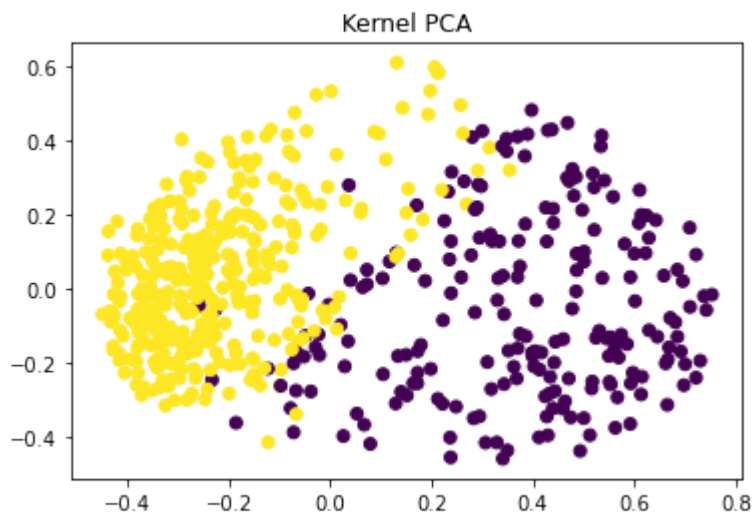
```
In [156... k pca = KernelPCA(n_components=2, kernel="rbf", gamma=1)
k pca_bc = k pca.fit_transform(df_bc_standardized)

plt.title("Kernel PCA")
plt.scatter(k pca_bc[:, 0], k pca_bc[:, 1], c=labels_bc_binary)
plt.show()
```



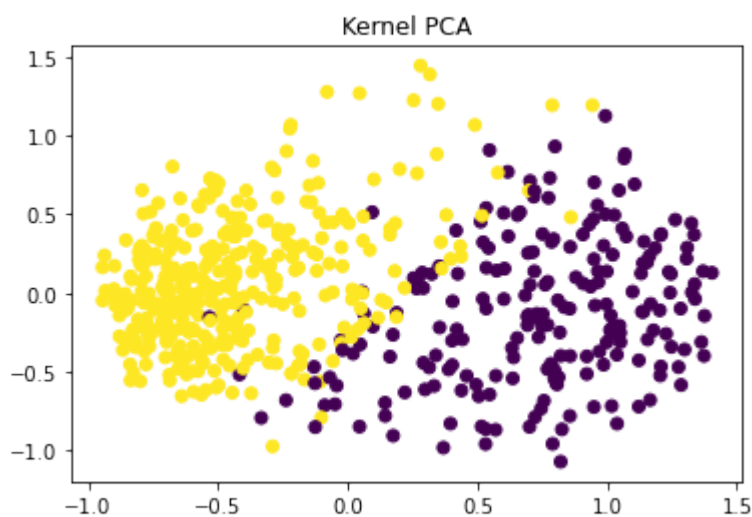
```
In [157... k pca = KernelPCA(n_components=2, kernel="rbf", gamma=0.01)
k pca_bc = k pca.fit_transform(df_bc_standardized)

plt.title("Kernel PCA")
plt.scatter(k pca_bc[:, 0], k pca_bc[:, 1], c=labels_bc_binary)
plt.show()
```



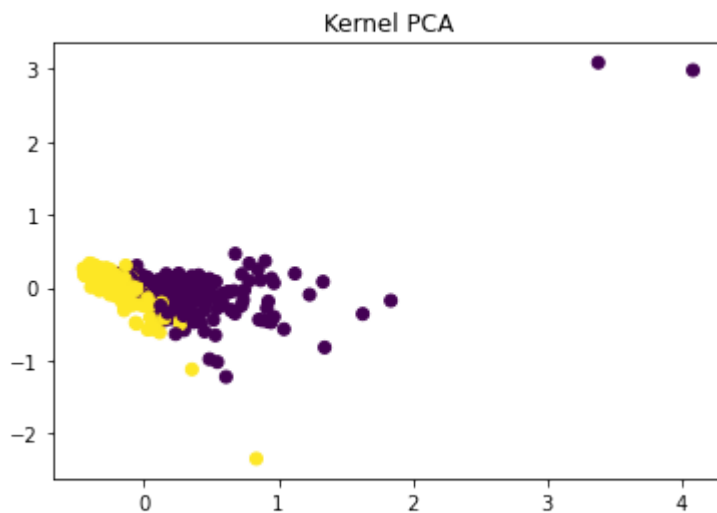
```
In [158... kpca = KernelPCA(n_components=2, kernel="sigmoid", gamma=0.1)
kpca_bc = kpca.fit_transform(df_bc_standardized)

plt.title("Kernel PCA")
plt.scatter(kpca_bc[:, 0], kpca_bc[:, 1], c=labels_bc_binary)
plt.show()
```



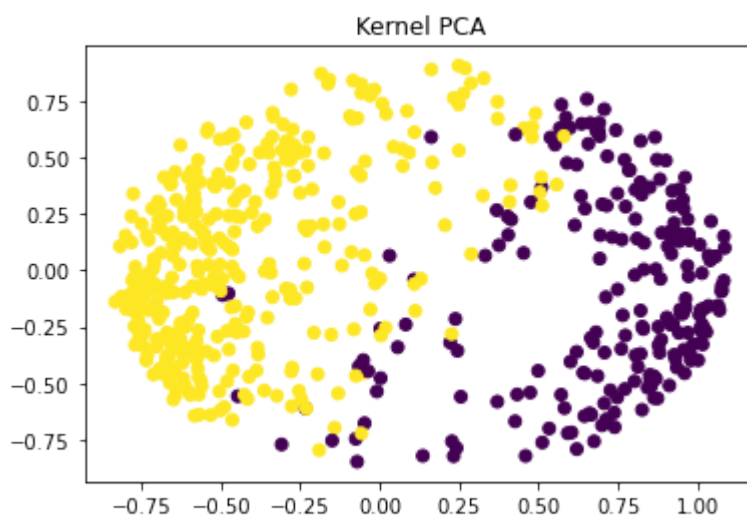
```
In [159... kpca = KernelPCA(n_components=2, kernel="poly", gamma=0.001, degree=10)
kpca_bc = kpca.fit_transform(df_bc_standardized)

plt.title("Kernel PCA")
plt.scatter(kpca_bc[:, 0], kpca_bc[:, 1], c=labels_bc_binary)
plt.show()
```



```
In [160... kpca = KernelPCA(kernel="cosine", gamma=0.5)
kpca_bc = kpca.fit_transform(df_bc_standardized)

plt.title("Kernel PCA")
plt.scatter(kpca_bc[:, 0], kpca_bc[:, 1], c=labels_bc_binary)
plt.show()
```



🔥 Comment

After testing different kernels, I was still unable to achieve linearly separable clusters. Maybe data is too complicated for such operation and we can't keep enough information after squashing it down into 2 dimensions.

In []:

Homework

- Download the MNIST data set (there is a function to load this set in libraries such as scikit-learn, keras). It is a collection of black and white photos of handwritten digits with a resolution of 28x28 pixels. which together gives 784 dimensions.
- Try to visualize this dataset using PCA and KernelPCA, don't expect full separation of the data

- Similar to the exercises, examine explained variance. draw explained variance vs number of principal Components plot.
- Find number of principal components for 99%, 95%, 90%, and 85% of explained variance.
- Draw some sample MNIST digits and from PCA of its images transform data back to its original space (https://scikit-learn.org/stable/modules/generated/sklearn.decomposition.PCA.html#sklearn.decomposition.PCA.inverse_transform)
Make an inverse transformation for number of components corresponding with explained variance shown above and draw the reconstructed images. The idea of this exercise is to see visually how depending on the number of components some information is lost.
- Perform the same reconstruction using KernelPCA (make comparisons for the same components number) https://scikit-learn.org/stable/modules/generated/sklearn.decomposition.KernelPCA.html#sklearn.decomposition.KernelPCA.inverse_transform

Useful links

<https://scikit-learn.org> <https://towardsdatascience.com/introduction-to-principal-component-analysis-pca-with-python-code-69d3fcf19b57>
<https://towardsdatascience.com/kernel-pca-vs-pca-vs-ica-in-tensorflow-sklearn-60e17eb15a64>

In []: