6.2: Regions Between Curves

Definition. (Area of a Region Between Two Curves)

Suppose f and g are continuous functions with $f(x) \ge g(x)$ on the interval [a, b]. The area of the region bounded by the graphs of f and g on [a, b] is

$$A = \int_a^b (f(x) - g(x)) dx.$$

Definition. (Area of a Region Between Two Curves with Respect to y)

Suppose f and g are continuous functions with $f(y) \ge g(y)$ on the interval [c, d]. The area of the region bounded by the graphs x = f(y) and x = g(y) on [c, d] is

$$A = \int_{c}^{d} (f(y) - g(y)) dy.$$