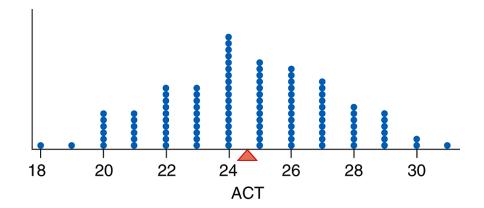
# 3.1: Summaries for Symmetric Distributions

### Definition.

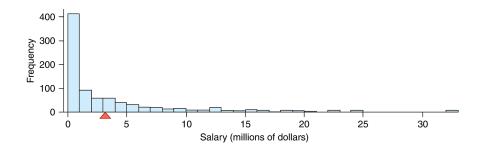
Given a collection of data  $\{x_1, x_2, \dots, x_n\}$ , the **mean** of the data is the arithmetic mean:

$$\bar{x} = \frac{x_1}{n} + \frac{x_2}{n} + \dots + \frac{x_n}{n} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

**Example.** An instructor at Peoria Junior College in Illinois collected data from two classes, including the students' ACT scores. Below is the distribution of self-reported ACT scores for one statistics class:



**Example.** The winnings of the top-ranked professional tennis players in the 2018 season are given in the graph below:

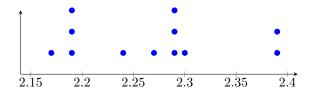


## Note:

- When the distribution is roughly symmetric, the mean represents a typical value in the data.
- The mean is *not* a good estimate of a typical value of a skewed distribution.

**Example.** According to GasBuddy.com (a website that invites people to submit prices at local gas stations), the prices of 1 gallon of regular gas at 12 service stations near the downtown area of Austin, TX, were as follows one winter day in 2018:

\$2.19	\$2.19	\$2.39	\$2.19
\$2.24	\$2.39	\$2.27	\$2.29
\$2.17	\$2.29	\$2.30	\$2.29



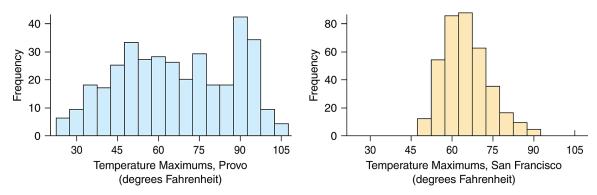
Find the mean price of a gallon of regular gas at these service stations, and interpret the result.

### Definition.

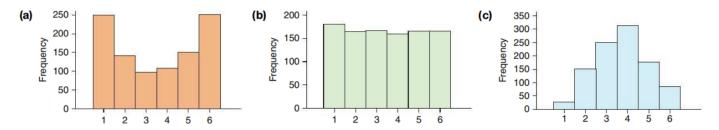
The **standard deviation** is a number that measures how far the typical observation is from the mean. For symmetric, unimodal distributions, a majority of the data is within one standard deviation of the mean. The standard deviation is given by

$$s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n - 1}}$$

**Example.** The histograms below show daily high temperatures in degrees Fahrenheit recorded over one year in Provo, Utah (left), and San Francisco, California (right). Which city do we expect to have a higher standard deviation?



**Example.** Below are three histograms representing distributions with the same mean. Which distribution has the largest standard deviation? Which has the smallest?



**Example.** Recall the data set of gas prices from before. Use StatCrunch to compute the standard deviation of this data set and interpret the result:

\*\*statcrunch.com\*\*

\$2.19	\$2.19	\$2.39	\$2.19
\$2.24	\$2.39	\$2.27	\$2.29
\$2.17	\$2.29	\$2.30	\$2.29

- 1. Click "Open StatCrunch"
- 2. Enter data into spreadsheet
- 3. Under the "Stat" menu, select "Summary Stats" then "Columns" or "Rows"

### Definition.

The **variance** is the standard deviation squared:

$$s^{2} = \frac{\sum (x_{i} - \bar{x})^{2}}{n - 1}$$