# 1.4: Straight Lines

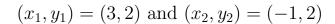
## Definition. (Slope of a Nonvertical Line)

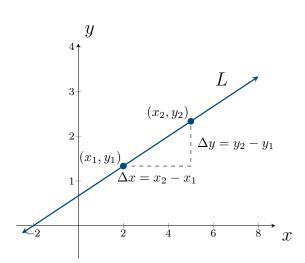
If  $(x_1, y_1)$  and  $(x_2, y_2)$  are any two distinct points on a nonvertical line L, then the slope m of L is given by

$$m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

**Example.** Compute the slope of the line passing through the points

$$(x_1, y_1) = (1, 1)$$
 and  $(x_2, y_2) = (4, 2)$ 





$$(x_1, y_1) = (4, 1)$$
 and  $(x_2, y_2) = (4, 4)$ 

#### Definition. (Point-Slope Form of an Equation of a Line)

An equation of the line that has slope m and passes through the point  $(x_1, y_1)$  is given by

$$y - y_1 = m(x - x_1)$$

**Example.** Find the equation of the line going through the points

$$(x_1, y_1) = (-2, 1)$$
 and  $(x_2, y_2) = (3, -2)$ 

$$(x_1, y_1) = (3, 4)$$
 and  $(x_2, y_2) = (-1, 4)$ 

$$(x_1, y_1) = (2, 0)$$
 and  $(x_2, y_2) = (2, 1)$ 

# Definition. (Slope-Intercept Form of an Equation of a Line)

An equation of the line that has slope m and intersects the y-axis at the point (0,b) is given by

$$y = mx + b$$

**Example.** Rewrite the equations in the previous example in slope-intercept form.

## Definition. (Parallel and Perpendicular lines)

Let  $L_1$  and  $L_2$  be lines with slopes  $m_1$  and  $m_2$  respectively. If  $L_1$  and  $L_2$  are parallel, then

$$m_1 = m_2$$
.

If  $L_1$  and  $L_2$  are perpendicular, then

$$m_1 = -\frac{1}{m_2}.$$

#### Example.

Find the line parallel to  $y = \frac{3}{2}x + 1$  that passes through the point (-4, 10).

Find the line perpendicular to  $y = \frac{3}{2}x + 1$  that passes through the point (-3, 4).

# Forms of Linear Equations

General form: Ax + By = C

Point-slope form:  $y - y_1 = m(x - x_1)$ 

Slope-intercept form: y = mx + b

Vertical line: x = a

Horizontal line: y = b